

## Unit 3 formative activities

### Activity 1

Attempt the following questions from the module core text:

- Chapter 2 Question 4 - The barber's paradox.
- Chapter 3 Question 4 - A Canadian variant of an old puzzle.

**Answer:** Not possible to execute as these pages are not included in the access provided to the core text.

### Activity 2

Read the paper by Palomino et al (2005) and review the 'crossing problem' diagram provided in the Lecturecast.

- Create a set of statements in first order logic (FOL) that represent the states shown – for example you may define two functions *left* and *right* and therefore the first state could be represented as:  $\text{Left}(F)$  and  $\text{left}(W)$  and  $\text{Left}(G)$  and  $\text{left}(C)$ . Define your own set of FOL statements for the entire diagram.

**Answer:**

To represent the crossing problem using First Order Logic (FOL), we need to define some predicates and functions. For this problem, we can define the following predicates:

- $\text{Left}(X)$ : Indicates that the entity X is on the left side of the river.
- $\text{Right}(X)$ : Indicates that the entity X is on the right side of the river.

Additionally, we define constants for the entities:

- F: The farmer
- W: The wolf
- G: The goat
- C: The cabbage

Let's represent the different states using these predicates:

#### Initial State:

Everyone is on the left side.

- $\text{Left}(F) \wedge \text{Left}(W) \wedge \text{Left}(G) \wedge \text{Left}(C)$

#### State 1:

Farmer takes the goat across the river.

- $\text{Right}(F) \wedge \text{Right}(G) \wedge \text{Left}(W) \wedge \text{Left}(C)$

#### State 2:

Farmer goes back alone.

- $\text{Left}(F) \wedge \text{Right}(G) \wedge \text{Left}(W) \wedge \text{Left}(C)$

**State 3:**

Farmer takes the wolf across the river.

- $\text{Right}(F) \wedge \text{Right}(W) \wedge \text{Right}(G) \wedge \text{Left}(C)$

**State 4:**

Farmer takes the goat back.

- $\text{Left}(F) \wedge \text{Right}(W) \wedge \text{Left}(G) \wedge \text{Left}(C)$

**State 5:**

Farmer takes the cabbage across.

- $\text{Right}(F) \wedge \text{Right}(W) \wedge \text{Right}(C) \wedge \text{Left}(G)$

**State 6:**

Farmer goes back alone.

- $\text{Left}(F) \wedge \text{Right}(W) \wedge \text{Right}(C) \wedge \text{Left}(G)$

**State 7:**

Farmer takes the goat across.

- $\text{Right}(F) \wedge \text{Right}(W) \wedge \text{Right}(G) \wedge \text{Right}(C)$

This sequence represents a safe crossing without the goat being left alone with the wolf or the cabbage. Each state follows the constraints given in the problem statement.

- *You have been provided with solutions to the ‘crossing problem’ written in Lisp (here), Prolog (here) and Maude (here). Compare your FOL clauses with the various implementations – which of the implementations provides the closest match to your FOL version?*

**Answer:** Prolog