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Technologies with Conflicting Goals



Image based CAPTCHA (Completely Automated Public Turing test to tell Computers and Humans Apart) is a type of **security measure** known as challenge-response authentication



Generative Adversarial Networks

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Unbelievably Real

- This person does not exist : thispersondoesnotexist.com



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Overview

- ❑ Developed by Ian Goodfellow
- ❑ In generative modeling, we'd like to train a network that models a distribution,
 - ❖ Such as a distribution over images.
- ❑ One way to judge the quality of the model is to sample from it
- ❑ Active area of research with rapid progress

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|---------------|
| 1 6 4 1 4 1 0 |
| 7 2 8 8 4 9 4 |
| 8 3 7 4 0 4 4 |
| 3 7 2 1 7 7 7 |
| 7 4 4 4 1 0 9 |
| 3 0 5 9 5 2 7 |
| 5 1 9 8 1 9 6 |

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2009



CC-LAPGAN: Dog

2015



2018

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Take a Step Back

Supervised Learning

- ❑ Data: (x, y)
 - ❖ x is data, y is label
- ❑ Goal: Learn a function to map $x \rightarrow y$
- ❑ Examples:
 - ❖ Classification,
 - ❖ Regression,
 - ❖ Object detection,
 - ❖ Semantic segmentation,
 - ❖ Image captioning,
 - ❖ ...

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Unsupervised Learning

- ❑ Data: x
 - ❖ Just data, no labels!
- ❑ Goal: Learn some underlying hidden structure of the data
- ❑ Examples:
 - ❖ Clustering,
 - ❖ Dimensionality reduction,
 - ❖ Feature learning,
 - ❖ Density estimation,
 - ❖ ...

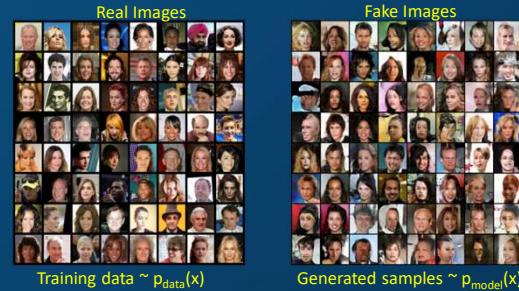
Makes Training
data cheap!

Holy grail:
Solve unsupervised learning
→ Understand structure of
visual world

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Generative Models

- Given the training data, generate new samples from same distribution



- Want to learn $p_{model}(x)$ similar to $p_{data}(x)$

- Addresses density estimation, a core problem in unsupervised learning

- Several flavors:

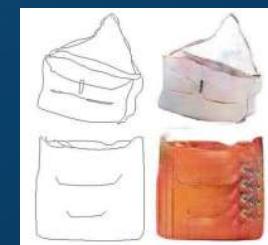
- Explicit density estimation: explicitly define and solve for $p_{model}(x)$
- Implicit density estimation: learn model that can sample from $p_{model}(x)$ without explicitly defining it

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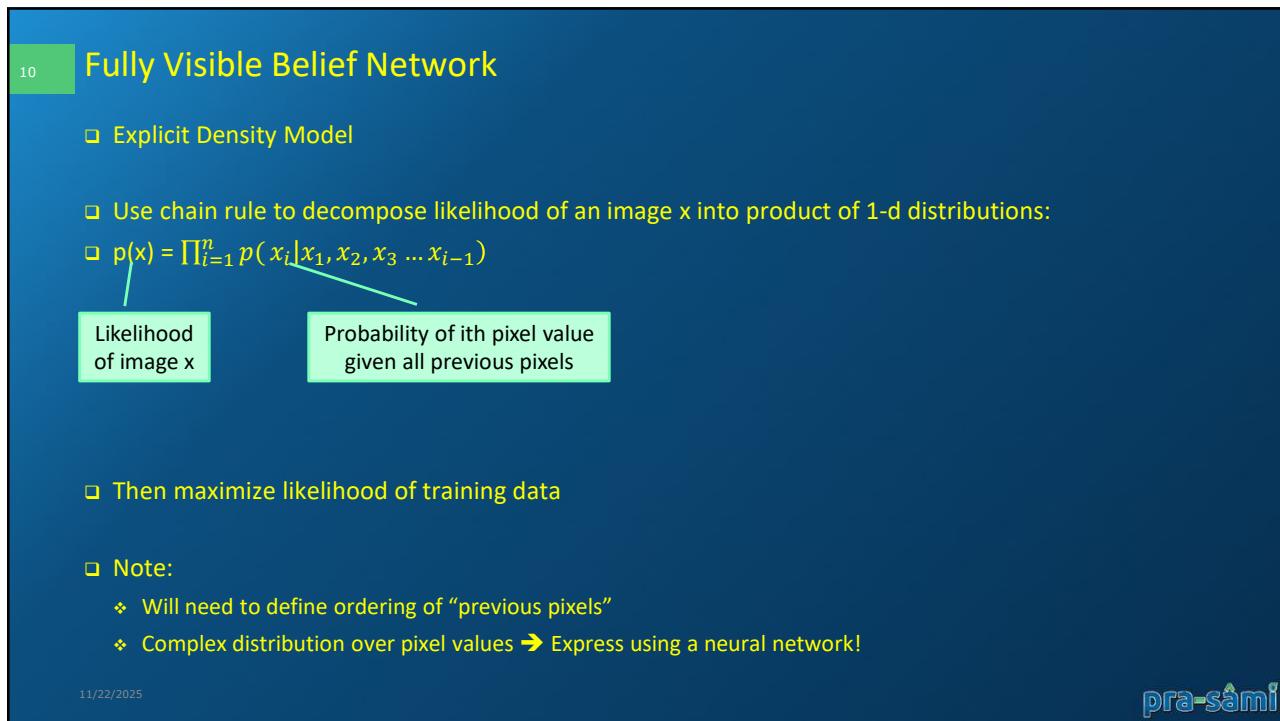
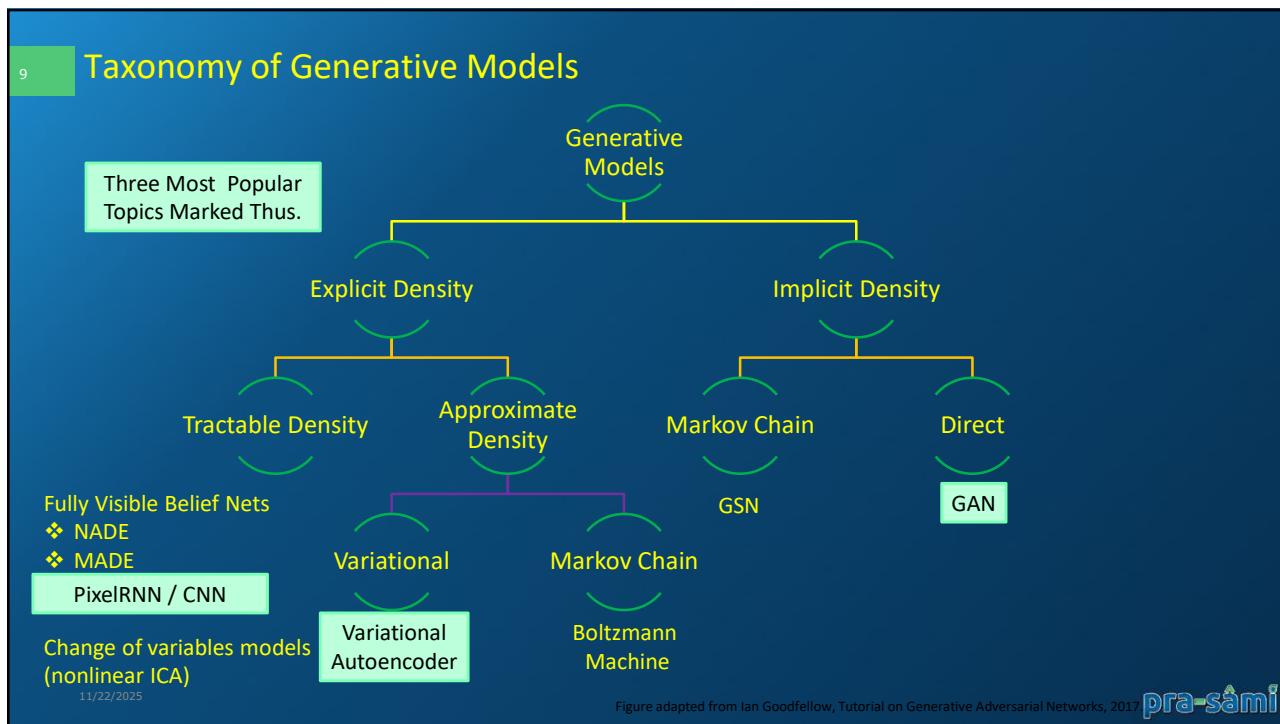
Why Generative Models?

- Realistic samples for artwork, super-resolution, colorization, etc.



- Generative models of time-series data can be used for simulation and planning
 - Such as reinforcement learning applications!
- Training generative models can also enable inference of latent representations that can be useful as general features

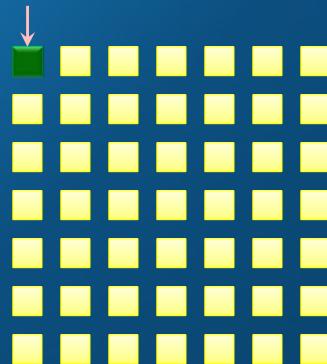
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PixelRNN [van der Oord et al. 2016]

- Generate image pixels starting from corner
- Dependency on previous pixels modeled using an RNN (LSTM)



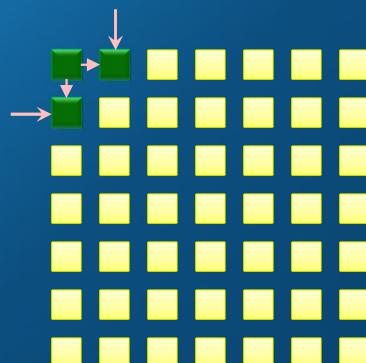
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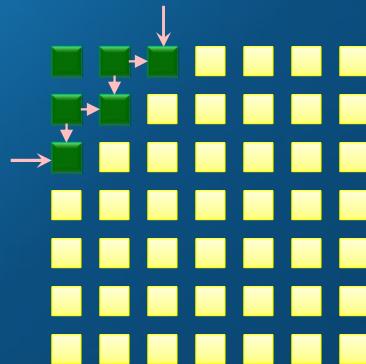
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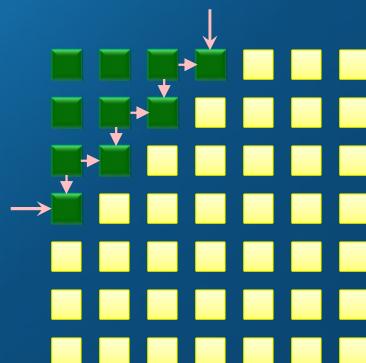


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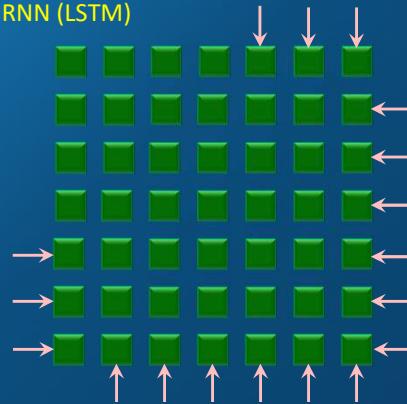


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PixelRNN [van der Oord et al. 2016]

- Generate image pixels starting from corner
- Dependency on previous pixels modeled using an RNN (LSTM)



- Drawback:
 - ❖ Very sequential generation, very slow!

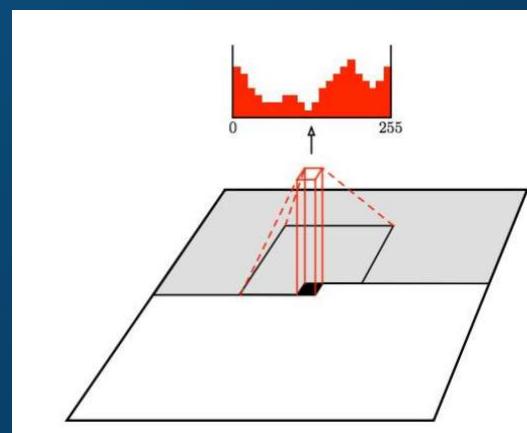
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PixelCNN [van der Oord et al. 2016]

- PixelCNN also generates image pixels starting from corner,
- Dependency on previous pixels now modeled using a CNN over context region
- Training: maximize likelihood of training images

$$p(x) = \prod_{i=1}^n p(x_i|x_1, x_2, x_3 \dots x_{i-1})$$
- Training is faster than PixelRNN
 - ❖ can parallelize convolutions since context region values known from training images
- Generation must still proceed sequentially
 ➔ still slow!



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Generation Samples



32x32 CIFAR-10



32x32 ImageNet

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PixelRNN and PixelCNN

Pros:

- Can explicitly compute likelihood $p(x)$
- Explicit likelihood of training data gives good evaluation metric
- Good samples

Con:

- Sequential generation → slow

Reference

- Van der Oord et al. NIPS 2016
- Salimans et al. 2017 (PixelCNN++)

Improving PixelCNN performance

- Gated convolutional layers
- Short-cut connections
- Discretized logistic loss
- Multi-scale
- Training tricks
- Etc...

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Overview

- Four modern approaches to generative modeling:
 - ❖ Generative adversarial networks
 - ❖ Reversible architectures
 - ❖ Autoregressive models
 - ❖ Variational autoencoders
- All four approaches have different pros and cons
- In this session we will focus on
 - ❖ Variational autoencoders i.e. VAEs
 - ❖ Generative Adversarial Networks i.e. GANs

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Variational Autoencoders (VAE)

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Difference between PixelCNN and VAE

- PixelCNNs define tractable density function, optimize likelihood of training data:

$$p(x) = \prod_{i=1}^n p(x_i|x_1, x_2, x_3 \dots x_{i-1})$$

- VAEs define intractable density function with latent z:

$$p_\theta(x) = \int p_\theta(z)p_\theta(x|z)dz$$

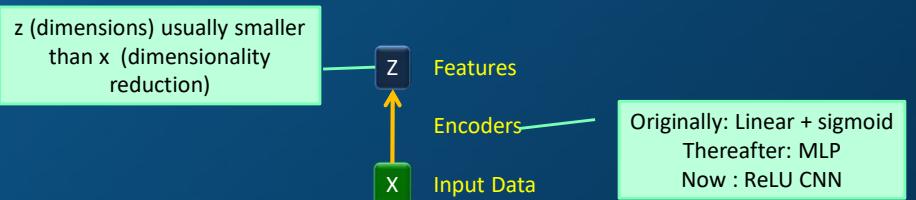
- Cannot optimize directly,
 - So we derive and optimize lower bound on likelihood instead
- Too lengthy, remained theoretical discussions...
- What if we give up on explicitly modeling density, and just want ability to sample?

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Background: Autoencoders

- Unsupervised approach for learning a lower-dimensional feature representation from unlabeled training data
- How to learn these features
 - Train such that features can be used to reconstruct original data
 - “Autoencoding” – encoding itself.



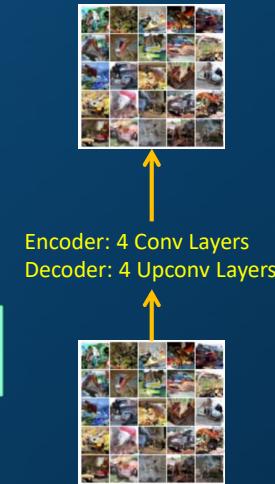
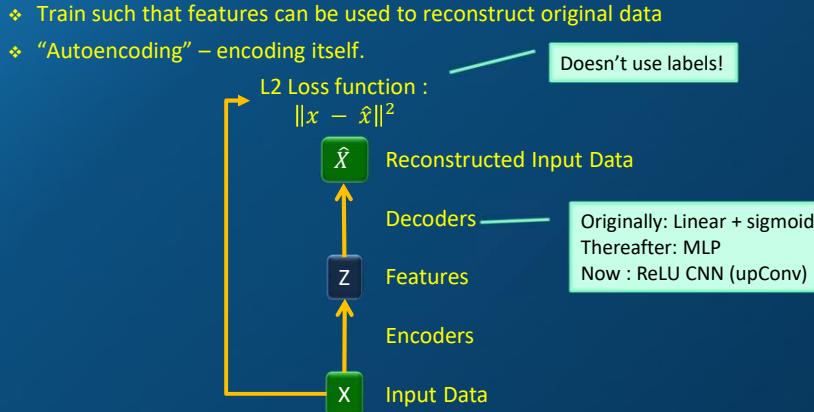
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Background: Autoencoders

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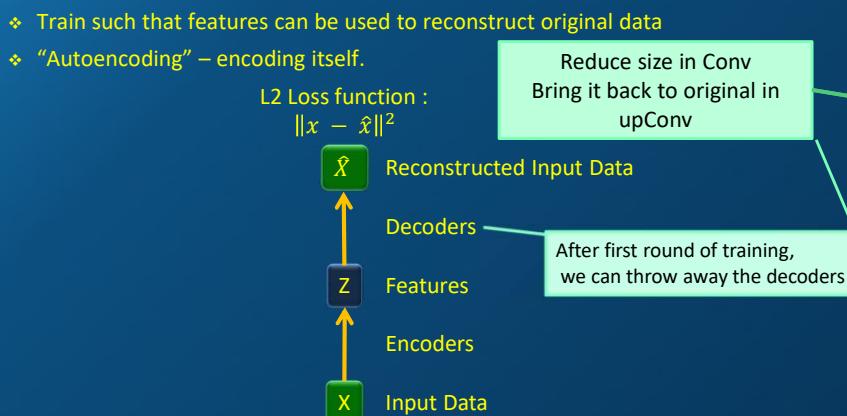
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Background: Autoencoders

- Unsupervised approach for learning a lower-dimensional feature representation from unlabeled training data

- How to learn these features
 - Train such that features can be used to reconstruct original data
 - “Autoencoding” – encoding itself.



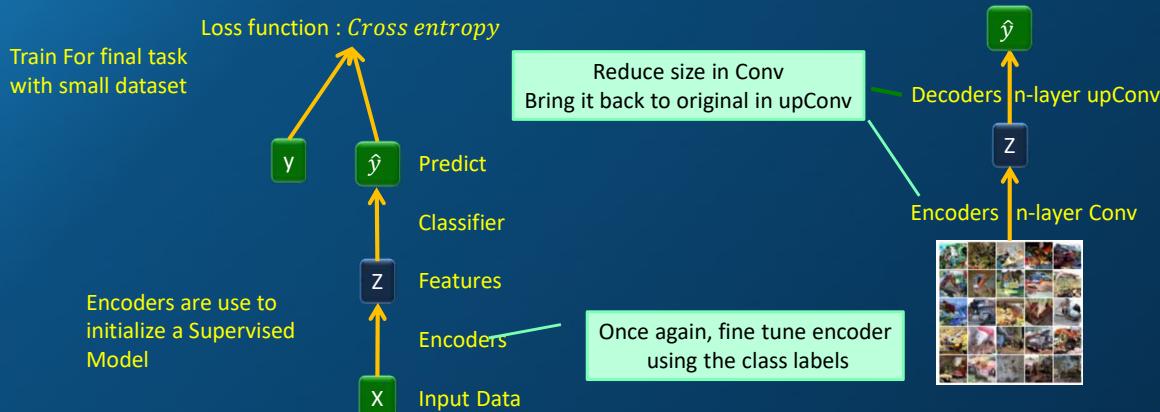
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Autoencoders

- Now job of decoder is done and we have optimized weights of the Encoder
- Use this encoder for your analysis



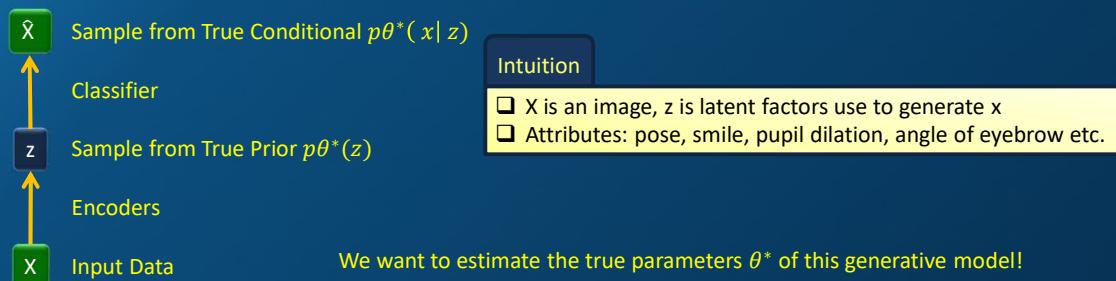
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Variational Autoencoders

- Probabilistic spin on auto encoders
 - Will let us sample from the generated data
- Assume that Training data is generated from some underlying unobserved (latent) representation z



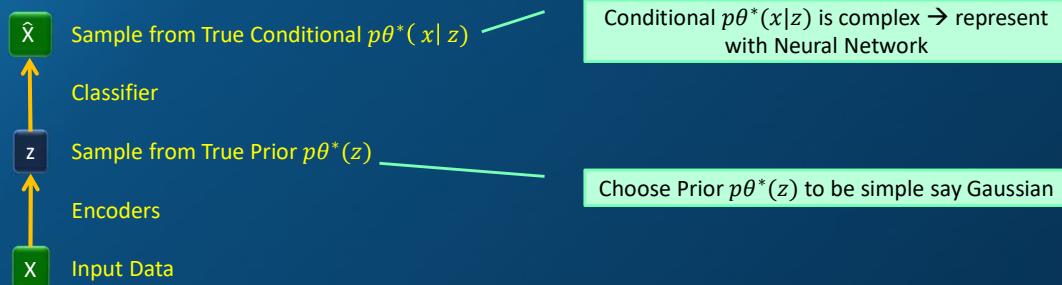
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Variational Autoencoders

- We want to estimate the true parameters θ^* of this generative model!
- How should we represent this model?



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Variational Autoencoders

- Straightforward way is to maximize likelihood of data model
 - ❖ $p_{\theta}(x) = \int p_{\theta}(z) * p_{\theta}(x|z) * dz$
 - ❖ We need to integrate as we are looking at all possible values of x
 - ❖ Hence it is not tractable.
- In details: data likelihood $p_{\theta}(x) = \int p_{\theta}(z) * p_{\theta}(x|z) * dz$
 - ❖ $p_{\theta}(z) \rightarrow$ ok, we can use Gaussian Prior probabilities
 - ❖ $p_{\theta}(x|z) \rightarrow$ Ok too as we can use a decode Neural Network
 - ❖ Integration is a problem, as we need to look at all possible values of z
- It turns out that posterior $p_{\theta}(x|z)$ is also intractable (difficult to converge)
 - ❖ $p_{\theta}(z|x) = p_{\theta}(x|z) * \frac{p_{\theta}(z)}{p_{\theta}(x)}$
- Solution:
 - ❖ Decoder model for $p_{\theta}(x|z)$ and a separate encoder model $q_{\theta}(z|x)$

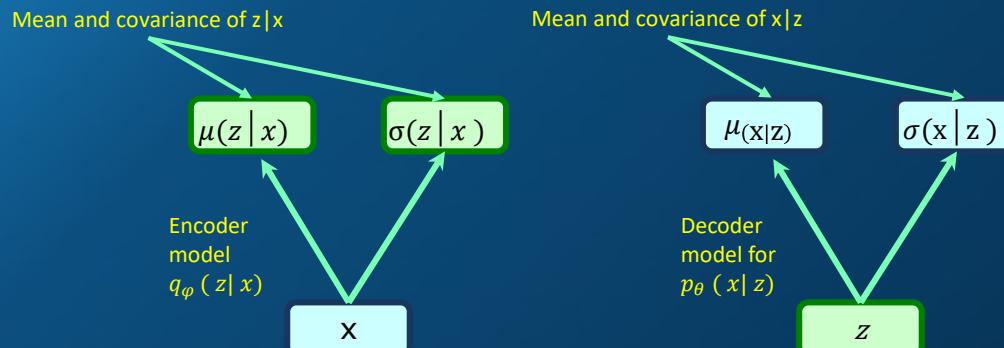
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Variational Autoencoder

- Since we are modeling probabilistic data generation, encoder and decoder networks are probabilistic



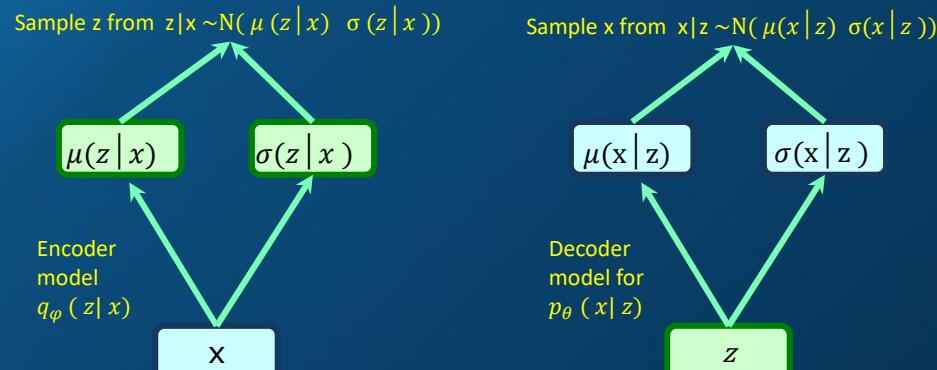
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Variational Autoencoder

- Since we are modeling probabilistic data generation, encoder and decoder networks are probabilistic

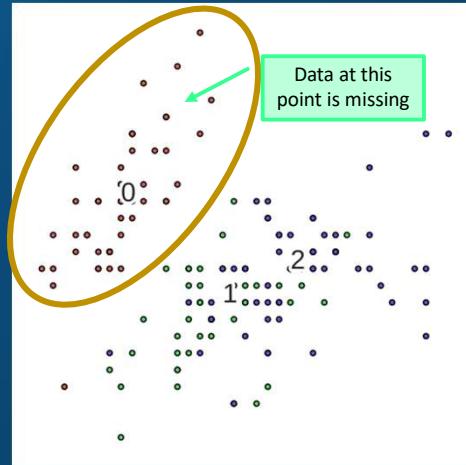


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Missing Data make it Intractable



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Explicit Density Models

- ❑ PixelCNNs define tractable density function, optimize likelihood of training data:

$$p(x) = \prod_{i=1}^n p(x_i|x_1, x_2, x_3 \dots x_{i-1})$$
- ❑ VAEs define intractable density function with latent z:

$$p_\theta(x) = \int p_\theta(z)p_\theta(x|z)dz$$
- ❑ Cannot optimize directly, derive and optimize lower bound on likelihood instead
- ❑ Too lengthy, remained theoretical discussions...
- ❑ What if we give up on explicitly modeling density, and just want ability to sample?
- ❑ GANs: don't work with any explicit density function! Instead, take game-theoretic approach: learn to generate from training distribution through 2-player game

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Generative Adversarial Networks

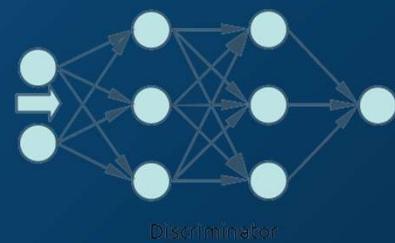
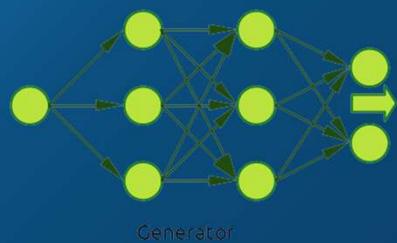
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Generative Adversarial Networks

- ❑ The idea behind Generative Adversarial Networks (GANs): train two different networks
 - ❖ The generator network tries to produce realistic-looking samples
 - ❖ The discriminator network tries to figure out whether an image came from the training set or the generator network
- ❑ The generator network tries to fool the discriminator network

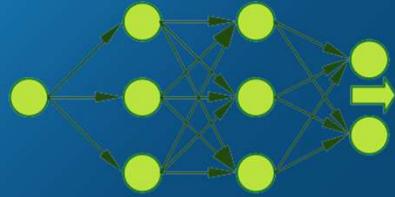


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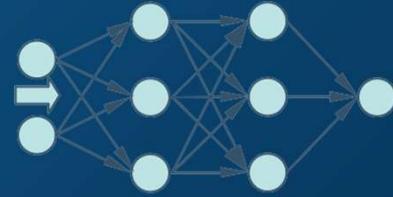
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Generative Adversarial Network



Generator



Discriminator

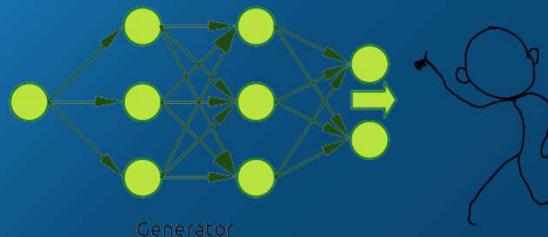


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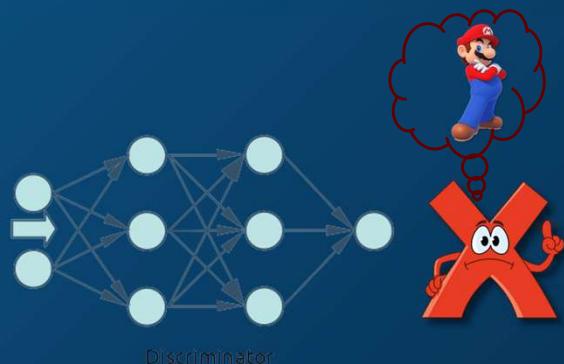
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Generative Adversarial Network



Generator



Discriminator

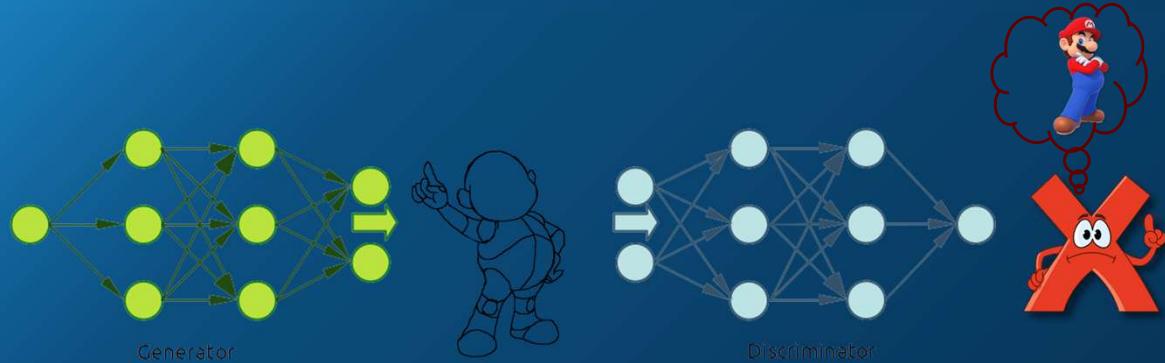


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Generative Adversarial Network

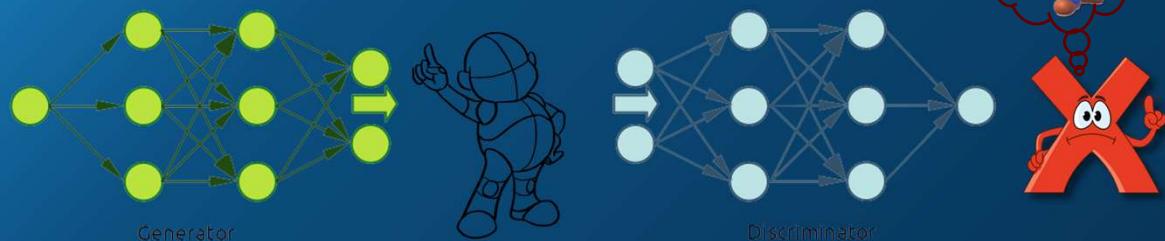


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Generative Adversarial Network

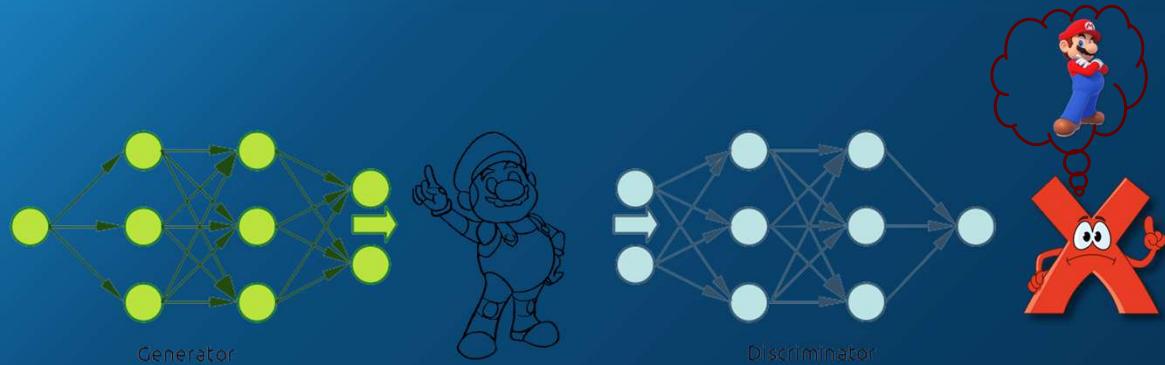


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Generative Adversarial Network

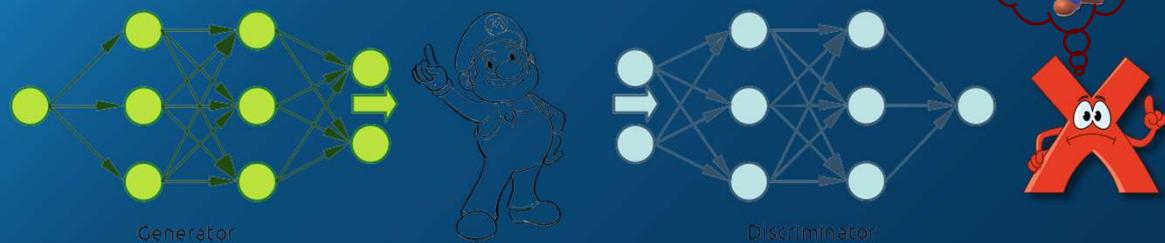


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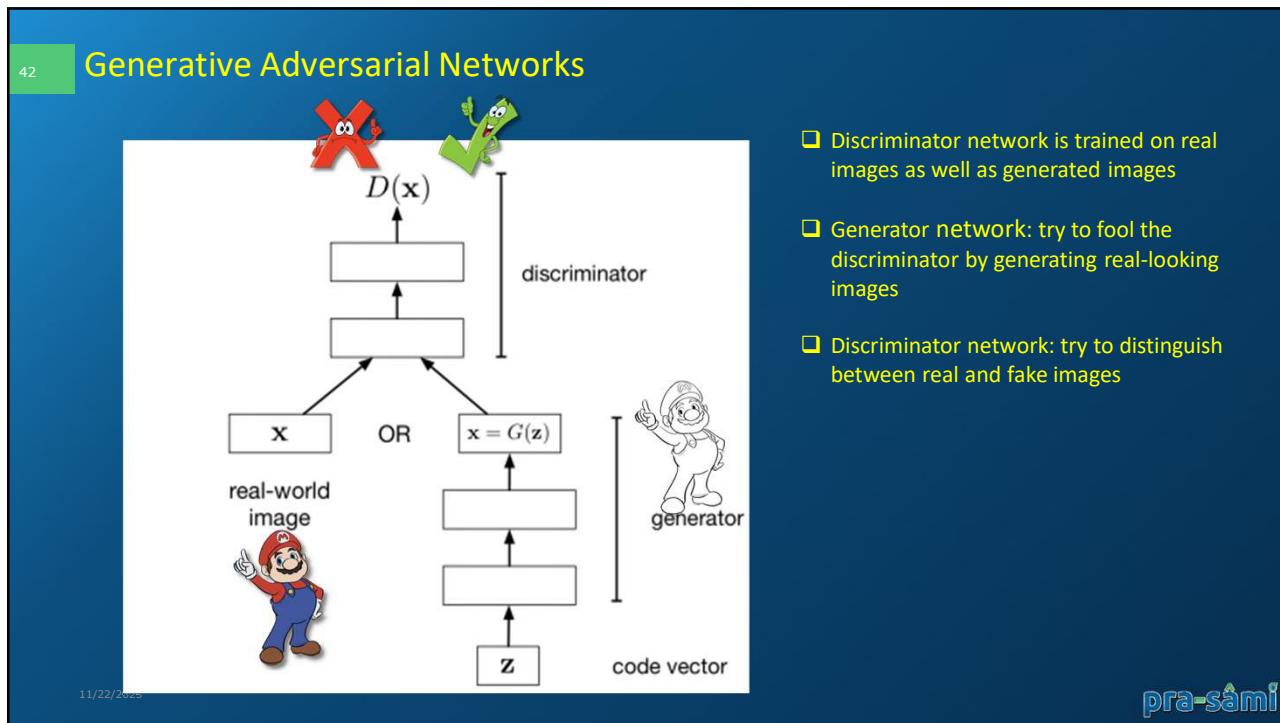
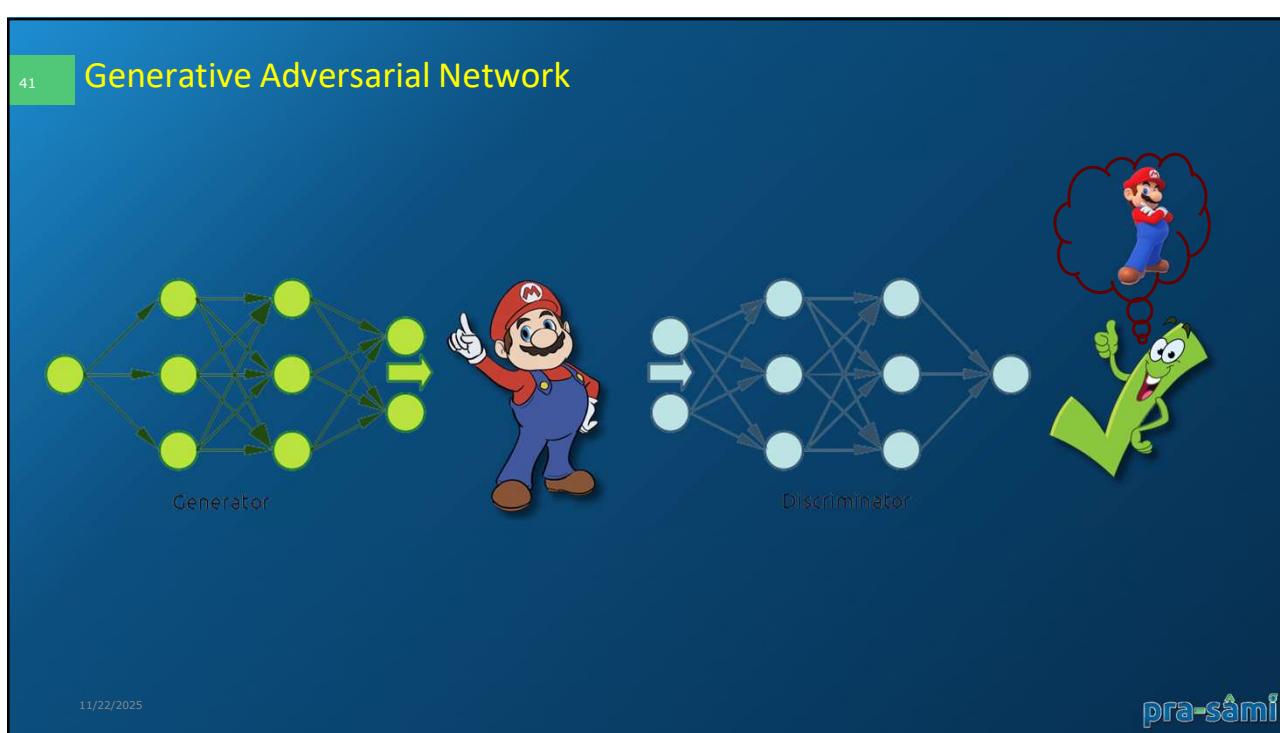
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Generative Adversarial Network



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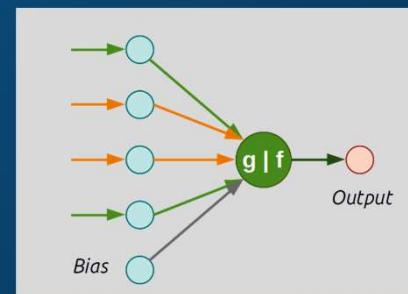
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Coding Gan

- Imagine a simplest 2×2 images
 - ❖ Depending upon features these shades may vary



- Let's also consider our simplest neural network



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GAN

- Imagine all images are slanted backward by 45°
- We have following images of faces



- The corresponding pixel on the images will be as follows:



- For argument sake let's take white pixel as 0 and black as 1
 - ❖ Gray shades will be somewhere in between



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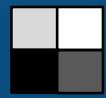
45

GAN

- We have following images of faces



- Images containing no face will appear as follows:

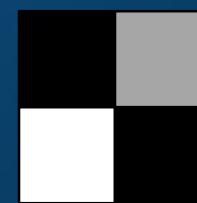
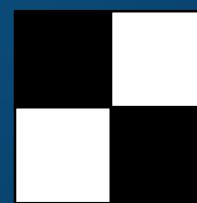
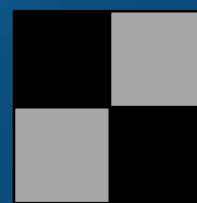


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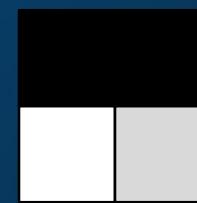
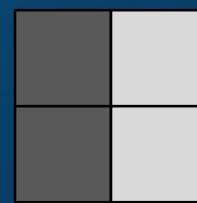
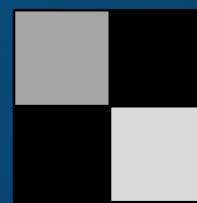
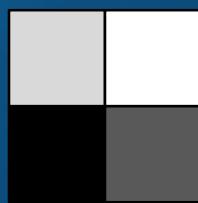
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What Agent will see

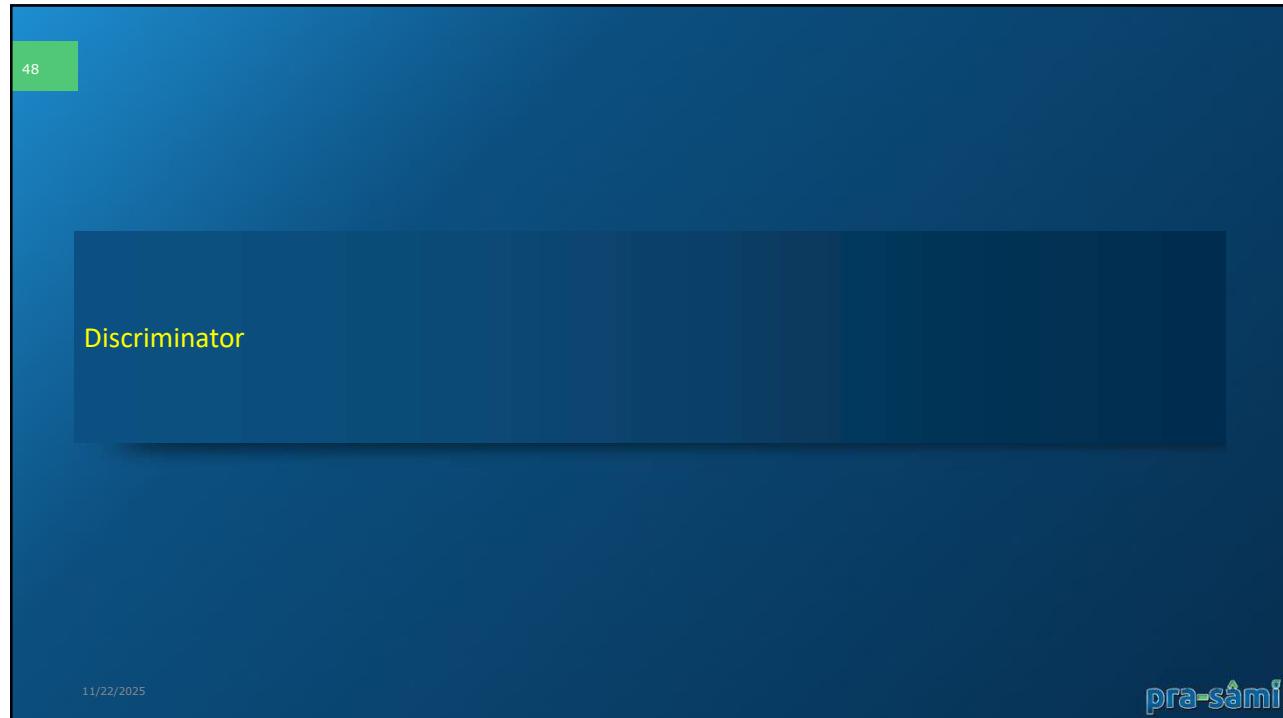
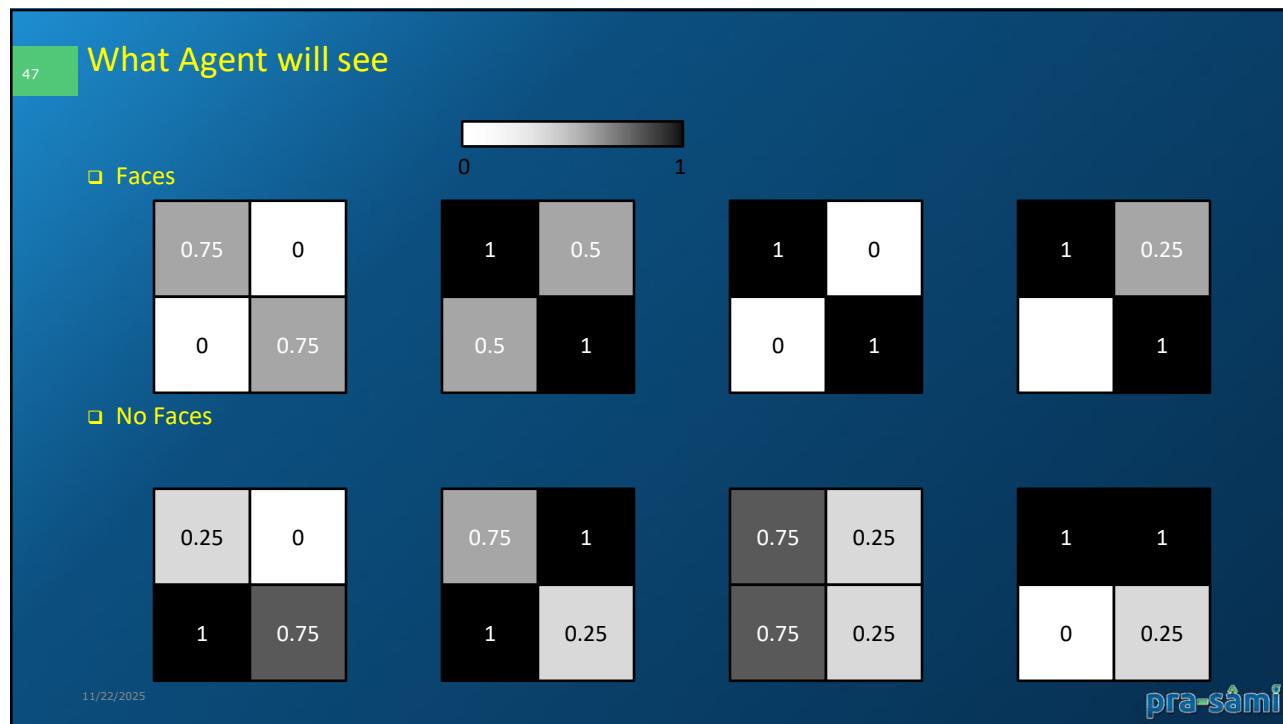
- Faces

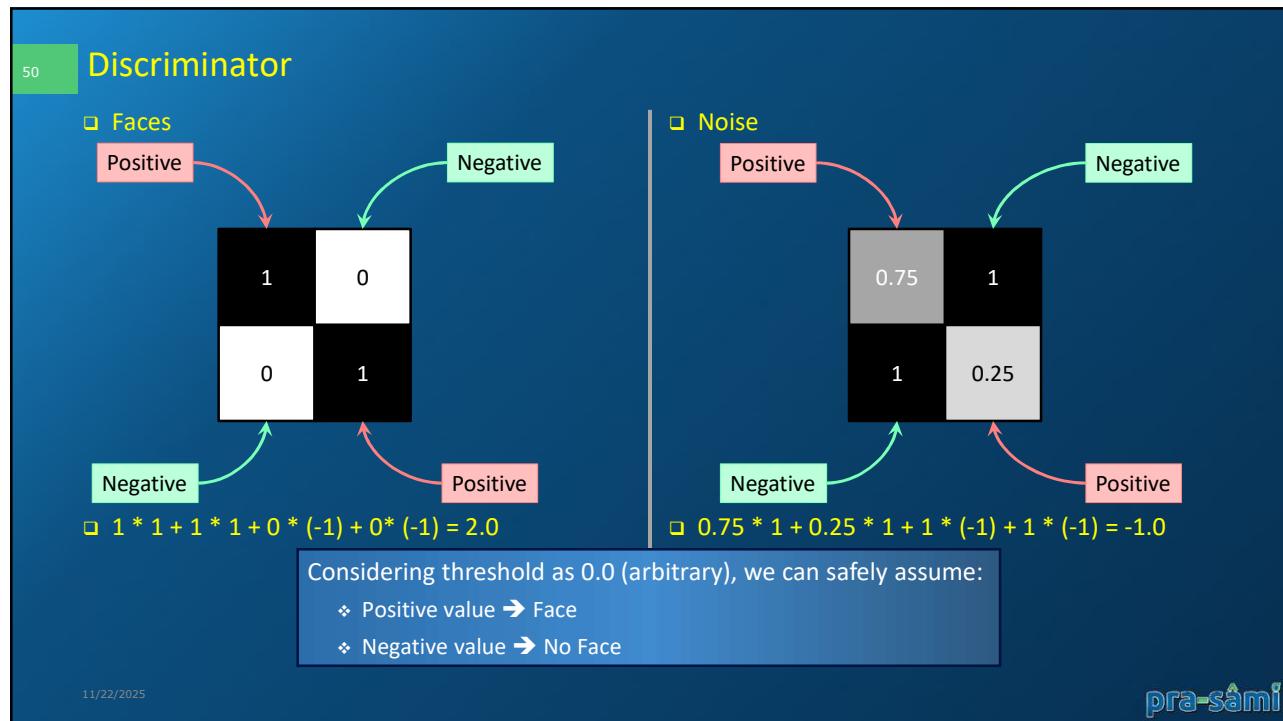
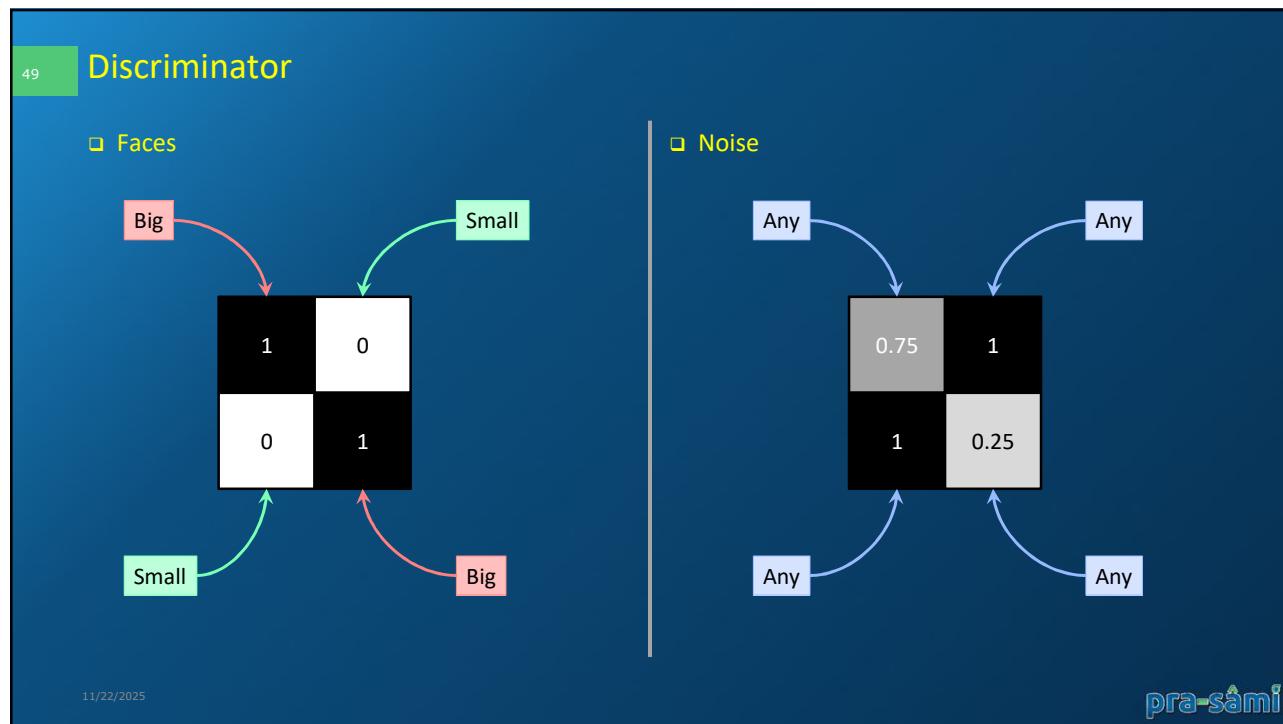


- No Faces



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51 **Discriminator**

$g = +1 * 1 + 0 * (-1) + 0 * (-1) + 1 * 1 - 1 = 1$
 $f = \sigma(g) \rightarrow \text{output} = 0.73$

Output

$g = +0.25 * 1 + 1 * (-1) + 0.5 * (-1) + 0.75 * 1 - 1 = -1.5$
 $f = \sigma(g) \rightarrow \text{output} = 0.18$

Output

sigmoid: $R(z) = \frac{1}{1+e^{-z}}$

sigmoid_prime: $\frac{d}{dz} R(z) = R(z)(1-R(z))$

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52 **Discriminator**

$g = +0.25 * 1 + 1 * (-1) + 0.5 * (-1) + 0.75 * 1 - 1 = -1.5$
 $f = \sigma(g) \rightarrow \text{output} = 0.18$

Output

▫ Thus

- ❖ for $f > 0.5$ it is face
- ❖ for $f < 0.5$ it is not a face

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Discriminator

- Imagine all images are slanted backward by 45°



| | |
|-----|-----|
| 0.5 | 0 |
| 0 | 0.5 |



| | |
|-----|-----|
| 1 | 0.5 |
| 0.5 | 1 |



| | |
|---|---|
| 1 | 0 |
| 0 | 1 |



| | |
|---|-----|
| 1 | 0.5 |
| 0 | 1 |



| | |
|------|------|
| 0.25 | 1 |
| 0.5 | 0.75 |

- So the discriminator knows that following:

❖ Face



Not a Face

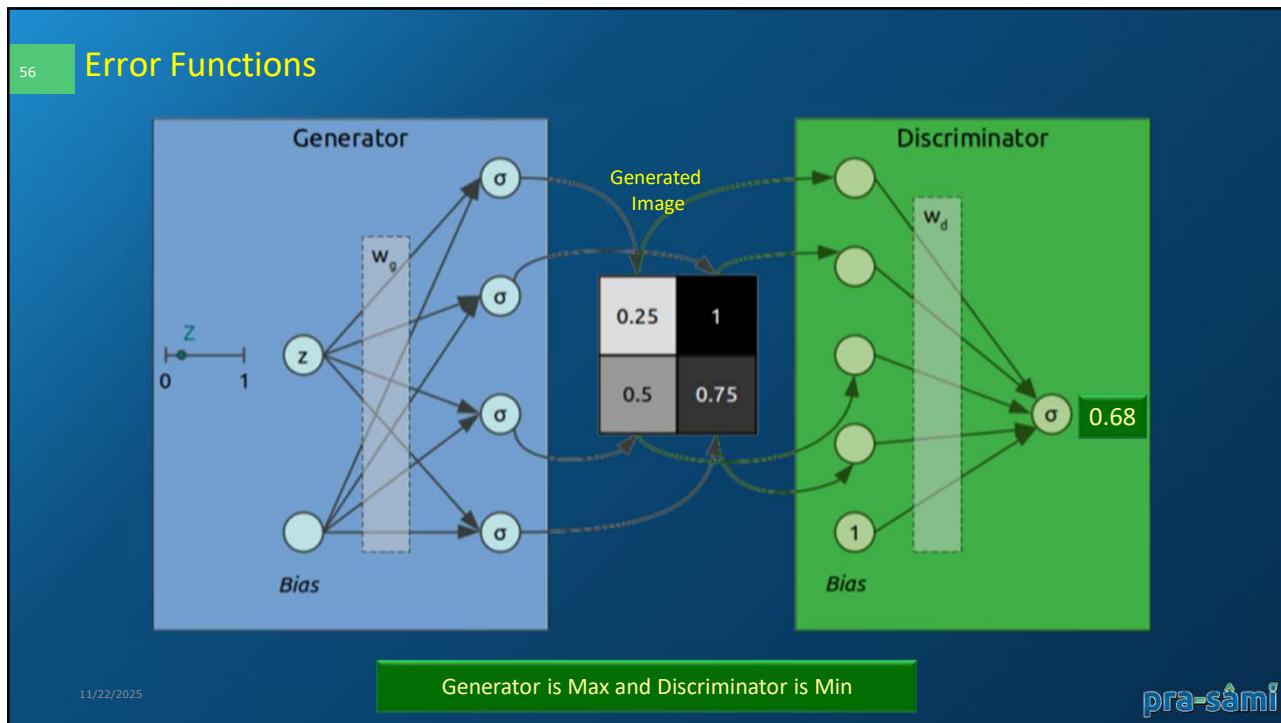
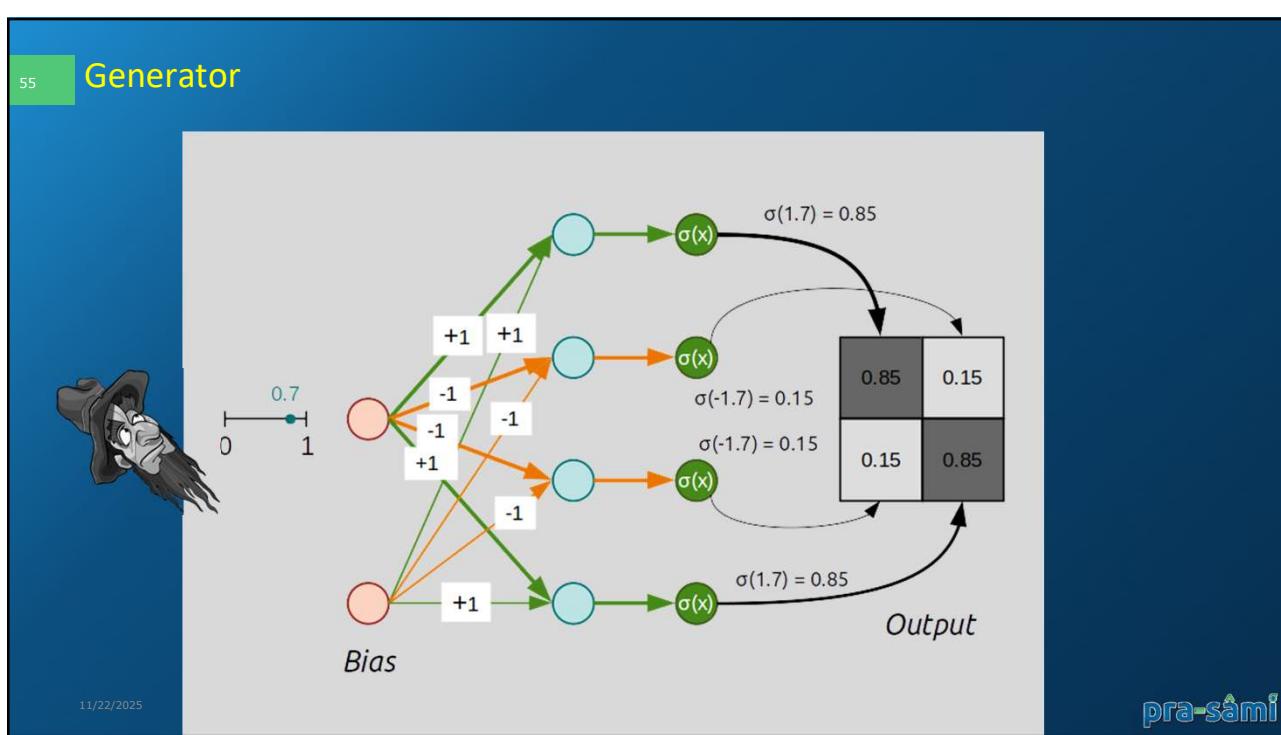


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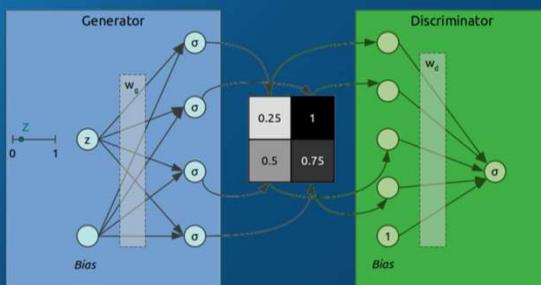
Generator

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Error Functions



- Generator and Discriminators are working against each other
- Discriminator tries to generate label as close to 0 as possible (Claiming it is fake)
 - ❖ Error function = $-\log(1-p)$
- Generator tries to generate labels as close to 1 as possible (Claiming it to be an image)
 - ❖ Error function = $-\log(p)$

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Error Functions

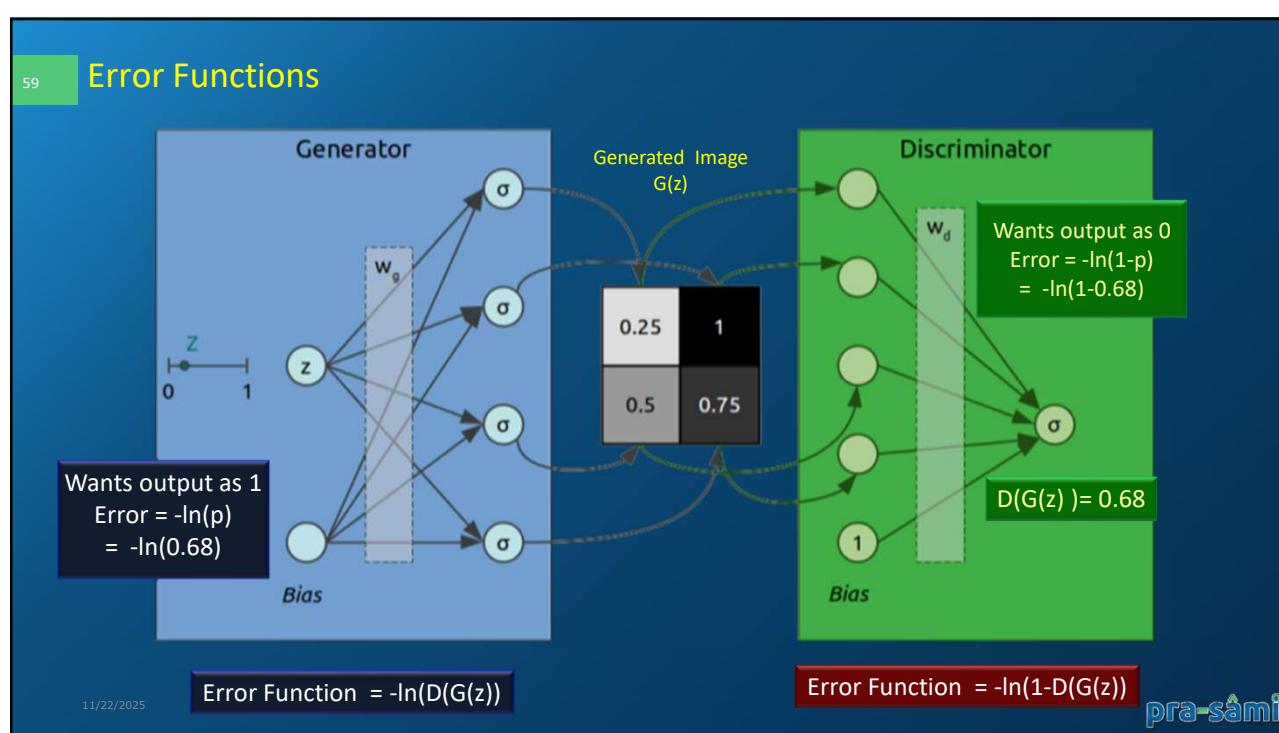
Discriminator

- If our value 0 and prediction is 0.1 → error is small
- If our value is 0 and prediction is 0.9 → error is large
- Consider negative log error
 - ❖ For pred = 0.1; error = $-\ln(1-0.1) = 0.11$
 - ❖ For pred = 0.9 error = $-\ln(1-0.9) = 2.30$
- Thus our error function is:
 - ❖ $-\ln(1-\text{pred})$

Generator

- If our value 1 and prediction is 0.1 → error is large
- If our value is 1 and prediction is 0.9 → error is small
- Consider negative log error
 - ❖ For pred = 0.1; error = $-\ln(0.1) = 2.30$
 - ❖ For pred = 0.9 error = $-\ln(0.9) = 0.1$
- Thus our error function is:
 - ❖ $-\ln(\text{pred})$

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- 60 Three Reasons that it's a Miracle GANs Work
- ❑ G has a reinforcement learning task
 - ❖ It knows when it does good (i.e., fools D) but it is not given a supervised signal
 - ❖ Reinforcement learning is hard
 - ❖ Back prop through D provides G with a supervised signal; the better D is, the better this signal will be
 - ❑ Can't describe optimum via a single loss
 - ❖ Will there be an equilibrium?
 - ❑ D is seldom fooled
 - ❖ But G still learns because it gets a gradient telling it how to change in order to do better the next round.
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Training GANs: Two-player game

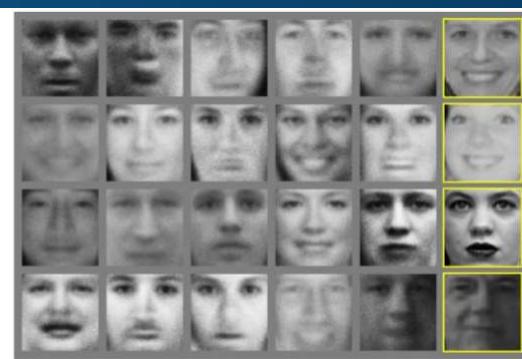
- ❑ Generator network: try to fool the discriminator by generating real-looking images
- ❑ Discriminator network: try to distinguish between real and fake images
- ❑ Train jointly in MiniMax game
- ❑ MiniMax objective function:
$$\min_{\theta_g} \max_{\theta_d} [E_{x \sim p_{data}} \log D_{\theta_d}(x) + E_{z \sim p(z)} \log(1 - D_{\theta_d}(G_{\theta_g}(z)))]$$
- ❑ Discriminator outputs likelihood in (0,1) of real image
- ❑ Discriminator (θ_d) wants to maximize objective such that $D(x)$ is close to 1 (real) and $D(G(z))$ is close to 0 (fake)
- ❑ Generator (θ_g) wants to minimize objective such that $D(G(z))$ is close to 1
 - ❖ Discriminator is fooled into thinking generated $G(z)$ is real

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Generative Adversarial Nets



Nearest neighbor from
training set

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Reflect...

- Which of the following are key components of a Generative Adversarial Network (GAN)?
 - a. Generator
 - b. Discriminator
 - c. Classifier
 - d. Loss function
- Answer : a, b, d

- Select the statements that correctly describe the training process of a GAN.
 - a. The generator aims to produce data that is indistinguishable from real data.
 - b. The discriminator provides feedback to the generator about the generated samples.
 - c. GANs are trained using supervised learning techniques.
 - d. The loss function for GANs involves both a generator loss and a discriminator loss.
- Answer: a, b, d

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Reflect...

- Choose the correct statements regarding the mode collapse phenomenon in GANs.
 - a. Mode collapse occurs when the generator produces diverse samples covering the entire data distribution.
 - b. Mode collapse happens when the generator focuses on generating only a limited set of samples.
 - c. Mode collapse is a desired behavior in GAN training.
 - d. Mode collapse is related to the overfitting of the discriminator.
- Answer : b

- Which regularization techniques are commonly used to stabilize GAN training?
 - a. Dropout
 - b. Batch normalization
 - c. L1 regularization
 - d. Gradient clipping
- Answer : a, b, d

- Select the statements that correctly describe the challenges associated with training Generative Adversarial Networks.
 - a. GANs may suffer from mode collapse.
 - b. Training GANs can be unstable.
 - c. GANs always converge to a globally optimal solution.
 - d. GANs require a large amount of labeled training data.
- Answer: a, b

- What is the role of the discriminator in a GAN?
 - a. To generate synthetic data.
 - b. To evaluate the quality of generated samples.
 - c. To provide feedback to the generator.
 - d. To discriminate between real and fake data.
- Answer: d

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