

Generative Adversarial Networks

Image Processing with Neural Network  
Session 22  
Pramod Sharma  
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2 Agenda

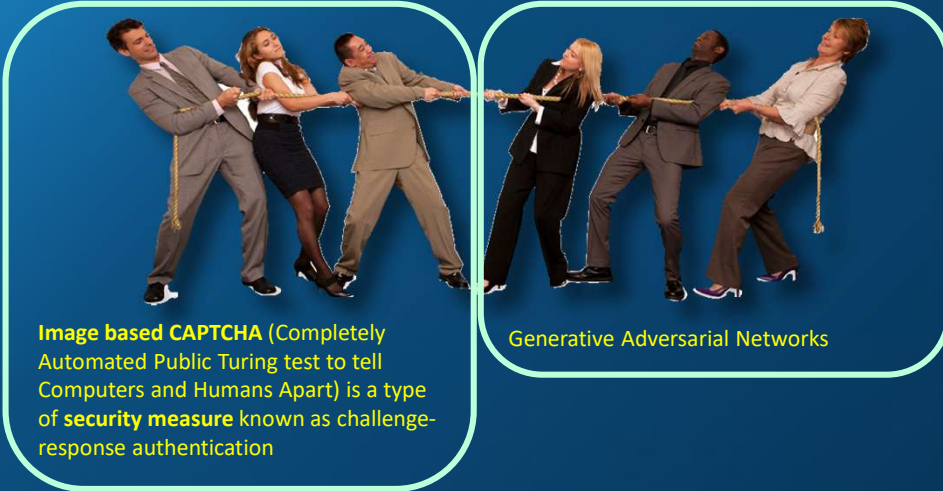
- PixelRNN / CNN
- Variational Autoencoder
- GAN

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## Technologies with Conflicting Goals



**Image based CAPTCHA** (Completely Automated Public Turing test to tell Computers and Humans Apart) is a type of **security measure** known as challenge-response authentication

Generative Adversarial Networks

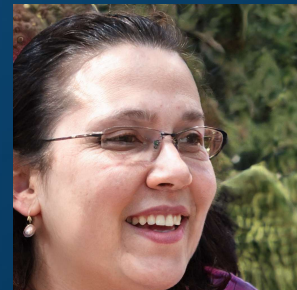
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## Unbelievably Real

- This person does not exist : [thispersondoesnotexist.com](http://thispersondoesnotexist.com)



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## Overview

- ❑ Developed by Ian Goodfellow
- ❑ In generative modeling, we'd like to train a network that models a distribution,
  - ❖ Such as a distribution over images.
- ❑ One way to judge the quality of the model is to sample from it
- ❑ Active area of research with rapid progress



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## Take a Step Back

### Supervised Learning

- ❑ Data:  $(x, y)$ 
  - ❖  $x$  is data,  $y$  is label
- ❑ Goal: Learn a function to map  $x \rightarrow y$
- ❑ Examples:
  - ❖ Classification,
  - ❖ Regression,
  - ❖ Object detection,
  - ❖ Semantic segmentation,
  - ❖ Image captioning,
  - ❖ ...

### Unsupervised Learning

- ❑ Data:  $x$ 
  - ❖ Just data, no labels!
- ❑ Goal: Learn some underlying hidden structure of the data
- ❑ Examples:
  - ❖ Clustering,
  - ❖ Dimensionality reduction,
  - ❖ Feature learning,
  - ❖ Density estimation,
  - ❖ ...

Makes Training  
data cheap!

Holy grail:  
Solve unsupervised learning  
→ Understand structure of  
visual world

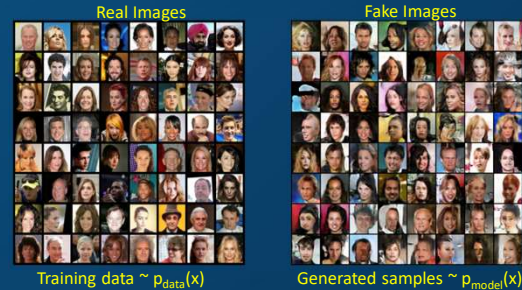
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## Generative Models

- Given the training data, generate new samples from same distribution



- Want to learn  $p_{model}(x)$  similar to  $p_{data}(x)$
- Addresses density estimation, a core problem in unsupervised learning
- Several flavors:
  - ❖ Explicit density estimation: explicitly define and solve for  $p_{model}(x)$
  - ❖ Implicit density estimation: learn model that can sample from  $p_{model}(x)$  without explicitly defining it

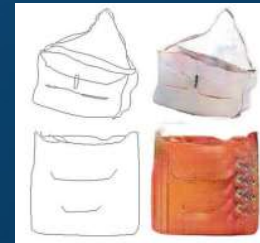
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## Why Generative Models?

- Realistic samples for artwork, super-resolution, colorization, etc.



- Generative models of time-series data can be used for simulation and planning
  - ❖ Such as reinforcement learning applications!
- Training generative models can also enable inference of latent representations that can be useful as general features

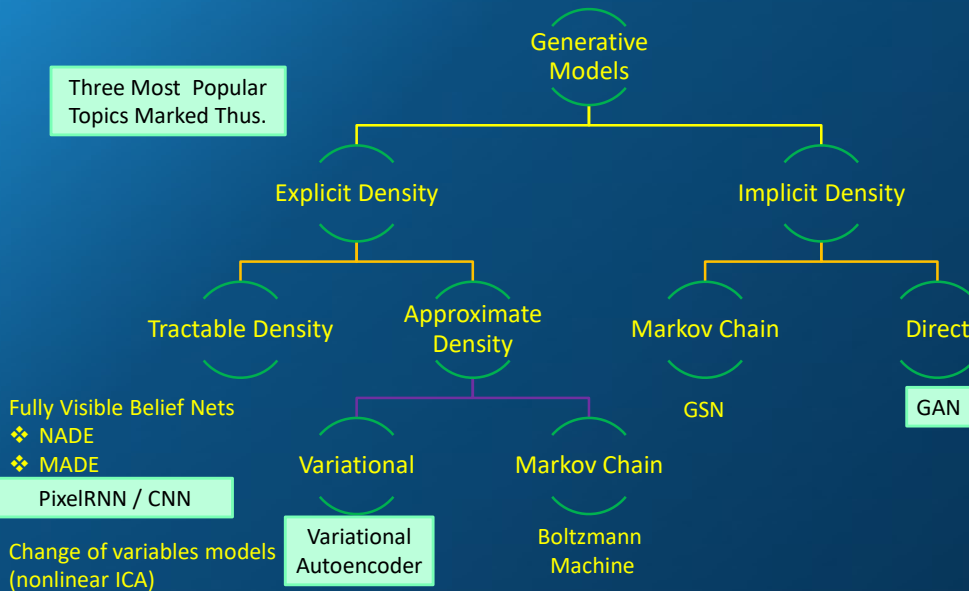
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## Taxonomy of Generative Models

Three Most Popular Topics Marked Thus.



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Figure adapted from Ian Goodfellow, Tutorial on Generative Adversarial Networks, 2017.

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## Fully Visible Belief Network

### Explicit Density Model

Use chain rule to decompose likelihood of an image  $x$  into product of 1-d distributions:

$$p(x) = \prod_{i=1}^n p(x_i | x_1, x_2, x_3 \dots x_{i-1})$$

Likelihood  
of image  $x$

Probability of  $i$ th pixel value  
given all previous pixels

Then maximize likelihood of training data

Note:

- Will need to define ordering of "previous pixels"
- Complex distribution over pixel values  $\rightarrow$  Express using a neural network!

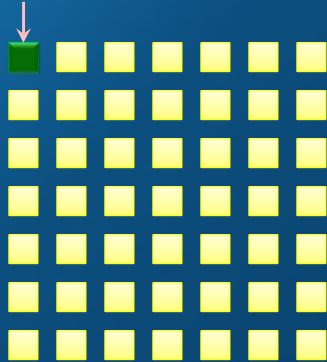
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## PixelRNN [van der Oord et al. 2016]

- Generate image pixels starting from corner
- Dependency on previous pixels modeled using an RNN (LSTM)



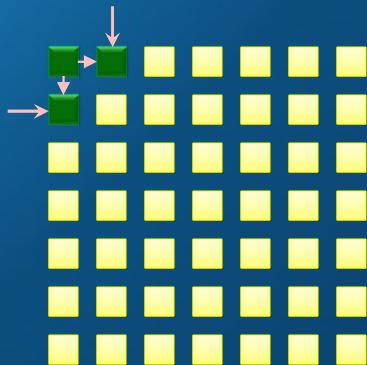
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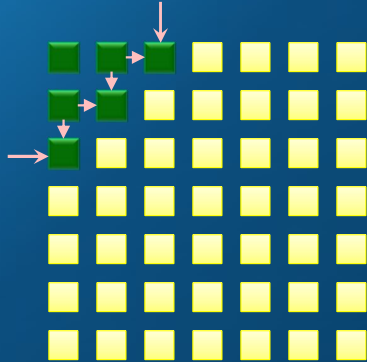
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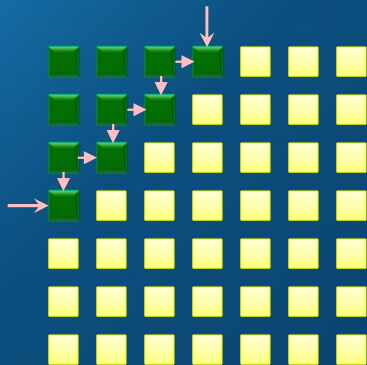
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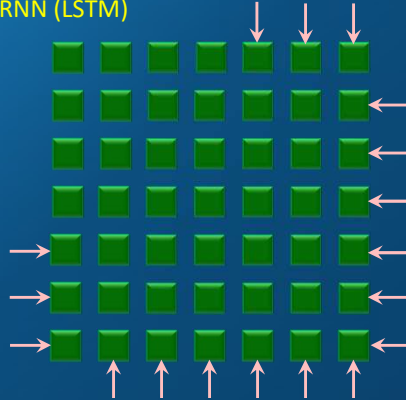
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## PixelRNN [van der Oord et al. 2016]

- Generate image pixels starting from corner
- Dependency on previous pixels modeled using an RNN (LSTM)



- Drawback:
  - ❖ Very sequential generation, very slow!

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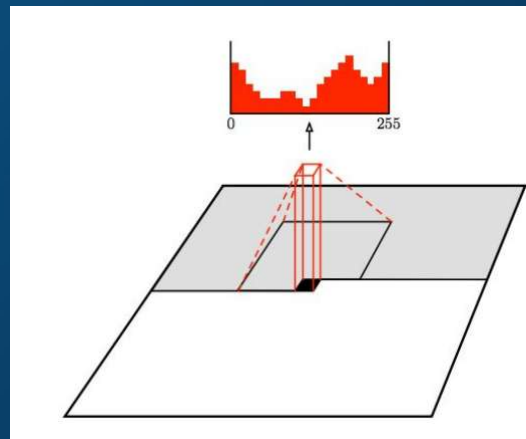
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## PixelCNN [van der Oord et al. 2016]

- PixelCNN also generates image pixels starting from corner,
- Dependency on previous pixels now modeled using a CNN over context region
- Training: maximize likelihood of training images

$$p(x) = \prod_{i=1}^n p(x_i | x_1, x_2, x_3 \dots x_{i-1})$$

- Training is faster than PixelRNN
  - ❖ can parallelize convolutions since context region values known from training images
- Generation must still proceed sequentially
  - ➔ still slow!



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## Generation Samples



32x32 CIFAR-10



32x32 ImageNet

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## PixelRNN and PixelCNN

### Pros:

- ❑ Can explicitly compute likelihood  $p(x)$
- ❑ Explicit likelihood of training data gives good evaluation metric
- ❑ Good samples

### Con:

- ❑ Sequential generation → slow

#### Reference

- Van der Oord et al. NIPS 2016
- Salimans et al. 2017 (PixelCNN++)

### Improving PixelCNN performance

- ❑ Gated convolutional layers
- ❑ Short-cut connections
- ❑ Discretized logistic loss
- ❑ Multi-scale
- ❑ Training tricks
- ❑ Etc...

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## Overview

- Four modern approaches to generative modeling:
  - ❖ **Generative adversarial networks**
  - ❖ Reversible architectures
  - ❖ Autoregressive models
  - ❖ **Variational autoencoders**
- All four approaches have different pros and cons
- In this session we will focus on
  - ❖ Variational autoencoders i.e. VAEs
  - ❖ Generative Adversarial Networks i.e. GANs

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## Variational Autoencoders (VAE)

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## Difference between PixelCNN and VAE

- PixelCNNs define tractable density function, optimize likelihood of training data:

$$p(x) = \prod_{i=1}^n p(x_i | x_1, x_2, x_3 \dots x_{i-1})$$

- VAEs define intractable density function with latent  $z$ :

$$p_{\theta}(x) = \int p_{\theta}(z) p_{\theta}(x|z) dz$$

- Cannot optimize directly,
  - ❖ So we derive and optimize lower bound on likelihood instead
- Too lengthy, remained theoretical discussions...
- What if we give up on explicitly modeling density, and just want ability to sample?

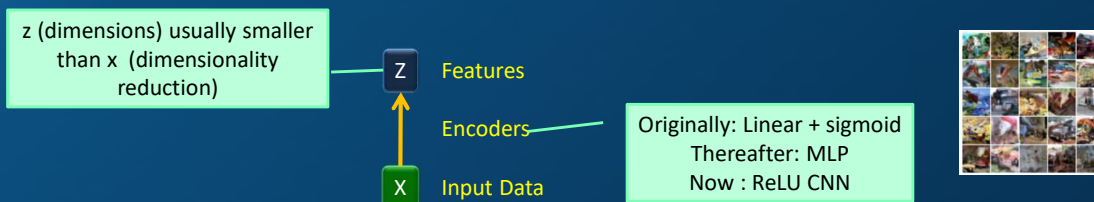
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## Background: Autoencoders

- Unsupervised approach for learning a lower-dimensional feature representation from unlabeled training data
- How to learn these features
  - ❖ Train such that features can be used to reconstruct original data
  - ❖ “Autoencoding” – encoding itself.



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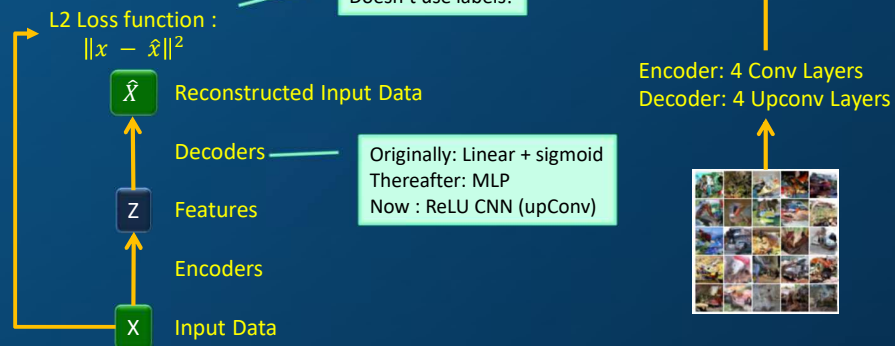
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## Background: Autoencoders

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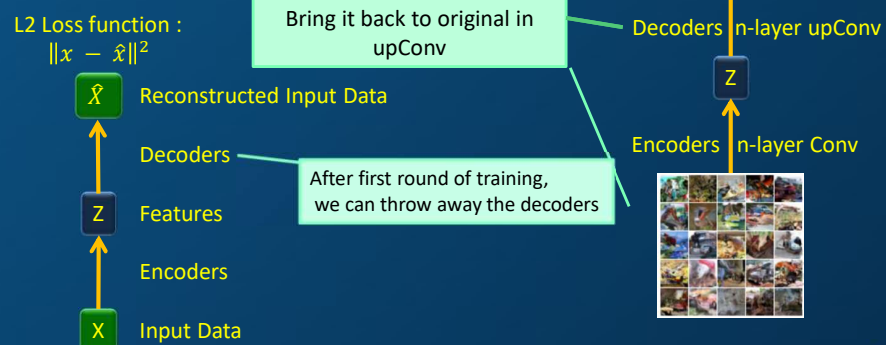
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## Background: Autoencoders

- Unsupervised approach for learning a lower-dimensional feature representation from unlabeled training data

- How to learn these features

- ❖ Train such that features can be used to reconstruct original data
- ❖ “Autoencoding” – encoding itself.



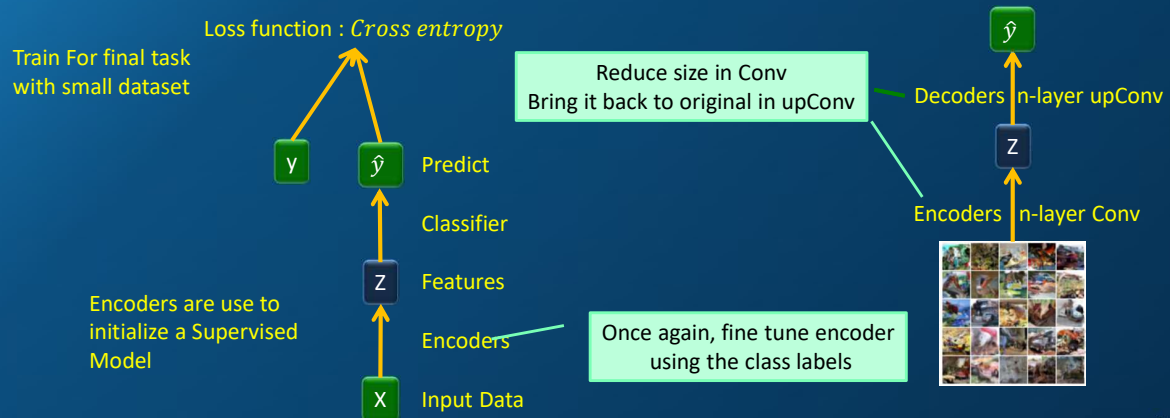
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## Autoencoders

- Now job of decoder is done and we have optimized weights of the Encoder
- Use this encoder for your analysis



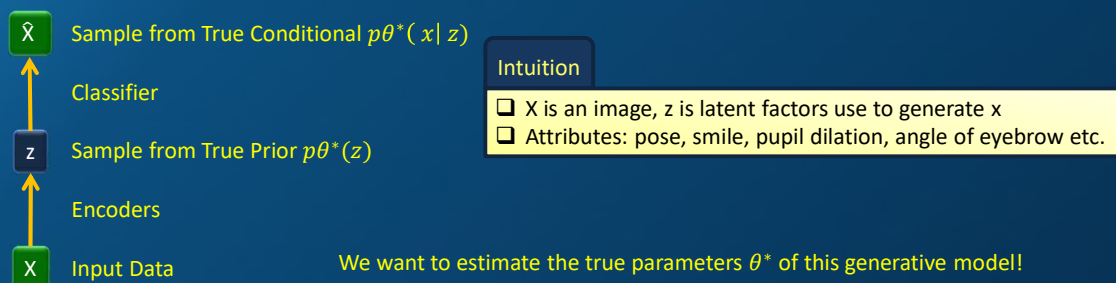
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## Variational Autoencoders

- Probabilistic spin on auto encoders
  - Will let us sample from the generated data
- Assume that Training data is generated from some underlying unobserved (latent) representation  $z$



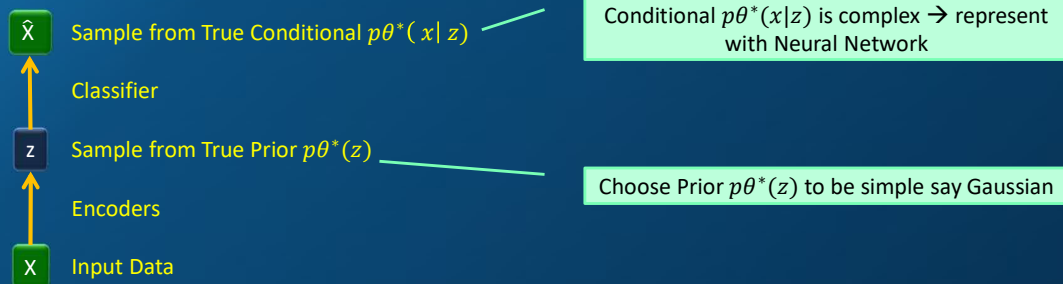
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## Variational Autoencoders

- We want to estimate the true parameters  $\theta^*$  of this generative model!
- How should we represent this model?



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## Variational Autoencoders

- Straightforward way is to maximize likely hood of data model
  - ❖  $p_\theta(x) = \int p_\theta(z) * p_\theta(x|z) * dz$
  - ❖ We need to integrate as we are looking at all possible values of x
  - ❖ Hence it is not tractable.
- In details: data likelihood  $p_\theta(x) = \int p_\theta(z) * p_\theta(x|z) * dz$ 
  - ❖  $p_\theta(z) \rightarrow$  ok, we can use Gaussian Prior probabilities
  - ❖  $p_\theta(x|z) \rightarrow$  Ok too as we can use a decode Neural Network
  - ❖ Integration is a problem, as we need to look at all possible values of z
- It turns out that posterior  $p_\theta(x|z)$  is also intractable (difficult to converge)
  - ❖  $p_\theta(z|x) = p_\theta(x|z) * \frac{p_\theta(z)}{p_\theta(x)}$
- Solution:
  - ❖ Decoder model for  $p_\theta(x|z)$  and a separate encoder model  $q_\theta(z|x)$

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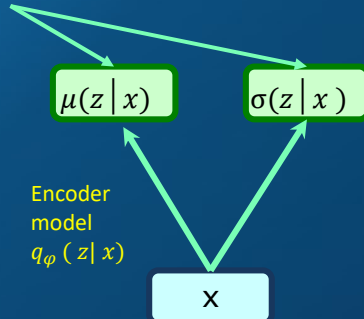
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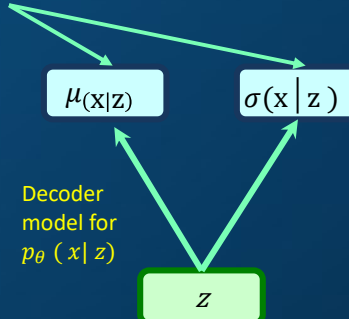
## Variational Autoencoder

- Since we are modeling probabilistic data generation, encoder and decoder networks are probabilistic

Mean and covariance of  $z|x$



Mean and covariance of  $x|z$



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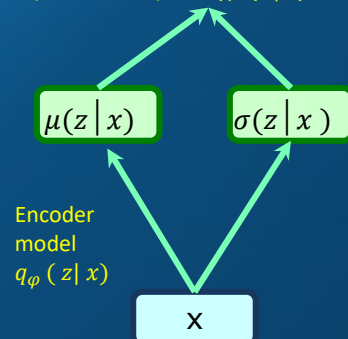
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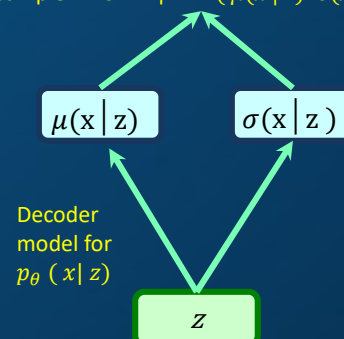
## Variational Autoencoder

- Since we are modeling probabilistic data generation, encoder and decoder networks are probabilistic

Sample  $z$  from  $z|x \sim N(\mu(z|x), \sigma(z|x))$



Sample  $x$  from  $x|z \sim N(\mu(x|z), \sigma(x|z))$



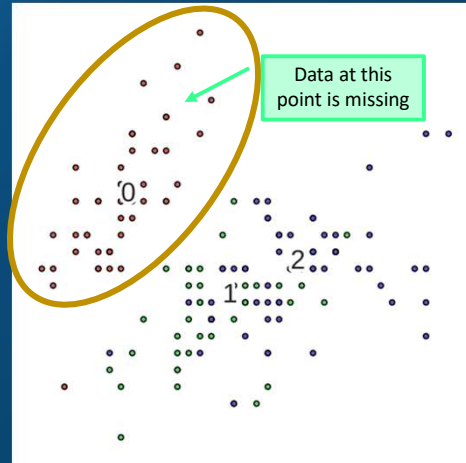
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## Missing Data make it Intractable



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## Explicit Density Models

- PixelCNNs define tractable density function, optimize likelihood of training data:

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$$p_{\theta}(x) = \int p_{\theta}(z) p_{\theta}(x|z) dz$$

- Cannot optimize directly, derive and optimize lower bound on likelihood instead
- Too lengthy, remained theoretical discussions...
- What if we give up on explicitly modeling density, and just want ability to sample?
- GANs: don't work with any explicit density function! Instead, take game-theoretic approach: learn to generate from training distribution through 2-player game

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## Generative Adversarial Networks

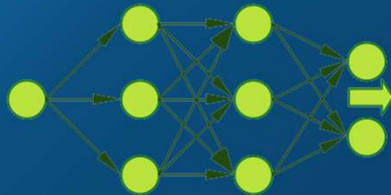
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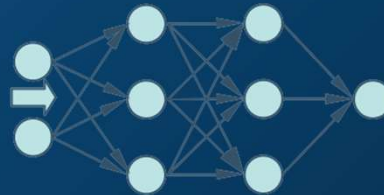
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## Generative Adversarial Networks

- The idea behind Generative Adversarial Networks (GANs): train two different networks
  - ❖ The generator network tries to produce realistic-looking samples
  - ❖ The discriminator network tries to figure out whether an image came from the training set or the generator network
- The generator network tries to fool the discriminator network



Generator



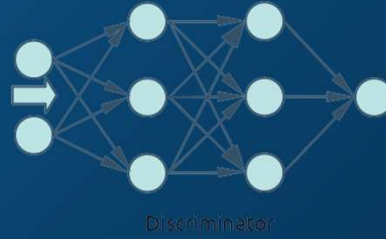
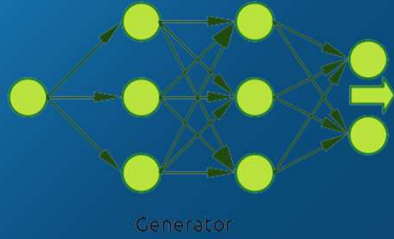
Discriminator

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## Generative Adversarial Network

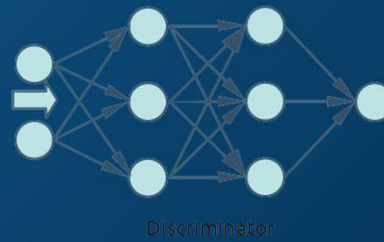
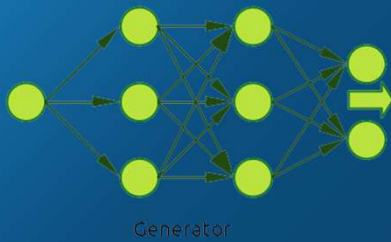


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## Generative Adversarial Network

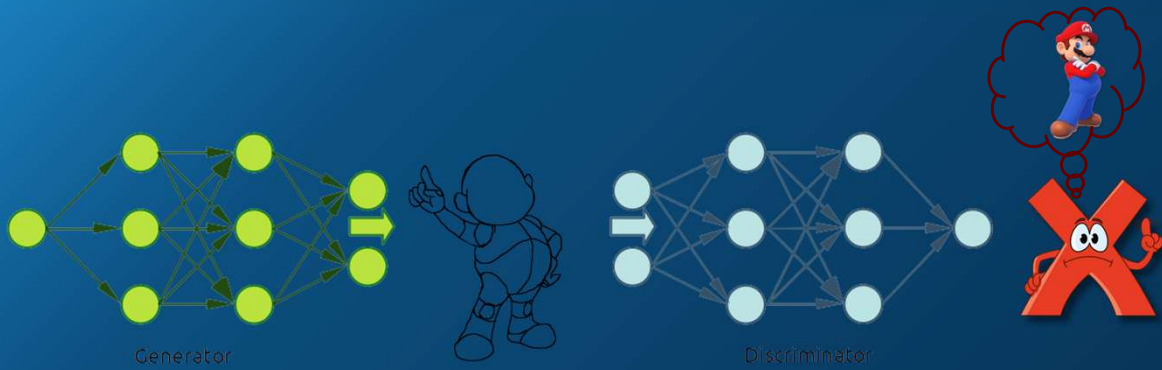


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## Generative Adversarial Network

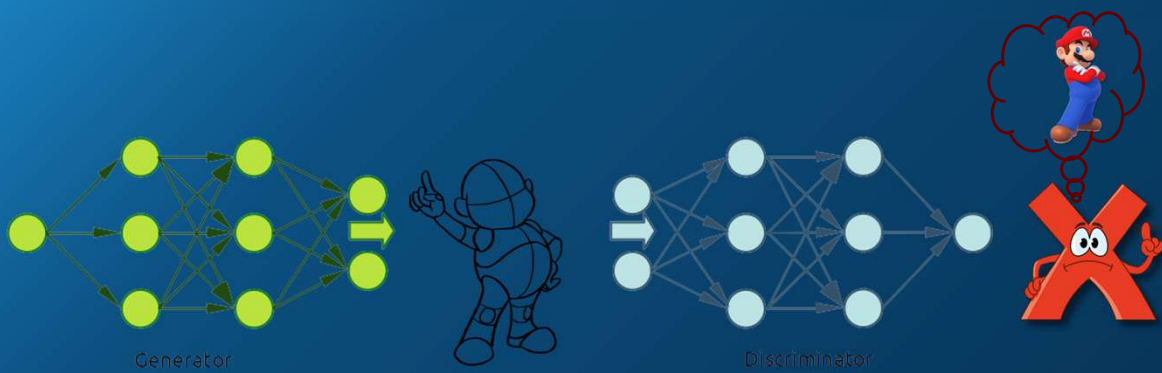


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## Generative Adversarial Network

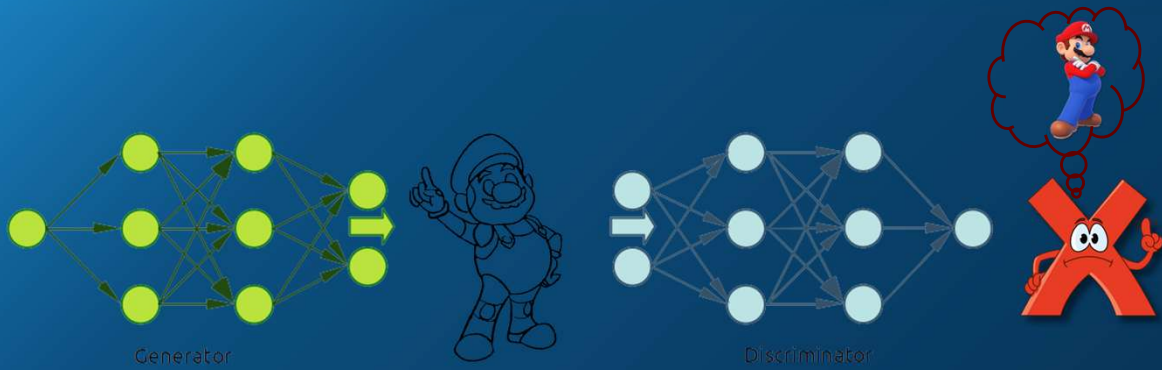


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## Generative Adversarial Network

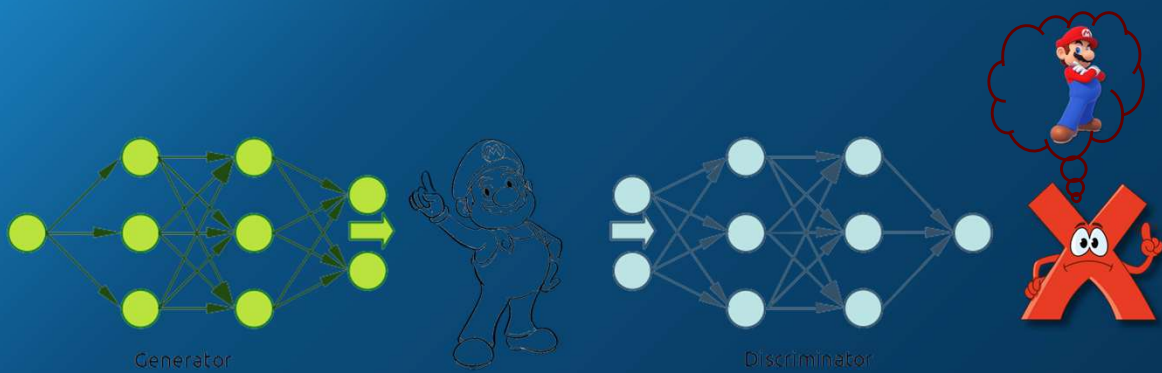


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## Generative Adversarial Network

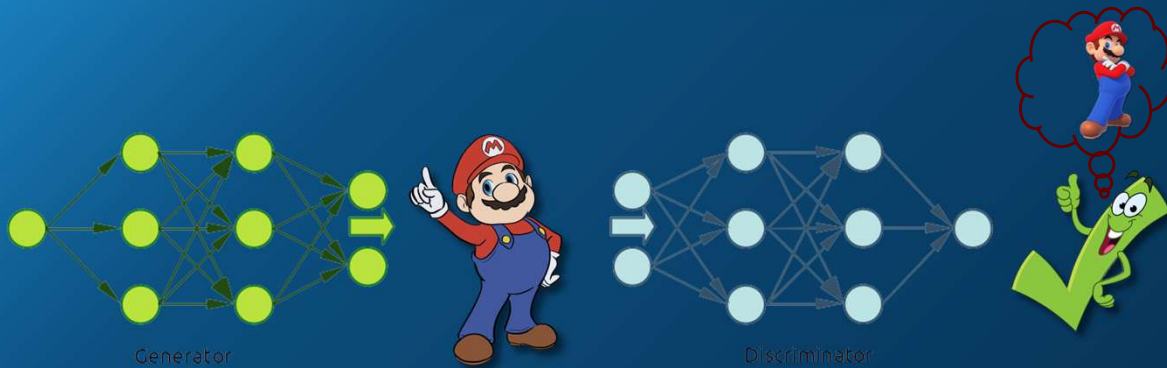


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## Generative Adversarial Network

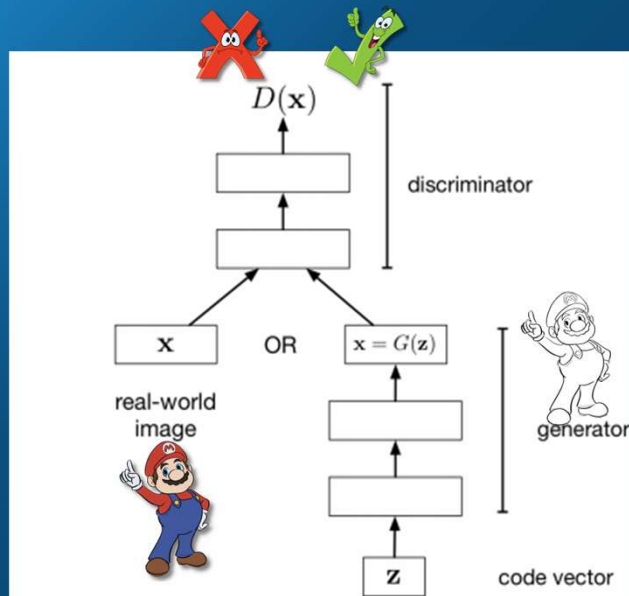


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## Generative Adversarial Networks



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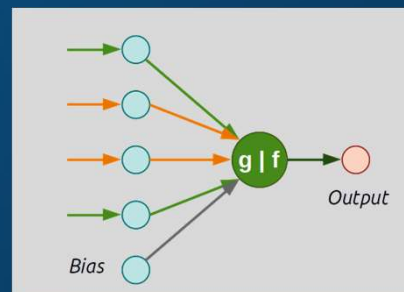
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- Discriminator network is trained on real images as well as generated images
- Generator network: try to fool the discriminator by generating real-looking images
- Discriminator network: try to distinguish between real and fake images

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## Coding Gan

- Imagine a simplest 2 x 2 images
  - ❖ Depending upon features these shades may vary
- Let's also consider our simplest neural network



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## GAN

- Imagine all images are slanted backward by 45°
- We have following images of faces



- The corresponding pixel on the images will be as follows:



- For argument sake let's take white pixel as 0 and black as 1
  - ❖ Gray shades will be somewhere in between



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## GAN

- We have following images of faces



- Images containing no face will appear as follows:



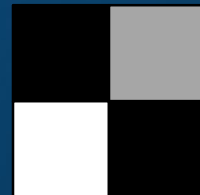
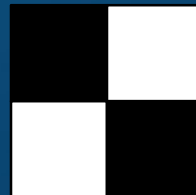
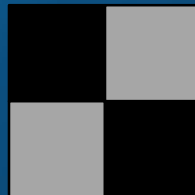
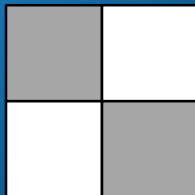
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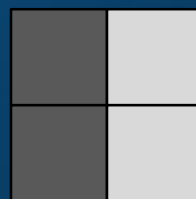
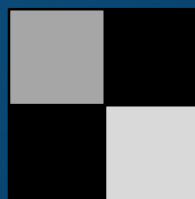
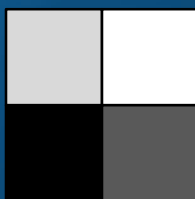
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## What Agent will see

- Faces



- No Faces



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## What Agent will see

### □ Faces

0.75	0
0	0.75



1	0.5
0.5	1

1	0
0	1

1	0.25
	1

### □ No Faces

0.25	0
1	0.75

0.75	1
1	0.25

0.75	0.25
0.75	0.25

1	1
0	0.25

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Discriminator

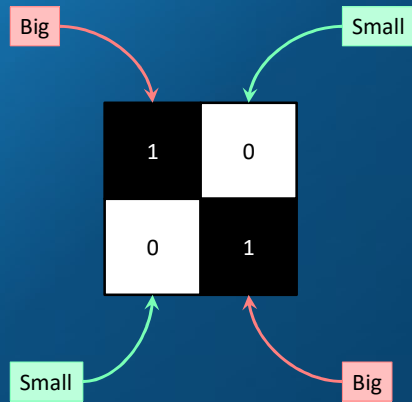
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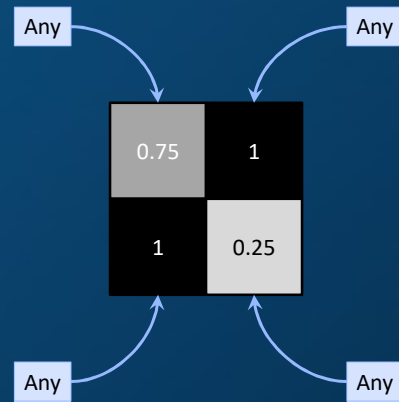
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## Discriminator

### □ Faces



### □ Noise



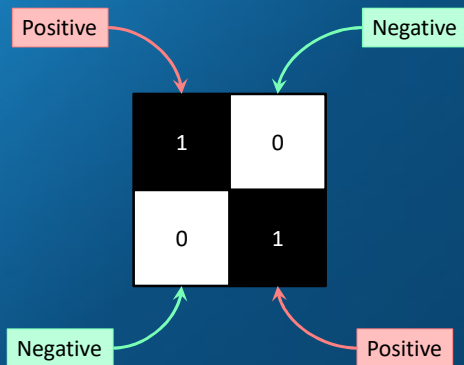
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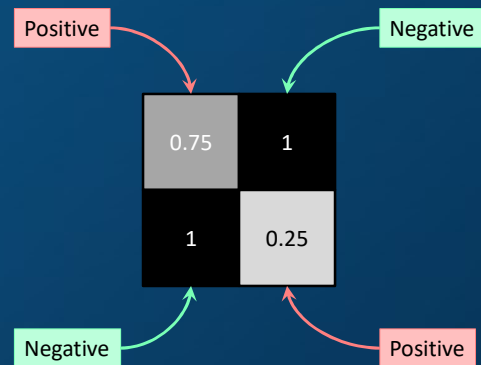
## Discriminator

### □ Faces



$$\square 1 * 1 + 1 * 1 + 0 * (-1) + 0 * (-1) = 2.0$$

### □ Noise



$$\square 0.75 * 1 + 0.25 * 1 + 1 * (-1) + 1 * (-1) = -1.0$$

Considering threshold as 0.0 (arbitrary), we can safely assume:

- ❖ Positive value → Face
- ❖ Negative value → No Face

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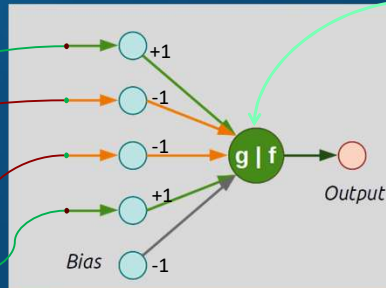
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## Discriminator

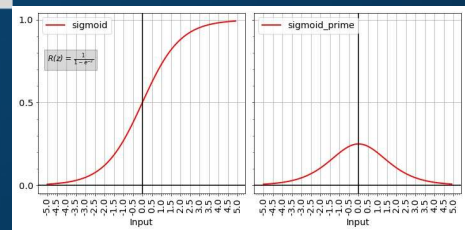


1	0
0	1



$$g = +1 * 1 + 0 * (-1) + 0 * (-1) + 1 * 1 - 1 = 1$$

$$f = \sigma(g) \rightarrow \text{output} = 0.73$$



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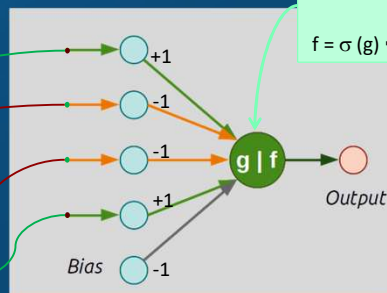
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## Discriminator



0.25	1
0.5	0.75



$$g = +0.25 * 1 + 1 * (-1) + 0.5 * (-1) + 0.75 * 1 - 1 = -1.5$$

$$f = \sigma(g) \rightarrow \text{output} = 0.18$$

□ Thus

- ❖ for  $f > 0.5$  it is face
- ❖ for  $f < 0.5$  it is not a face

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## Discriminator

□ Imagine all images are slanted backward by 45°



0.5	0
0	0.5



1	0.5
0.5	1



1	0
0	1



1	0.5
0	1



0.25	1
0.5	0.75

□ So the discriminator knows that following:

❖ Face


Not a Face


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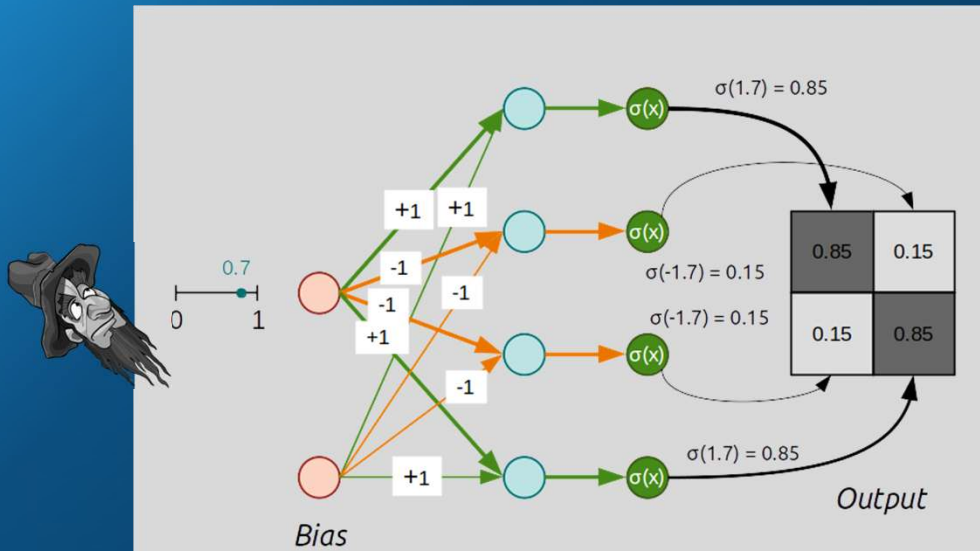
## Generator

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## Generator

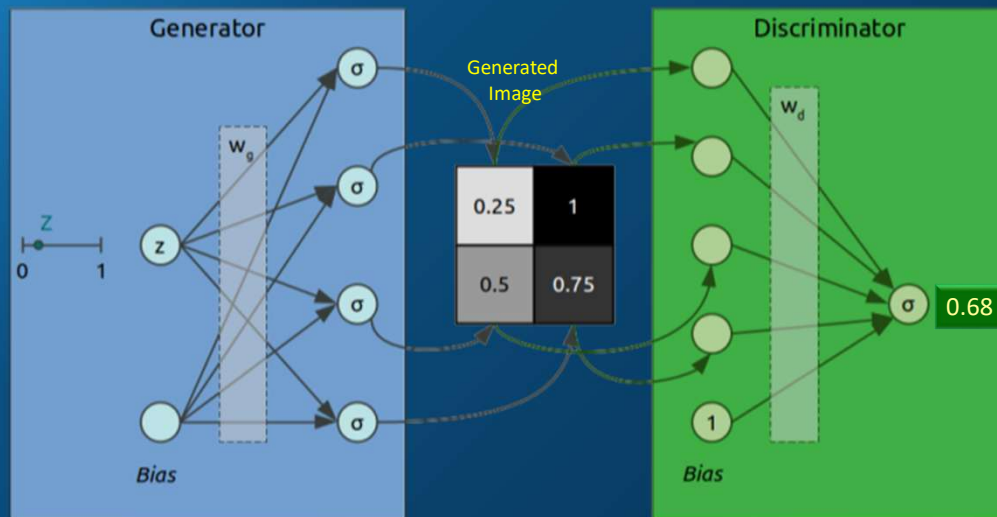


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## Error Functions



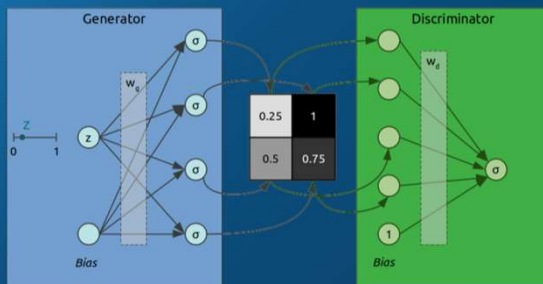
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Generator is Max and Discriminator is Min

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## Error Functions



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- ❑ Generator and Discriminators are working against each other
- ❑ Discriminator tries to generate label as close to 0 as possible ( Claiming it is fake)
  - ❖ Error function =  $-\log(1-p)$
- ❑ Generator tries to generate labels as close to 1 as possible (Claiming it to be an image)
  - ❖ Error function =  $-\log(p)$

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## Error Functions

### Discriminator

- ❑ If our value 0 and prediction is 0.1 → error is small
- ❑ If our value is 0 and prediction is 0.9 → error is large
- ❑ Consider negative log error
  - ❖ For pred = 0.1; error =  $-\ln(1 - 0.1) = 0.11$
  - ❖ For pred = 0.9 error =  $-\ln(1 - 0.9) = 2.30$
- ❑ Thus our error function is:
  - ❖  $-\ln(1-\text{pred})$

### Generator

- ❑ If our value 1 and prediction is 0.1 → error is large
- ❑ If our value is 1 and prediction is 0.9 → error is small
- ❑ Consider negative log error
  - ❖ For pred = 0.1; error =  $-\ln(0.1) = 2.30$
  - ❖ For pred = 0.9 error =  $-\ln(0.9) = 0.1$
- ❑ Thus our error function is:
  - ❖  $-\ln(\text{pred})$

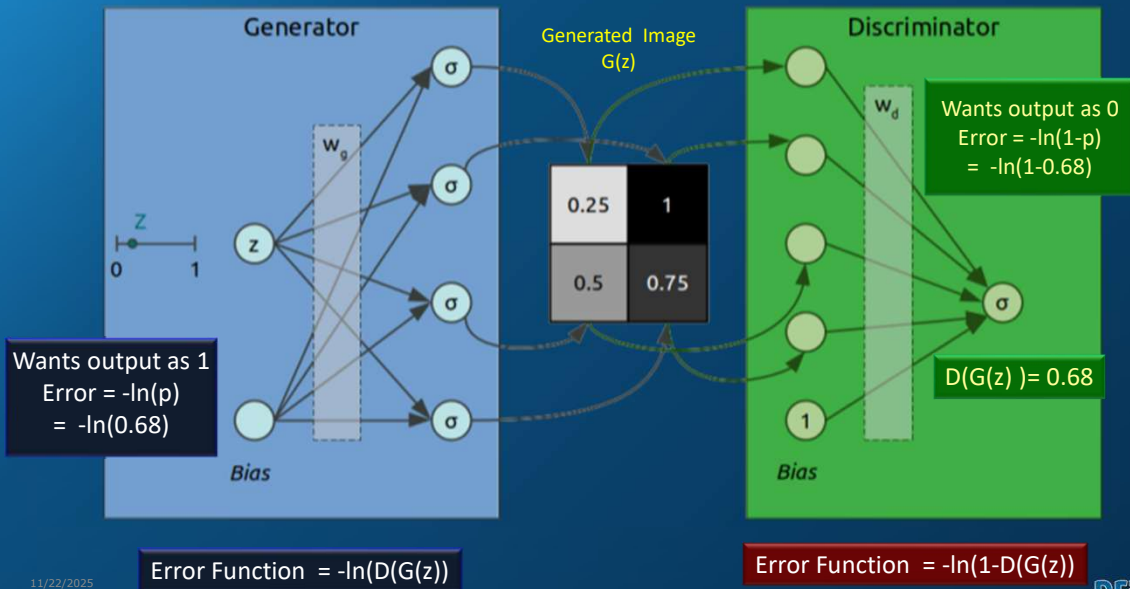
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## Error Functions



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## Three Reasons that it's a Miracle GANs Work

- ❑ G has a reinforcement learning task
  - ❖ It knows when it does good (i.e., fools D) but it is not given a supervised signal
  - ❖ Reinforcement learning is hard
  - ❖ Back prop through D provides G with a supervised signal; the better D is, the better this signal will be
- ❑ Can't describe optimum via a single loss
  - ❖ Will there be an equilibrium?
- ❑ D is seldom fooled
  - ❖ But G still learns because it gets a gradient telling it how to change in order to do better the next round.

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## Training GANs: Two-player game

□ Generator network: try to fool the discriminator by generating real-looking images

□ Discriminator network: try to distinguish between real and fake images

□ Train jointly in MiniMax game

□ MiniMax objective function:

$$\min_{\theta_g} \max_{\theta_d} [E_{x \sim p_{data}} \log D_{\theta_d}(x) + E_{z \sim p(z)} \log(1 - D_{\theta_d}(G_{\theta_g}(z)))]$$

□ Discriminator outputs likelihood in (0,1) of real image

□ Discriminator ( $\theta_d$ ) wants to maximize objective such that  $D(x)$  is close to 1 (real) and  $D(G(z))$  is close to 0 (fake)

□ Generator ( $\theta_g$ ) wants to minimize objective such that  $D(G(z))$  is close to 1

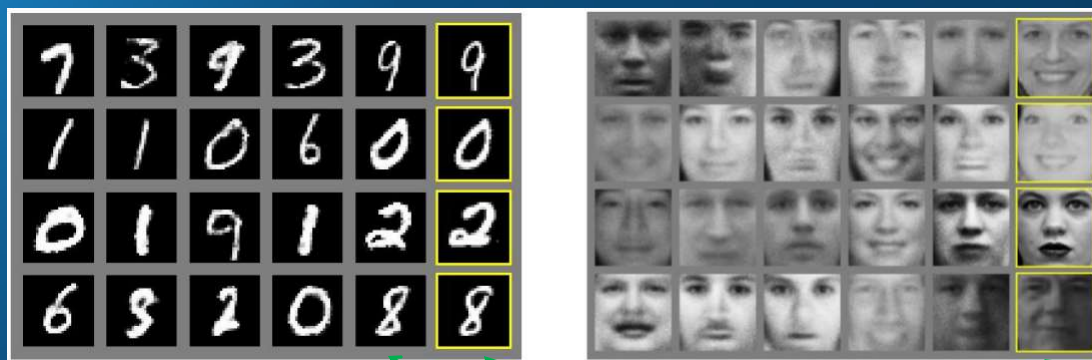
❖ Discriminator is fooled into thinking generated  $G(z)$  is real

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## Generative Adversarial Nets



Nearest neighbor from training set

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## Reflect...

- ❑ Which of the following are key components of a Generative Adversarial Network (GAN)?
  - a. Generator
  - b. Discriminator
  - c. Classifier
  - d. Loss function
- ❑ Answer : a, b, d
  
- ❑ Select the statements that correctly describe the training process of a GAN.
  - a. The generator aims to produce data that is indistinguishable from real data.
  - b. The discriminator provides feedback to the generator about the generated samples.
  - c. GANs are trained using supervised learning techniques.
  - d. The loss function for GANs involves both a generator loss and a discriminator loss.
- ❑ Answer: a, b, d

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- ❑ Which applications can benefit from the use of Generative Adversarial Networks?
  - a. Image generation
  - b. Style transfer
  - c. Text summarization
  - d. Speech recognition
- ❑ Answer : a, b, d
  
- ❑ What is the purpose of the generator in a GAN?
  - a. To discriminate between real and fake data.
  - b. To generate synthetic data.
  - c. To evaluate the quality of generated samples.
  - d. To provide feedback to the discriminator.
- ❑ Answer : b

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## Reflect...

- ❑ Choose the correct statements regarding the mode collapse phenomenon in GANs.
  - a. Mode collapse occurs when the generator produces diverse samples covering the entire data distribution.
  - b. Mode collapse happens when the generator focuses on generating only a limited set of samples.
  - c. Mode collapse is a desired behavior in GAN training.
  - d. Mode collapse is related to the overfitting of the discriminator.
- ❑ Answer : b
  
- ❑ Which regularization techniques are commonly used to stabilize GAN training?
  - a. Dropout
  - b. Batch normalization
  - c. L1 regularization
  - d. Gradient clipping
- ❑ Answer : a, b, d

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- ❑ Select the statements that correctly describe the challenges associated with training Generative Adversarial Networks.
  - a. GANs may suffer from mode collapse.
  - b. Training GANs can be unstable.
  - c. GANs always converge to a globally optimal solution.
  - d. GANs require a large amount of labeled training data.
- ❑ Answer: a, b
  
- ❑ What is the role of the discriminator in a GAN?
  - a. To generate synthetic data.
  - b. To evaluate the quality of generated samples.
  - c. To provide feedback to the generator.
  - d. To discriminate between real and fake data.
- ❑ Answer: d

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