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Data Management and Analytics using SAS

Academic Year 2001-21

DMAS Assessment 3: Lab Report

Introduction

Earthquakes are devastating events that often cause structural damage and loss of lives. Being able to understand the characteristics of earthquakes can lead to better forecasting, to allow us to prepare and react more effectively. Richter magnitude scale was developed in order to quantify the strength of an earthquake. Richter magnitude is just one measure of earthquake strength.

In this report we will examine a dataset that contains 23741 records from earthquakes over several years. We assume earthquakes are independent events.

Our dataset contains the following variables.

id - ID of record (Numeric)

lat - Latitude of earthquake (Numeric)

Long - Longitude of earthquake (Numeric)

dist - Distance travelled by earthquake in a particular direction (Numeric)

depth - Depth of earthquake (Numeric)

md - Magnitude of earthquake, estimated from the duration of seismic wave-train (Numeric)

richter - Intensity of earthquake (Numeric)

mw - Moment magnitude scale value of earthquake (Numeric)

ms - Surface wave magnitude scale value of earthquake (Numeric)

mb - Bodywave magnitude value, measured using P-waves (Numeric)

country - Country of earthquake (Character)

direction - Direction of earthquake (Character)

The first step is to view our data from earthquake dataset. We notice that the variable *mw* has a lot of empty values. We assume that the observations with missing values are random and we omit these observations.

For the purpose of this report, we will also need a new variable *xm* which is the maximum of *md*, *mw*, *ms*, *mb* and *richter*. We add a new column to our dataset called *xm* and our new summarized dataset is.

Summary of earthquake dataset

Variable	Label	Minimum	Mean	Median	Maximum
<i>id</i>	ID	21.00	12258.71	10939.50	23741.00
<i>lat</i>	Latitude	30.29	38.00	38.18	45.75
<i>long</i>	Longitude	18.34	30.47	27.85	48.00
<i>dist</i>	Distance (km)	0.10	3.05	2.30	81.60
<i>depth</i>	Depth (km)	1.00	27.36	17.05	225.00
<i>md</i>	Magnitude	0.00	2.91	4.30	7.20
<i>richter</i>	Richter	0.00	4.34	4.50	7.20
<i>mw</i>	Moment Magnitude	0.00	4.48	4.70	7.70
<i>ms</i>	Surface-wave Magnitude	0.00	2.89	4.20	7.90
<i>mb</i>	Bodywave Magnitude	0.00	2.95	4.40	7.10
<i>xm</i>	Maximum Magnitude	3.40	4.63	4.70	7.90

As we can see from the graph the data from the dataset give us the following information:

- Latitude
Our data are limited from 30 to 46 degrees of latitude.
- Longitude
Our data are limited from 18 to 48 degrees of longitude. In comparison with Latitude our data cover south and South east Europe to West Asia.
- The variables *md*, *ms*, *mb* range from 0 to less than 8.

Our main objectives for this report are:

- a. We should investigate if there is evidence that the average value of *xm* is different than 4.1? (*xm* is the maximum of *md* *mw* *ms* *mb* and *Richter*.)
- b. To find out if there is a difference between countries on the average moment magnitude scale.
- c. Create a model for Richter based on other attributes of earthquake.
- d. Classify an earthquake as serious or not.
- e. Compare model from d) with a model with response variable serious and explanatory variable *xm*.

Exploratory analysis

The CORR Procedure

10 Variables:		lat	long	dist	depth	md	richter	mw	ms	mb	xm
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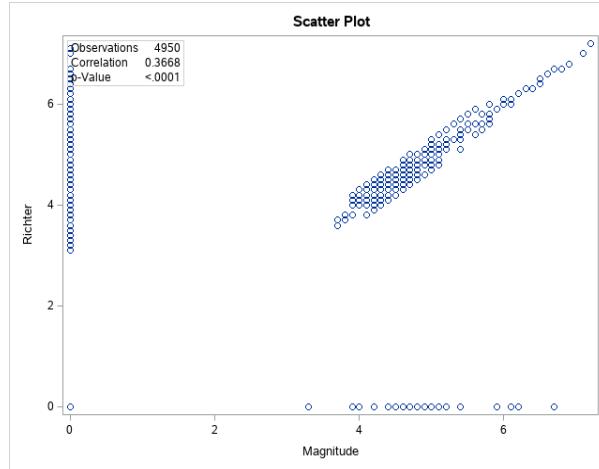
Simple Statistics							
Variable	N	Mean	Std Dev	Sum	Minimum	Maximum	Label
lat	4950	37.99586	2.45495	188080	30.29000	45.75000	Latitude
long	4950	-0.71670	0.10461	-3548	-1.18286	-0.51893	Longitude
dist	1731	3.04697	4.17998	5274	0.10000	81.60000	Distance (km)
depth	4950	27.35826	27.09753	135423	1.00000	225.00000	Depth (km)
md	4950	2.90602	2.35268	14385	0	7.20000	Magnitude
richter	4950	4.34327	0.92002	21499	0	7.20000	Richter
mw	4950	4.47758	1.04875	22164	0	7.70000	Moment Magnitude
ms	4950	2.89269	2.35988	14319	0	7.90000	Surface-wave Magnitude
mb	4950	2.95248	2.34734	14615	0	7.10000	Bodywave Magnitude
xm	4950	4.63489	0.67495	22943	3.40000	7.90000	Maximum Magnitude

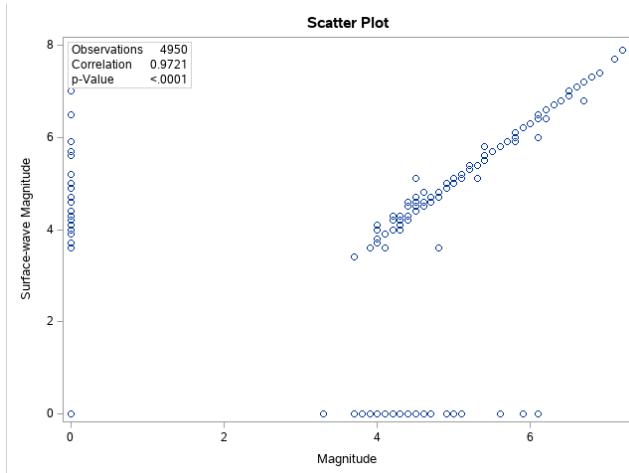
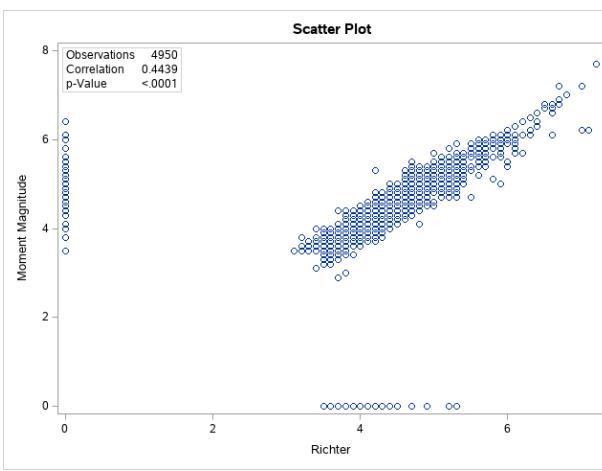
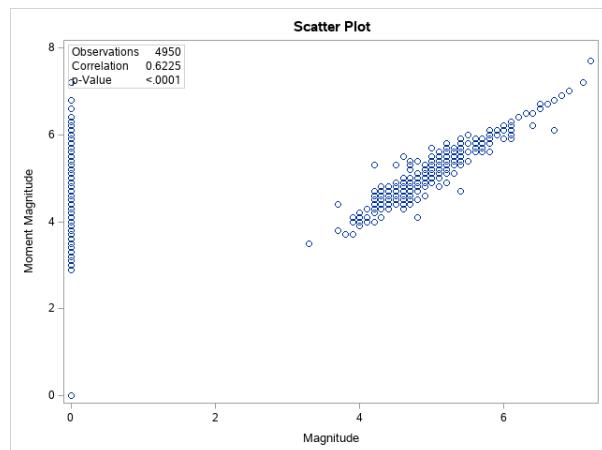
Pearson Correlation Coefficients											
Prob > r under H0: Rho=0											
Number of Observations											
	lat	long	dist	depth	md	richter	mw	ms	mb	xm	
lat Latitude	1.00000	0.28815	0.00977	-0.17720	0.09940	0.09491	0.04190	0.10291	0.09813	0.06653	
	4950	<.0001	0.6847	<.0001	<.0001	<.0001	0.0032	<.0001	<.0001	<.0001	4950
long Longitude	0.28815	1.00000	0.12425	0.00100	0.14142	0.10593	0.12292	0.13601	0.14272	0.09767	
	<.0001	4950	<.0001	0.9439	<.0001	<.0001	<.0001	<.0001	<.0001	<.0001	4950
dist Distance (km)	0.00977	0.12425	1.00000	0.01436	0.02580	0.02787	-0.01180	0.01423	0.02010	0.03309	
	0.6847	<.0001	1731	1731	0.5503	0.2834	0.2465	0.6238	0.5540	0.4032	0.1688
depth Depth (km)	-0.17720	0.00100	0.01436	1.00000	0.31697	0.11167	0.21437	0.31695	0.32161	0.23645	
	<.0001	0.9439	0.5503	1731	4950	<.0001	<.0001	<.0001	<.0001	<.0001	4950
md Magnitude	0.09940	0.14142	0.02580	0.31697	1.00000	0.36681	0.62248	0.97209	0.96499	0.70894	
	<.0001	<.0001	0.2834	<.0001	4950	<.0001	<.0001	<.0001	<.0001	<.0001	4950
richter Richter	0.09491	0.10593	0.02787	0.11167	0.36681	1.00000	0.44387	0.41411	0.38686	0.59681	
	<.0001	<.0001	0.2465	<.0001	4950	<.0001	<.0001	<.0001	<.0001	<.0001	4950
mw Moment Magnitude	0.04190	0.12292	-0.01180	0.21437	0.62248	0.44387	1.00000	0.63981	0.62789	0.78142	
	0.0032	<.0001	0.6238	<.0001	4950	<.0001	<.0001	<.0001	<.0001	<.0001	4950
ms Surface-wave Magnitude	0.10291	0.13601	0.01423	0.31695	0.97209	0.41411	0.63981	1.00000	0.98036	0.74343	
	<.0001	<.0001	0.5540	1731	4950	<.0001	<.0001	4950	<.0001	<.0001	4950
mb Bodywave Magnitude	0.09813	0.14272	0.02010	0.32161	0.96499	0.38686	0.62789	0.98036	1.00000	0.71876	
	<.0001	<.0001	0.4032	1731	4950	<.0001	<.0001	4950	<.0001	<.0001	4950
xm Maximum	0.06653	0.09767	0.03309	0.23645	0.70894	0.59681	0.78142	0.74343	0.71876	1.00000	
	<.0001	<.0001	0.1688	1731	4950	<.0001	<.0001	4950	<.0001	<.0001	4950

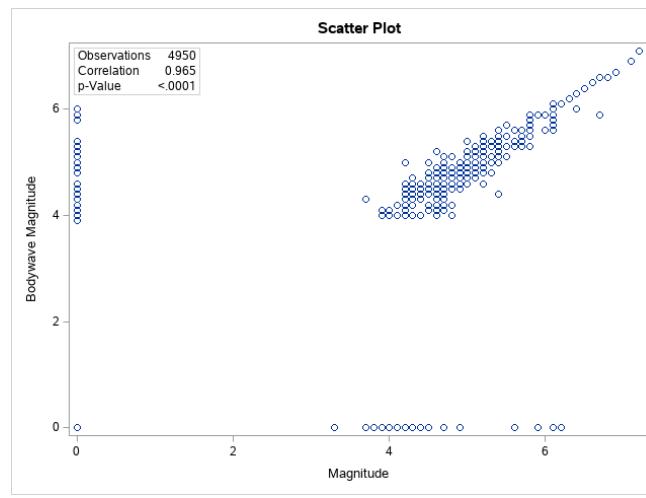
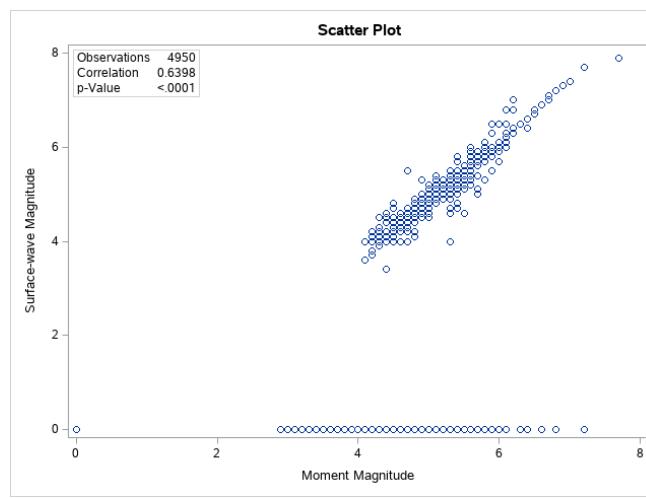
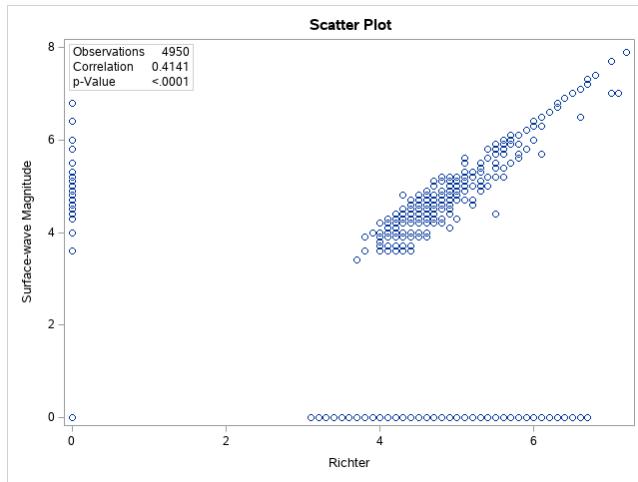
Magnitude										
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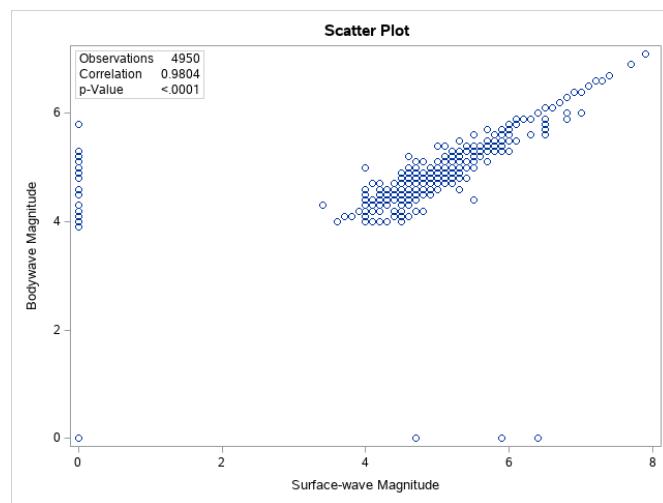
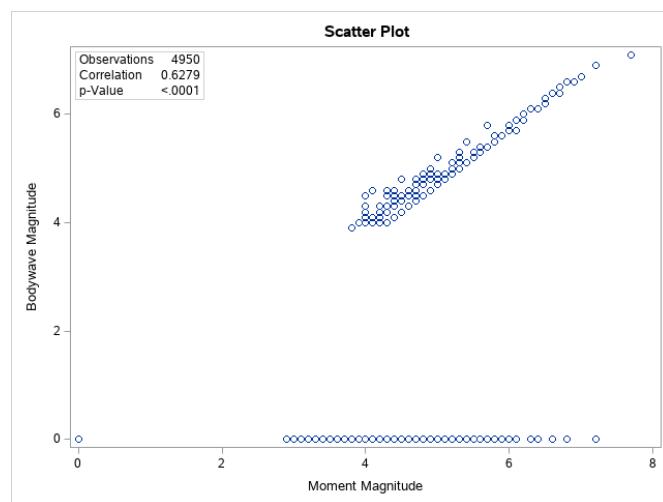
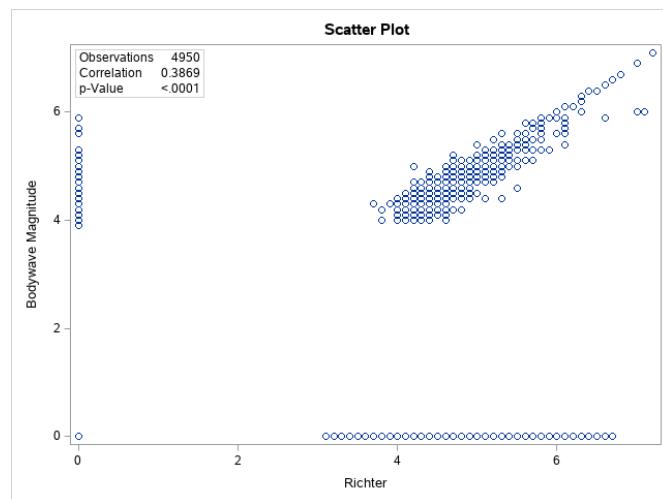
From the above table we can see that we can reject that correlation is equal to 0 in the following pairs:

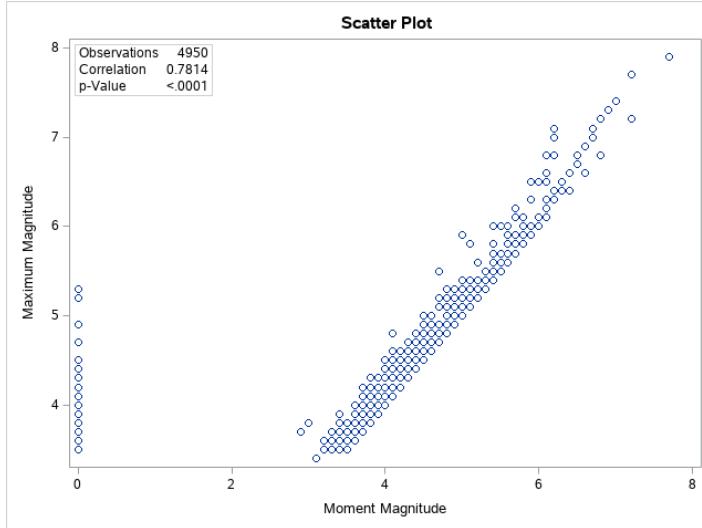
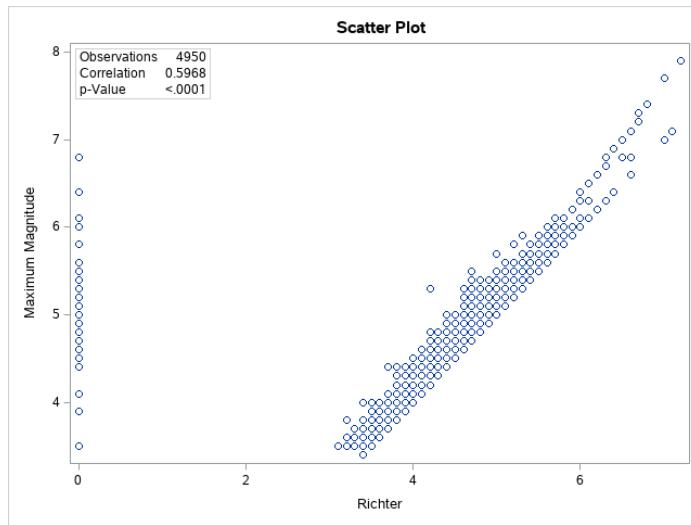
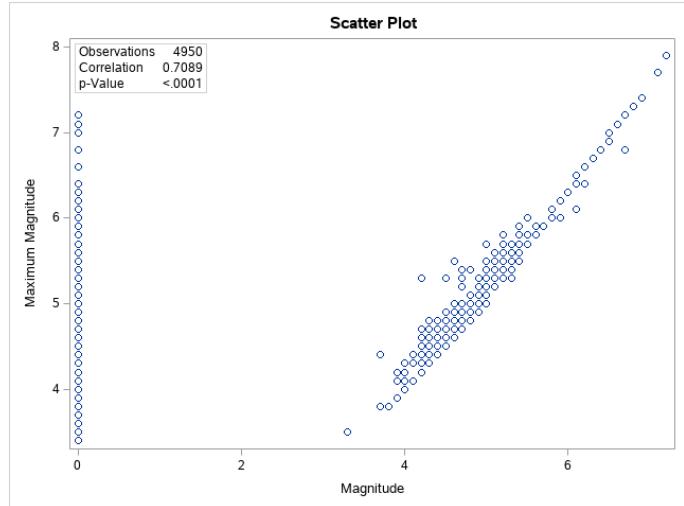
- Lat (Latitude) with Longitude, Depth, Magnitude, Richter, Moment Magnitude, Surface-wave Magnitude, Bodywave Magnitude, Maximum Magnitude.
- Long (Longitude) with Latitude, Distance, Magnitude, Richter, Moment Magnitude, Surface-wave Magnitude, Bodywave Magnitude, Maximum Magnitude.
- Distance (km) with Longitude,
- Depth (km) with Latitude, , Magnitude, Richter, Moment Magnitude, Surface-wave Magnitude, Bodywave Magnitude, Maximum Magnitude.
- Magnitude with Latitude, Longitude, Depth, Richter, Moment Magnitude, Surface-wave Magnitude, Bodywave Magnitude, Maximum Magnitude.
- Richter with Latitude, Longitude, Depth, Magnitude, Moment Magnitude, Surface-wave Magnitude, Bodywave Magnitude, Maximum Magnitude.
- Moment Magnitude (mw) with Latitude, Longitude, Depth, Magnitude, Richter, Surface-wave Magnitude, Bodywave Magnitude, Maximum Magnitude.
- Surface-wave Magnitude (ms) with Latitude, Longitude, Depth, Magnitude, Richter, Moment Magnitude, Bodywave Magnitude, Maximum Magnitude.
- Bodywave Magnitude (mb) with Latitude, Longitude, Depth, Magnitude, Richter, Moment Magnitude, Surface-wave Magnitude, Maximum Magnitude.
- Maximum Magnitude (xm) with Latitude, Longitude, Depth, Magnitude, Richter, Moment Magnitude, Surface-wave Magnitude, Bodywave Magnitude.

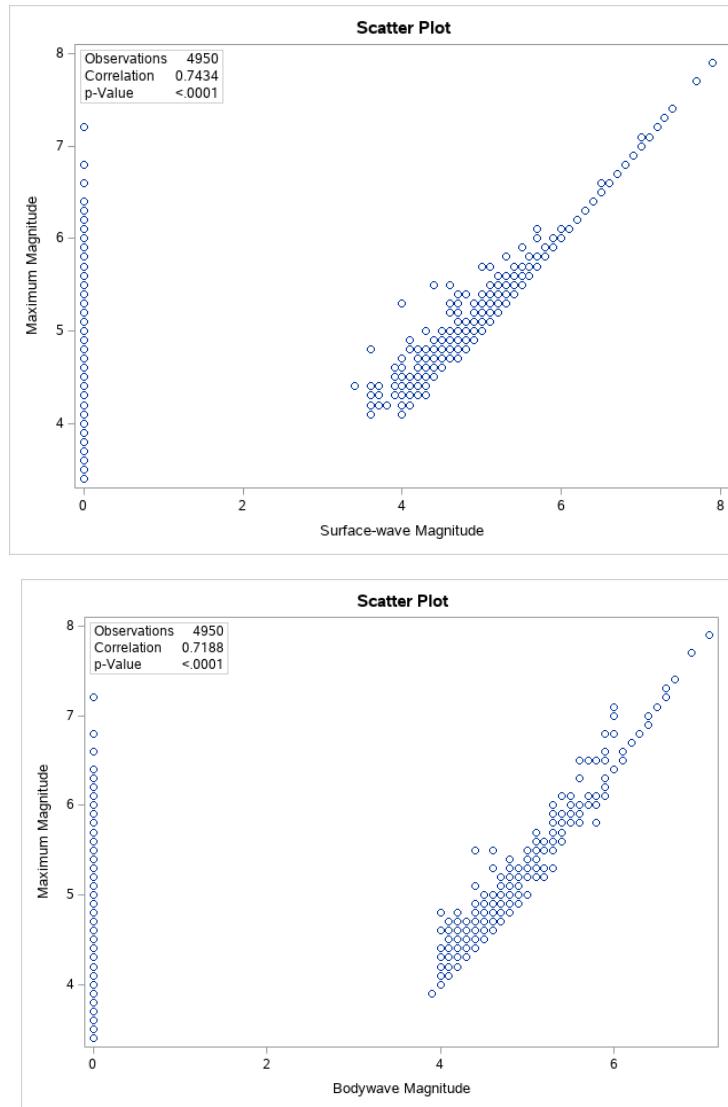








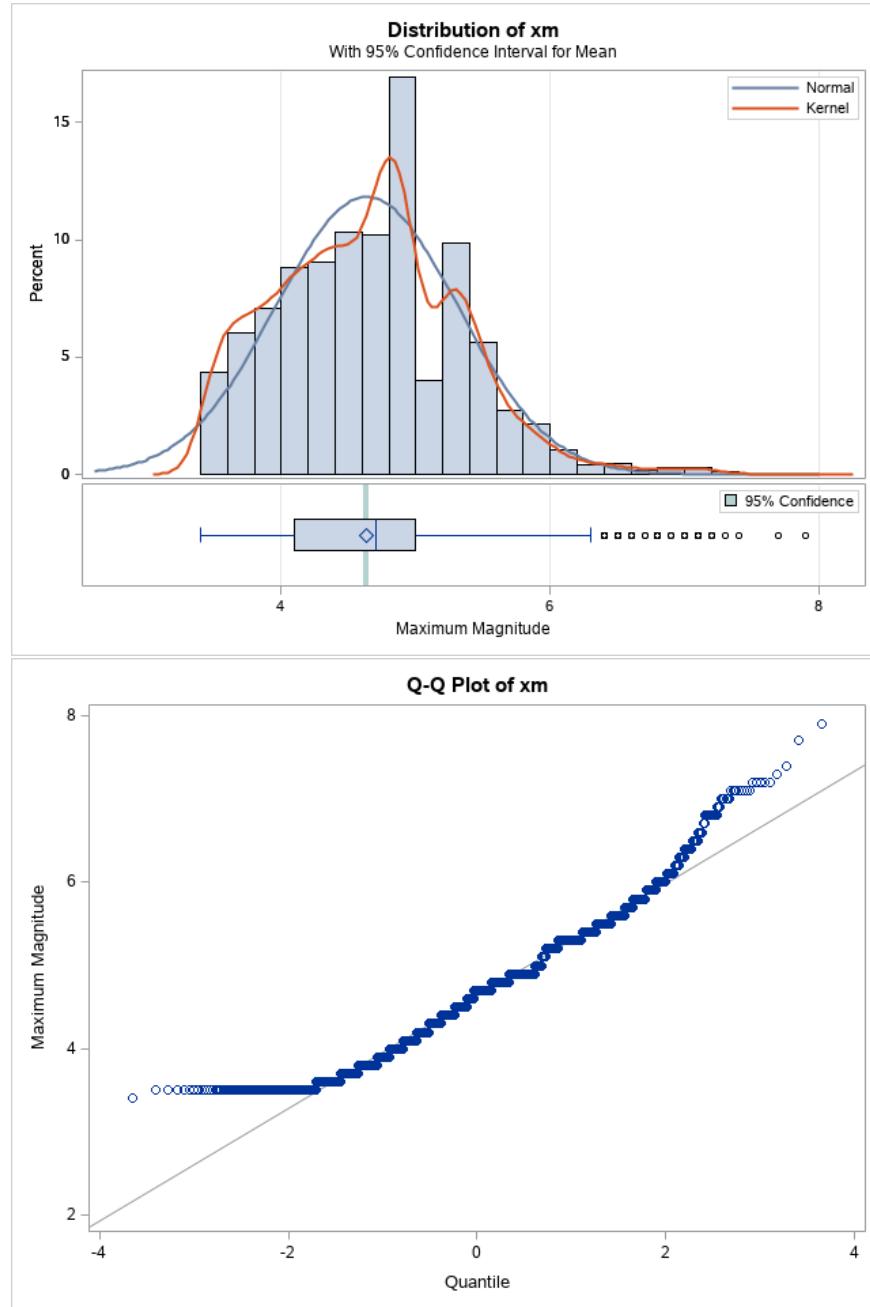




From the above plots and from the correlation matrix we can see variables that seems to correlate with each other. On most of the above plots we can also see a number of points that seems to have no correlation between the two variables of the plot. That might be a mistake of our data or outliers.

Formal Analysis

a. We start by performing a one sample t-test on xm with Null hypothesis that $xm=4.1$



Before we proceed with the t-test we make the following assumptions.

1. Observations are independent
2. X_m follows a normal distribution.

As we can see from the plots in the previous page xm seems to follow a normal distribution so our assumption about independence are true based on our observations.

One sample t-test. Is xm different to 4.1?

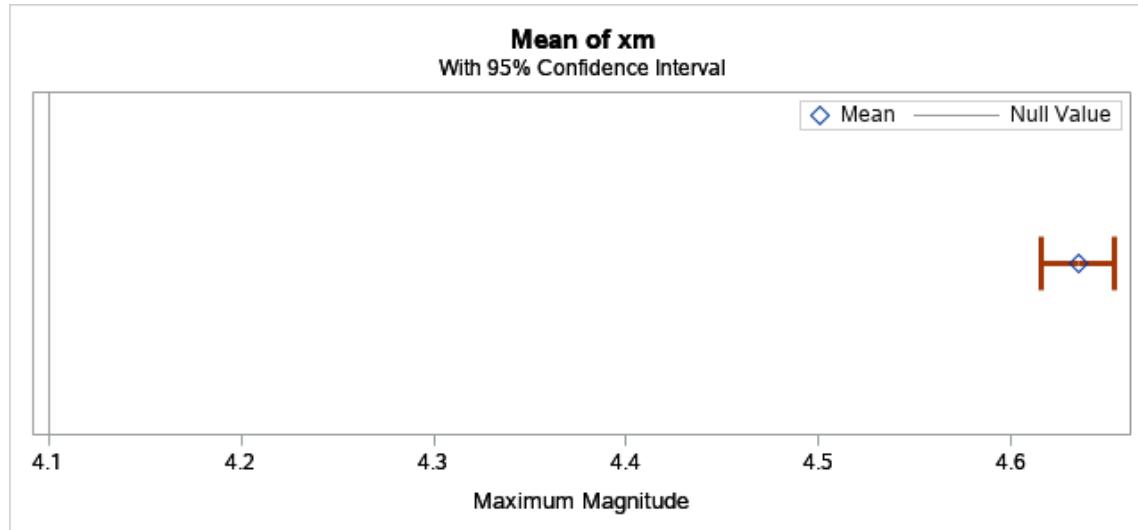
The TTEST Procedure

Variable: xm (Maximum Magnitude)

N	Mean	Std Dev	Std Err	Minimum	Maximum
4950	4.6349	0.6750	0.00959	3.4000	7.9000
Mean	95% CL Mean	Std Dev		95% CL Std Dev	
4.6349	4.6161	4.6537	0.6750	0.6619	0.6885
DF		t Value		Pr > t	
4949		55.76		<.0001	

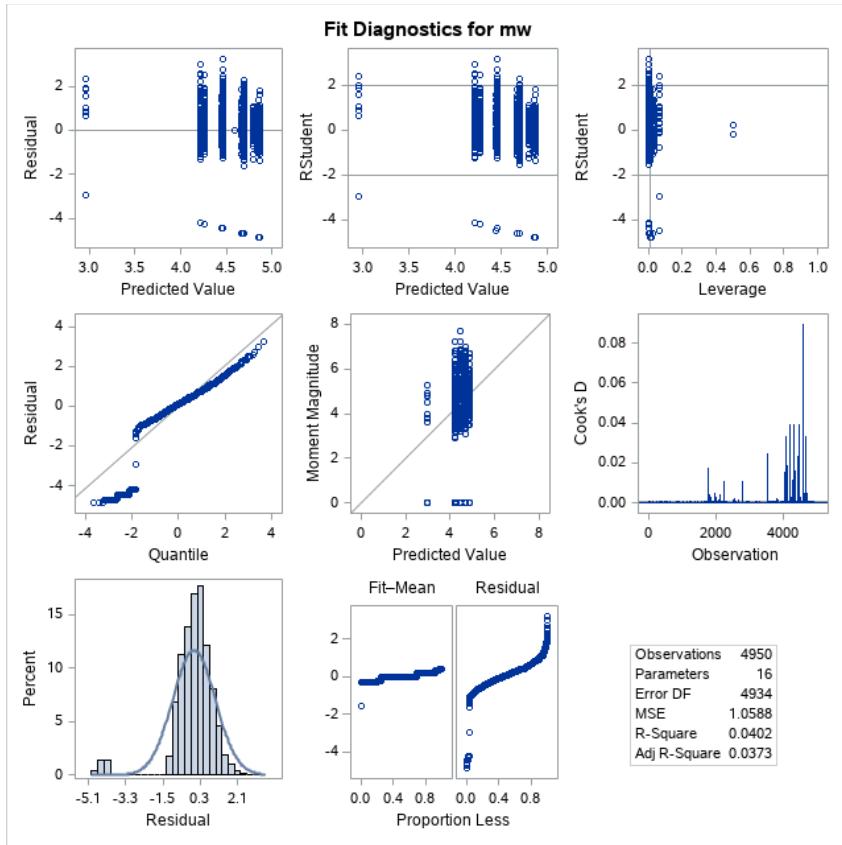
As we can see from the previous table we can reject H_0 hypothesis that xm average is 4.1.

We can also see that from the 95% confidence interval.



b.In order to find if there is a difference in the average moment magnitude scale value of an earthquake between countries we can apply an anova.

First we check our assumptions



Based on the plots on the previous page we can see that the distribution is a normal distribution and the Q-Q plot lie on a diagonal line although it has some outliers.

Applying one way ANOVA on our data we have.

One Way ANOVA with Country as explanatory

The GLM Procedure

Class Level Information		
Class	Levels	Values
country	16	aegean_sea albania azerbaijan blacksea bulgaria egypt georgia greece iran iraq macedonia mediterranean romania russia syria turkey

One Way ANOVA with Country as explanatory

The GLM Procedure

Dependent Variable: mw Moment Magnitude

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	15	218.931125	14.595408	13.78	<.0001
Error	4934	5224.339784	1.058845		
Corrected Total	4949	5443.270909			
R-Square		Coeff Var		Root MSE	mw Mean
0.040221		22.98123		1.029002	4.477576
Source	DF	Type I SS	Mean Square	F Value	Pr > F
country	15	218.9311248	14.5954083	13.78	<.0001
Source	DF	Type III SS	Mean Square	F Value	Pr > F
country	15	218.9311248	14.5954083	13.78	<.0001

From the tables and with significance level 5% there is enough evidence to reject our null hypothesis that across different countries mw is equal.

c. Next, we try to fit a regression with Richter as a response and all the other variables as potential explanatory variables (excluding id and xm)

The GLMSELECT Procedure

Forward Selection Summary					
Step	Effect Entered	Number Effects In	NumberParms In	AIC	SBC
* Optimal Value of Criterion					
0	Intercept	1	1	1315.9747	-411.5689
1	mw	2	2	850.2743	-871.8128
2	ms	3	3	814.5323	-902.0983
3	md	4	4	731.2843	-979.8898
4	lat	5	5	723.9075	-981.8102
5	long	6	6	717.7797*	-982.4816*

The selected model is the model at the last step (Step 5).

Effects:	Intercept lat long md mw ms
Root MSE	0.74455
Dependent Mean	4.41236
R-Square	0.2963
Adj R-Sq	0.2942
AIC	717.77967
AICC	717.84468
SBC	-982.48160

Parameter Estimates				
Parameter	DF	Estimate	Standard Error	t Value
Intercept	1	0.587929	0.574883	1.02
lat	1	0.042659	0.014445	2.95
long	1	0.009208	0.003232	2.85
md	1	-0.244064	0.025751	-9.48
mw	1	0.369401	0.025703	14.37
ms	1	0.295062	0.026465	11.15

$$\text{Richter} = 0.587929 + 0.042659 * \text{lat} + 0.009208 * \text{long} - 0.244064 * \text{md} + 0.369401 * \text{mw} + 0.295062 * \text{ms}$$

d. An earthquake with Richter over 5 is considered a serious earthquake. We wish to make a regression model with serious as a response variable and with the other variables as potential explanatory variables. (excluding id, mw, richter, xm)

Summary of Forward Selection						
Step	Effect Entered	DF	Number In	Score Chi-Square	Pr > ChiSq	Variable Label
1	ms	1	1	151.1198	<.0001	Surface-wave Magnitude
2	md	1	2	38.7273	<.0001	Magnitude
3	mb	1	3	22.9398	<.0001	Bodywave Magnitude
4	depth	1	4	3.5886	0.0582	Depth (km)
5	long	1	5	3.1335	0.0767	Longitude

Type 3 Analysis of Effects			
Effect	DF	Wald Chi-Square	Pr > ChiSq
long	1	3.1236	0.0772
depth	1	4.2655	0.0389
md	1	26.6632	<.0001
ms	1	66.3388	<.0001
mb	1	31.0878	<.0001

Analysis of Maximum Likelihood Estimates					
Parameter	DF	Estimate	Standard Error	Wald Chi-Square	Pr > ChiSq
Intercept	1	-5.7708	1.5772	13.3879	0.0003
long	1	1.8177	1.0285	3.1236	0.0772
depth	1	-0.00754	0.00365	4.2655	0.0389
md	1	-0.6810	0.1319	26.6632	<.0001
ms	1	3.3795	0.4149	66.3388	<.0001
mb	1	-2.2714	0.4074	31.0878	<.0001

Odds Ratio Estimates			
Effect	Point Estimate	95% Wald Confidence Limits	
long	6.158	0.820	46.222
depth	0.992	0.985	1.000
md	0.506	0.391	0.655
ms	29.355	13.017	66.202
mb	0.103	0.046	0.229

Association of Predicted Probabilities and Observed Responses			
Percent Concordant	84.2	Somers' D	0.684
Percent Discordant	15.8	Gamma	0.684
Percent Tied	0.0	Tau-a	0.198
Pairs	433808	c	0.842

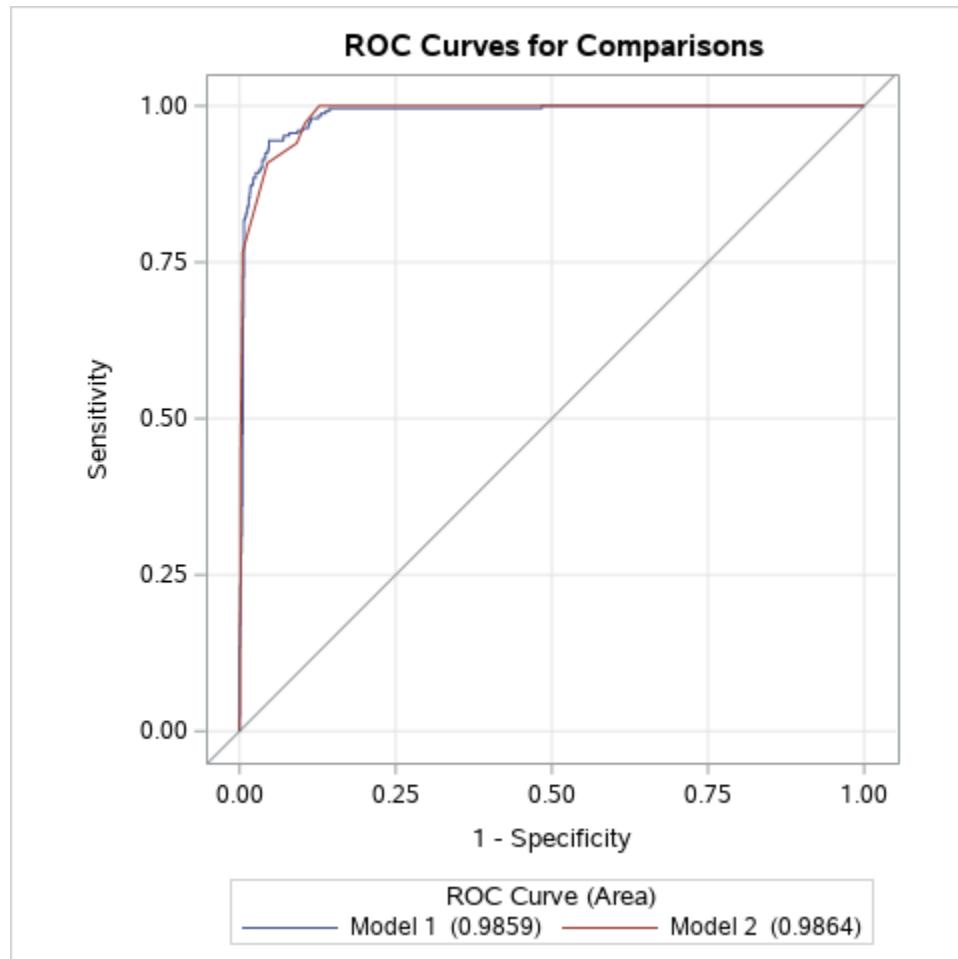
Serious = -5.7708 + 1.8177*long -0.00754*depth -0.6810*md+ 3.3795*ms -2.2714*mb

e. We will fit now a regression with serious as the response and xm as the only explanatory variable and compare our model to the model from objective d.

Parameter Estimates and Wald Confidence Intervals			
Parameter	Estimate	95% Confidence Limits	
Intercept	-53.3001	-57.9254	-48.6748
xm	10.0719	9.1945	10.9494

$$\text{Serious} = -53.3001 + 10.0719 \cdot xm$$

In order to compare the two models from "d" and "e" we start by dividing our dataset to separate training and test sets.



ROC Association Statistics						
ROC Model	Mann-Whitney			Somers' D	Gamma	Tau-a
	Area	Standard Error	95% Wald Confidence Limits			
Model 1	0.9859	0.00298	0.9801 0.9918	0.9719	0.9719	0.2742
Model 2	0.9864	0.00231	0.9818 0.9909	0.9727	0.9814	0.2745

ROC Contrast Test Results			
Contrast	DF	Chi-Square	Pr > ChiSq
Comparing Models	1	0.0322	0.8576

From the plot we can see that the two models are almost the same. As we can see from the last table the null hypothesis that the curves are the same is not rejected. Hence, we don't have evidence that Model 1 (model with multiple variables) is better than Model 2. So, we prefer model 2 as our model since its simpler.

Conclusions

Earthquakes are devastating events that often cause structural damage and loss of lives. Being able to predict the characteristics of earthquakes would be helpful in order to minimize the damage. In this report we rejected the assumption that the average maximum value of earthquakes parameters is 4.1 and we also found that earthquakes magnitude differs between countries. We proceeded with trying to find a model for the intensity of the earthquakes. Our model tried to predict Richter based on latitude, longitude, Magnitude(md), Moment Magnitude, and Surface-wave Magnitude with low success. ($R_{adj}=0.29$). Finally, we tried to make a model that could predict a serious earthquake (Richter>5). Our first model contained longitude, depth, Magnitude(md), Surface-wave Magnitude, and Bodyweight Magnitude. Our second model was simpler. It contained only the maximum of the earthquake parameters (Magnitude(md), Moment Magnitude, Surface-wave Magnitude, Bodyweight Magnitude, and Richter). Comparing the two models we found them to be almost identical. We decided to keep our second model since it was simpler.