# Personal income inequality and aggregate demand\*

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#### Abstract

This paper presents a theoretical and empirical investigation of how changes in the size distribution of income can affect aggregate demand and the demand regime of an economy. After presenting empirical evidence for the US economy that the propensity to save increases significantly from the bottom to the top quintile of wage earners, we demonstrate that more equal distributions always lead to higher output in the traditional neo-Kaleckian macroeconomic model. We also present conditions under which a reduction of income inequality among workers turns demand more wage-led. This view is supported by the results of an econometric study for the United States (1967-2010) which show that the rise after 1980 in income inequality has made the US economy more profit-led.

*Keywords:* Income inequality, demand regimes, Neo–Kaleckian model, personal and functional income distribution.

JEL classification numbers: D31, E25, C32

Area 4: Macroeconomics, Monetary Economics and Financial Economics

<sup>\*</sup>We benefited from comments by Lance Taylor. Armon Rezai thanks the Sao Paulo School of Economics for its hospitality. The usual disclaimer applies.

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### 1 Introduction

As the unprecedentedly large share of income held by the top 1% was incorporated into the slogan of the Occupy Wall Street movement, the substantial rise in income inequality in the United States since the 1970s became acknowledged by a wider public. In the economic literature, the main reference for this topic is Piketty and Saez (2003) who compile a series for the top shares of income and wages from 1913 to 1998 to conclude that income inequality has not only been increasing as a whole in the recent decades, but also that the working rich have replaced the rentiers at the top of the US income distribution. Palma (2011) extends the empirical analysis to a large number of countries and shows that inequality within countries has been the major cause of the global trend in income inequality in the past decades. One possible explanation for this pattern can be found in the work by Mohun (2012), which presents evidence of an increase in the share of supervisory workers in total wages. This phenomenon serves as main motivation for this paper which aims at studying the implications of a rising inequality among wage earners for aggregate demand and its relationship to functional income distribution. The proponents of the Occupy Wall Street movement have, among other things, called for reform of the tax system to reduce income inequality. Our theoretical and empirical work traces through the generally positive macroeconomic implications of such policy proposals.

The macroeconomic effects of changing the functional distribution of income has been investigated extensively in both the theoretical and empirical economic literature. Already Keynes (1936) recognized the distributive effects on demand, e.g. in his condemnation of high-saving rentiers and bear speculators. Kaldor (1955) first formalized the idea that savings propensities are different between profit earners and wage earners making aggregate demand sensitive to a redistribution of income. This assumption has then been combined with Kaleckian mark-up pricing (Kalecki, 1971) and an independent investment function in the so-called Neo-Kaleckian models developed seminally by Rowthorn (1982), Dutt (1984), Taylor (1985) and Bhaduri and Marglin (1990). The crucial role played by the functional distribution of income in the determination of both consumption and investment in these models has given rise to the concepts of wage- and profit-led demand regimes, depending on which effect dominates.

Based on these ideas, empirical investigations of the overall effect of redistributing toward wages for different countries, time periods or specifications of demand and distributive variables have yielded contradicting results. Estimations of full macro models tend to show profit–led demand regimes (Franke, Flaschel, and Proaño, 2006; Chiarella, Franke, Flaschel, and Semmler, 2004; Barbosa-Filho and Taylor, 2006). However, more recent studies have highlighted the role of the wage share in determining the level of competitiveness and the trade balance, concluding that demand tends to be profit–led with trade, even if domestic demand—consumption vs. investment—is wage–led (Bowles and Boyer, 1995; Naastepad and Storm, 2007; Ederer and Stockhammer, 2007; Hein and Vogel, 2008).

This paper extends the short-run Neo-Kaleckian framework to address a different kind of bias in such empirical and theoretical arguments: the size distribution of income. As the evidence presented in Piketty and Saez (2003) and below highlights, rising inequality in the United States in the recent decades has been characterized by an increase in the share of income held by the top wage earners in addition to a falling wage share. One possible

approach to this problem, taken by Dutt (1992), Lavoie (1996), and Tavani and Vasudevan (2012), is to add an unproductive managerial class to the basic Kaleckian framework and examine the effects of wage inequality between managers and workers. Indeed, by also endogenizing the functional distribution of income and wage inequality itself, the authors find that redistribution toward workers leads to a decline in both inequality and the degree of capacity utilization.

This paper has a similar motivation, but follows a different strategy. Instead of adding a third class to the Kaleckian framework, we provide both an empirical and a theoretical explanation for the savings rate to be an increasing function of wage inequality. Based on this extension, we ask two main questions: (i) how has this increase in the top share of income affected aggregate demand for a given level of the wage share? and (ii) did this increase contribute to the weak response of consumption to the wage share, thus turning the demand-regime more profit-led?

In an attempt to answer these questions, the paper organizes as follows. First, based on stylized facts regarding the relationship between savings rates and income inequality in the United States, Section 2 extends the standard Neo-Kaleckian model to account for different size distributions of wage income. While greater inequality necessarily reduces aggregate demand, we show that the effect of inequality on the demand regime of the economy depends on various parameters due to multiplier effects. Second, in Section 3, we present an econometric study examining the role of income inequality in determining the demand regime for the United States from 1967 to 2010. We find that the increase in inequality after 1980 has made the economy more profit-led.

## 2 Macroeconomic effects of the size distribution of income

## 2.1 Empirical Motivation

Most Neo-Kaleckian models assume that savings rates are different for different income classes. While this assumption is plausible, it is usually taken at face value without presenting empirical evidence. In this section we present such evidence for the US economy. In doing so, we use data for the quintiles of income before taxes from the Consumer Expenditure Survey as provided by the Bureau of Labor Statistics.<sup>1</sup>

In Figure 1 we report the savings rates for each quintile of income after taxes. We computed these by calculating (1 - C/Y), where C is the average annual expenditure and Y is the average annual income of each quintile. Savings rates increase strongly with income. Whereas the top 20% saved about 40% of their income in 2005, the middle 20% saved less than 10% and the bottom 20% borrowed to finance a substantial part of their expenditure.

#### Distribution of income clearly matters for aggregate saving.

The negative values observed for the lower quintiles show the importance of private debt accumulation in financing household expenditures in the US economy over the reported period. It is interesting to note that as the top 20 % started to concentrate more of the total income after taxes (as shown in Figure 2 below and discussed in Palma (2011)), their average

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<sup>&</sup>lt;sup>1</sup>Tables from 1984 to 2010 are available at http://www.bls.gov/cex/.

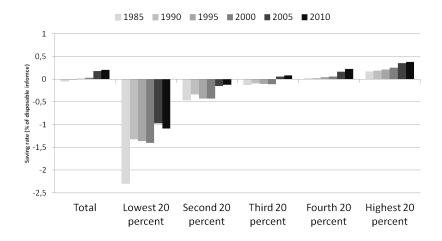


Figure 1: Savings rate per income quintile in the United States (1985-2010)

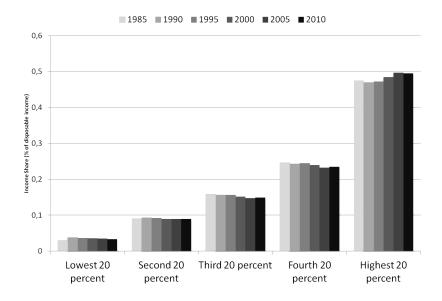


Figure 2: Income share per income quintile in the United States (1985-2010)

savings rate has also increased. A common feature throughout all income quintiles is the jump in savings rates after 2000, possibly showing the private sector's effort to de-leverage.

The distribution of income in the US economy has become more unequal over the past 30 years. Figure 2 presents the share of income after taxes held by each quintile for selected years. The figure shows how unequally income is distributed and how this inequality has been rising in the United States. Almost half of total income is held by the richest 20% in 2010. These two observations serve as the main motivations for the theoretical and empirical analysis that follows.

The stylized facts have two main implications. First, as long as the paradox of thrift holds, an increase in the average savings rate as caused by a rise in income inequality between different categories of workers necessarily leads to lower aggregate demand. Second, the assumption of differential savings within the category of wage earners is clearly justified and

needs to be accounted for in the conventional analysis of the relationship between changes in functional distribution of income and aggregate demand.

#### 2.2 Theoretical argument

Most neo-Kaleckian models restrict themselves to differences in the saving behavior out of different sources of income. Their focus lies on the distribution between wages and profits, the functional income distribution.<sup>2</sup> We find this surprising as these models can easily incorporate personal income inequality. We proceed by presenting an intuitive explanation of how income inequality affects the macroeconomy; a detailed application using a specific functional form for the saving function and a Pareto distribution of income is relegated to Appendix A.

Aggregate income is determined by independent investment and consumption/saving decisions. We retain the Steindlian-Kaldorian formulation for the investment function, in which investment I depends positively on the rate of capacity utilization u and on the rate of profit r, as well as on the autonomous component  $\gamma_0$  representing so-called "animal spirits". We modify the saving function  $S_w$  such that the propensity to save out of wages  $s_w$  now depends on the size distribution of income among workers, captured in the inequality measure  $\sigma$ . The more unequal the distribution, the higher  $\sigma$  and the higher the overall saving propensity:  $s_w' > 0$ . With this small, but important modification we can state the model equations. We use the model presented in chapter 5 of Taylor  $(2004)^3$ .

$$g^{i} = \frac{I}{K} = \gamma_{0} + \gamma_{u}u + \gamma_{r}r = \gamma_{0} + (\gamma_{u} + \gamma_{\pi}(1 - \psi))u$$

$$g^{s}_{w} = \frac{S_{w}}{K} = s_{w}[\sigma] \psi u$$

$$g^{s}_{\pi} = \frac{S_{\pi}}{K} = s_{\pi} \pi u = s_{\pi} (1 - \psi) u$$
(1)

With macroeconomic balance between savings and investment requiring that

$$\dot{u} = g^i - g_w^s - g_\pi^s = 0. (2)$$

Substituting equations (1) into (2), we obtain the standard expression for short-run equilibrium output

$$u^* = u|_{\dot{u}=0} = \frac{\gamma_0}{-(\gamma_u + \gamma_\pi (1 - \psi) - s_w[\sigma] \psi - s_\pi (1 - \psi))} = \frac{\gamma_0}{-\Delta} > 0.$$

Output is determined by autonomous investment,  $\gamma_0$ , times the multiplier,  $\Delta$ . We assume that the Keynesian stability condition holds, i.e.  $\frac{d\dot{u}}{du} = \Delta < 0$ .

<sup>&</sup>lt;sup>2</sup>As mentioned in the introduction, one exception are models which incorporate a third class to the model to represent managers in the form of unproductive labor.

 $<sup>^{3}</sup>$ As in Taylor (2004), all variables will be given as ratios of the capital stock K. The rate of capacity utilization u will be approximated by the output-capital ratio by assuming that capital productivity, namely the ratio of potential output to capital, is constant.

Inequality affects the economy's overall saving decisions. As wage income is redistributed from low- to high-saving classes, leakage increases and aggregate demand falls as one would predict under the Paradox of Thrift. Put formally, this implies

$$\frac{du^*}{d\sigma} = \frac{\gamma_0}{\Delta^2} \frac{d\Delta}{d\sigma} = -u^* \frac{\psi}{-\Delta} \frac{ds_w[\sigma]}{d\sigma} < 0.$$
 (3)

It is clear that redistribution among wage earners always stimulates demand and increases output. This effect is represented by a shift from point A to B in Figures 3 and 4.

The usual debate on redistribution focuses on functional income redistribution, assuming equal distribution within factors. While this assumption might be innocuous for profit earners, the empirical evidence presented in section 2 demonstrates clearly that this does not hold for wage earners. Moreover, the assumption of unequal distribution of wages affects the response of output to the functional income redistribution, i.e. the demand regime. The demand regime of an economy is defined as

$$\frac{du^*}{d\psi} = u \frac{1}{-\Delta} ((s_{\pi} - s_w[\sigma]) - \gamma_{\pi}) \leq 0. \tag{4}$$

If an increase in the wage share increases capacity utilization, the economy is said to be 'wage-led', if the opposite holds the economy is considered 'profit-led'. In this model, it is clear from expression (4), that the economy is wage-led if the saving differential between capitalists and workers  $(s_{\pi} - s_{w})$  is large and investment responds weakly to lower profitability as represented by a low  $\gamma_{\pi}$ . The first effect of functional income distribution decreases overall leakage in the economy, the second effect prevents injections to fall as  $\psi$  increases.

Personal income distribution influences saving out of wages, it thereby also affects the demand regime of the economy, a feature that has received much attention over the past 20 years ((Bowles and Boyer, 1995; Taylor, 2004; Barbosa-Filho and Taylor, 2006; Chiarella, Franke, Flaschel, and Semmler, 2004; Franke, Flaschel, and Proaño, 2006; Ederer and Stockhammer, 2007; Hein and Vogel, 2008)). Basic intuition tells us that an increase in inequality, caused by a rising share of income held by the top wage earners, increases the average saving out of wage income. This weakens the positive demand effects of a functional income redistribution, namely the fall in leakages. However, the changes in the savings rate also reduces the multiplier and capacity utilization with more subtle effects on investment and saving and, overall, ambiguous effects on the demand regime. To see this more clearly, we differentiate the expression (4) with respect to  $\sigma$ 

$$\frac{d\frac{du^*}{d\psi}}{d\sigma} = -\frac{u}{(-\Delta)}\frac{ds_w}{d\sigma} - \frac{du^*}{d\psi}\frac{1}{(-\Delta)}\frac{ds_w}{d\sigma} \leq 0.$$
 (5)

The first term in the inequality captures the immediate effect of saving out of wages on the demand regime: higher functional income inequality increases saving out of wages, which lowers the differential between saving out of profits and out of wages. Higher inequality pushes the demand regime toward more 'profit-ledness'. However, there are repercussions through the effect of inequality on the multiplier (saving and investment behavior). This mechanism is captured in the second term of the inequality in (5). This term depends on (and takes the sign of) the demand regime itself and is positive when the economy is wage-led and negative otherwise.

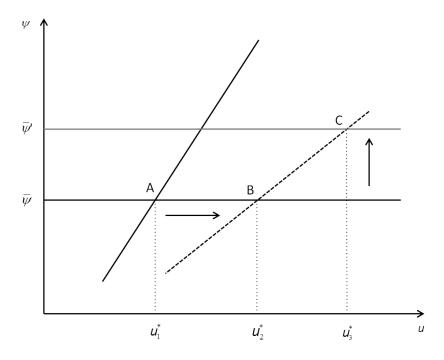


Figure 3: Response of aggregate demand to a reduction in wage inequality in the wage-led case

Hence, while egalitarian policies of income redistribution always increase capacity utilization in this model, their effect on the demand regime of the economy is ambiguous. If the economy is wage-led, redistribution always pushes the economy toward wage-ledness, as represented in Figure 3. This holds also true if the economy is "weakly profit-led". Only if the economy is "strongly profit-led" (strong investment responds to profitability and low functional saving differentials), personal income equality leads to more profit-ledness. The ambiguous change in the slope of the demand curve following a reduction in inequality in the profit-led scenario is represented in Figure 4, giving rise to different responses to an exogenous increase in the wage share (points C and D).

Barbosa-Filho and Taylor (2006) found that the US economy is profit-led. In this case, sole theoretical considerations cannot identify the effect of personal wage income inequality on the US economy's demand regime. In the next section we reestimate their model accounting for personal income inequality to inform this question empirically.

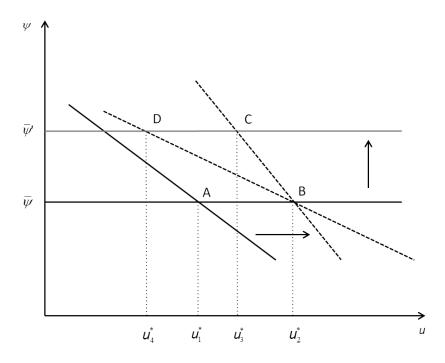


Figure 4: Response of aggregate demand to a reduction in wage inequality in the profit-led case

## 3 Empirical analysis

## 3.1 Methodology and Data

One of the main difficulties in estimating demand regimes lies in a potential endogeneity problem between measures of aggregate demand and income distribution. Indeed, as addressed by the literature focused on Goodwin cycles (Goodwin, 1967), income distribution not only affects, but may also be affected by aggregate demand if lower unemployment leads to an increase in the power of bargaining of workers. Two main approaches to address this problem can be found in the empirical literature. The first has involved the use of instrumental variables to control for each of the two directions of causality (see for instance Nikiforos and Foley (2012)). The second has been to estimate a system of dynamic equations simultaneously in a Vector Autoregression (VAR) or a Vector Error Correction (VEC) model, thus taking both directions of causality into account. The latter approach was the one used in Barbosa-Filho and Taylor (2006), who by means of a two-dimensional VAR model for capacity utilization and the wage share have found demand in the United States to be profit-led. Based on these results, the empirical study done in this section will investigate the role of income inequality in determining such demand regime by making use of a similar method: a two-dimensional Threshold Vector Autoregression (TVAR).

The idea of the threshold autoregressive model first developed by Tong (1990) is to allow for a non-linearity in the dynamic relationship that is estimated. In other words, a threshold defined by the level of a certain variable is searched so as to minimize the sum of squared residuals and the estimated coefficients are different in the so-called low and high regimes. The regime-switching (threshold) autoregressive model was extended to the multivariate con-

text by Tsay (1998), giving rise to the Threshold Vector Autoregressive model (TVAR). <sup>4</sup>A two-dimensional TVAR will be estimated for the degree of capacity utilization and the labor share, using a measure of the size distribution of income as the threshold variable. In other words, the model allows us to investigate whether the level of income inequality affects the response of aggregate demand to the functional distribution of income.

The quarterly series for the degree of capacity utilization was calculated as the ratio between actual output (obtained from the Bureau of Labor Statistics) and potential output.<sup>5</sup> The series for the labor share is also provided from the Bureau of Labor Statistics at quarterly frequency. Both series will be used in logarithmic form in the estimations. Finally, income inequality will be measured by the Gini Coefficient provided by the U.S. Census Bureau (2010)<sup>6</sup> from 1967 to 2010 annually. The conversion from annual to quarterly data was made by cubic interpolation.

A two-dimensional TVAR for the labor share and capacity utilization (in logarithmic form) was then estimated using two lags and the Gini coefficient as a threshold variable (lagged by one period), for the period 1967-2010. The threshold value was selected automatically based on a grid search which minimized the sum of squared residuals of the corresponding estimation.<sup>7</sup>

Linear accumulated impulse response functions to Cholesky standard deviation innovations were computed for the two regimes separately using the corresponding coefficients and the residuals of each TVAR<sup>8</sup>.

#### 3.2 Results

The results of the TVAR estimation for the period 1967-2010 are presented in Table 1 in the Appendix. The selected threshold for the Gini coefficient determining the low and high inequality regimes was 0.406, which corresponds to the value attained in 1981. The low (high) inequality regime, which comprises 32.9% (67.1%) of the total of observations, thus corresponds to the years before (after) 1981. Both regimes are shown to be characterized by profit-led demand, with the total effect of the labor share  $\Psi$  in the equation for capacity utilization u being negative even if it is positive for the first lag (due to higher consumption).

Figure 5 presents the accumulated response of the degree of capacity utilization to a standard deviation shock in the labor share for the low and high inequality regimes<sup>9</sup>. The figure shows that in the high inequality regime the impact of an increase in the wage share in capacity utilization is more negative. In other words, results of the TVAR suggest that the

<sup>&</sup>lt;sup>4</sup>Different types of models have been developed to address non-linearities in time series since Tong's original threshold autoregressive model. See Hansen (2011) for a survey of such developments applied to economics.

<sup>&</sup>lt;sup>5</sup>As in Barbosa-Filho and Taylor (2006), the series for potential output was derived from the output series using a Hodrick-Prescott filter.

<sup>&</sup>lt;sup>6</sup>Current Population Survey, Annual Social and Economic Supplements, available at http://www.census.gov/hhes/www/income/data/historical/household/h04.html

<sup>&</sup>lt;sup>7</sup>The R program is available from authors upon request.

<sup>&</sup>lt;sup>8</sup>Since exogenous shocks may generate a switch from one regime to the other, generalized non-linear impulse response functions based on initial conditions are developed in Koop, Pesaran, and Potter (1996), but will not be estimated here.

<sup>&</sup>lt;sup>9</sup>The impulse response functions for the other direction of causality – the effect of aggregate demand on distribution – are presented in the appendix but will not be analyzed here.

#### **Accumulated Response of Utilization to Labor Share**

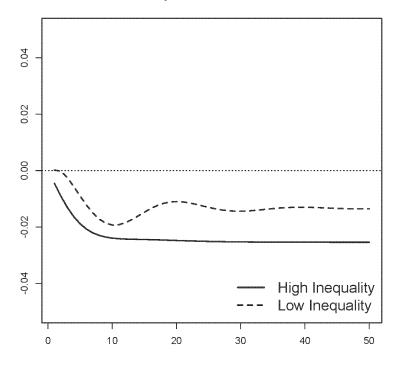


Figure 5: Accumulated impulse response function of the degree of capacity utilization to a standard deviation shock in the labor share in the low and high inequality regimes for the United States (1967-2010)

increase in income inequality has turned demand more profit-led in the United States over this period. Hence, these results seem to confirm the theoretical argument presented in the previous section which corresponds to the weakly profit-led case.

## 4 Discussion

Income distribution has become more unequal in the past decades, reversing much of the gains from post-WWII. This holds true for shifts toward profits in the functional income distribution and shifts toward high-income earners within wage income. While these shifts have gained the attention of the wider public through the 'Occupy Wall Street' movement, the academic debate has focused almost exclusively on the impact of changes in the functional income distribution.

Empirical evidence clearly shows that wage earners have different saving rates depending on the disposable income. Saving rates rise from negative for the bottom 20% to as high as 40% for the top 20% in the year 2010. Given these differences in saving behavior, we analyze the effects of recent increases in wage income inequality on aggregate demand and the economy's demand regime.

While the Paradox of Thrift predicts that output falls as inequality rises, the effects of changes in the functional income distribution on output under different wage income distributions is ambiguous. Higher wage equality makes the economy more wage-led. If the economy is profit-led, the sign of this effect is ambiguous and depends on the level of demand regime itself. These nonlinear effects in the IS curve complements recent work on nonlinearities by Nikiforos and Foley (2012) who present empirical evidence for a non-linear distribution schedule.

Since our theoretical model cannot clearly identify the effects of wage income inequality on the demand regime, we proceed empirically by estimating a non-linear version of the model by Barbosa-Filho and Taylor (2006) in order to determine the effect of income inequality on the demand regime for the post-WWII US economy. The linear estimation by the authors had suggested that the US economy is profit-led. Our estimations show the US may have become more profit-led in times of high inequality.

These findings add to recent evidence that the standard Kaleckian model incompletely captures interactions between demand and distribution when applied to today's advanced economies: Dutt (2006) extends the model to account for consumer debt, Rezai (2011) and von Arnim, Tavani, and de Carvalho (2012) highlight the importance of open-economy issues. We introduce personal income distribution as a third omitted and potentially important bias.

Our results have clear and important implications for economic policy. As the Great Recession keeps unfolding and the political climate shifts increasingly against traditional economic stimuli to prop up demand, taxes-and-transfer schemes can proof effective. While the demand effects of increases in money wages might be repressed by concurrent increases in inflation under mark-up pricing rules, the demand effect of redistribution from profits toward wages depends on the economy's demand regime. Our findings suggest that egalitarian policies within wage earners increase demand irrespective of such considerations. Lowering wage income inequality always increases aggregate demand due to the Paradox of Thrift. Moreover, lowering inequality among wage earners can, and in fact in the US economy does, tilt the economy in a wage-led direction, providing arguments for progressive and expansionary policy in the form of redistribution in functional income on economic – rather than mere social – grounds in the future.

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# **Appendix**

## A An application of the model

In this section we present the derivation of the aggregate saving function for an economy in which wage income follows a Pareto distribution. We pick the Pareto distribution for two reasons: first, since income cannot be negative, the probability density function needs a lower limit under which it has measure 0. This limit is defined as parameter k for the Pareto distribution. Second, Yakovenko (2012) demonstrates that the distribution of personal income in the US exhibits a 'fat' tail. The Pareto distribution has such a fat tail.

Let personal income equal  $y > \kappa$ , then the probability density function (pdf) of a Pareto distribution is

$$f(y) = \frac{\frac{k \alpha}{y^{\alpha - 1}} \text{ if } \kappa \le y}{0 \text{ if } \kappa > y}$$

The median,  $\mu$ , and median,  $\nu$ , of a Pareto are defined as

$$\mu = \frac{\kappa \alpha}{\alpha - 1}$$
 for  $\alpha > 1$  and  $\nu = 2^{1/\alpha} \kappa$ .

We assume that personal saving decision of household i depends the income of household i,  $y_i$ , and the income of the median household,  $y_v$ . Household i's saving is defined as

$$S_i = a_0 y_i + a_1(y_i - y_v).$$

Aggregate saving is the sum of all saving:

$$S_w = \int \left[ a_0 \ y_i + a_1(y_i - y_v) \right] \ f(y) \ dy = a_0 \ \mu + a_1(\mu - \nu) = \left[ a_0 \ + a_1(1 - \frac{\nu}{\mu}) \right] \mu.$$

 $\mu$  eqals average income, which has to be related to the macro variables of the Kaleckian model of section 2. Average income times population size has to equal aggregate wage income:  $\mu L \equiv \psi X$  or  $\mu \equiv \psi u k$ . A Pareto distribution has 2 degrees of freedom,  $\kappa$  and  $\alpha$ . We use  $\kappa$  to ensure that the identity is satisfied,

$$\kappa \equiv \frac{\alpha - 1}{\alpha} \psi \, u \, k.$$

Normalizing population size to 1,  $L \equiv 1$ , and substituting this expression into the saving function, we obtain a saving function of the form used in our theoretical model

$$\frac{S_w}{K} = \left[ a_0 + a_1 \left(1 - \frac{2^{1/\alpha} \alpha - 1}{\alpha}\right) \right] \psi u = s_w [\alpha] \psi u.$$

with  $s_w[\alpha]$  the average propensity to save (APS). The second parameter of the Pareto distribution,  $\alpha$ , captures the degree of wage income inequality. As  $\alpha$  increases, more income is concentrated at the bottom and the more equal wage income distribution.

 $s_w[\alpha]$  has both properties used for the comparative statics used in section 2: first, average aggregate saving falls as the economy becomes more equal and, second, under equally distributed income, the analysis conflates to the traditional assumption of a constant APS:

$$\frac{ds_w}{d\alpha} < 0$$

$$\lim_{\alpha \to \infty} s_w \to a_0$$

Our results therefore hold for specific (and realistic) assumptions on the distribution of income across wage earners.

#### **B** Econometric results

#### **Accumulated Response of Labor Share to Capacity Utilization**

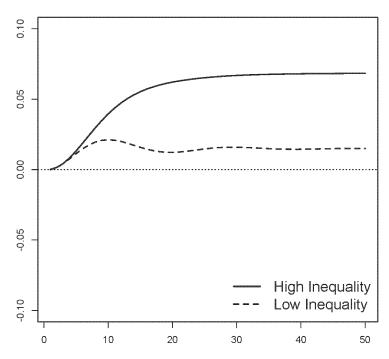


Figure 6: Accumulated impulse response function of the labor share to a standard deviation shock in the degree of capacity utilization in the low and high inequality regimes for the United States (1967-2010)

	Equation for <i>u</i>		Equation for Ψ	
	Low Inequality	High Inequality	Low Inequality	High Inequality
$u_{-1}$	1.3095***	1.4477***	-0.0039	0.0732
$u_{-2}$	-0.5941***	-0.6297***	0.2071*	0.0948
$\Psi_{-1}$	0.8536***	0.2956**	0.5271***	0.7473***
$\Psi_{-2}$	-0.9124***	-0.3181**	0.1603	0.2652**
Intercept	0.2456	0.0932	1.3061***	-0.053

Signif. Codes: \*\*\* 1%; \*\*5%; \*10%

Threshold value: 0.406469

Percentage of Observations in each regime: 32.9% 67.1%

Table 1: Results of the two-dimensional TVAR estimation for the United States (1967-2010) using the Gini Coefficient as a threshold.