Aalto University School of Science Degree Programme in Computer Science and Engineering

Gonçalo Marques Pestana

# Energy Efficiency in High Throughput Computing

Tools, techniques and experiments

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Supervisors: Professor Jukka K. Nurminen Advisor: Zhonghong Ou (Post-Doc.)



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## Abbreviations and Acronyms

2k/4k/8k mode COFDM operation modes

3GPP 3rd Generation Partnership Project

ESP Encapsulating Security Payload; An IPsec security

protocol

FLUTE The File Delivery over Unidirectional Transport pro-

tocol

e.g. for example (do not list here this kind of common

acronymbs or abbreviations, but only those that are essential for understanding the content of your thesis.

note Note also, that this list is not compulsory, and should

be omitted if you have only few abbreviations

## Contents

$\mathbf{A}$	bbre	viations and Acronyms	4
1	Intr	roduction	7
	1.1	Overview	7
		1.1.1 The LHC example	7
	1.2	Problem Statement	8
	1.3	Scope of the Thesis	9
	1.4	Contributions	9
	1.5	Structure of the Thesis	9
2	Bac	kground	11
	2.1	Energy efficiency in Scientific Computing	11
		2.1.1 CERN and the LHC experiment	11
	2.2	Energy performance and measurement	13
		2.2.1 Importance of measuring energy consumption	13
	2.3	ARM architecture	13
		2.3.1 Literature review	13
	2.4	Scheduling based on dynamic energy pricing	14
		2.4.1 Summary	14
		2.4.2 General notes	16
		2.4.3 Paper's notes	17
		2.4.3.1 New articles	22
3	Ene	ergy measurement tools and techniques	23
	3.1	Tools and techniques for energy measurement	23
	3.2	Power efficiency measurements with x86-64 and ARMv7 $$	25
		3.2.1 Tools and techniques	26
4	Exp	periments	27
	4.1	Experiments methodology	27
		4.1.1 Environment for Power and Performance measurements	28

		4.1.2 First Set of Experiments	28
		4.1.3 Second Set of Experiments	28
		4.1.4 Third Set of Experiments: RAPL in NUMA environment	28
		4.1.5 Fourth Set of Experiments	28
	4.2	Results	28
5	Ana	lysis	39
	5.1	First Set of Experiments	39
		5.1.1 Comparison ARM and Intel architectures	42
		5.1.2 Tools and techniques	42
	5.2	Second Set of Experiments	42
		5.2.1 Comparison ARM and Intel architectures	
		5.2.2 Tools and techniques	42
	5.3	Third Set of Experiments	42
6	Low	ering the energy bill in a multi energy price environment	43
7	Futi	ıre Work	44
8	Con	clusions	45
$\mathbf{A}$	Firs	t appendix	49

## Chapter 1

## Introduction

#### 1.1 Overview

Nowadays, Moore's Law continues to increase the number of transistors per chipset and the overall technology development at a geometric rate. However, the energy consumption of the systems have begun to halt the usage of the technology at its full potential. It is well known that energy efficiency is an important research topic in computer science, for energy has become a major growth bottleneck for the systems. In addition, the increasing concerns with energy consumption and its social, economical and environmental impact in our society has given a bigger dimension to the discussion.

There are two major approaches to tackle the energy bottleneck in the current technology panorama. One, is to develop techniques and technologies to better harvest, transform and store energy to be used by the systems. This approach aims to provide the needed energy for technology to reach its full potential. The second path is to improve the energy efficiency of the systems. This Thesis focuses on a specific area of the later approach.

The concerns with energy consumption and its impact in the current applications affect industries ranging from mobile devices to big data centers. Given the several layers and complexity of the systems nowadays, there are considerable number of directions to improve the energy efficiency of the systems. Throughout this Thesis, we will focus on improving the energy consumption in High Performance Computing (HPC) applied to Scientific Research.

#### 1.1.1 The LHC example

In some applications, a single computing unit does not have enough resources to accomplish its tasks. A recurrent strategy is to distribute computational tasks across a set of computing units that might be spread geographically.

The Large Hadron Collider (LHC) [ref] at the European Laboratory for Particle Physics (CERN) in Geneva, Switzerland, is an example of a scientific project whose computing resource requirements are larger that those likely to be provided in a single computing unit. Thus, data processing and storage are distributed across the Worldwide LHC Computing Grid (WLCG) [ref], which uses resources from 160 computer centers in 35 countries. Such computational resources have enabled the CMS [ref] and ATLAS [ref] experiments to discover the Higgs Boson [ref, ref], amongst other scientific achievements. The WLHC requires a massive amount of computational resources (250,000 x86 cores in 2012) and, proportionally, energy. In the future, with planned increases to the LHC luminosity [ref], the dataset size will increase by 2-3 orders of magnitude, posing even more challenges in terms of energy consumption.

The LHC is an example of a massive computational system that needs to improve its energy efficiency to reach its full potential in the present and future time. Throughout this Thesis, we will focus primarily on the LHC case. When appropriate, we will use authentic data and current technology use by the CMS to study and to draw conclusions with respect to energy efficiency.

#### 1.2 Problem Statement

A considerable amount of research has been done on leveraging Reduced Instruction Set Computing (RISC) architectures to minimize energy consumption on mobile and energy constrained devices. In such cases, energy consumption is a priority given the inherent reduced amount of energy available.

The large quota of ARM architectures in the mobile market supports the fact that RISC is a good fit for mobile and energy constrained devices.

Similarly to mobile devices, the HPC community has being considering energy efficiency as a priority in the foreseeable future. However, studies focusing on viability of RISC architectures on HPC as a way to minimize energy consumption are not abundant in the research technology. Furthermore, to the knowledge of the author, there are no major implementations of such technologies being used in HPC systems nor in scientific computing.

It is still unclear whether RISC architectures are a good match to HPC computing or not. There are open points regarding whether the performance constraints of RISC architectures and the high performance requirements of HPC workload are acceptable. In addition, it is still unclear if RISC architectures.

tures are more energy efficient under HPC workloads than the conventional Complex Instruction Set Computing (CISC) architectures.

Therefore, it is of our interest to study the potential impact of RISC architectures in the HPC and scientific computing industry. In our opinion, there are two major lacks that need to be fulfilled: Firstly, there are lack of comparisons between RISC and CISC architectures under authentic scientific workloads. Secondly, there are scarce proposal for solutions using RISC in the HPC and scientific computing.

#### 1.3 Scope of the Thesis

The purpose of this Thesis is to answer whether RISC architectures are a potential fit to HPC and scientific computing from a energy efficiency perspective. We focus mainly on comparing RISC - most notably ARM chipsets - and widely used CISC architectures such as Intel processors. For the endeavor, we use authentic HPC workload from the CMS collider at CERN.

In order to accomplish the task, we start by investigating the best and most accurate ways to measure power consumption and compare different architectures. After, we run several experiments in different chipsets using authentic workloads from LHC and software used by the CMS team to process the data generated by the collider. We compare the results and draw conclusions from them. Finally, based on our learnings, we frame a methodology for lowering the electrical bill of data centers running under a multi energy pricing policy, by leveraging the scheduling of machines with different efficiency profiles.

#### 1.4 Contributions

- Our main findings are ..

## 1.5 Structure of the Thesis

This thesis is structured as following. Firstly, we define the context and scope of the thesis by reviewing relevant and up to date research work. Secondly, we outline measurements tools and best techniques for energy measurement and performance in the scientific computing context. Thirdly, we outline the experiments methodology for comparing the performances of the architectures and respective results. In the Chapter 5, we analyze and draw conclusions

based on the results obtained in the experiments. In the Chapter 6, we present some thoughts on how to lower the energy bill by implementing our learnings thus far. Finally, we wrap up by outlining possible future work and presenting the conclusions of this thesis.

## Chapter 2

## Background

#### 2.1 Energy efficiency in Scientific Computing

Power consumption and energy efficiency have become a paramount research topic in computer science, for energy has become a major growth bottleneck in several systems. Moreover, the increasing concerns with energy consumption and its social, economical and environmental impact in our society has given a bigger dimension to the discussion. Given its importance, many research studies have looked into energy efficiency and power consumption. There is a vast panoply of studies with different approaches toward improving energy efficiency. For example, to use GPU for data processing [10], [12] or improve energy efficiency by using RISC architectures [15] [6], [5], . Several other directions have been taken toward energy efficient computing [16] [11], [20] and the number of related works keeps growing.

Scientific computing is often characterized by requiring enormous data storage capacity, high processing capabilities and complex configuration [22]. High processing capabilities and massive data storage are requirements that potentially require massive amounts of energy. Thus, the scientific computing community is looking into energy efficiency with special interest.

#### 2.1.1 CERN and the LHC experiment

The European Research for Nuclear Research (CERN) [1] is a particle physics research laboratory sited in the Franco-Swiss border where thousands of engineers and physicists from about 21 state members conduct researches about the fundamental structures of the Universe. In order to perform experiments that support the researchers studies, they have built several particle accelerators and detectors. The most outstanding collider is the Large Hadron Collider (LHC). The LHC consists of a 27-kilometer ring of superconducting

magnets that boost the particles while traveling through it. The particles are accelerated in two beams, traveling inside the LHC in opposite directions. When the beams are traveling close to the speed of light, they are made to collide in the different colliders. After each collision, particles and subatomic particles are projected due to the collision, which is tracked and recorded by the colliders. The data acquired from the collisions is then filtered and the most interesting information is stored in the CERNs datacenters for posterior reconstruction and processing. Given the frequency of the collisions and the massive amount of data to store and process from each collision, the LHC is an example of a scientific computing endeavor which energy resources are critical to manage efficiently.

According to [6], the computing requirements for HPC have increased particularly in recent years. Most notably, a project with the magnitude and complexity of the LHC is a sound example of it. To achieve results like the discovery of the Higgs boson [4] [8] and other significant scientific advances, a massive amount of computational resources - and thus energy was necessary. Given the enormous amount of resources needed for storing and processing the data, it was not viable to concentrate all the tasks in one single super-node. Thus, the solution was to distribute the processing tasks across several partners and institutions through a distributed network of nodes, called the Worldwide LHC Computing Grid (WLCG). The WLCG [3] is a grid computing platform where more than 170 computing centers spread across 40 countries [3] collaborate to store and process the data coming from the LHC experiment. According to [3], the WLCG alone is responsible for the distribution, storage and processing of more than 30 Petabytes annually. According to [6], the equivalent capacity of WLCG in 2012 was between 80,000 and 100,000 x86-64 cores. In the future, other projects and researches will demand even more processing capacity from the WLCG. For example, as stated by [6], in order to upgrade the luminosity of the LHC detectors to its full potential, the datasets will increase size by two to three orders of magnitude, with processing power increasing in proportion.

These outstanding numbers, in addition to the price of energy and the increasing concerns with green computing, highlight the importance of developing more efficient and methods and techniques high performance computing, both in the scientific computing in general and in the LHC computing grid in particular.

#### 2.2 Energy performance and measurement

#### 2.2.1 Importance of measuring energy consumption

The study conducted by [16], shows that engineers have been considering energy consumption as an important factor when developing software. It consists on an empirical study that aims to understand the opinions and problems of software developers about energy efficiency. The data that sustain the conclusions are mined from a well-known technical forum (StackOverflow [2]). Although the study is focused in an application-level energy efficiency, it shows that developers are aware of the importance of energy efficiency in computational systems. When trying to understand in depth what questions arise more frequently, it is shown that measurement techniques is amongst the most asked questions by developers. In addition, the study ascertains that the "lack of tool support" is an important handicap for the development of energy efficient software.

#### 2.3 ARM architecture

#### 2.3.1 Literature review

#### In [6]:

- After 2015, processors have hit scaling limits. Two different paths started to be taken on the processor industry: development of multiprocessor architectures that allow to run parallel tasks and the time clock frequency which have been increasing throughout the years stabilized.
- Most High Physics Computing systems run in clusters of several cores. Additional cores are parallelized and can run at the same time, which allows the system to scale. However, also commodities such memory, I/O streams and energy scale proportionally in such architectures.
- In [5], a server-purpose ARM machine is compared with the recent Intel architectures, such as the recent Intel Xeon Phi and a dominating Intel product intended for HPC workloads (Intel Xeon E5-2650). The workload for comparing the architectures was ParfullCMS. They based the results on performance (events per second) and scalability over power (watts). In addition to performance and energy consumption comparisons, the paper describes the porting endeavors of the CMSSW to an ARMv8 64-bits architecture.
- In [5], they use an APM X-Gene 1 running on a development board. It consists of a 8 physical core processor running at 2.4GHz with 16GB DDR3 memory. As the authors highlight, the firmware for managing processor

ACPI power states was not yet available when the study was made. Thus, it is expected that the energy performance will improve once the firmware is available [5].

Under the circumstances of the experiment, the overall results show that APM X-Gene is 2.73 slower than Intel Xeon Phi. From the energy consumption performance (events per second per watt), the Intel Xeon E-2650 is the most efficient, with APM X-Gene presenting similar performances despite the absence of platform specific optimizations. Therefore, [5] concludes by stating that the APM X-Gene 1 Server-On-Chip ARMv8 64-bit solution is relevant and potentially interesting platform for heterogeneous high-density computing.

# 2.4 Scheduling based on dynamic energy pricing

#### 2.4.1 Summary

There are several studies exploring inter data center solutions to lower the electricity bill by leveraging the spacial-time dynamic of energy pricing. The emphasis is given to job scheduling across data centers that are located in different places. The main idea is to exploit the fact that energy prices are change based on location and time. The research community is mostly concerned with fairness, server availability, queue delays, bandwidth costs with job migration and quality of service.. In addition there are several research studies related with migration of cloud computing jobs. Studies that in one way on another address this perspective are [19], [7], [18], [17], [13], amongst others.

Besides inter center solutions, the research community has been addressing the power consumption of the computing nodes specifically from a data center perspective. This perspective is closer to what we are trying to achieve with our solution. For example, one work that seems closer to our solution is [23]. In this study, the authors achieve better energy performance in a dynamic pricing environment with HPC systems by judiciously scheduling parallel jobs - which have different energy profiles - depending on the energy pricing of the moment. The main difference to out solution is that the performance of the machines are not taken into consideration when scheduling the jobs, but rather the job energy profiling.

Another research study that related to our solution is [21]. They came up with an optimal algorithm and two heuristic algorithms to schedule tasks to heterogeneous processors. In addition, they also take into consideration the

memory allocation in heterogeneous memory in order to minimize energy consumption while meeting the assumed deadlines. Their work, though, seems to go further than our solution since it considers heterogeneous memory allocation as well. They consider is a computing process executing several tasks in a parallel computing environment. The system consists in a variety of different computational node, each of one with a given number of processors. All computational nodes are connected by a high-speed network. Thus, all the processors can cooperate and realize complementary and parallel tasks. From the energy point of view, the processors of each computational node have an energy profile assigned and have a certain frequency, which will be taken into consideration when scheduling the task. The work dates from end of 2014, which indicates that this is a trendy and hot subject, but it seems that our approach is been used already.

A similar idea has been explored in [24]. They present only heuristic algorithms to schedule tasks on heterogeneous computing systems, based on efficiency and energy consumption. They develop heuristic algorithms due to the fact that an optimal solution for the needed scheduling is NP-complete.

Our solution takes a different perspective when compared with the inter data center solutions. Studies like [21] and [24] do not take the dynamics of electrical pricing into consideration. However, their algorithm is already quite complex and proved NP-complete, to the point they have to come up with heuristic algorithms to apply it in the real world.

Therefore, our approach may have some novelty in a really narrow and still unexplored idea: to develop a scheduling algorithm for heterogeneous HPC that takes into consideration the nodes' energy profile, the dynamic electricity price and also, eventually, the tasks' energy profiling. The algorithm would schedule the jobs in order to minimize the energy consumption and energy bill (note: energy consumption and energy bill are not the same thing), while the deadline is met.

However, there are some open points that we still have might want to consider. First, as [23] mentions, it is important to insure that the hardware existent in the data center is used at its full potential, in order to not waste the investment made when it was purchased. Our solution, though, does not insure that since the idea is to power down/idle machines that are less power efficient in high-peak times. Secondly, from a practical perspective, if we consider only the scheduling between ARM and Intel architectures, it seems not likely that the data center will haver the same software running over both architectures at the same time, give the expertise and investment needed to have the application stack running properly in both architectures (as we witness with CERN's efforts). If we decide to abstract from that point and see the machine's architectures as a black box, then that's not a

problem. Thirdly, comparing with other recent research works such as [21], our algorithm model seems to be over simplifying the problem to an extent that might hinder our purposes of creating a practical and energy efficient scheduling algorithm for heterogeneous HPC under dynamic electrical pricing.

#### 2.4.2 General notes

- Intra data center judicious job scheduling based on the heterogeneous architecture of the machines.
- Minimize the electricity costs in data centers by leveraging the dynamical electricity pricing models and heterogeneous computing.
- Online computation schedule the jobs. Jobs are in a queue in a serial fashion and are scheduled depending on the decision of the algorithm at a given time. On the other hand, there are the static scheduling algorithms. These algorithms know all the data they need beforehand and map the jobs to the machines taking that into consideration.
- There are several studies that aim to leverage the potential of geographical load balancing to provide significant cost savings (see [24, 28, 31, 32, 34, 39] in [11])
  - Make a problem specification as in [17]
- In our solution, we could also coinsider different stages of functioning such as idling and turning of the machines, depending on the expected workload and the server configuration. The problem might be to understand if we have (or not) knwoledge of the server utilization in the future and its workloads. Actually, this is an important factor to consider wether we have or not idea of the future workload.
- It would be interesting to test and simulate our model and algorithm using, for example, workloads and electricity prices in a Google data center. As many studies do, show the potential of our approach by simulating scnarios based on real case data.
- As [23] briefly mentions, does Dynamic Voltage and Frequency Scaling (DVFS) have the same results than our heterogeneous approach in a homogeneous data center? i.e. are the benefits of a more efficient processor such as ARM surpassed (or the same) as an INTEL working under a DVFS? The principle seems the same: when energy consumption is smaller (in ARM or INTEL under low DVFS), the jobs take longer to accomplish. This said, is ARM more efficient than INTEL under low DVFS?
- Should our work be an extension on [23] where, instead of scheduling the workload taking into consideration the job's energy profile, also consider the machine's energy performance?

#### 2.4.3 Paper's notes

#### In [14]:

Demand side management are programs implemented by the utility companies to control and influence the user-side behavior. For example, electrical companies often fluctuate the energy price depending on the user's demand.

There is need to encourage household owners to \*shift\* high demand energy consumptions outside the peak hours, in order to reduce the peak-to-average (PAR) in load demand. [ - we aim towards the shifting of schedule different machines depending on the PAR]

Direct load control (DLC) gives the utility companies the possibility to remotely control the household's applications (dim or turn of lights, turn of thermal equipment, amongst others). Though, this model arises some problems related with household's privacy [- see more 'A direct load control model for virtual power plant management' - what if DLC would be implemented for servers and in a heterogeneous scheduling scenario? Would it bing any advantage or liability?]

An alternative to DLC is smart pricing, where users are encouraged to voluntarily and individually shift their loads out of the peak-hours be increasing the energy prices when the load is big.

One problem with this approach is synchronization: when a large number of users shift their peak at the same time for a low-peak time, the PAR may not be reduced due to the amount of users churning energy at low-peak time. [- this might happen as well with our scheduling strategy. If the amount of users running our scheduling system at the same time is the same, it does not help to reduce the PAR and the prices might get worst]

The paper suggests that households should synchronize their energy usage and schedule their energy applications not only according to the price of the energy at a given time, but also taking into consideration what others are consuming as well. Thus, by acting in synchronization, the group of users can optimize the energy the overall energy consumption and its pricing.

They propose an incentive-based energy consumption pricing model for the smart grid, where the energy source is shared by several users. The meters communicate between each other in a distributed network to find the optimal energy consumption for each user.

Based on game theory, it is shown that through an incentive-based pricing scheme, an optimal scheduling - where users consume less energy and pay less money - can be achieved.

#### In [19]:

Because of the magnitude of energy costs in data centers, it is important to lower the energy consumption in data centers. The servers are composed of heterogeneous machines from the performance and energy efficiency. In addition, the data centers may be disposed in different geographical locations and, thus, have different energy tariffs. The authors of [19], claim that the key idea to lower the energy bill in data centers is to have energy efficiency servers and schedule the jobs to where energy is more affordable at a given time.

In the context of servers distributed over different geographical locations, it is also important to satisfy fairness and delay constraints. This scenario is less critical when the server is not distributed, as in our case.

In [19], the authors present an online scheduler that distributes batch workloads across multiple data centers geographically distributed. The scheduler aims to minimize the energy consumption of the set of servers having into consideration fairness and delay requirements.

The scheduler is inspired on the technique developed by Lyapunov ['Resource allocation and cross-layer control in wireless networks'] that optimized time-varying systems.

The algorithm takes a queue of jobs schedule them to the different servers having in consideration the (1) server availability, (2) energy price and (3) job fairness distribution. Consequently, the algorithm is tuned to calculate the tradeoff between energy pricing, fairness and queueing delay.

#### - The model:

The data center model takes into consideration the possibility of the energy prices to vary over time. The state of the data center can be represented at a given time by a tuple of (i) server availability and (2) energy price.

The job model is characterized by a tuple of (1) service demand - job length - and (2) the set of data centers the job can be scheduled.

The scheduler can turn on/off a server when needed. The scheduling is done based on the server availability and job queue and thus, what matters is the energy consumed by the server when it is 'idle' or 'busy'.

The scheduler also considers he model fairness (which is not important to our study, since we focus in a non-distributed server) and queuing delay. Queuing delay defines the time a job will take to start to be processed, according to relation of the number of jobs scheduled and machine availability.

In [19], the scheduler developed takes into consideration the server availability, energy costs, fairness and queuing delay to schedule random jobs arrivals. It opportunistically schedules jobs when (and to where) energy prices are low.

Comparing to our study, though, we do not consider geographically distributed servers but rather, we have schedule the jobs based on the heterogeneous set of machines existing on the server.

#### In [7]:

This study aims to exploit the temporal and geographical variation of electricity prices, in the context of data centers. They study algorithms to schedule (migrate) jobs in data center based on the energy cost and availability.

When the servers are in different geographical location, costs with data migration have to be taken into consideration, namely bandwidth costs of moving the application state and data between data centers. The bandwidth costs increase proportional to the amount of data migrated between servers.

Their study focuses on inter data center optimization, rather than intra data center optimization (as our study is aiming for)

The algorithm differs from others in 3 major differences: First, they consider migration of batches of jobs. Second, the algorithm has into consideration the future influence of the job scheduling, providing robustness against any future deviations of the energy price. Finally, they also take into consideration the bandwidth costs associated with job migration across data servers.

The main point is to provide a good tradeoff between the energy pricing and the job migration, taking into consideration the bandwidth prices.

Comparing to our study, we do not approach the problem from an inter data center perspective, but rather from an intra data center, by scheduling the jobs to machines depending on their energy performance and the actual energy prices. One interesting idea from this study that can be used, is the usage of an online algorithm that takes into consideration the expected prices and also the actual prices.

In [18]: In [18], they try to systematically study the problems of how minimize the electricity cost in data centers while guaranteeing minimal quality of service. To that end, they take into consideration the local and time diversity of electricity prices.

The contributions are twofold: In one hand, they show that local and time dependent electricity pricing can be leveraged to minimize total energy price of clusters of data centers. On the other hand, they present a mixed-integer optimization formula with linear programming formulation to show that the energy pricing of clustered data centers can be improved under such conditions.

To model the total of electricity costs, they assume that all the servers have a similar power profile - which means that all the servers, disregarding their locations, have the same workload. They calculate the power consumed by the server by multiplying the total of servers at a certain region by the total of workload they have.

Again, the time constraints and delays considered in a inter data center study does not need to be considered in out work.

They obtain the most efficient solution, they approximate an optimization problem through a linear programming formulation and then, convert the linear programming formulation to a minimum cost flow problem.

This work dates from 2010 and don't take into consideration the bandwidth costs of migrating the batches between data centers. Even though that is not an issue in our study, this is taken into consideration in other works such as [7]. Again, it is part of the set of studies on inter datacenter and electrical costs optimizations that location and time based pricing allows.

In [17]: The authors of [17] show that existing systems may be able to save millions of dollars by judiciously schedule workload to servers taking into consideration the temporal and geographical variation of energy prices. The results are based in historical data collected on Akamai's CDN.

In [23]: In [23], the authors leverage the fact that parallel jobs have distinct energy profiles. Taking it into consideration, they study the impact of scheduling jobs according to the energy prices at a given moment and the job's energy profiles. So, the study aims to reduce the electricity bill by scheduling and dispatching jobs according to their energy profile. Their solution has a negligible impact on the system's utilization and scheduling fairness.

Their basic idea is to schedule jobs with low energy profile during on-peak electricity time and, on the other hand, schedule jobs with high energy profile during the off-peak electricity time. In addition, the scheduling is done in such a way that it is guaranteed that there is no degradation of the overall system performance.

The authors take an intra data center approach, since it considers a solution that can be put into practice at a data center level.

The authors claim that "A key challenge in HPC scheduling is that system utilization should not be impacted. HPC systems require a tremendous capital investment, hence taking full advantage of this expensive resources is of great importance to HPC centers.". This may make impractical and wreck our solution, because of the inevitability of turning off (or idle) great amounts of computing resources. Although, internet data centers (cloud data centers) may be a good match to our solution: usually there are much less resources being used at a given time than in HTC computing [need confirmation, partially mentioned in this article].

The scheduling algorithm used places jobs in a time-window. The jobs are chosen to run based on job fairness, job energy profile and energy prices at a given time. A greedy algorithm and 0-1 Knapsack based policy are used to minimize the electrical costs.

Their results show that gains in the order of 23% can be obtained without impact on the overall system.

According to the survey carried by [23], the dynamic energy pricing has been implemented in the biggest markets in Europe, North America, Oceania and China, while Japan was at the time starting to test it on its major cities.

They develop two power aware job policies: 1) greedy approach, where jobs are allocated based on their energy profiles and 2) 0-1 Knapsack based policy, where both job profile and system utilization are taking into consideration.

#### In [13]:

The authors of [13] present a novel task scheduling algorithm for HPC systems which considers two main points: reducing the energy consuption of the overall system and minimize the schedule length. An HP system is defined by the authors as set of distributed computing machines with different configurations connected through a high speed link to compute paralell applications.

They assume a that all the information needed to schedule the taksk is known beforehand. The scheduling algorithm assigns then the jobs to the different machines. Thus, the scheduling algorithm is said to be static, in opposition to, for example, the online algorithms.

One of the particularities of the algorithm is to reduce the impact of duplication-based algorithms. The duplication-based algorithms schedule jobs across machines redudantly, in order to maximize performance by eliminating intercommunication between tasks. However, from the energy consumption point of view, it is not the ideal situation since more than one processor are performing the same job.

Once again, this research work aims at improve the energy efficiency of HPC systems at a distributed level and do not focus, as our approach, on inter data center solutions.

#### In [21]:

In [21], the authors address the problem of an energy aware scheduling for heteregenous data allocation and task scheduling. The problem consists in finding the best taks scheduling in a heterogeneous system that meet the deadlines while minimizing the energy consumption.

The processors and memories come in different flavors nowadays in HPC systems, making complex the task of efficiently scheadule processor power and memory space in an energy efficient way. The problem of finding an optimal processor and data scheduling becomes critical when trying to minimize energy consumption and meet imposed deadlines.

As the study shows, there are several research efforts tackling the task scheduling problems on heterogenous computing and, most notably for our research, [?].

They present an optimal algorithm and two heuristical algorithms to solve

the HDATS problem, since the optimal algorithm takes too long to solve problems until 100 nodes. The optimal solution has two phases: First is uses the DFG\_Assign\_CP algorithm to better map each task to node. Secondly, it choses the data assignment to whose total energy consumed is reduced and the deadlines met.

They consider:

- Heteregenous processors
- Heteregenous memories
- Precedence constrained inputs
- Input/output of each task
- Processor execution times
- Data access times
- Time constraints
- and Energy consumption

When solving the data allocation and task scheduling problem, which is an approach much more solid and complete than ours.

#### In [24]

The authors of [24] claim that, unfortunatelly, there are not many studies of processor scheduling algorithms that take into consideration both time and energy. In this study, they explore heuristical scheduling algorithms focused on high performance computing and green computing. They work on heuristical algorithms and not in the optimal algorithm, because the optimal algorithm is proven to be NP-complete.

#### 2.4.3.1 New articles

In [25], the authors designed an online algorithm for dynamic pricing of VM resources across data centers in different geographical locations. The authors claim novelty by considering efficient strategies for joint dynamic pricing, job scheduling and resource provisioning.

The authors of [26], [9] also leverage the dynamic electricity pricing models for data centers.

## Chapter 3

# Energy measurement tools and techniques

The most recent scientific applications have to process and store a considerable volume of data. It is foreseeable that the volume of data will increase considerably in the future, as technology and requirements enhance. In addition to the physical limitations in terms of power density, this phenomenon also increase considerably the costs with energy in a HTC system. Thus, energy consumption has become a major concern amongst the scientific community.

#### re-write and re-organize everything from now on

In order to find and develop better solutions for improving energy efficiency in High Energy Physics (HEP) computing, it is important to understand how energy is used by the HEP systems themselves. We describe several tools and techniques that facilitate researchers to reach that goal.

As energy efficiency becomes a concern, new solutions have been considered to develop energy efficient systems. One potential solution is to replace the traditional Intel x86 architectures by low power architectures such as ARM. A comparison of the energy efficiency between ARMv7 and x86 Intel architecture is conducted in this article. The experiments use CMS workloads and rely on the techniques and tools described earlier to perform the measurements.

# 3.1 Tools and techniques for energy measurement

When optimizing power usage, there are two granularities at which one can look at a computing system. The coarser granularity takes into account

the behavior of the whole node (or some of its passive parts, e.g. the transformer) as part of a rack in a datacenter. This is usually investigated when engineering and optimizing computing centers. Alternatively, a more detailed approach is to look into the components which make up the active parts of a node, in particular the CPU and its memory subsystem since these are responsible for a sizeable fraction of the consumed power. They are also the place where the largest gains in terms of efficiency can be obtained through optimizations in the software.

If one is simply interested in the coarse power consumption by node, external probing devices can be used: monitoring interfaces of the rack power distribution units, plugin meters and non-invasive clamp meters (allowing measurement of the current pulled by the system by induction without making physical contact with it). They differ mostly in terms of flexibility. Their accuracy is typically a few percent for power, whereas their time resolution is in the order of seconds. This is more than enough to optimize electrical layout of the datacenters or to provide a baseline for more detailed studies.

A alternative approach takes into account the internal structure of a computing element of an HTC system, as shown in figure 3.1. Nowadays, every board manufacturer provides on-board chips which monitor energy consumption of different components of the system. These allow energy measurements of fine grained detail, as it is possible to individually monitor energy consumption of components such as the CPU, its memory subsystem, and others. An example of this chip monitors is the Texas Instruments TI INA231 [?] current-churn and power monitor which is found on the ARMv7 developer board which we used for our studies. It is quite common in the industry. Compared to external methods, these on-board components provide high accuracy and reasonably high precision measurements (millisecond level).

A special and slightly different case of these on-board monitors is a new technology called Running Average Power Limit (RAPL), provided by Intel beginning from the Sandy Bridge family of processors.

Contrary to other solutions, which are implemented as discrete chips, RAPL is embedded as part of the CPU package itself and provides information on the CPUs own subsystems. In particular RAPL provides data for three different domains: **package** (pck), which measures energy consumed by the system's sockets, **power plane 0** (pp0), which measures energy consumed by the CPU core(s), and **dram**, which accounts for the sum of energy consumed by memory in a given socket, therefore excluding the on-core caches [?]. As for the discrete components case, the timing resolution of measurements is in the millisecond range [?]. This is fine enough to permit exploiting such data to build an energy consumption sampling profiler for applications, similar to how performance sampling profilers work (see sec-

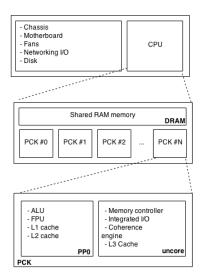


Figure 3.1: Components that contribute for power consumption in HPC

tion ??). Finally, in addition to power monitoring of the sockets, RAPL can limit the power consumed by the different domains. This feature, usually referred as power capping, allows the user to define the average power consumption limit of a domain in a defined time window and allows more accurate independent measurements of the non limited components.

## 3.2 Power efficiency measurements with x86-64 and ARMv7

In this section, we demonstrate the potential of some of the tools we previously described. To that end, we perform several measurements of workloads from CERN, running on different architectures. The workloads used in the experiment run on top of Intel x86-64 architecture, traditionally used in HTC and data centers and 32 bit ARMv7 architectures (for similar studies for 64bit ARMv8 and Xeon Phi, please refer to [?]). The ARM architecture, initially developed for mobile devices, has been considered [6?] as a potential alternative to Intel in HTC, given its energy efficient computing. We also present a brief comparison between ARM and Intel architectures from the energy consumption perspective, based on the results obtained.

#### 3.2.1 Tools and techniques

For the Intel architecture, we used the RAPL technology to perform measurements of the energy consumed by the package, DRAM and cores (figure 3.1). The external measurements for the baseline were performed using a rack PDU, which provides an online API to gather the energy consumed by the system on the rack at a sampling rate of 1 second. For the ARM board, we used the Texas Instrument power monitor chip TI INA231 which allows reading of the energy consumed by the cores and dram at a sampling rate of microseconds. The chip was embedded in the board from the vendor. For the external measurements, we used an external plug-in power monitor with a computer interface for gathering and storing the results. In both cases we read the data as it was exposed to the system via the sysfs / devfs knobs.

## Chapter 4

## **Experiments**

### 4.1 Experiments methodology

The experiments were performed in different sets. Whereas the first two sets of experiments aim to provide a straightforward comparison between ARM and Intel technologies, the third set of experiments aims to study the influence of a NUMA environment in hight performance computing from an energy consumption perspective. The last set of experiments were done using the same machine as in the first set, but using different workloads and measurement tools. In each set, we used different techniques and tools to perform the energy measurements. The techniques and tools used to perform the measurements are described and analyzed in depth in Section 3.

The first part of this chapter outlines the scope, methodology and measurement tools used for each set. The latest part shows the results of the experiments, which are analyzed in the next chapter.

Throughout the rest of the document, the different experiments will be termed as first (FSE), second (SSE), third set of experiments (TSE) and fourth set of experiments (FtSE).

Code name	Architecture	CPU	Cores	RAM	Notes
ARM_odroid	ARMv7™	A15 and/or A7 cores (big.LITTLE technology)	4	2 GB	Development board with TI INA231 chip
ARM_server	ARMv7-A™	A15 and/or A7 cores (big.LITTLE technology)	4	4 GB	Server without TI INA231 chip
Intel_cern	Intel Sandy Bridge™	CPU E5-2650	32	252 GB	System on a rack with RAPL

Figure 4.1: Specifications of the machines used for experiments

# 4.1.1 Environment for Power and Performance measurements

outline CMSSW, architectures, and workloads

#### 4.1.2 First Set of Experiments

Done at Aalto. Explain methodology and scope.

#### 4.1.3 Second Set of Experiments

Done at CERN. Explain methodology and scope.

# 4.1.4 Third Set of Experiments: RAPL in NUMA environment

Done at CERN. Explain methodology and scope.

#### 4.1.5 Fourth Set of Experiments

Done at CERN. Explain methodology and scope.

#### 4.2 Results

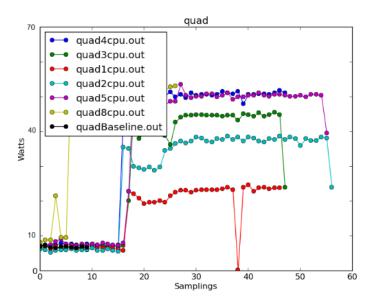


Figure 4.2: Full single threading CMS experiments on Intel Quad

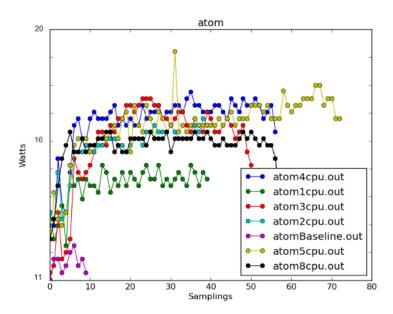


Figure 4.3: Full single threading CMS experiments on Intel Atom

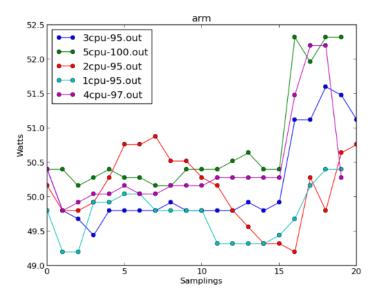


Figure 4.4: Full single threading CMS experiments on ARMv7 server

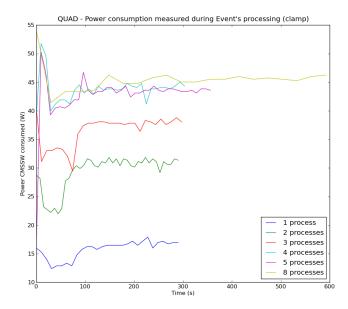


Figure 4.5: Full single threading CMS experiments on Intel Quad - event processing only

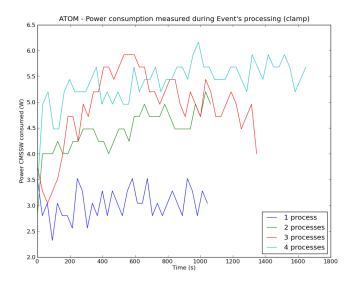


Figure 4.6: Full single threading CMS experiments on Intel Atom - event processing only  $\frac{1}{2}$ 

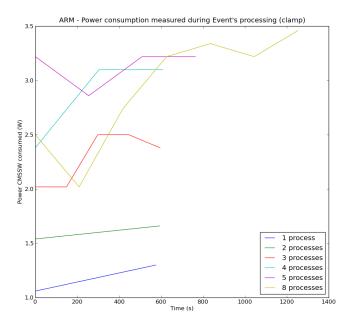


Figure 4.7: Full single threading CMS experiments on ARMv7 server - event processing only

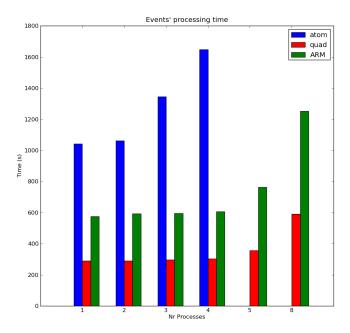


Figure 4.8: Processing time comparison

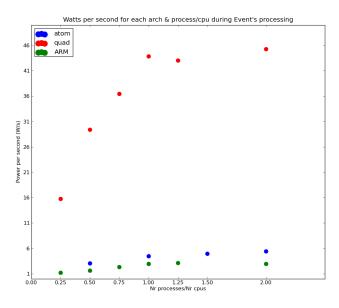


Figure 4.9: Energy efficiency comparison between architectures

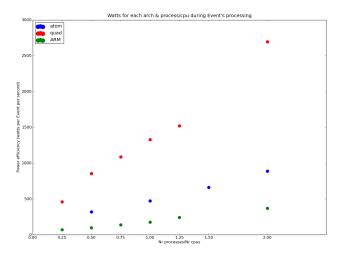


Figure 4.10: Processing stage comparison between architecturesi - 2

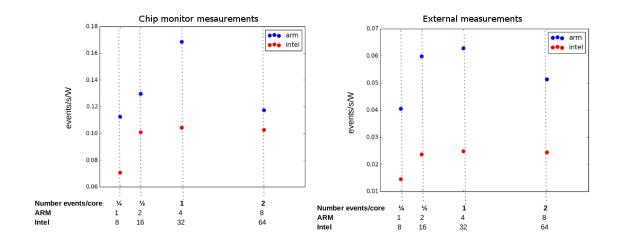


Figure 4.11: Multithreaded Par<br/>FullCMS comparison Intel Xeon vs $\ensuremath{\mathsf{ODROID}}$  ARMv7

## 1. RAPL measurements

	avg pck [W]	avg pp0 [W]	avg dram [W]	power eff. [ev/s/W]
A. 32 threads	24.64	11.28	11.61	0.029023
B. 4 processes x 8 threads	39.65	26.20	12.01	0.068764
C. 8 processes x 4 threads	40.41	26.95	12.02	0.070478
D. 2 processes x 32 threads	30.95	17.55	11.85	0.045032

Figure 4.12: RAPL measurements with different load combinations

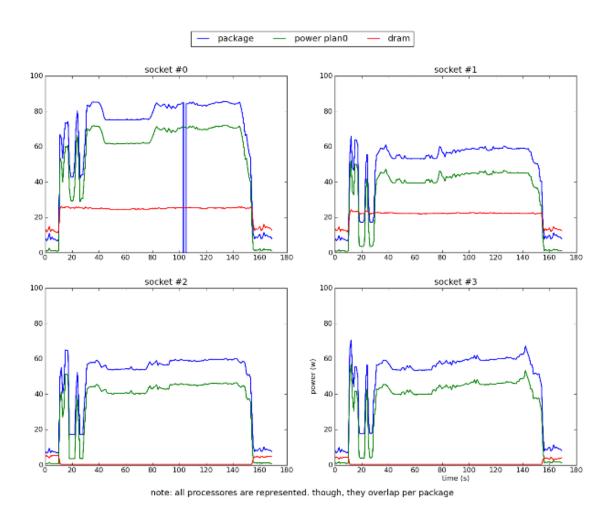


Figure 4.13: RAPL measurements of NUMA nodes - 16 processes with no explicit binding

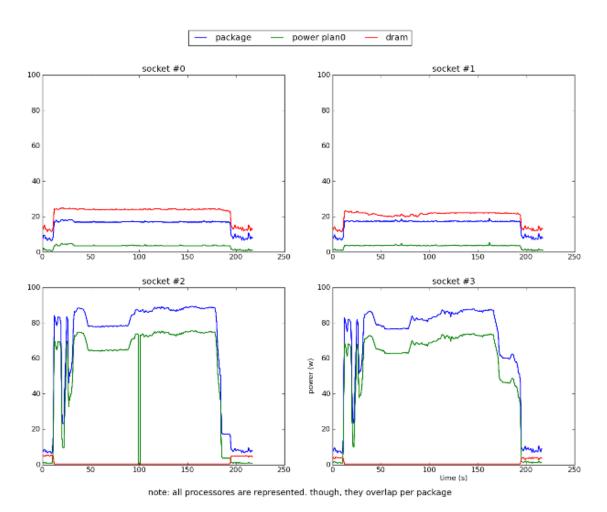


Figure 4.14: RAPL measurements of NUMA nodes - 16 processes. Explicit binding on node #2 and node #3 binding

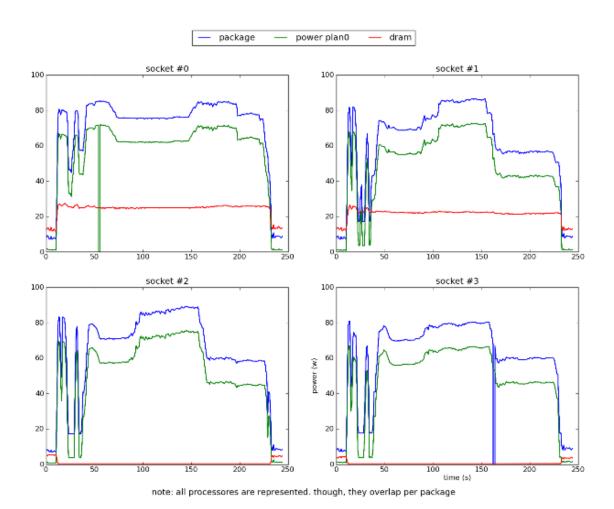


Figure 4.15: RAPL measurements of NUMA nodes - 32 processes with no explicit binding

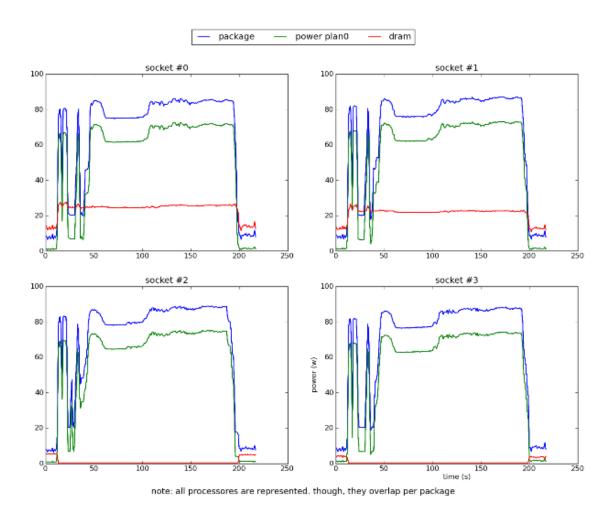


Figure 4.16: RAPL measurements of NUMA nodes - 32 processes. Processes distributed evenly explicitly - 8 processes per node.

# Analysis

The scope of the analysis presented in this section is twofold: to compare the platforms from an energy efficiency perspective and analyze the tools and techniques used on the different experiment sets.

Whereas the first two sections analyze the energy efficiency of the platforms studied and the particularities of the tools and techniques used, the last section covers the results and issues which arose when using RAPL to measure the energy consumption in a NUMA environment.

In the final of this section, we outline the highlights of the analysis for each set of experiments.

## 5.1 First Set of Experiments

ARM server vs ATOM and QUAD, using clap and software-based experiments

In figures 4.2, 4.3 and 4.4, it is plotted the physical measurements from the beginning of the workload until the end.

#### Stages

All the experiment sets show 3 stages. The stages can be better identified when plotting the memory workload against cpu usage, rather than the energy consumption measurements (see Figures in GDrive-Add?). The three stages consist in different phase of the experiment. The first stage consists on the initialization process. During this stage mostly memory is being used, rather than cpu workload. The second stage is the connection phase. It has the goal of fetching the meta data fetching from the CERN servers needed to perform the reconstruction of the events. Anew, during this stage, the cpu load is low when compared to the memory workload. Lastly, the third stage corresponds to the event

processing phase. Therefore, the last stage is cpu intensive and the one that is performing the useful computation for the reconstruction of events.

#### Stages comparison

Regardless the number of processes running, the time for the three stages is constant in all the experiment sets, if the cpu is not overcommitted. When the number of processes exceed the number of available cores, the time to process the events increases since there are no available cores to process the events concurrently. In the overcommitted situation, the time increase follows a ratio  $nr_{-}of_{-}processes/nr_{-}of_{-}cores_{-}available$ . For example, if the number of processes running is 6 and the number of cores available is 4, the time needed to process the events increases roughly 2/3 compared to when the cpu is not overcommitted.

#### Importance of the stages

Unarguably, the most important stage when studying the energy efficiency of workload in CERN is the third stage. There are two main reasons for that: first, the CMSSW configuration at either CERN, 2nd and 3rd tiers has proxies and caches that speedup the second stage [refs]. Lastly, given the amount of data to be processed in the last phase and thus the energy consumed by the event processing stage, the energy consumed by the former stages becomes irrelevant. Therefore, in the remainder of the chapter we focus our analysis on the event processing stage only. The energy measurements of only the third stage are shown in the figures 4.5, 4.6 and 4.7.

#### Relation number processes/number cores

The relation between the number of processes and number of cores and the influence of its ratio is clear in the figures 4.5, 4.6 and 4.7. As expected, when the CPU is overcommitted the task takes more time than otherwise. For the QUAD 4.5 and ARM 4.7 architectures, it is clear that when the number of processes is bigger than 4, the task takes more time to be processes. In the ATOM architecture 4.6, the same happens when the number of processes exceed 2. More detailed information about this behavior can be drawn by analyzing the data acquired by the software-based tools during the experiments [include ps, powertop, ect.. plots?]

#### Time comparison

When comparing the time taken by the different architectures to process the same task 4.8, the pattern is evident. Regardless the number of

processes launched, the QUAD architecture is faster than ATOM and ARM, whereas ATOM is faster than ARM. This fact is due to the architectures characteristics and its specifications, most notably the CPU clock speed.

#### Energy efficiency comparison

The energy efficiency metric used in this study is the ratio of performance per power consumed. Performance consist on the average of events computed per second for each architecture. More details about the reasons why Events were considered the main data unit for CERN workloads are explained in the Methodology Section. Given the above mentioned metrics, it is clear that systems are proportionally energy efficient with its ratio performance per watts. Therefore, by analyzing the Figure 4.9, it is evident that given the architectures and its configurations, ARM architecture outperforms in terms of energy efficiency its concurrence in all considered scenarios. In addition, we conclude that between Intel architectures, ATOM is more energy efficient than QUAD architecture.

#### Measuring tools: external monitoring

For this set of experiments, the external samples were acquired and recorded manually. This factor had a visible impact on the resolution of the measurements. Clearly, the plot shows spikes and rough transitions between samples. Moreover, the error tends to increase proportional to the human interaction with the experiment. Therefore, it is more effective to use digital and automated ways to sample and log the data acquired during the measurements. The advantages of using digital and automated ways to sample and log data can be seen further on in the SSE.

#### Measuring tools: software-based monitoring

In this particular set of experiments, the software monitoring tools used were of particular help to distinguish the different stages, which existence was unknown before the experiment. The software-based tools can be used as a decision support and for system behavior learning. Thus, even if the output is does not directly show information about energy consumption of the system, it can be important to support and explain expected - and unexpected - behaviors.

## 5.1.1 Comparison ARM and Intel architecures

## 5.1.2 Tools and techniques

## 5.2 Second Set of Experiments

ARM board and Intel Xeon, using on chip and external measurements

## 5.2.1 Comparison ARM and Intel architecures

## 5.2.2 Tools and techniques

## 5.3 Third Set of Experiments

Intel Xeon, using RAPL to measure energy consumed by the different nodes, with different types of binding

# Lowering the energy bill in a multi energy price environment

- Use the greedy and jobshop models to schedule works across different energy profile machines.
  - Use experiments done to characterize the machines
  - Code scheduling algorithm

Future Work

# Conclusions

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# Appendix A

# First appendix

This is the first appendix. You could put some test images or verbose data in an appendix, if there is too much data to fit in the actual text nicely.