

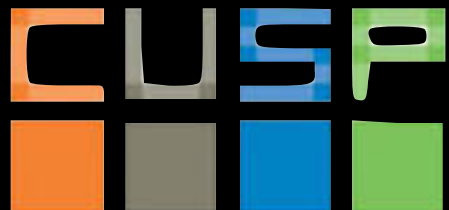
# Urban Informatics

Fall 2017

dr. federica bianco [fbianco@nyu.edu](mailto:fbianco@nyu.edu)

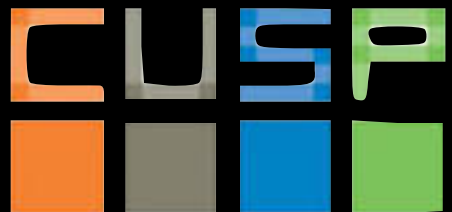


@fedhere



## Recap:

- Good practices with data: falsifiability, reproducibility
- Basic data retrieving and munging: APIs, Data formats
- SQL
- Basic statistics: distributions and their moments
- Hypothesis testing:  $p$ -value, statistical significance
- Statistical and Systematic errors
- Goodness of fit tests
- Likelihood
- OLS
- topics in Geospatial analysis

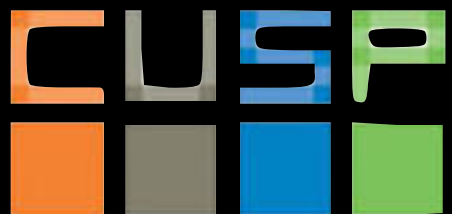


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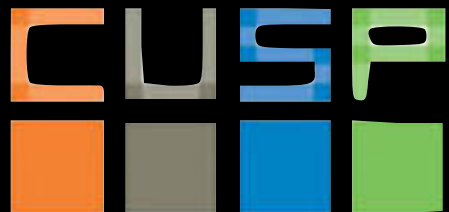
## Today

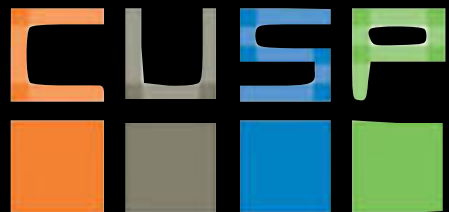
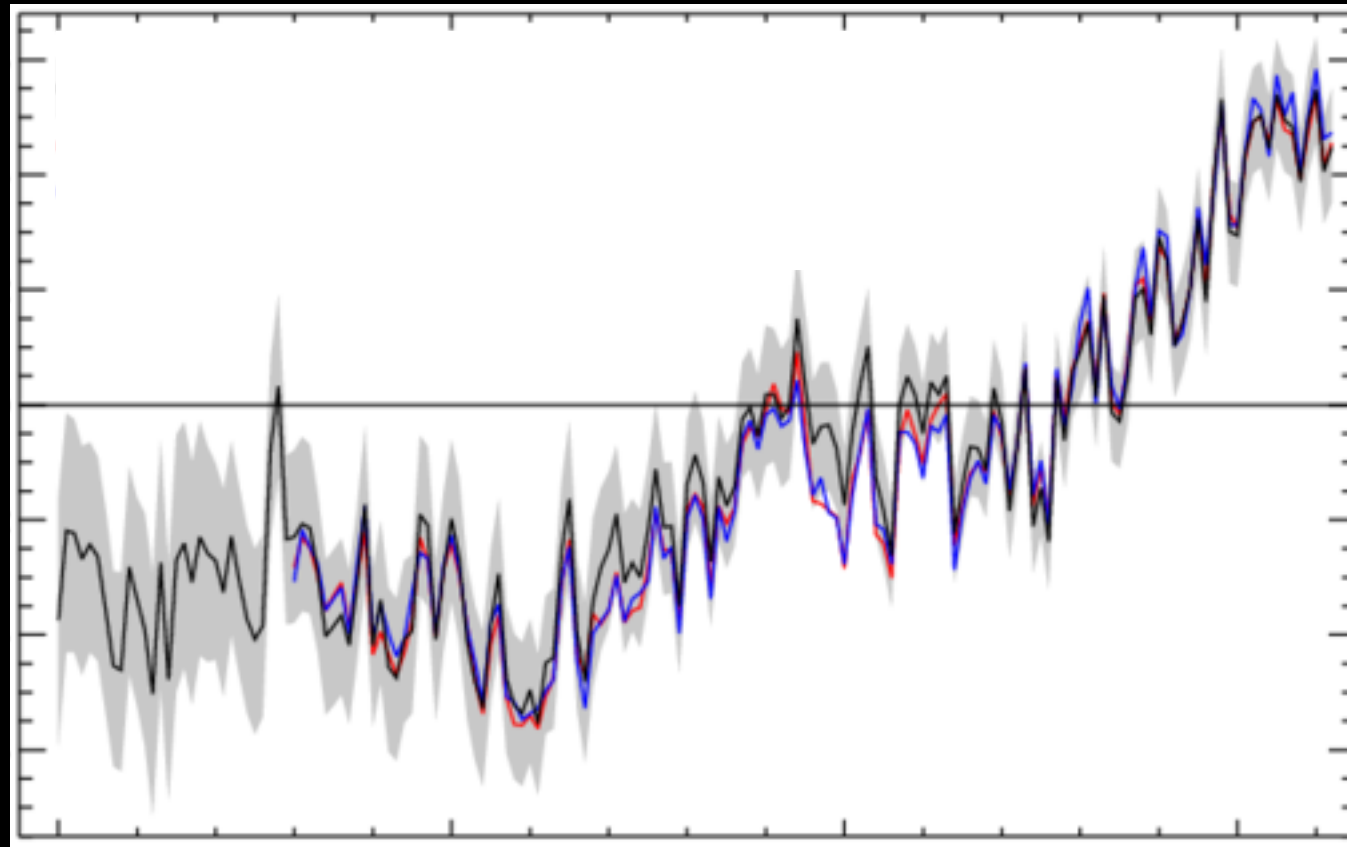
- Topics in (time) series analysis

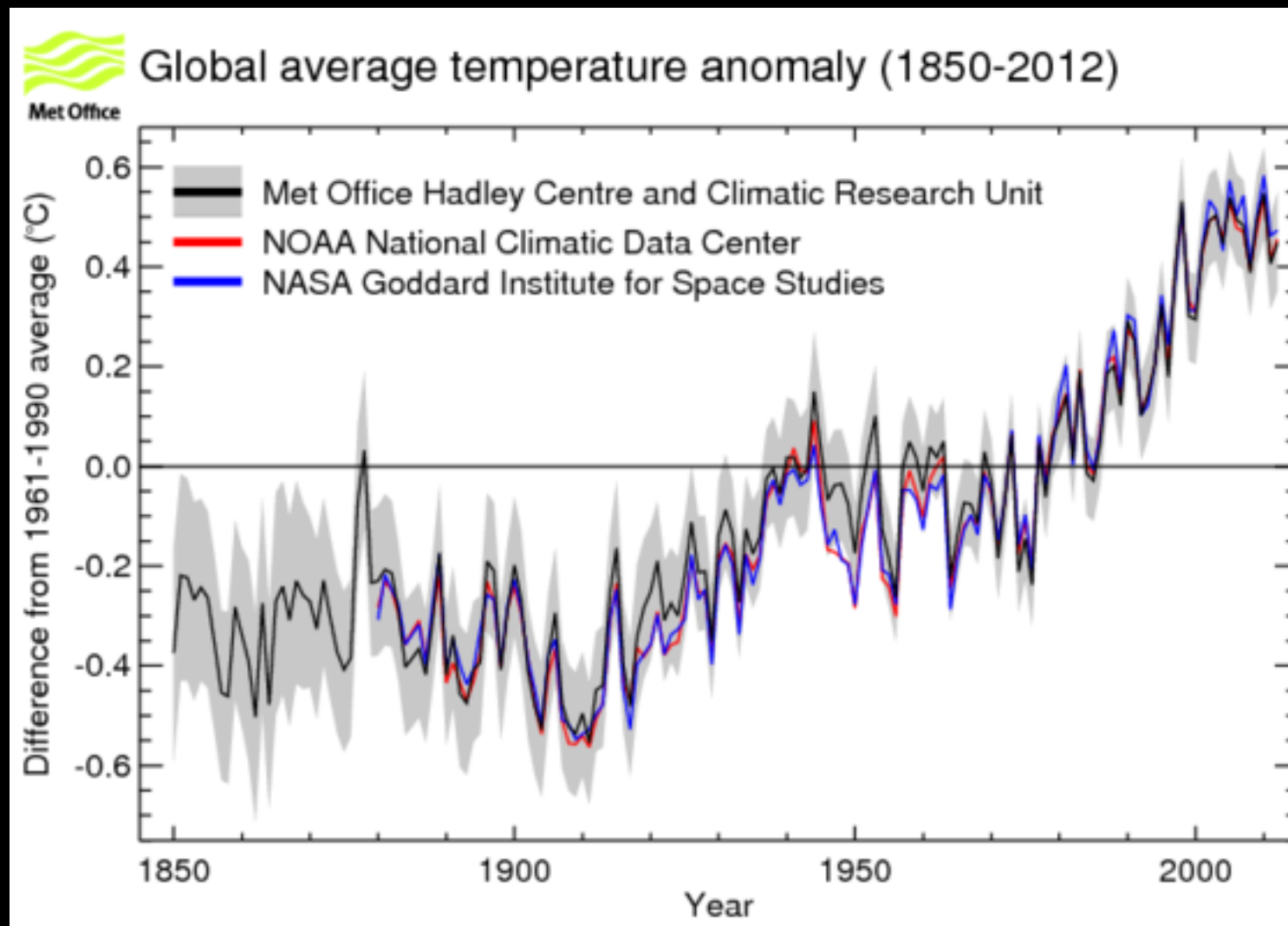


# Topics in (time) series analysis

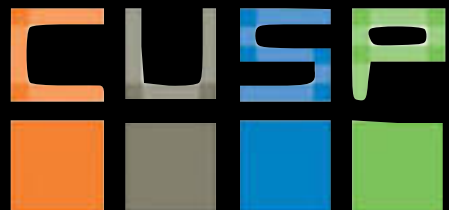
- smoothing
- de-trending
- event detection
- point of change detection
- period finding (Fourier analysis)
- clustering

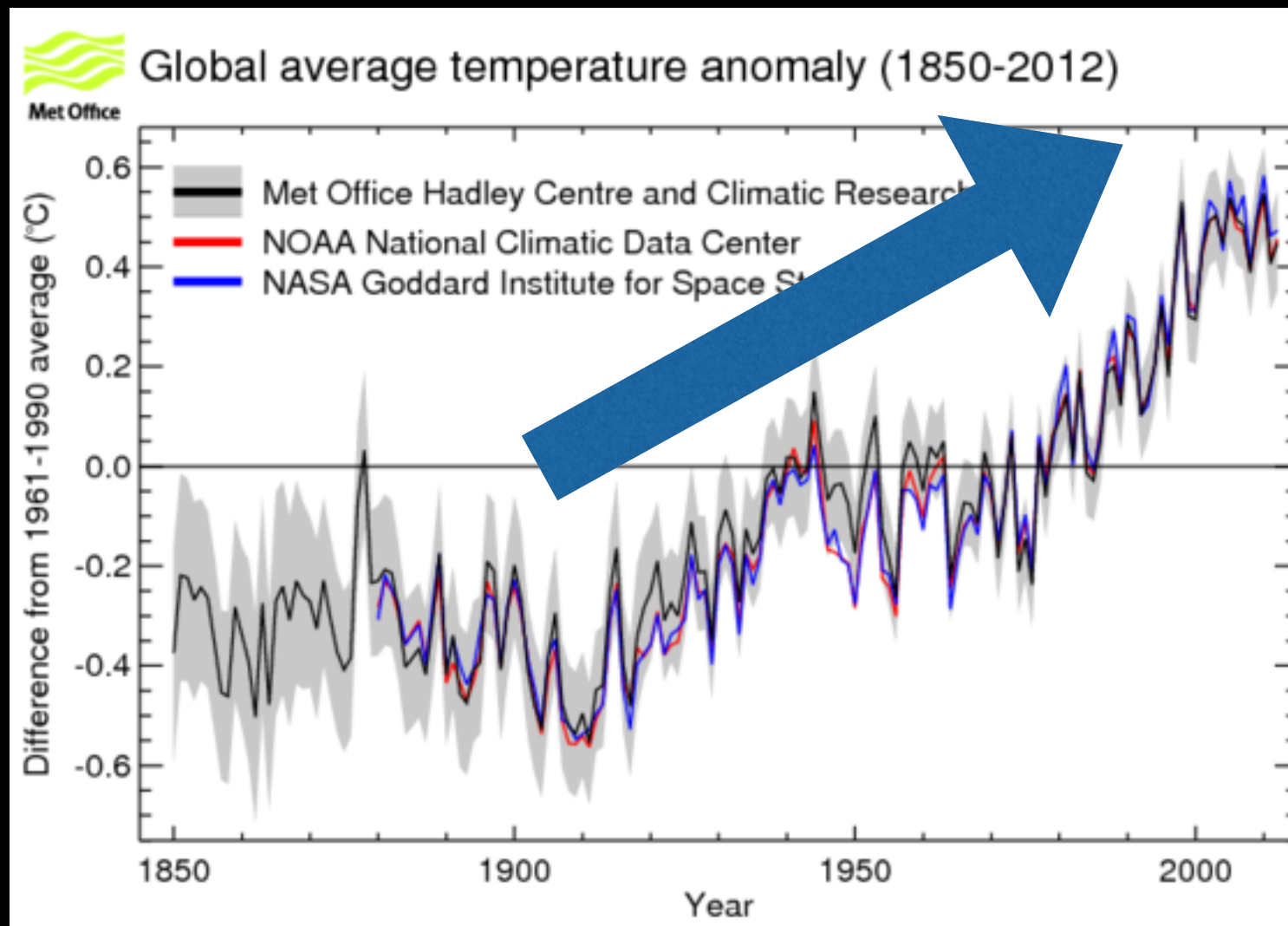




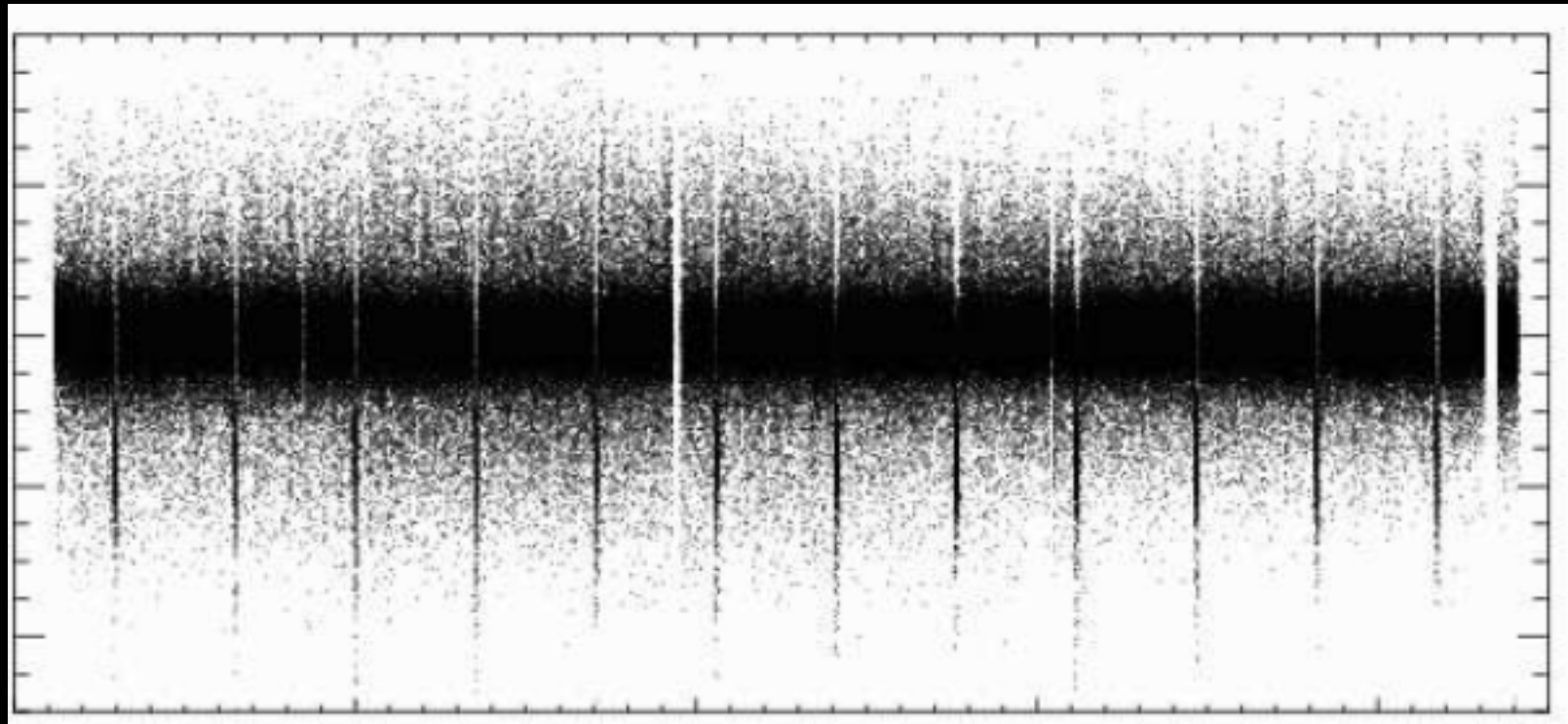


Trend

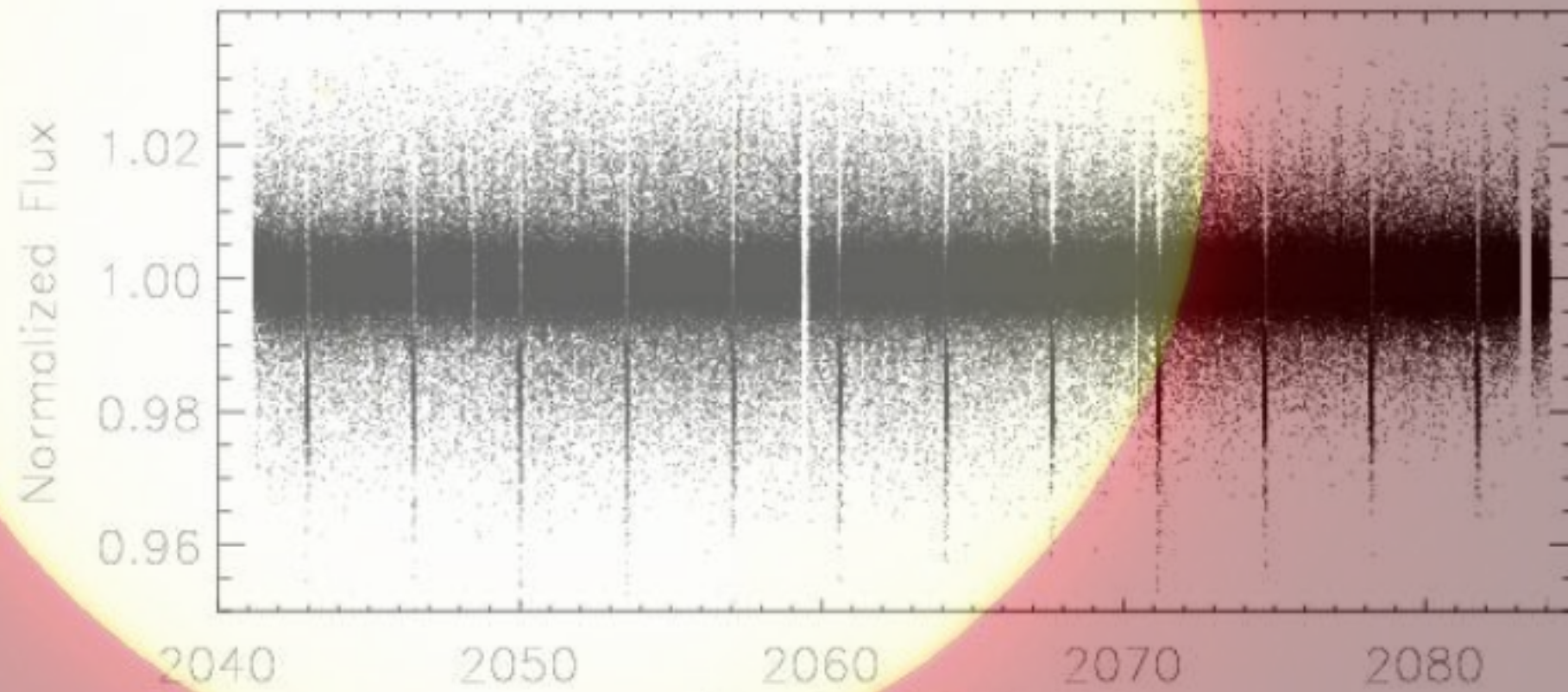




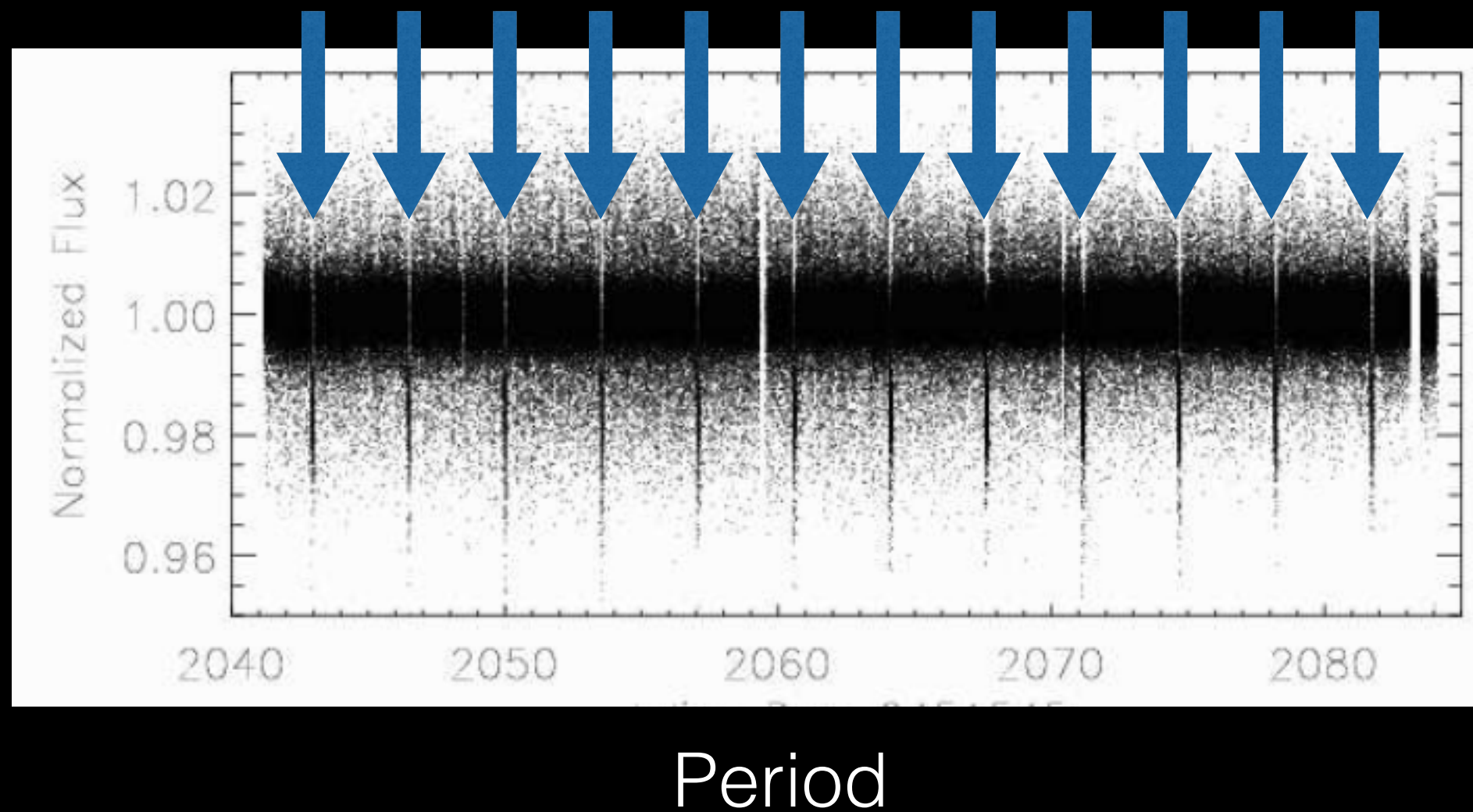
Trend



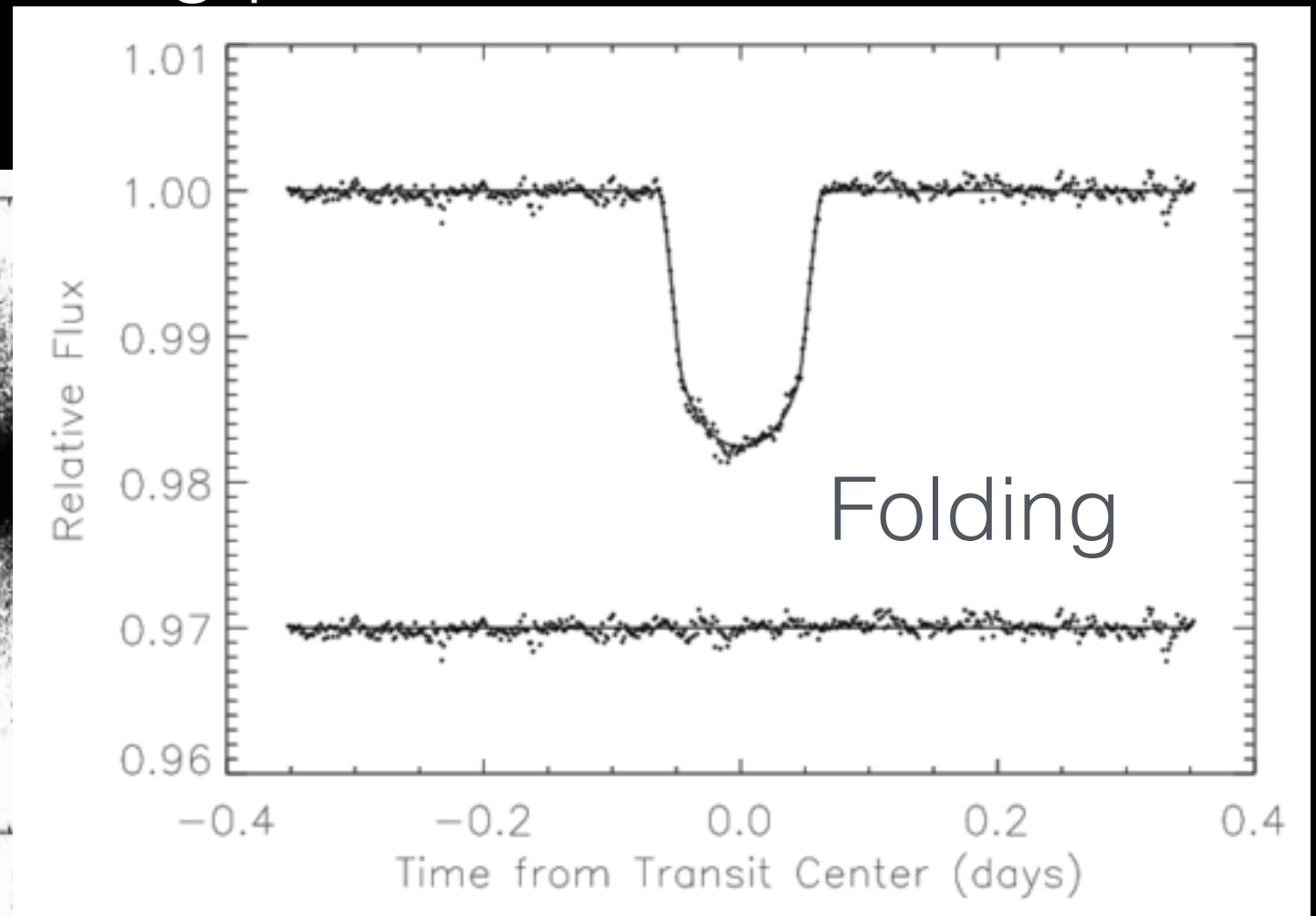
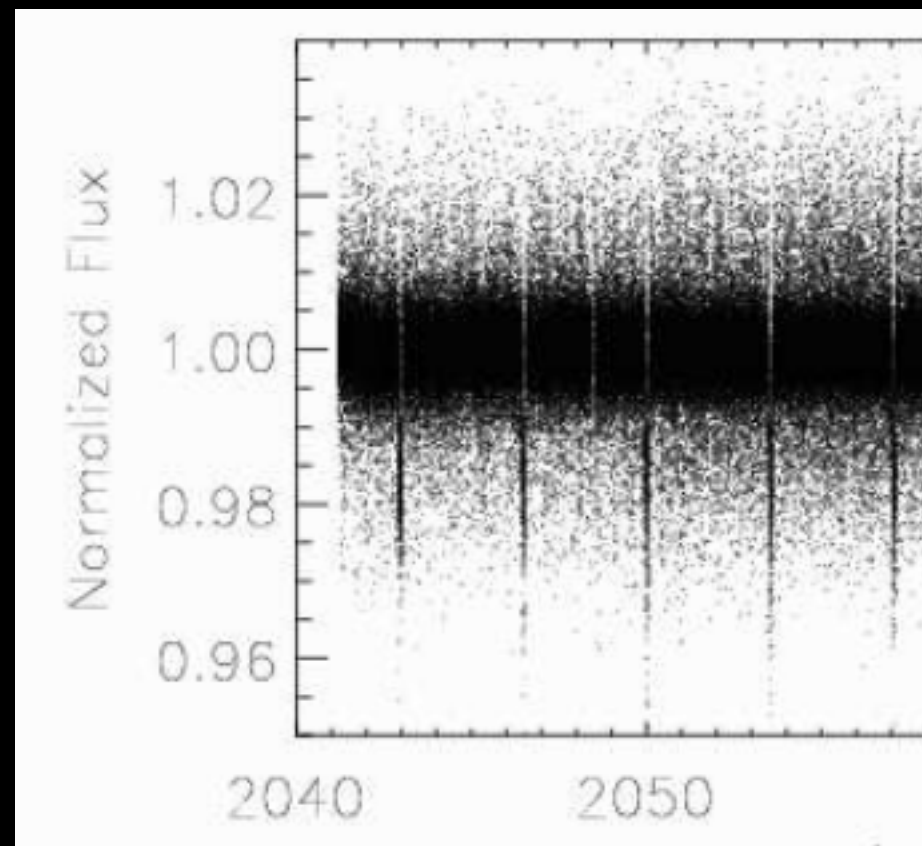




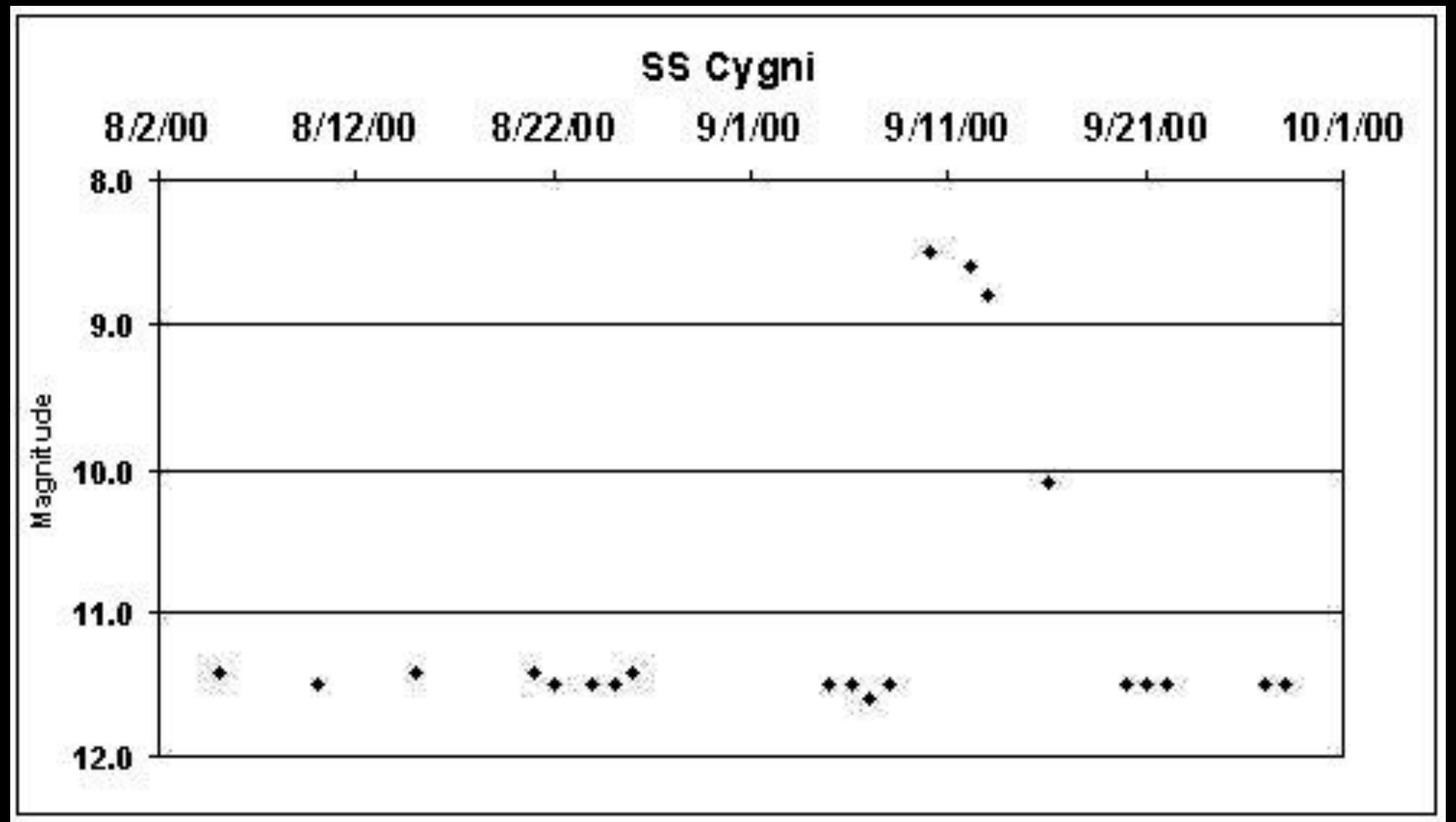
HD 209458, the first transiting planet to be discovered.

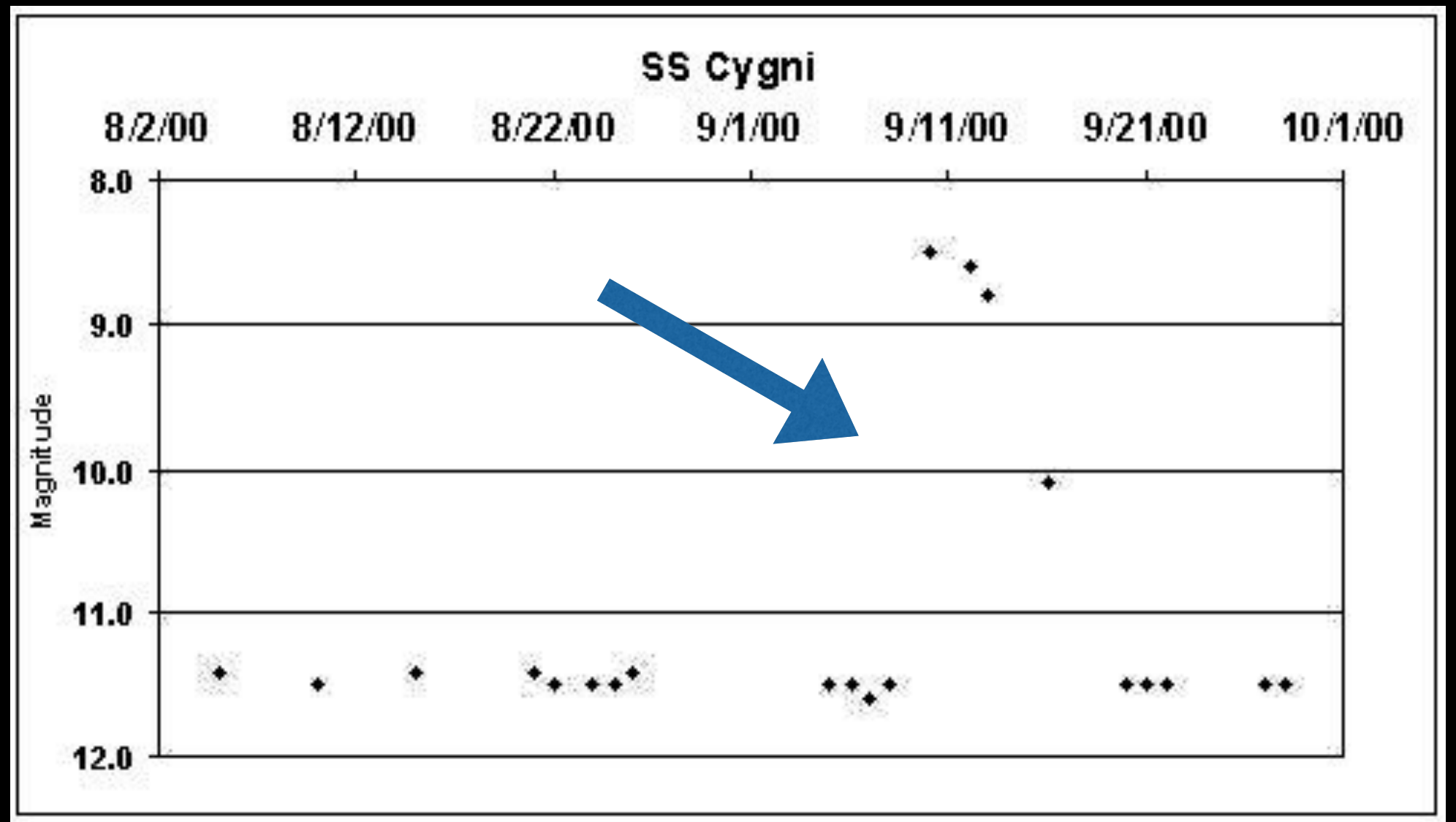


HD 209458, the first transiting planet to be discovered.



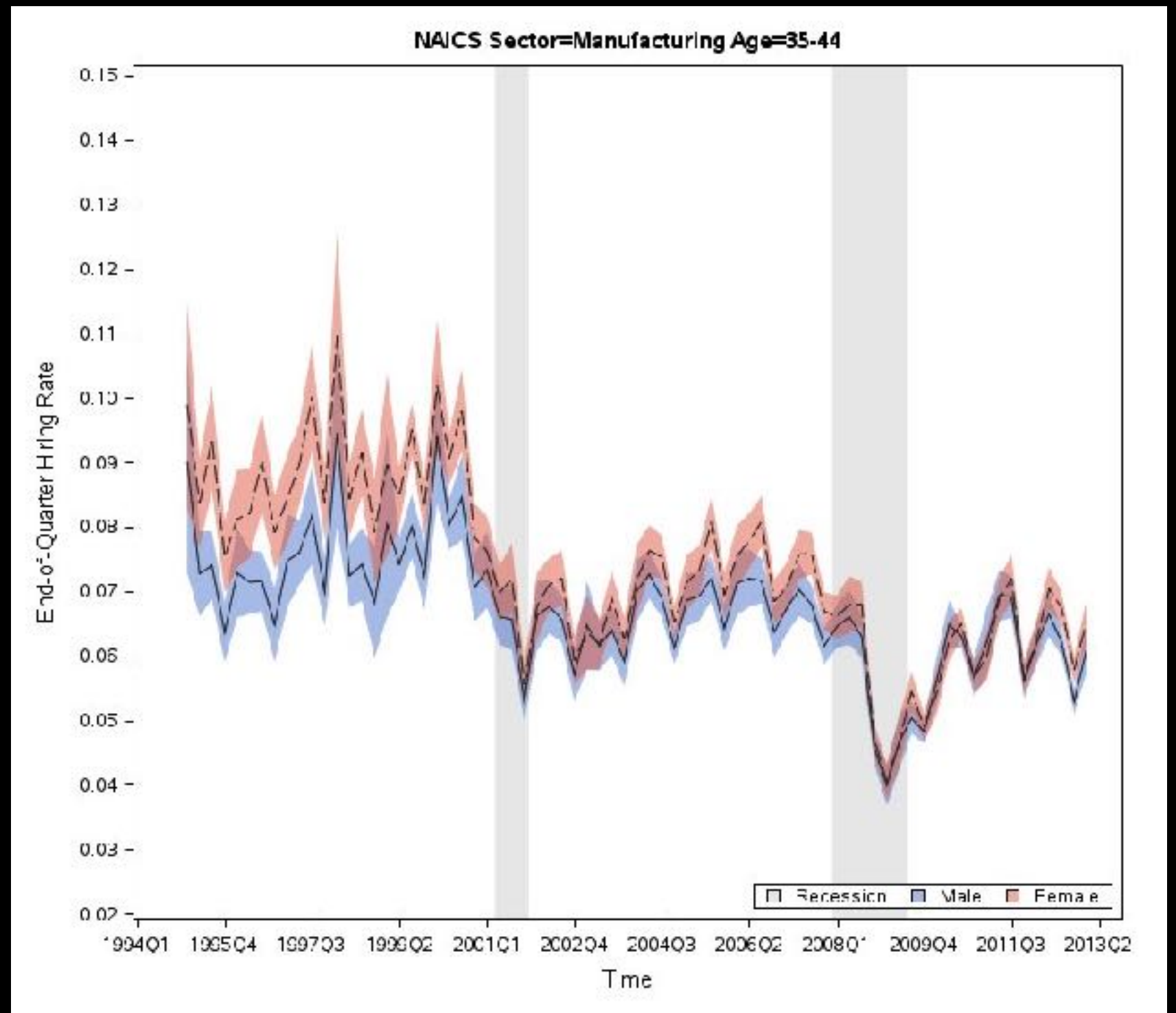
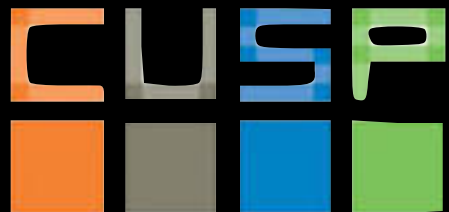
Period

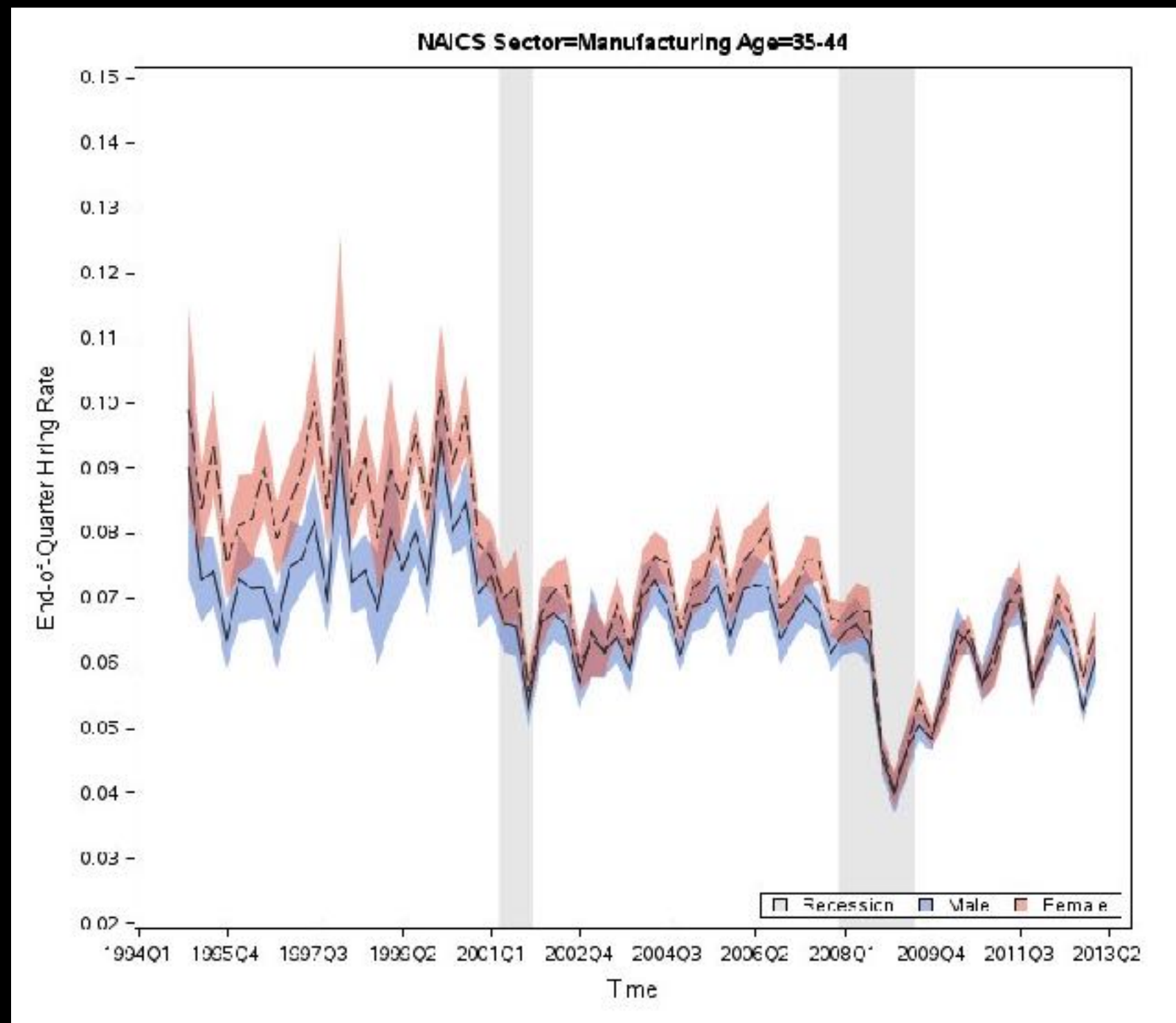
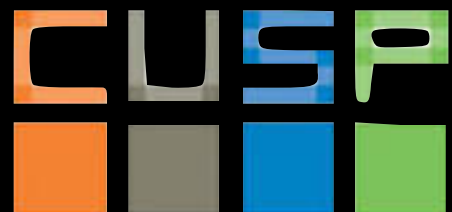




event detection

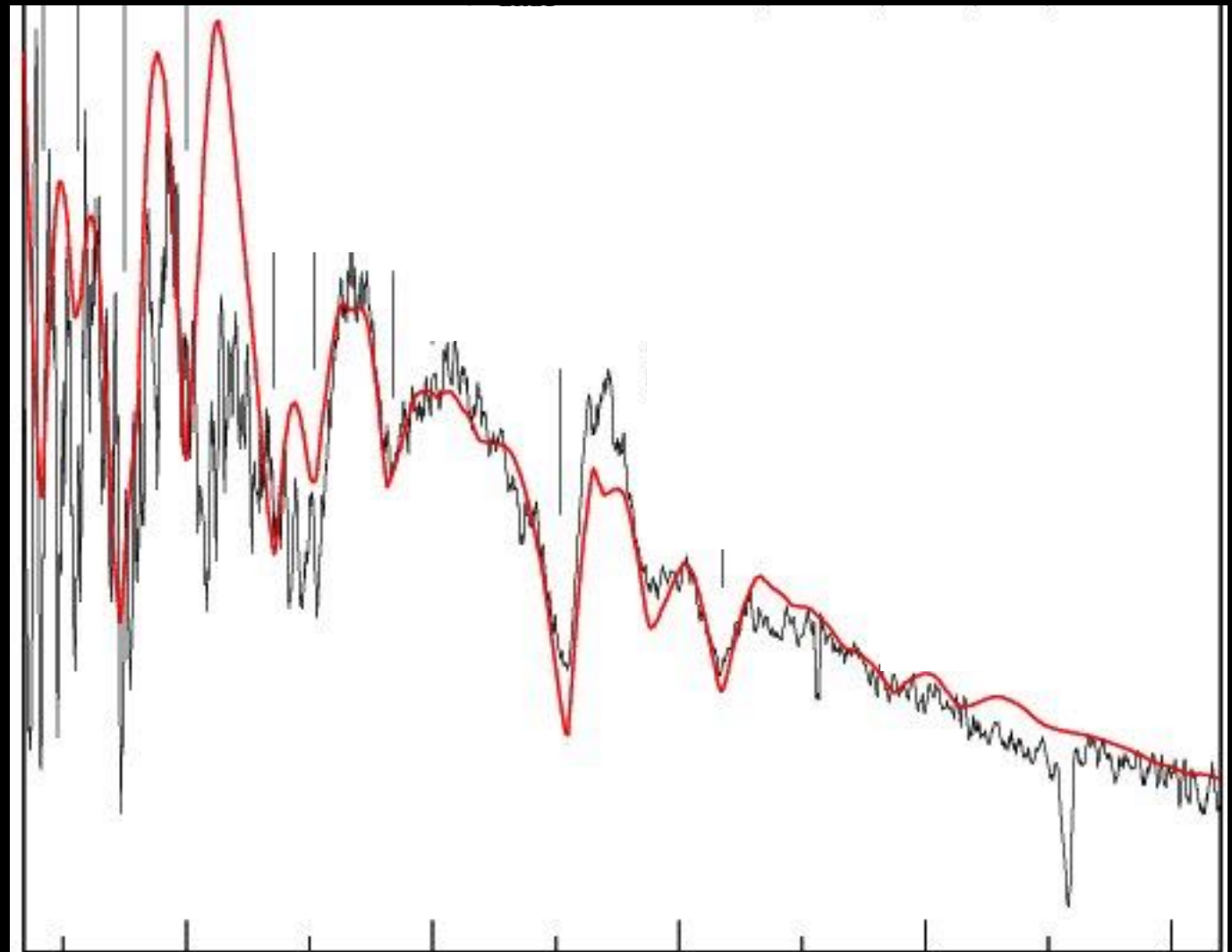






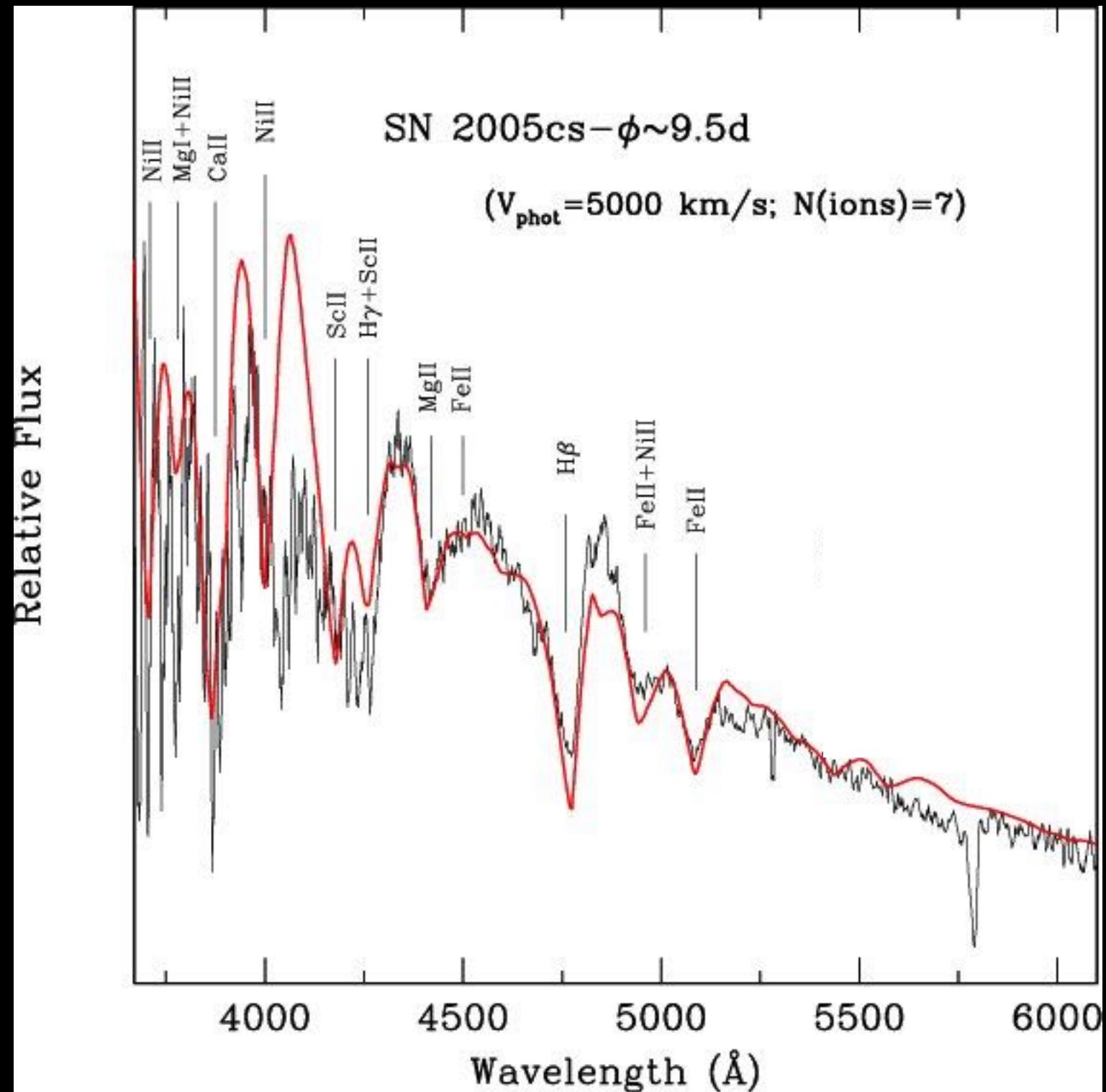
point of change detection

VIII: Topics in Time series

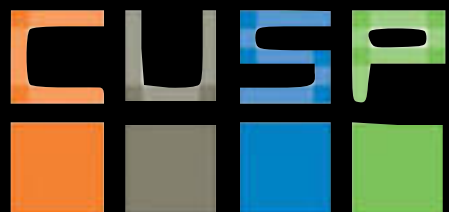
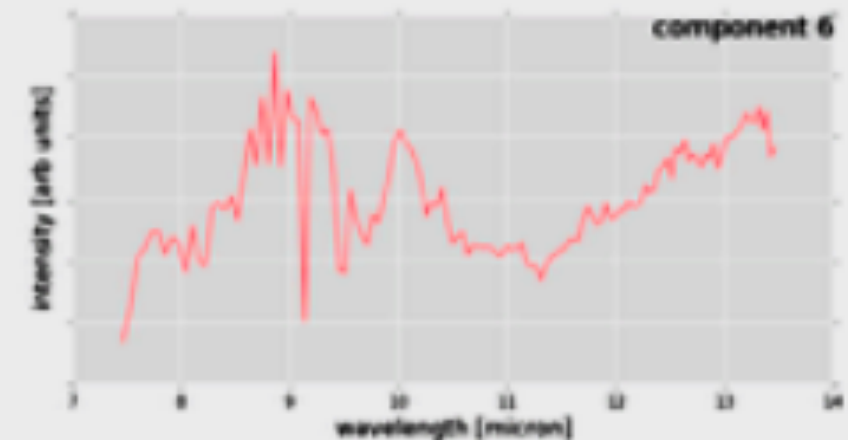
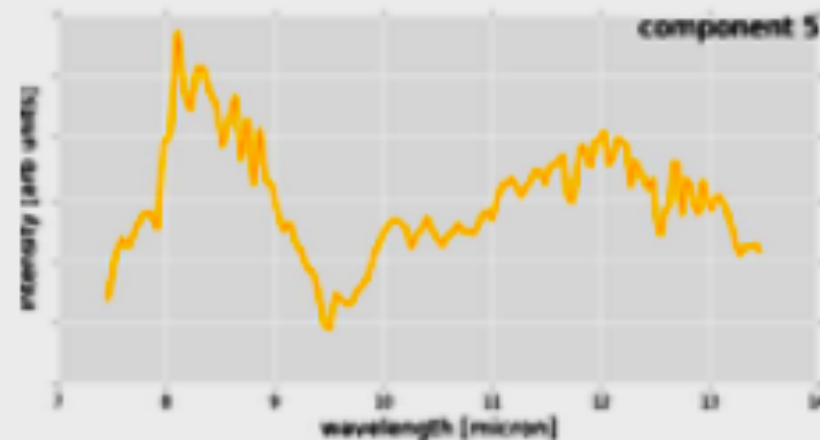
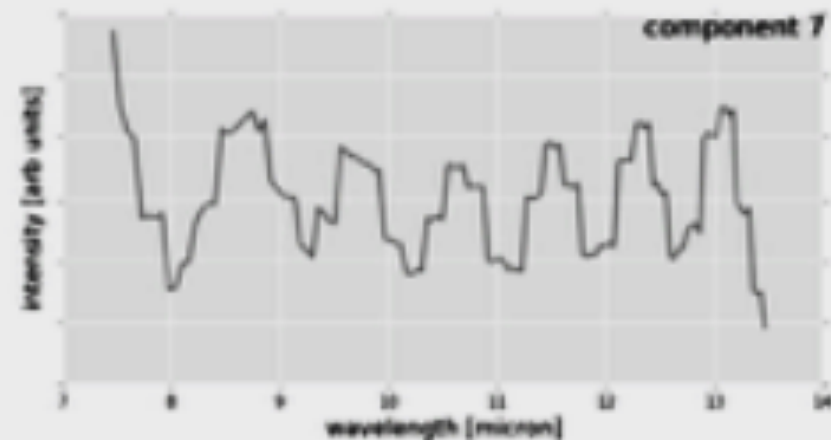
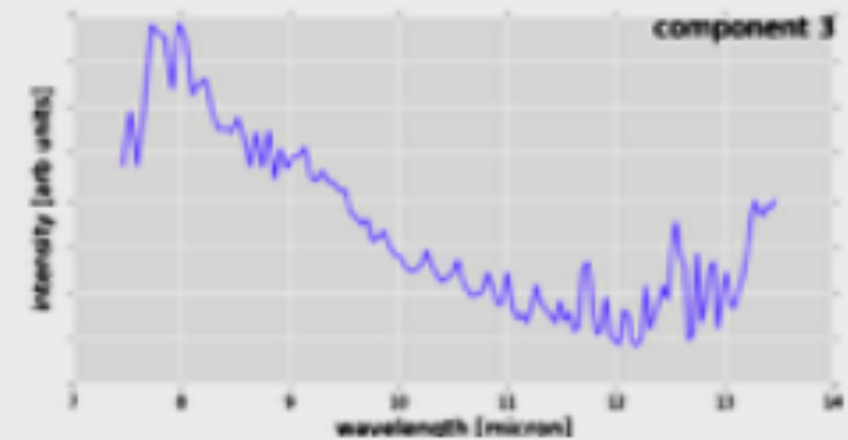
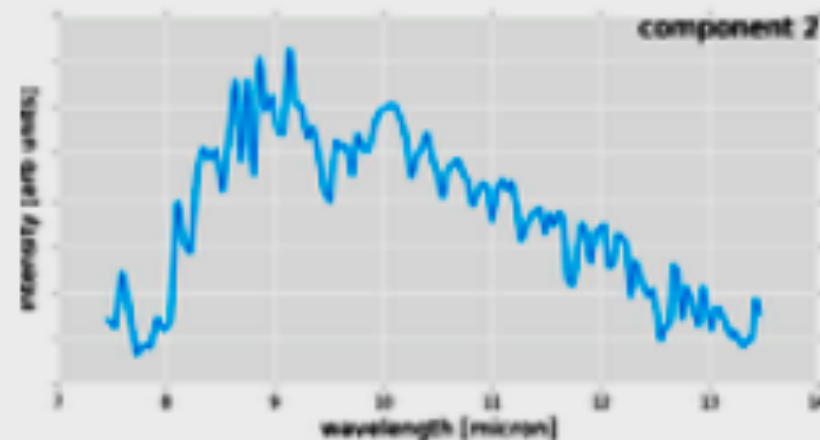
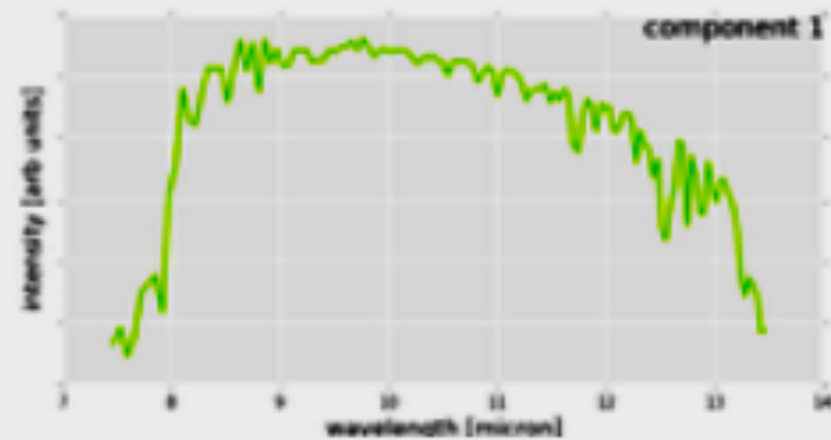




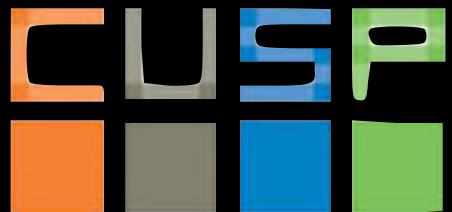
they do not have to be *TIME* series!



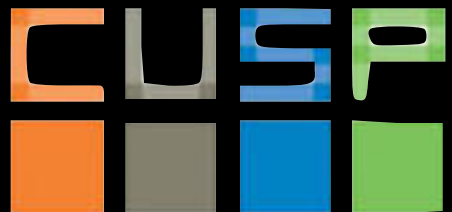
# CUSP-UO spectra of urban lights for light technology assessment



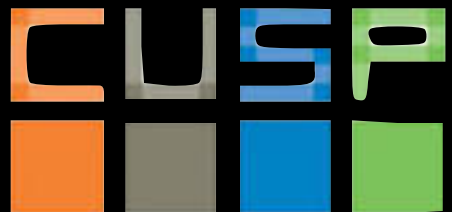
- anomaly detection



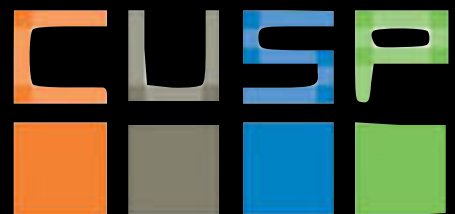
- anomaly detection
- identification of trends



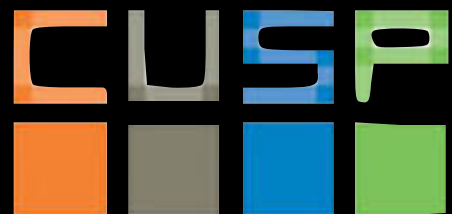
- anomaly detection
- identification of trends
- point of change detection



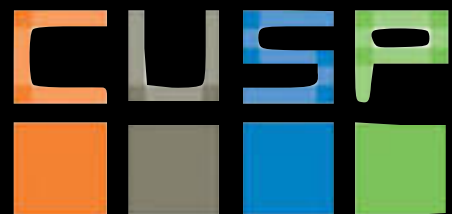
- anomaly detection
- identification of trends
- point of change detection
- prediction



- anomaly detection
- identification of trends
- point of change detection
- prediction
- periodicity detection



- anomaly detection
- identification of trends
- point of change detection
- prediction
- periodicity detection
- classification (clustering)





## *Problem*

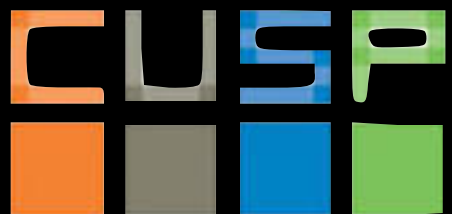
- anomaly (event) detection

## *Method*

**Thresholding**



[https://github.com/fedhere/Ulnotebooks/blob/master/  
timeseries/FSNYdeaths.ipynb](https://github.com/fedhere/Ulnotebooks/blob/master/timeseries/FSNYdeaths.ipynb)



## *Problem*

- anomaly (event) detection

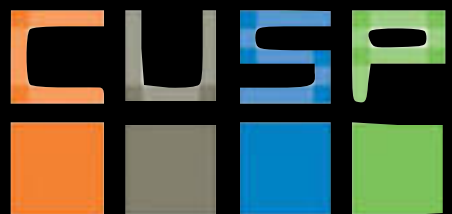
## *Method*

**Thresholding**



- take the mean (possibly a local mean)
- take the standard deviation (possibly a local stdev)
- find points that deviate from the mean by more than  $N$  standard deviation

<https://github.com/fedhere/Ulnotebooks/blob/master/timeseries/FSNYdeaths.ipynb>



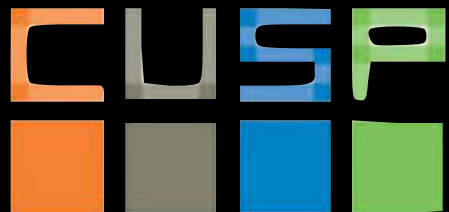
## *Problem*

- anomaly (event) detection
- identification of trends

## *Method*



[https://github.com/fedhere/Ulnotebooks/blob/master//  
timeseries/stationarity.ipynb](https://github.com/fedhere/Ulnotebooks/blob/master/timeseries/stationarity.ipynb)



## *Problem*

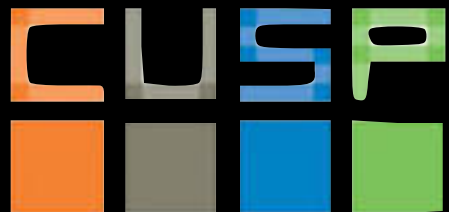
- anomaly (event) detection
- identification of trends

## *Method*

Stationary data  
Smoothing (Rolling mean)  
ADF Fuller test for unit root



[https://github.com/fedhere/Ulnotebooks/blob/master//  
timeseries/stationarity.ipynb](https://github.com/fedhere/Ulnotebooks/blob/master/timeseries/stationarity.ipynb)



## *Problem*

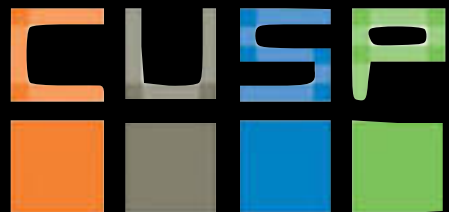
- anomaly (event) detection
- identification of trends
- point of change search

## *Method*

Bayesian  
Point of Change Search



[https://github.com/fedhere/Ulnotebooks/blob/master/  
timeseries/pointOfChange.ipynb](https://github.com/fedhere/Ulnotebooks/blob/master/timeseries/pointOfChange.ipynb)



## *Problem*

- anomaly (event) detection
- identification of trends
- point of change search

## *Method*

Bayesian  
Point of Change Search

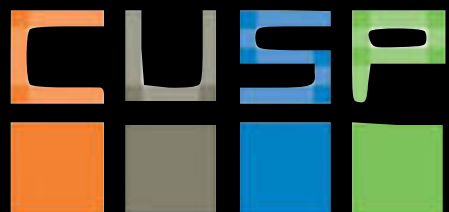


<https://github.com/fedhere/Ulnotebooks/blob/master/timeseries/pointOfChange.ipynb>

<https://www.slideshare.net/FrankKelly3/change-point-detection-with-bayesian-inference>

Adam, MacKay 2007

Rasmussen 2001

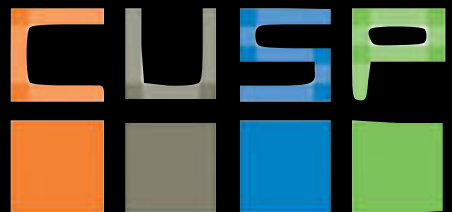


## *Problem*

- anomaly (event) detection
- identification of trends
- point of change search
- periodicity

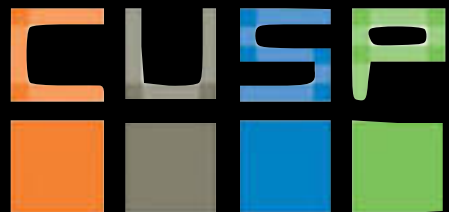
## *Method*

**Fourier Transforms**



## Fourier

$$F(\omega) = \frac{1}{2\pi} \int f(t) e^{-i\omega t} dt$$

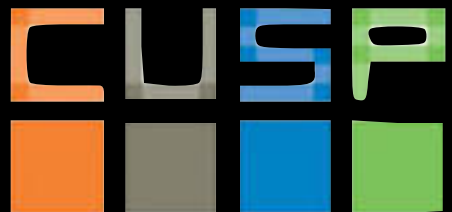




## Fourier

$$F(\omega) = \frac{1}{2\pi} \int f(t) e^{-i\omega t} dt$$


takes a function in time domain



## Fourier

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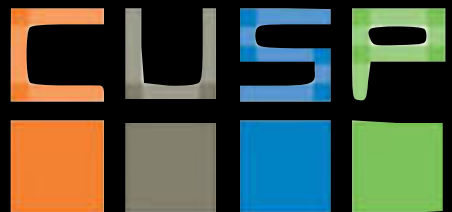
takes a function in time domain  
to a function in frequency domain



## Fourier

$$F(\omega) = \frac{1}{2\pi} \int f(t) e^{-i\omega t} dt$$

takes a function in space domain  
to a function in spatial frequency domain

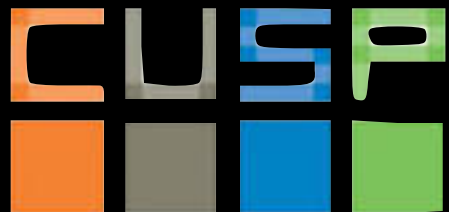


## Fourier

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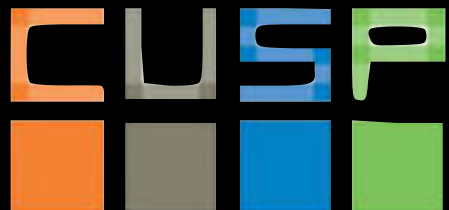
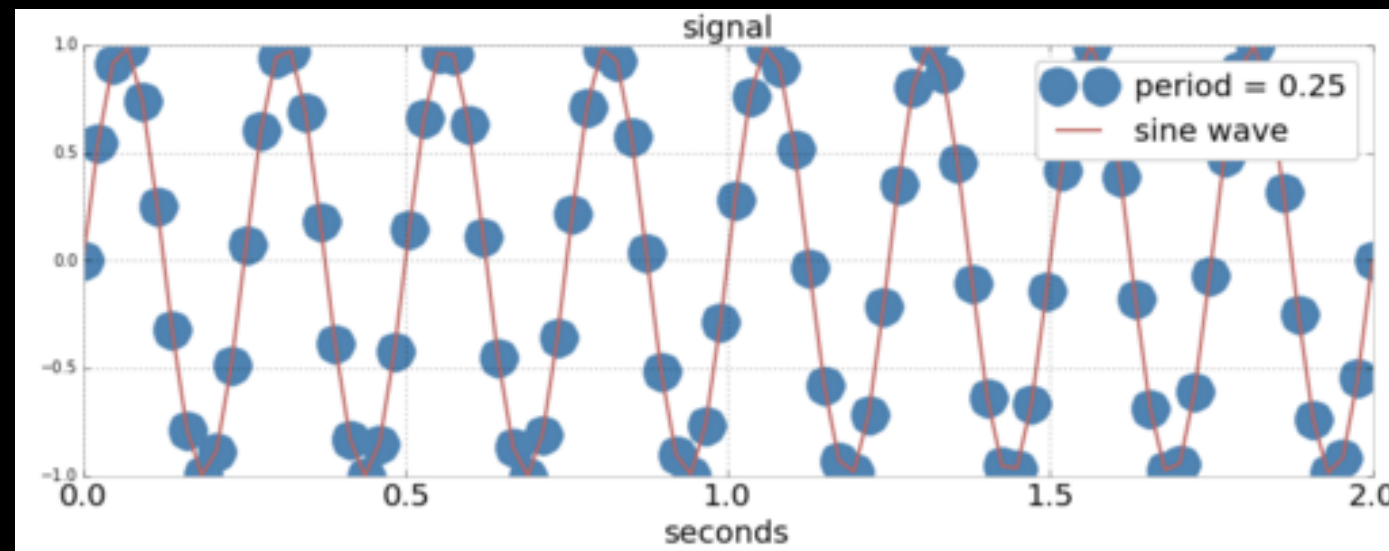
takes a function in time domain  
 $f(t)$  is measured in seconds

to a function in frequency domain  
 $f(t)$  is measured in 1/seconds  
or Hz



a time series

## Fourier

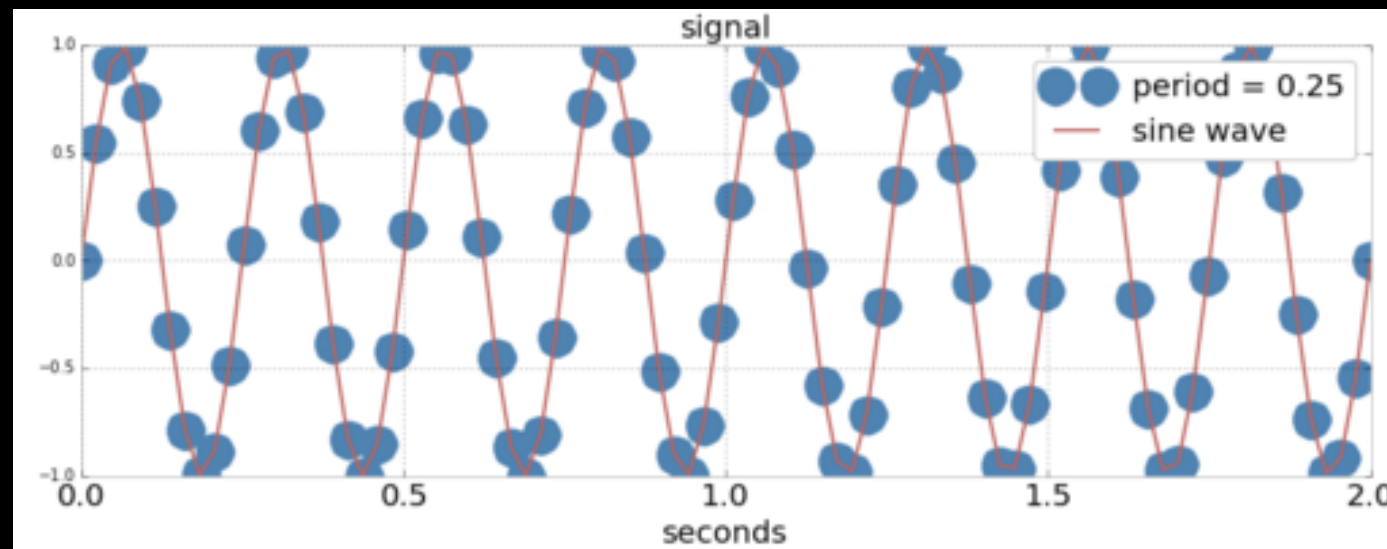


The square of the real part of the Fourier transform  
this is called a Power spectrum.

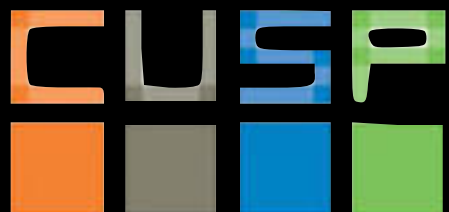
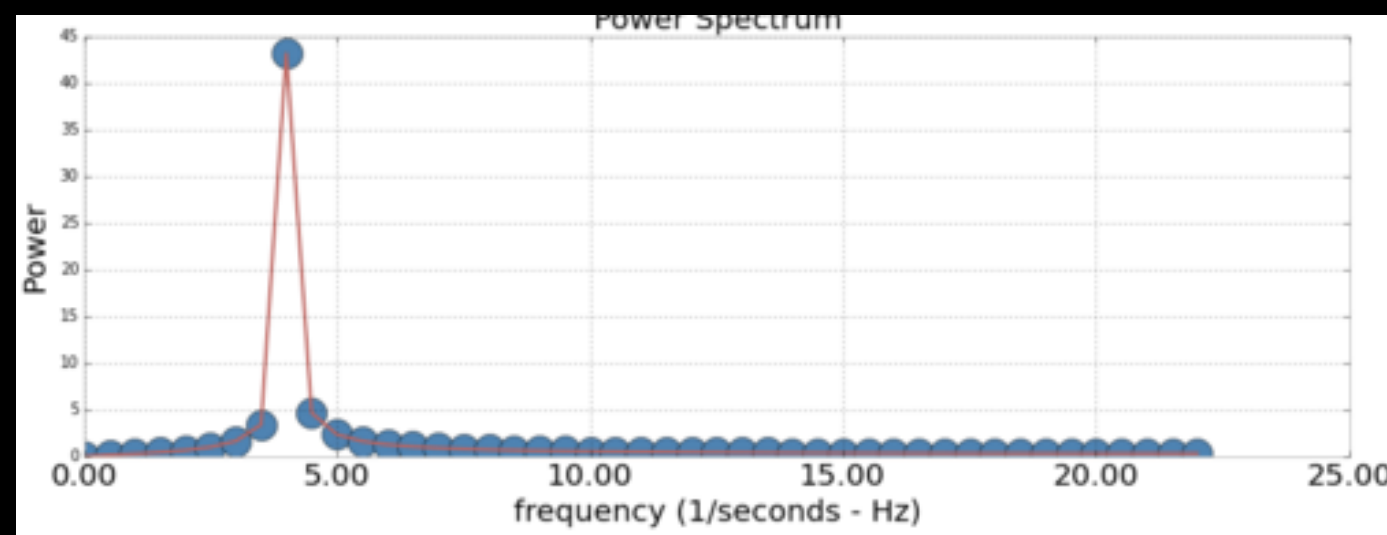
High value of the power spectrum indicate periodicity at the  
corresponding frequency

## Fourier

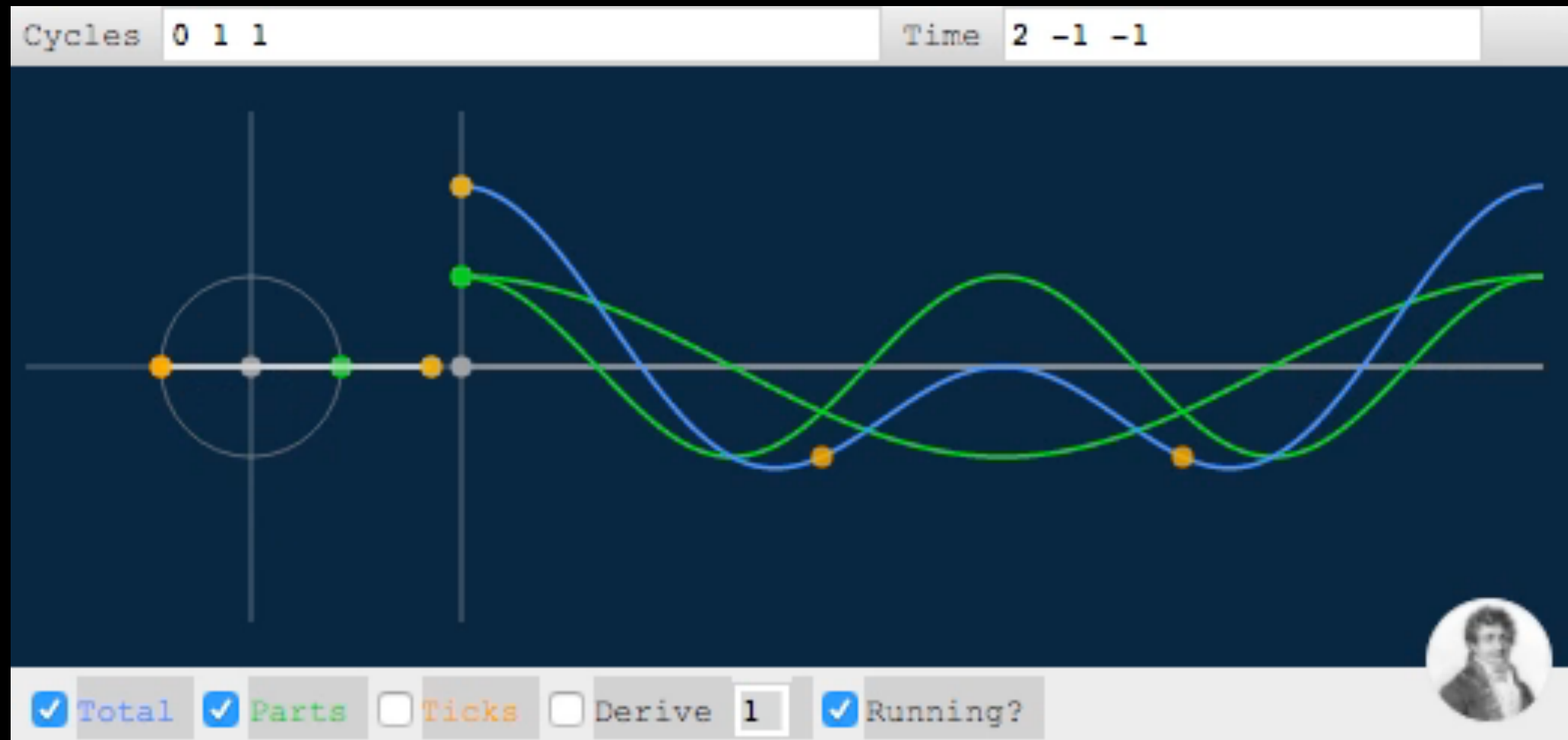
a time series



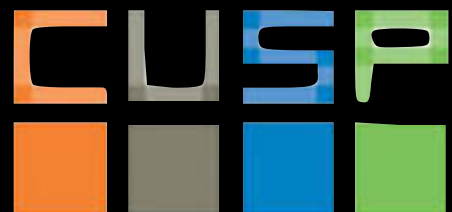
its power  
spectrum



# Cosine and Sine... just in case



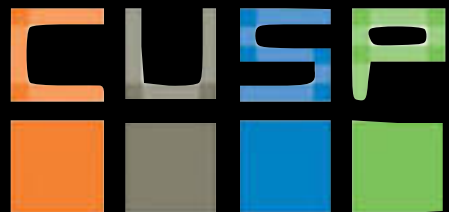
<http://www.businessinsider.com/7-gifs-trigonometry-sine-cosine-2013-5>



Fourier



[https://github.com/fedhere/Ulnotebooks/blob/master/  
timeseries/fourier.ipynb](https://github.com/fedhere/Ulnotebooks/blob/master/timeseries/fourier.ipynb)





## *Problem*

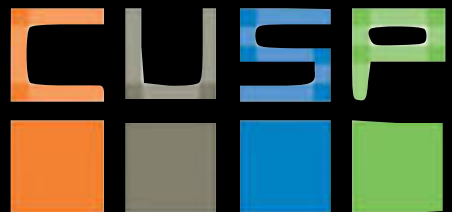
- event detection
- identification of trends
- periodicity
- prediction

## *Method*

**ARMA/ARIMA**



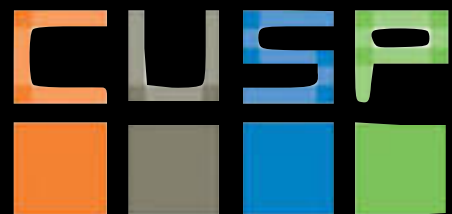
<http://www.econ.ohio-state.edu/dejong/note2.pdf>



# ARIMA

Autoregression

$$x(t) = a_1 x(t-1) + \epsilon_t$$

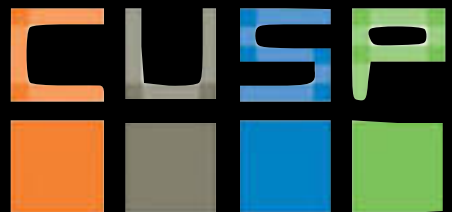


# ARIMA

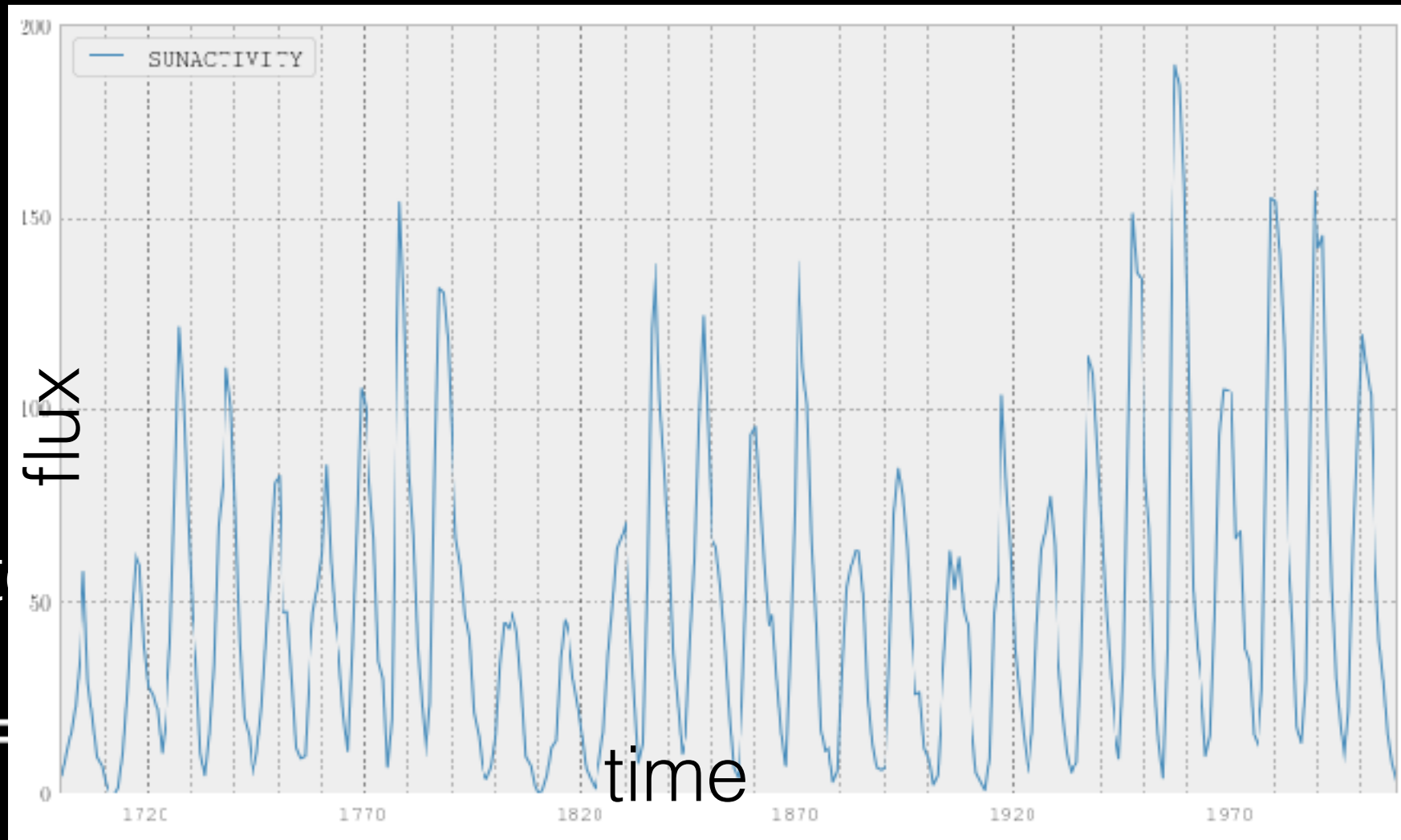
Autoregression

$$x(t) = a_1 x(t-1) + \epsilon_t$$

$$x(t) = a_1 x(t-1) + a_2 x(t-2) + \dots + a_n x(t-n) + \epsilon_t$$



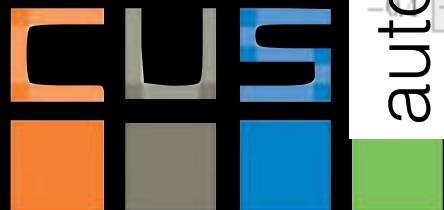
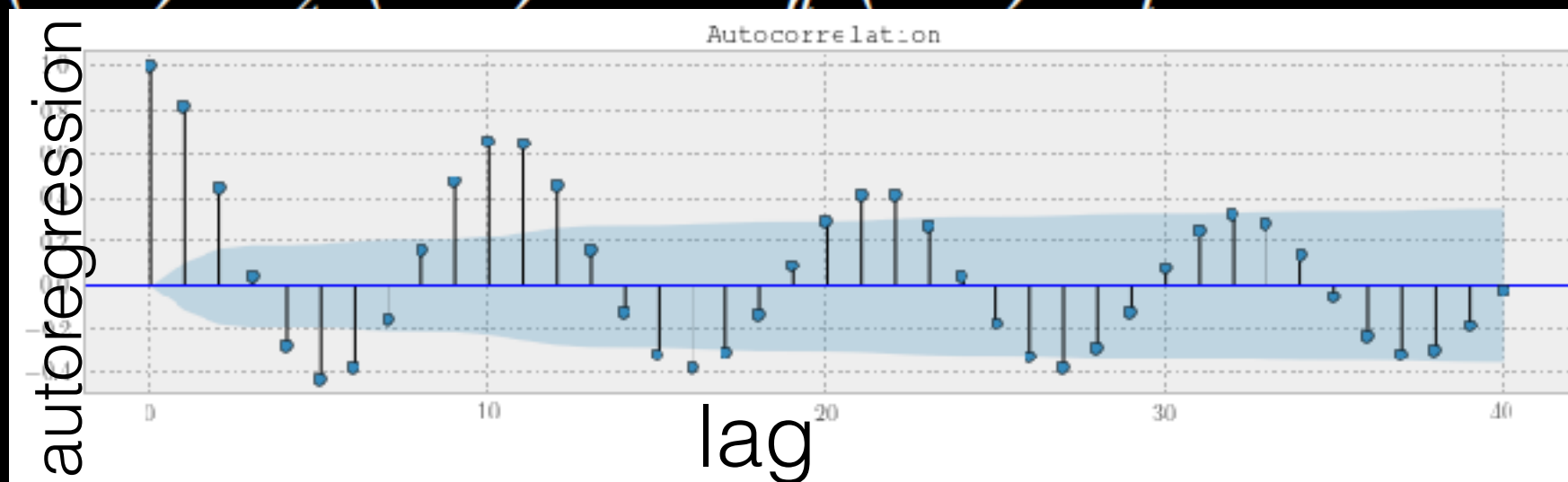
[http://statsmodels.sourceforge.net/devel/examples/notebooks/generated/tsa\\_arma\\_0.html](http://statsmodels.sourceforge.net/devel/examples/notebooks/generated/tsa_arma_0.html)



Aut

$x(t)=$

$$x(t)=a_1x(t-1)+a_2x(t-2)+\dots+a_nx(t-n)+\epsilon_t$$



## ARIMA

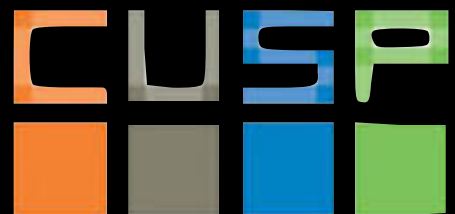
Autoregression

$$x(t) = \sum_{i=1}^p a_i x_{t-i} + \varepsilon_t$$

Moving Average Model

$$x(t) = \sum_{i=1}^q \theta_i \varepsilon_{t-i} + \varepsilon_t + \mu$$

 jupyter



# Integration

$$x'(t) = x(t) - x(t-i)$$

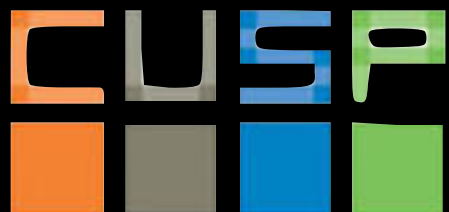
## ARIMA

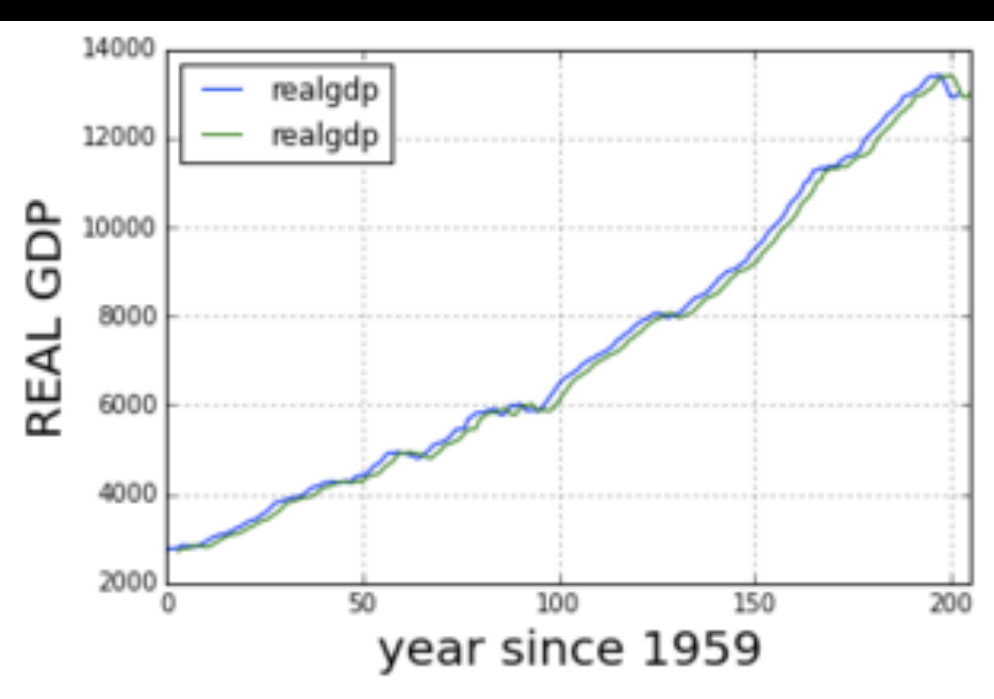
### Autoregression

$$x(t) = \sum_{i=1}^p a_i x_{t-i} + \varepsilon_t$$

### Moving Average Model

$$x(t) = \sum_{i=1}^q \theta_i \varepsilon_{t-i} + \varepsilon_t + \mu$$

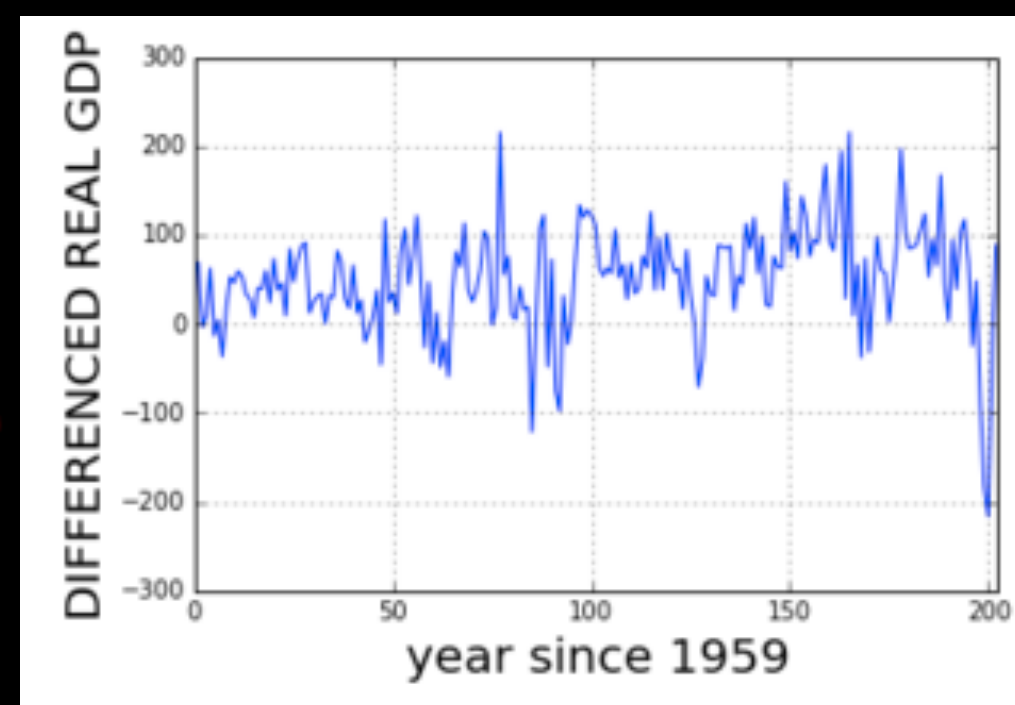




Integration

$$x'(t) = x(t) - x(t-i)$$

ARIMA



Autoregression

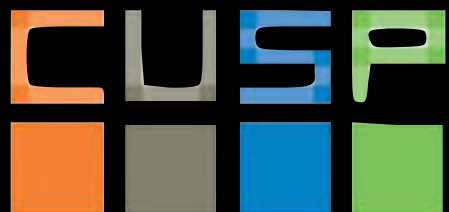
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 jupyter

[https://github.com/fedhere/Ulnotebooks/blob/master/ARMA\\_microdata.ipynb](https://github.com/fedhere/Ulnotebooks/blob/master/ARMA_microdata.ipynb)



## Homework:

### Mandatory Reading

Kim Larsen (MultiThreaded, SF) blog post on bayesian vs non-bayesian *tsa*

<http://multithreaded.stitchfix.com/blog/2016/04/21/forget-arma/>

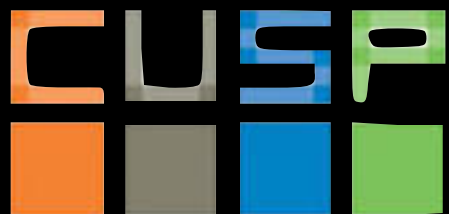
(in class I mentioned JVP Seattle bike-share analysis (now optional reading). I switched cause I think this is more interesting. But it is also a bit more difficult. Still the concepts are accessible to all of you. The code is in R, but you do not have to work with it, and it is R is straightforwardly readable

**Optional Reading:** an excellent analysis of time series

by Jake Vander Plas

(UW e-science center)

<https://jakevdp.github.io/blog/2014/06/10/is-seattle-really-seeing-an-uptick-in-cycling/>





# Homework:

## Data:

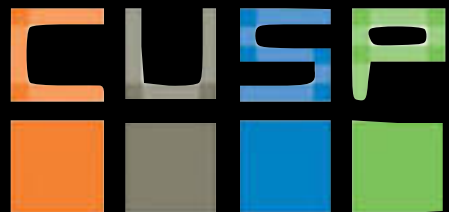
MTA subway fares. It is a complete dataset of rides logged by card swipes for 600 Manhattan stations.

It contains 23 different subway card types (e.g. monthly pass, daily pass, Act for Disability pass... i will give you this as a list)

Each time series (per station, per ticket type) contains the number of swipes per week for 194 weeks from 05/21/2010 to 02/21/2014.

it is given to you as a python data cube.

you can load it as `np.load("MTA_Fare.npy")` and you will end up with a python numpy array of shape (600,23,194)



# Homework:

## Goal 1:

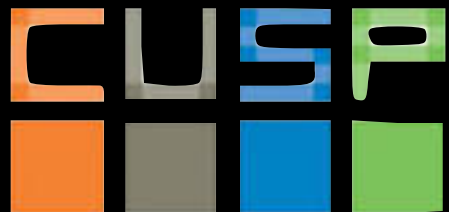
Some of the time series are stationary, some show a downward trend: Identify the time series with the most prominent downward trend.

## Goal 2:

Event detection: Identify the most prominent event. There is a very significant drop ( $>3$ -sigma) in *all* time series. Identify it and figure out what it is due to.

## Goal 3:

Several stations show a prominent annual periodicity. Identify the 5 stations that show the most prominent periodic trend on an annual period. Figure out what the increase in rides is due to.



## Homework Hints:

### Goal 1:

Some of the time series are stationary, some show a downward trend: Identify the time series with the most prominent downward trend.

work with all time series individually. you can use the rolling mean to find trends: compare rolling mean near beginning and end of time series.

### Goal 2:

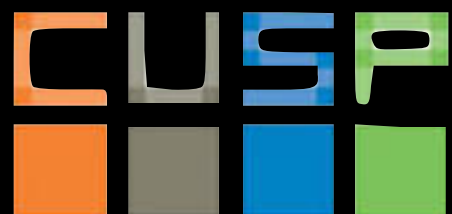
Event detection: Identify the most prominent event. There is a very significant drop ( $>3$ -sigma) in *all* time series.

Identify it and figure out what it is due to.

Since I am telling you the event is in all time series you can work with averages: for example average over all rise types per station. Since i am telling you it is a highly significant event you can find it by thresholding

### Goal 3:

Several stations show a prominent annual periodicity. Identify the 5 stations that show the most prominent periodic trend on an annual period. Figure out what the increase in rides is due to.



Work in Fourier space: find the series that have the most prominent peak at  $\sim 1$  year frequency

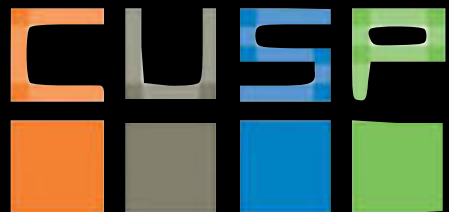
## Homework ExtraCredit:

### Cluster:

Cluster the time series: you can use KMeans for example to identify common trends. or PCA. Since this is extra credit I will leave it entirely to you to figure out the details.

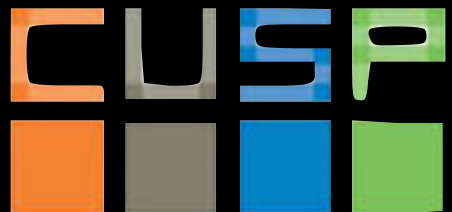
for KMeans for e.g.:

```
#i am flattening the first 2 dimensions of the cube to cluster all
light curves for all stations and all types
tots = data.transpose(2,0,1).reshape(data.shape[2],
data.shape[1]*data.shape[0]).T
#removing empty light curves
tots = tots[tots.std(1)>0]
#ith Kmeans you have to choose the number of clusters ahead km
= KMeans(n_clusters=10)
#and standardize the lightcurves before clustering
vals = ((tots.T - tots.mean(1))/tots.std(1)).T
km.fit(vals)
```



## Key points:

- Time series analysis may be done for a number of purposes: classification, prediction, event detection, period finding
- smoothing, binning, detrending (difference, regression)
- prediction tools: autoregression, ARMA, ARIMA
- period finding (Fourier analysis)



## References:

Stationary and non stationary time series

<http://www.cas.usf.edu/~cconnor/geolsoc/html/chapter11.pdf>

Change point detection

<https://www.ncbi.nlm.nih.gov/pmc/articles/PMC5464762/>

ARMA & ARIMA

<http://www.econ.ohio-state.edu/dejong/note2.pdf>

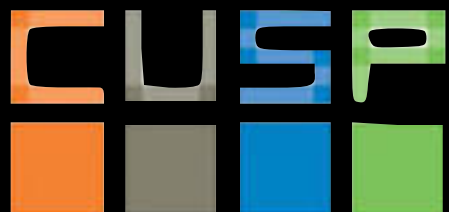
Time series classification in python, which we did not cover but you should read about!

<http://alexminnaar.com/time-series-classification-and-clustering-with-python.html>

A basic but quite intuitive Fourier Transform tutorial

<http://www.thefouriertransform.com/>

Fourier Transform for Imaging: it is actually a very common image analysis technique and urban science relies a lot on imaging and computer-vision techniques <http://homepages.inf.ed.ac.uk/rbf/HIPR2/fourier.htm>



## References on clustering

Clustering: Science or Art??

Ulrike von Luxburg, Robert C. Williamson, Isabelle Guyon, 2009

<http://users.cecs.anu.edu.au/~williams/papers/P184.pdf>

Determining the number of groups from  
measures of cluster stability

G. Bel Mufti, P. Bertrand and L. El Moubarki, 2005

[http://citeseerx.ist.psu.edu/viewdoc/download?  
doi=10.1.1.98.4941&rep=rep1&type=pdf](http://citeseerx.ist.psu.edu/viewdoc/download?doi=10.1.1.98.4941&rep=rep1&type=pdf)

Clustering technique-based least square support vector machine for  
EEG signal classification

Siulya, Yan Lia, Peng (Paul) Wenb, 2010

(This is in the field of neuroscience, but it discusses clustering of time  
series. You should have access to it from an NYU internet connection)

<http://www.sciencedirect.com/science/article/pii/S0169260710002907>

