MSML610: Advanced Machine Learning

Knowledge Representation

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References:

- Mostly papers and Internet
- AIMA 7: Logical agents
- AIMA 8, First-order logic
- AIMA 9: Inference in first-order logic
- AIMA 10, Knowledge representation

• Knowledge Representation

- Basics of Knowledge Representation
- Examples of Logic
- Logical Agents
- Ontologies
- Reasoning in Ontologies
- Propositional logic
- First-order Logic
- Non-classical Logics

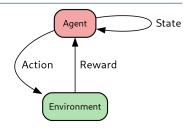
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What is Knowledge Representation?

- Knowledge Representation (KR) is the study of how to formally encode information so that machines can reason with it
 - E.g., rules, logic, ontologies, semantic networks
 - It is at the heart of symbolic AI and complements learning-based approaches
- Defines:
 - structure (how knowledge is organized)
 - semantics (what it means)
- Serves as a bridge between perception (data) and reasoning (logic)
 - Essential for explainability and transparency in intelligent systems
- Enables machines to:
 - Draw conclusions
 - Perform planning
 - Answer queries
 - ...

Expressiveness vs. Tractability

- Tradeoff in Al / ML
 - Expressiveness: richness of concepts that can be captured
 - Tractability: whether reasoning can be performed efficiently
 - More expressive languages lead to harder computation



- Choosing the right knowledge representation formalism depends on the application needs
 - Atomic
 - Treats each state as a single, indivisible entity
 - E.g., depth-first search algorithms (e.g., E3 in Chess)
 - Simple and fast but limited in capturing complex relationships
 - Factored
 - E.g., propositional logic
 - E.g., $P_{1,1}$: "Pit in square (1,1)", $B_{1,2} \Leftrightarrow (P_{1,1} \vee P_{2,2} \vee P_{1,3})$
 - Captures relationships between variables but can't express complex structures
 - Structured
 - E.g., first-order logic
 - $\forall x \ \forall y \ Father(x,y) \Rightarrow Parent(x,y) = "A \ father of a person is their parent"_{5/104}$

Symbolic vs. Sub-symbolic Representation

- Symbolic knowledge representation uses discrete, human-readable symbols
 - E.g., logic, knowledge graphs
 - Interpretable and suitable for rule-based reasoning
 - Struggle with ambiguity
- Sub-symbolic knowledge representation uses learned, distributed representations
 - E.g., vector embeddings
 - E.g., deep learning excels at perception and pattern recognition
 - Lack transparency
- Neuro-symbolic approaches blends the two approaches
 - Reason over learned concepts using structured logic

Neuro-symbolic Approach: Conceptual Spaces

- Conceptual spaces are frameworks for representing knowledge using geometric structures
 - A concepts is a region in a multidimensional space defined by quality dimensions
 - Similarity between objects is modeled by spatial distance
 - Each dimension represents an interpretable feature

Example

- Dimensions: Color, Size, Shape
- "Apple" occupies a region that is typically red / medium-sized / round
- "Banana" occupies a different region: yellow / medium / curved and long
- Differences from Symbolic Representations
 - Symbolic systems use discrete symbols without structure
 - E.g., Apple vs Banana

Benefits

- Natural modeling of similarity and vagueness
- Useful for grounding symbols in perception (link between sensory inputs and symbolic language)

Procedural vs Declarative Approaches

Procedural approach

- Focuses on how a task is done
- Encodes desired behavior directly into the program
- E.g., a robot programmed with specific steps to navigate a maze

Declarative approach

- Specifies what the goal is, not how to achieve it
- Describes relationships between actions and goals
- Leaves solution search to the system
- E.g., describing the goal "reach the exit" and letting the system find the path

Comparison

- Procedural: more control, less flexibility
- Declarative: more abstraction, easier to modify or extend

• Integration of approaches

- Many successful AI systems use a hybrid
- Declarative knowledge can be compiled into procedural code
- E.g., a planner generates procedures (plans) from declarative goals

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Propositional Logic

- Uses atomic statements (propositions) and logical connectives
 - Syntax
 - Atomic formulas: P, Q
 - Connectives: NOT (\neg) , AND (\land) , OR (\lor) , IMPLIES (\Longrightarrow)
 - Semantics
 - Based on truth tables
 - Each proposition has a binary truth value: true or false
 - Inference mechanisms
 - Modus ponens: from P and $P \implies Q$, infer Q
 - Resolution: derive contradictions to infer conclusions
- Applications: best used in closed and well-defined environments
 - Digital circuit design
 - Rule-based systems
 - Simplified AI models
- Limitations
 - · Cannot represent objects, relations, or quantifiers
 - Not suitable for open or dynamic domains

First-Order Logic (FOL)

- Extension of propositional logic
 - Introduces predicates, variables, and quantifiers
 - Variables x
 - Predicate Human(x)
 - Universal quantifier "for all" ∀
 - Existential quantifier "there exists" ∃
 - E.g., $\forall x (Human(x) \implies Mortal(x)) = "All humans are mortal"$
 - Represents more complex and structured knowledge than propositional logic
 - Can model properties, relationships, and quantification over objects
- Inference mechanisms
 - Unification: matches predicates with variables
 - Resolution: deduces new facts from known statements
 - Model checking: verifies truth of statements under specific interpretations
- Computational properties
 - Inference is semi-decidable: valid conclusions may require infinite time
 - More powerful but computationally more complex than propositional logic
- Applications
 - Knowledge representation
 - Automated theorem proving
 - Semantic web and ontologies

Rule-Based Systems (1/2)

- A rule-based system uses "if-then" rules to derive conclusions or make decisions
 - It mimics human decision-making by applying logical rules to a set of facts

Key Components

- Knowledge base: stores facts and rules
- Inference engine: applies rules to known facts to infer new facts or take actions
- · Working memory: holds current facts being considered

How It Works

- Match: find rules whose conditions match current facts
- Conflict resolution: decide which rule to apply if multiple rules match
- Act: apply the chosen rule to modify facts or trigger actions
- Repeat: continue until no more rules can be applied
- E.g.,
 - Rule: If a patient has a fever and a rash, then suggest measles
 - Fact: Patient has a fever and a rash
 - Conclusion: Suggest measles

Rule-Based Systems (2/2)

Pros

- Easy to modify and update rules
- Transparent and explainable reasoning
- Good when expert knowledge can be clearly articulated

Cons

- Hard to scale to very large or complex domains
- Cannot handle uncertainty without extensions (e.g., probabilistic reasoning)
- Rule conflicts and maintenance can become challenging

Applications

- Expert systems (e.g., medical diagnosis, technical troubleshooting)
- Business rule engines
- Game AI
- Legal reasoning tools

Reasoning and Inference in Logic

- Logical inference is the process of deriving new facts from known ones using formal rules
 - Used to make decisions and answer questions based on a Knowledge Base
- Knowledge base (KB):
 - A structured set of facts and rules used for logical reasoning
- Inference engine:
 - Mechanism that applies logical rules to a KB to derive conclusions or answer queries
 - Forward chaining:
 - Starts with known facts and applies inference rules to extract more data
 - E.g., given $A \rightarrow B$ and A, infer B
 - Backward chaining:
 - Begins with a goal and works backward to find supporting facts
 - E.g., to prove B, check if $A \rightarrow B$ and then prove A
 - Resolution:
 - A complete inference rule for propositional and first-order logic
 - Useful in automated theorem proving
 - Entailment ($KB \models \alpha$):
 - Sentence α is entailed by KB if it is true in all models where KB is true

Grounding

Grounding

- Connect abstract symbols to real-world entities or observations
- E.g., link Apple to the fruit "apple"
- Make representations meaningful beyond syntax
 - Enable agents to act meaningfully in the real world
 - Avoid purely symbolic manipulation without real-world relevance

Challenges

- Noisy, incomplete sensory data
- Complex, context-dependent mapping from inputs to concepts

Applications

- Robotics: object recognition, manipulation
- Natural language understanding
- Autonomous agents, cognitive systems



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Reflex Agents

- Reflex agents act based on the current percept, ignoring percept history
 - Operate using a condition-action rule: "if condition, then action"
 - Rely on predefined rules
 - Have no internal state or memory
 - E.g., a thermostat: "if temperature < threshold, turn on the heater"
- Pros
 - Fast and efficient in well-defined environments
- Cons
 - Struggle with complex or partially observable environments
 - · Cannot plan ahead or learn from experience
- Application
 - Simple or fully observable environments where quick reactions are sufficient

Knowledge-based Agents

- Intelligence is achieved by reasoning on an internal representation of knowledge
- Knowledge-based agents:
 - Form representations of a complex world
 - Use inference to derive new representations
 - Deduce actions from new representations
 - Accept tasks as goal descriptions
 - Achieve competence by learning new knowledge
 - Adapt to changes by updating knowledge
 - Utilize a knowledge base to store information
 - Explain actions based on knowledge
 - E.g., medical diagnosis system infers diseases, suggests treatments
 - E.g., chess program uses move database to plan strategy
 - · Handle incomplete or uncertain information through probabilistic reasoning

Logic / Knowledge Base (1/2)

- Knowledge base (KB) is a set of:
 - ullet Sentences lpha expressing assertions (observed, assumed or derived) about the world
 - E.g., "it rains", "the ground is dry", "the ground is wet"
 - Rules
 - . E.g, "If it rains, the ground gets wet"
- Knowledge representation language is a formal way of creating sentences about the world
- \bullet Syntax specifies all the sentences α that are well-formed in a logic / knowledge base
 - E.g., in arithmetic the sentence:
 - "x + y = 4" is well-formed
 - "x4y+=" is not well-formed
- **Semantics** is the meaning of sentences (i.e., their truth) with respect to each possible world
 - E.g., the sentence x + y = 4
 - Is true in the world (model) in which x = 2, y = 2
 - Is false in the world x = 1, y = 1

Logic / Knowledge Base (2/2)

- Axiom is a sentence taken as given
 - Not derived from other sentences
- Inference is the process of deriving new sentences from old ones
 - It should be done in a "logical" way
- Truth values of a sentence
 - In most logics every sentence is either true or false
 - Fuzzy logic allows sentences to have different degrees of truth
 - $Belief(\alpha) = 0.5$
 - Probabilistic logic allows sentences to have different probability of being true
 - $Pr(\alpha) = 0.3$

Model and Possible Worlds: Examples

- Example: represent worlds where there is rain and wet ground
 - In each possible world/model, values are assigned to all relevant variables
 - "Possible worlds" can be thought of as real the environments
 - Model m is a mathematical abstraction of "possible world"
 - E.g., m is (Rain = F, WetGround = T)
 - Each possible world is a complete assignment of truth values to all relevant propositions
 - World 1: (Rain = T, WetGround = T)
 - World 2: (Rain = T, WetGround = F)
 - World 3: (Rain = F, WetGround = T)
 - World 4: (Rain = F, WetGround = F)
- Example: represent worlds with "men and women sitting at a table"
 - Model represents all possible worlds as (x men, y women)
 - Sentence x + y = 4 is true in certain worlds, false in others
 - In worlds with x = 2 men and y = 2 women,



Satisfaction of a Sentence in a Model

- A model m fixes all the variables $x_1, ..., x_n$ used in sentences
 - E.g., (Rain = T, WetGround = T)
- If a sentence α is true in model m, we say "the model m satisfies the sentence α "
 - E.g., the model (Rain = T, WetGround = F) satisfies $\alpha : Rain = T$
 - Note: this seems backwards, since in our common way of reasoning, the world is fixed and sentences are evaluated as true or false
- $M(\alpha)$ is the set of all the models in which α is true
 - E.g.,
 - α : Rain = T
 - $M(Rain = T) = \{(Rain, WetGround), (Rain, \neg WetGround)\}$

Logical Entailment

- Logical entailment between sentences is the fact that a sentence follows logically from another sentence in a KB
- " α entails β " (written $\alpha \models \beta$) iff (by def) in every model in which α is true, β is also true
 - Equivalent to $M(\alpha) \subseteq M(\beta)$
- E.g., in the "rain and wet ground" world
 - α : "Rain \implies WetGround" entails β : "(Rain = T, WetGround = T)"
- E.g., in the "sitting table" world
 - α : "x = 0", β : " $x \cdot y = 0$ "
 - α entails β since in any model in which x=0 is true, also $x\cdot y=0$ is true, regardless of the value of y

Intuition:

- Entailment is not related to a proof, it just "preserves truth" across all models
- "If you believe your KB, you must believe the entailed sentences"

Logical Entailment vs Implication

- Entailment and implication are related but distinct
 - Logical entailment is about truth following from known facts
 - Implication is about a relationship between two statements
- Logical entailment ($KB \models \alpha$):
 - ullet Means lpha is always true in any world where KB is true
 - E.g.,
 - KB: "It is raining", "If it rains, the ground is wet"
 - Entailed: "The ground is wet"
- Implication $(A \Longrightarrow B)$:
 - A statement in logic that says: "If A is true, then B is true"
 - Doesn't guarantee A or B is true by itself
 - Implication is true unless A is true and B is false

 - E.g.,
 A: "It is raining", B: "The ground is wet"
 - $A \implies B$ is the statement "If it is raining, then the ground is wet"
 - This statement can be true even if it's not raining
- Intuition:
 - Entailment is "meta-level truth-following"
 - Implication is "within the logic"

Model Checking Procedure

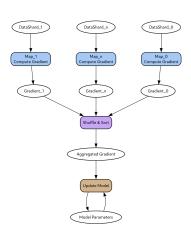
- M(KB) represents all the models / possible worlds that are true given our KB
- Problem:
 - We want to verify whether "a sentence α is entailed by KB" ($KB \models \alpha$)
- Solution:
 - According to the definition, we need to verify that α is true in all the models in which $K\!B$ is true
 - I.e., $M(KB) \subseteq M(\alpha)$
- E.g., model checking procedure (brute force)
 - 1. Enumerate all the models / possible worlds
 - 2. Find which models are possible given the KB, i.e., M(KB)
 - 3. Check whether the sentence α is true in all the models that are compatible with the $K\!B$

Sound and Complete Inference Algorithm

- Inference: a syntactic process of deriving new sentences from others, using formal rules of a proof system (e.g., modus ponens, resolution, etc.)
 - You know: "If it rains, the ground gets wet."
 - You see: "It is raining."
 - You infer: "The ground must be wet."
- The ideal inference algorithm is both sound and complete
- Sound inference algorithm
 - Derives only sentences entailed from KB
 - "Whatever the inference algorithm finds, it's correct", i.e., no false positives
 - E.g., model checking is sound
 - It works only when the space of models is finite
 - When it works, it is truth preserving
- Complete inference algorithm
 - Can derive any sentence entailed from KB
 - "The inference algorithm doesn't miss anything," i.e., no false negatives

Isomorphism between Model and Possible Worlds

- A sound and complete inference algorithm should yield conclusions guaranteed to be true in any world where the premises are true
- In other words, even if the inference operates on "syntax" (the internal representation):
 - "Sentences in the representation" correspond to "aspects of the real world"
 - "Entailment between sentences in the representation" corresponds to "implication between aspects of the real world"



Entailment vs Inference vs Implication

Logical entailment

- A entails B: if the fact A is true and that automatically guarantees that fact B must also be true
- E.g., Rain entails WetGround iff in every possible world where Rain is true, WetGround is also true
 - Rain = T, $WetGround = F \rightarrow violation$
 - Since there is at least one counterexample, Rain does not entail WetGround

Inference

- This is what you (a person or a computer) figure out based on what you know
- You start with some truths, then reason your way to new truths
- It's "reasoning inside the logic system"

Implication

- "If A, then B"
- It doesn't say whether A is true; it just says, if it happens, then B follows
- It's a "statement inside the logic system"

Grounding

- Grounding is the operation of linking abstract symbols to reality
 - \bullet E.g., words, variables in the representation $\dots \to$ objects, entities, or situations in the real world
 - It is the bridge between representation in a KB and the world
- How can we know that a KB accurately reflects the real world?
 - We can't be sure!
 - Do we live in a simulation? What is reality?
- We assume that is correct
 - Agent's sensors create a sentence in the KB when something happens in the real world
 - IF smell = burning THEN food_is_burning
 - Agent learns rules and acts

 IF food is burning THEN turn off
 - IF food_is_burning THEN turn_off_stove
- We assume that "learning" (going from particular cases to general cases) is typically correct
 - Learning is still fallible
 - E.g., smell = burning because maybe somebody is cooking on a grill

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Ontologies (in computer science)

Ontology:

- Is a formal, explicit representation of a domain
- Describes the types of things that exist and how they relate to each other
 - Classes: types of things
 - Individuals: specific objects
 - Properties: how things are related

• Examples:

- A medical ontology defines relationships between diseases, symptoms, and treatments
- A geographical ontology describes cities, states, and countries
- Semantic web (an extension of the current web to give meaning to information)

Goal

- Provide a vocabulary for a domain of knowledge
- Enable machines and humans to understand and share information consistently
- Enable reasoning about entities and their relationships

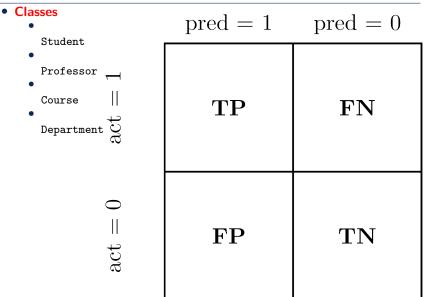
• Related Concepts

- Schema: database-oriented structure, often more rigid than ontologies
- Taxonomy: simpler hierarchical tree-like classification
- Knowledge base: a collection of facts and rules, sometimes built from an entology

Ontologies: Components

- Classes / Concepts:
 - · Represent general concepts in a domain
 - E.g., Person, City, Car
- Individuals / Instances:
 - Specific, concrete examples of classes
 - E.g., GP (an instance of Person), Rome, Ferrari 458
- Properties / Relations:
 - Describe interactions or associations between classes or instances
 - E.g., isMortal, locatedIn, hasAge
- Attributes / Data values
 - Specify data associated with instances
 - E.g., (GP, hasAge, <your_guess>)
- Constraints
 - Rules that restrict the kinds of values a property can take
 - E.g., (Ferrari 458, mustBe, red)
- Axioms:
 - · Logical statements that define rules and constraints
 - E.g., all humans are mortal: $\forall x (Person(x) \implies Mortal(x))$
- Hierarchies:
 - Organize classes and properties into parent-child relationships
 - E.g., Student is a subclass of Person

Ontology: Example University



• Properties: relationships between Classes

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Example of Reasoning Tasks (1/4)

Subsumption

- "Is class A a subclass of B?"
- Check whether one concept is more general than another
- E.g., if Person subsumes Student, every Student is necessarily a Person
- Important for building taxonomies and ontologies

Satisfiability:

- "Can an instance of a concept exist?"
- Test if a concept is logically consistent (i.e., without contradiction)
- E.g., if the concept FlyingPenguin requires flying but is also defined as a penguin (which cannot fly), it might be not satisfiable

Classification

- Organize concepts into a hierarchy
- Automatically organize concepts into a hierarchy by checking subsumption relationships
- E.g., given definitions of Animal, Bird, and Penguin, classification places
 Penguin under Bird, and Bird under Animal

Example of reasoning tasks in KR (2/4)

Instance Checking

- "Is a specific individual an instance of a concept?"
- E.g., is GP an instance of Student?

Consistency Checking

- "Is the entire knowledge base free of contradictions?"
- E.g., no Person is both Alive and Dead at the same time

Realization

- "What is the most specific class an instance belongs to?"
- E.g., discovering that GP is a Professor rather than just a Human

Retrieval

- Find all individuals that satisfy a certain condition
- E.g., retrieve all instances classified as TeachingAssistant

Example of reasoning tasks in KR (3/4)

Query Answering

- Answer complex queries about the knowledge base
- E.g., "Find all Person that study at the university and are not Student"

Abduction

- Given an observation, infer the best explanation
- E.g., seeing a Person carrying a backpack and wearing flip-flops in the snow and infer that is likely a Student

Deduction

- Infer consequences that logically follow from facts and rules
- E.g., if John is a Student in ComputerScience then he can attend MSML610

E.g., of reasoning tasks in KR (4/4)

Belief Revision

- Update the knowledge base when new, possibly conflicting, information arrives
- E.g., learning that not every student in ComputerScience can take MSML610 and revise a previous rule

Temporal Reasoning

- Reason about events over time
- E.g., If EventA happens before EventB, then EventB cannot Cause EventA

Causal Reasoning

- Infer causes and effects among entities or events
- E.g., inferring that (Storm, Cause, Flooding) based on temporal and physical knowledge

Ontologies tools: Protege Example

- Protégé is a free, open-source platform for building ontologies
 - Developed at Stanford
- Provides tools to construct and visualize ontologies
 - Users can define classes, properties, individuals, and relationships
- Enable reasoning over ontologies using plugins
 - E.g., checking consistency, inferring new knowledge
- Supports:
 - Major ontology languages
 - OWL (Web Ontology Language)
 - RDF (Resource Description Framework)
 - Multiple serialization formats
 - RDF/XML, Turtle, OWL Functional Syntax
- Use cases:
 - Domain-specific knowledge modeling (e.g., biomedicine, law)
 - Semantic Web applications
 - Al systems that require structured knowledge

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Propositional Logic

- Propositional logic is a formal system for reasoning about statements that can be true or false
 - Syntax defines the allowable sentences
 - · Consists of proposition symbol and logical connectives
 - E.g., *P* ∧ *Q*
 - Semantics is the way in which the truth of sentences is determined
 - Truth tables or deduction rules evaluate the truth value of complex sentences
 - E.g., if P is true and Q is false then $P \wedge Q$ is false
- Atomic representation
 - No internal structure within atomic propositions
- Uses:
 - SAT solvers
 - Tools for determining if a propositional logic formula can be satisfied
 - E.g., used in hardware verification and scheduling problems
 - Expert systems
 - Systems that use logic rules to mimic human decision-making
 - E.g., medical diagnosis systems
 - Rule-based agents
 - · Agents that operate based on a set of predefined rules
 - E.g., automated customer service chatbots

Proposition symbol

- Proposition symbol
 - Is an atomic sentence consisting of a single symbol
 - E.g., P, Q, North
 - Doesn't have truth value, it is just a symbol for a real-world statement
 - Stands for a proposition that can be true or false
 - E.g., $K_{E,5}$ = "the Knight is in E5"
 - $K_{E,5}$ is not composed of any other symbol, it is an atomic symbol
 - True and False are proposition symbols with inherent truth values

Sentences

- Atomic sentence:
 - Is a sentence composed of a single proposition symbol
- Complex sentence:
 - Is constructed from simpler (sentences) using parentheses and logical connectives
 - Note: it is a recursive definition that allow to build more complex sentences
- Each sentence (atomic or complex) can be only true or false
- Common logical connectives
 - Not: ¬
 - And: ∧ (looks like an "A" for "and")
 - Or: ∨ (comes from Latin "vel" which means "or")
 - Implies: ⇒
 - If and only if: \iff

Proposition Logic: Weather Example

- Proposition symbols are
 - Rain = "it's raining"
 - Cold = "it's cold"
 - *Sunny* = "it's sunny"
 - *Snow* = "it's snowing"
 - Cloudy = "it's cloudy"
- Atomic sentence can be positive (e.g., Rain) or negated (e.g., $\neg Rain =$ "it's not raining")
- Negation
 - E.g., $\neg(Rain \lor Cloudy) =$ "it's not the case that it's raining or cloudy"
- Conjunction
 - E.g., $Rain \wedge Cold = "it's raining and it's cold"$
- Disjunction
 - E.g., Rain ∨ Snow = "it's either raining or snowing"
- Implication is a sentence containing a premise (aka antecedent), the connective ⇒, and a conclusion (aka consequent)

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Grammar in BNF form

- Use BNF to formally represent the grammar of propositional logic
- Ambiguous, i.e., the same sentence can be parsed in multiple ways
 - E.g., $\neg A \lor B = (\neg A) \lor B \text{ or } \neg (A \lor B)$?
- To eliminate ambiguity define the precedence for each operator
 - E.g., ¬ has higher precedence than ∧, ∨ so: ¬A ∨ B means (¬A) ∨ B

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Semantics of propositional logic

- ullet Semantics are rules for determining the truth of a sentence lpha with respect to a model m
 - We want to determine if a sentence is true or false, given a possible world
- In propositional logic, a model m fixes the truth value (true or false) for every proposition symbol/atomic sentence, e.g.,
- The models are abstractions of the real world and have no a-priori connection to a specific world, e.g.,
 - $P_{1,2}$ is just a symbol and can mean:
 - "There is a pit in [1, 2]" or
 - "I'm in Paris today and tomorrow"

Computing the truth value of a sentence

- The truth value of a sentence can be derived from the truth of the proposition symbols (recursively from the model m), e.g.,
- If the KB is based on proposition symbols $P_{1,2}, P_{2,2}, P_{3,1}$:

$$m = \{P_{1,2} = F, P_{2,2} = F, P_{3,1} = T\}$$

- All sentences α are constructed from atomic sentences (assigned by the model m) and the five connectives:
 - $\neg P$ is T iff P is F in m
 - $P \wedge Q$ is T iff P and Q are both true in m
 - $P \lor Q$ is T iff P or Q are true in m
 - $P \implies Q$ is true unless P is true and Q is false in m
 - $P \iff Q$ is true iff P and Q are both true or both false in m
- Truth table contains the truth value of a sentence (no matter how complex) for each possible assignment of truth values to its components

• E.g.,
$$X = A \wedge B \vee C$$

A B C X

FFFF

Interpretation of Implication

- In a logical implication $P \implies Q$ there is no causation between P and Q
 - E.g., "5 is odd implies that Tokyo is the capital of Japan" is a true sentence in propositional logic (although very odd)
- Pathological cases for implication
 - An implication is true whenever the antecedent is false
 - . E.g., "5 is even implies pigs fly" is true
 - E.g., "5 is even implies Sam is smart" is true, even if Sam is not smart
 - The reason is that $P\Longrightarrow Q$ is saying "If P is true, I claim that Q is true. Otherwise I am making no claim"

Model Checking is Sound and Complete

- Model checking algorithm:
 - Enumerate all models (truth tables)
 - Check if α is true for every model where KB is true
- The model checking algorithm is:
 - Sound
 - "Any inference made by the algorithm is correct"
 - Implements the definition of entailment
 - Complete
 - "Any true sentence is inferred correctly by the algorithm"
 - ullet Works for any KB and lpha
 - Always terminates (finite number of models)
- Complexity of model checking with n variables
 - Time complexity is $O(2^n)$ (NP-complete)
 - Worst case is exponential
 - Average case is better than exponential
 - Space complexity is O(n) since enumeration is depth-first

Propositional Theorem Proving

- ullet To prove a desired sentence lpha under a knowledge base KB
 - \bullet Apply rules of inference to construct a proof of α
 - Any sentence can have only one of the following truth values:
 - 1. True
 - 2. False
 - 3. Undecidable under the KB
- Theorem proving vs. model checking:
 - Model checking involves enumerating all models to show the sentence is true/false in all models where KB is true
 - If the proof is short, theorem proving can be more efficient than model checking

Logical equivalence of sentences

- Two sentences α and β are logically equivalent $\alpha \equiv \beta$
 - Iff they are true in the same set of models:

$$M(\alpha) = M(\beta)$$

• Iff they entail each other:

$$\alpha \models \beta \land \beta \models \alpha$$

• E.g., $P \lor Q \equiv Q \lor P$

Logical equivalences (1/2)

Commutativity of ∧ and ∨

$$(\alpha \wedge \beta) \equiv (\beta \wedge \alpha)$$
$$(\alpha \vee \beta) \equiv (\beta \vee \alpha)$$

Associativity of ∧ and ∨

$$(\alpha \wedge \beta) \wedge \gamma \equiv \alpha \wedge (\beta \wedge \gamma) \equiv \alpha \wedge \beta \wedge \gamma$$
$$(\alpha \vee \beta) \vee \gamma \equiv \alpha \vee (\beta \vee \gamma) \equiv \alpha \vee \beta \vee \gamma$$

Distributivity of ∧ over ∨

$$\alpha \wedge (\beta \vee \gamma) \equiv (\alpha \wedge \beta) \vee (\alpha \wedge \gamma)$$

Distributivity of ∨ over ∧

$$\alpha \vee (\beta \wedge \gamma) \equiv (\alpha \vee \beta) \wedge (\alpha \vee \gamma)$$

Double negation elimination:

$$\neg(\neg\alpha)\equiv\alpha$$

Logical equivalences (2/2)

• Contraposition:

$$(\alpha \implies \beta) \equiv (\neg \beta \implies \neg \alpha)$$

• Implication elimination:

$$(\alpha \implies \beta) \equiv (\neg \alpha \lor \beta)$$

Biconditional elimination:

$$(\alpha \iff \beta) \equiv (\alpha \implies \beta) \land (\beta \implies \alpha)$$

• De Morgan:

$$\neg(\alpha \land \beta) \equiv (\neg\alpha \lor \neg\beta)$$
$$\neg(\alpha \lor \beta) \equiv (\neg\alpha \land \neg\beta)$$

Valid sentence

- A valid sentence α is true for all the models
 - E.g., *P* ∨ ¬*P*
 - Aka "tautology"
 - Every tautology is equivalent to the sentence *True*
- ullet Contradiction is a sentence lpha that is false for all the models
 - E.g., *P* ∧ ¬*P*
 - Every contraction is equivalent to the sentence False

Deduction theorem

• The sentence α entails β (written $\alpha \models \beta$) iff the sentence $\alpha \implies \beta$ is a tautology, i.e., is equivalent to True

Satisfiability

- A sentence α is satisfiable iff α is true for some model
- SAT problem is about determining satisfiability of sentence in propositional logic
 - \bullet One can enumerate all the possible models until one is found to satisfy the sentence α
 - It is NP-complete
- A sentence α is un-satisfiable iff α is never true (i.e., a contradiction)
- · Validity and satisfiability
 - α is valid (i.e., a tautology) iff $\neg \alpha$ is un-satisfiable
 - By contrapositive α is satisfiable iff $\neg \alpha$ is not valid ($\neg \alpha$ is not a tautology)

Proof by contraction

- The sentence $\alpha \models \beta$ is true iff the sentence $(\alpha \lor \neg \beta)$ is un-satisfiable (i.e., a contradiction)
- In other words in a proof by contradiction:
 - Assume α
 - Assume that the sentence β is false and
 - Prove that this leads to a contradiction
 - Thus β must be true

- Knowledge Representation
- Propositional logic
- First-order Logic
 - Syntax
 - Semantics
- Non-classical Logics

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Natural languages

- Natural languages (e.g., English, Italian) are:
 - Expressive
 - Medium for communication rather than representation
 - Ambiguous
 - E.g., "spring" is both a "season" and "something that goes boing"
 - Context-dependent
 - · Meaning depends on the sentence and context
 - E.g., "Look!"
- Sapir-Whorf hypothesis
 - Understanding of the world is influenced by language
 - Language influences thought (even through arbitrary grammatical features, e.g., gender of nouns)
 - Some languages lack words for certain concepts (e.g., direction)

Programming languages

- A programming language (e.g., C++, Python) is a formal language
 - Data structures represent facts
 - Code updates data structures in a domain-specific way
- Cons:
 - Programming is procedural (vs declarative)
 - Programming languages lack:
 - 1. A general mechanism for deriving facts from other facts
 - Code updates data structures based on programmer's domain knowledge
 - 2. Expressiveness to handle partial information
 - A variable represents a single value or unknown
 - · Can't easily handle partial information or quantify uncertainty
 - E.g., "A white knight is in b1 or in f6"
- Declarative language (e.g., propositional logic, first order logic)
 - Knowledge and inference are separate:
 - 1. Knowledge represents the domain-specific problem
 - 2. Inference is domain independent
 - Compositional semantics
 - The meaning of a sentence is a function of the meaning of its parts

Propositional logic

- E.g., *P* ∧ *Q*
- Pros
- Declarative
 - Semantics is based on relation between sentences and possible worlds
 - Can deal with partial information
 - E.g., "A white knight is in b1 or in f6" is represented with $WK1_{b1} \vee WK2_{f6}$
 - Compositional semantics
 - The meaning of a sentence is a function of the meaning of its parts
 - Context independent
 - Unambiguous
- Cons
 - Can't concisely describe environment with many objects, e.g.,
 - In English "The pawn is in a cell around b6" requires all the possible states to be enumerated

First-Order Logic (FOL): Intro

- First-order logic (FOL) extends propositional logic by:
 - Introducing quantifiers (∀, ∃)
 - Using predicates to represent properties and relations
- Combines pros of propositional logic with pros of natural language
 - Built around objects and relations
 - Allows to express facts about some or all objects, e.g.,
 - "Some humans have blue eyes"
 - "Squares neighboring the Wumpus are smelly"
- FOL provides expressive power to represent structured, relational knowledge

First-Order Logic: Syntax

- Constants: represent specific objects (e.g., Socrates)
- Predicates: describe properties or relations (e.g., Human(x))
- Functions: map tuples of objects to objects (e.g., Mother(x))
- Variables: placeholders (e.g., x, y)
- Quantifiers: $\forall x$ (for all x), $\exists x$ (there exists an x)

Sentences

- Term is a logical expression that refers to an object in a FOL model
- Atomic sentence = predicate symbol (i.e., which corresponds to relations) followed by a list of terms in parenthesis (i.e., constant or function symbol) Predicate(Term1, Term2, ...)
 - E.g., Brother(Richard, John), under the model / interpretation, Richard is the brother of John
 - E.g., Married(Father(Richard), Mother(John))
- Complex sentences = sentences using logical connectives complex, with the same syntax and semantics as in propositional logic
- Variable is a term that represents a possible object
 - Typically represented as lowercase letter (e.g., x, y, z)
 - can be used as argument of a function, e.g., LeftLeg(x)
- Equality symbol signifies that two terms refer to the same object
- E.g., Father(John) = Henry

Quantifiers and Scope

- Quantifiers express properties of entire collections of objects, instead of enumerating objects by name (like in propositional logic)
- Universal quantifier: $\forall x P(x)$
 - Universal quantifier makes a statement about every object
 - Statement is true if P(x) is true for all x
- Existential quantifier: $\exists x P(x)$
 - Existential quantifier makes a statement about some object (without naming it)
 - True if P(x) is true for at least one x
- Scope determines the portion of a formula a quantifier applies to
- Variables are bound by quantifiers or free (unbound)
- Sentences with no free variables are called closed formulas
- Example:
 - $\forall x (Cat(x) \rightarrow Mammal(x))$

Nested quantifiers

- = express more complex sentences using multiple quantifiers
- The order of quantifiers is important, so one can use parentheses to clarify
- Example:
 - "Brothers are siblings": $\forall x, y Brother(x, y) \implies Sibling(x, y)$
 - $\forall x, y Sibling(x, y) \iff Sibling(y, x)$ (symmetric relationship)
 - "Everybody loves somebody": $\forall x \exists y Loves(x, y)$
 - "There is someone loved by everyone": $\exists y \forall x Loves(x, y)$

Connection between \forall and \exists

• The two quantifiers are connected through negation and De Morgan rules

$$(\forall x \neg P) \iff (\neg \exists x)$$
$$\neg(\forall x P) \iff (\exists x \neg P)$$
$$(\forall x P) \iff (\neg \exists x \neg P)$$
$$(\exists x P) \iff (\neg \forall x \neg P)$$

- Knowledge Representation
- Propositional logic
 - Syntax
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First-order logic: Semantics

- Semantics define how sentences are interpreted in a domain
- Symbols represent entities, relationships, and functions in the domain
 - Constant symbols represent specific objects
 - E.g., Alice, GP, CS101
 - Predicate symbols represent relationships among objects
 - E.g., EnrolledIn(Student, Class), Teaches(Professor, Class), IsStudent(x), IsProfessor(x)
 - Function symbols represent mappings between objects
 - E.g., AdvisorOf(Student), DepartmentOf(Professor)
- An interpretation maps the world to its mathematical description, and vice versa
 - There are many possible interpretations
 - The intended interpretation is the one that is the most natural
 - ullet E.g., map the symbol $\emph{GP}
 ightarrow$ me
- Example:
 - Sentence: $\forall x (Human(x) \rightarrow Mortal(x))$
 - True if for every x in the domain, Human(x) implies Mortal(x)

Inference in First-Order Logic

- Goal: derive new sentences from existing ones using sound rules
- Universal Instantiation:
 - From $\forall x P(x)$ infer P(c) for any constant c
- Existential Instantiation:
 - From $\exists x P(x)$ infer P(c) with a new constant c
- Modus Ponens and other propositional rules apply
- FOL inference is semi-decidable:
 - If a sentence is entailed, a proof can be found
 - If not entailed, proof search may not terminate

Representing Knowledge in FOL

- FOL enables representation of:
 - General rules: $\forall x (Bird(x) \rightarrow CanFly(x))$
 - Specific facts: Bird(Tweety)
- Complex relations captured through predicates:
 - Loves(Romeo, Juliet), GreaterThan(3, 2)
- Functions express object construction:
 - FatherOf (John)
- Knowledge base built from axioms and facts
- Enables reasoning about objects, properties, and their relationships

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Ontological commitment

- Ontological commitments are assumptions about reality made by a language
- Different formal models make different assumptions on how the truth of sentences is defined:
 - Propositional logic:
 - The world consists of facts that are either true or false
 - First-order logic:
 - The world consists of objects with relations among them that hold or do not hold
 - Temporal logic:
 - · Facts about objects and relations hold at particular times or intervals
 - Higher-order logic:
 - Relations of first-order logic are objects themselves
 - E.g., can make assertions about relations (e.g., "all relations are transitive")

Epistemological commitment

- Epistemological commitment is a possible states of knowledge by an agent with respect to each fact
 - Ontological commitment = what exists in the world
 - Epistemological commitment = what an agent believes about facts
- E.g,
 - Propositional logic, first-order logic
 - 3 possible states of belief regarding any sentence: true, false, or unknown
 - Probability theory
 - There is a degree of belief in [0, 1] about each sentence

Non-monotonic Logic

- Non-monotonic logic is a type of logic where adding new information can invalidate previous conclusions
- Contrast with Classical (Monotonic) Logic
 - In classical logic, once something is proven, it stays proven even if more information is added
 - In non-monotonic logic, conclusions can change as new facts are learned

• E.g.,

- Initial knowledge: "Birds typically fly"
- Conclusion: "Tweety is a bird, so Tweety can fly"
- New information: "Tweety is a penguin"
- Revised conclusion: "Tweety cannot fly"

Why it Matters

- Real-world situations often involve incomplete or evolving knowledge
- Non-monotonic logic allows systems to reason flexibly and adapt to new circumstances

Default reasoning

- Default reasoning is reasoning where assumptions are made by default in the absence of contrary evidence
 - It allows conclusions based on typical situations unless exceptions are found
- Key Idea
 - Assume the most likely case unless specified otherwise
 - If new information contradicts the assumption, revise the conclusion
- E.g.,
 - Default rule: "Typically, birds can fly"
 - Fact: "Tweety is a bird"
 - Conclusion: "Tweety can fly"
 - New fact: "Tweety is a penguin"
 - Revised conclusion: "Tweety cannot fly"
- Why It Is Useful
 - In real life, information is often incomplete or uncertain
 - Default reasoning allows systems to function reasonably without knowing everything

Non-Monotonic Logic: University Example

Initial Facts

- Alice is a Student
- Alice belongs to the ComputerScience department
- CS101 is a Course offered by the ComputerScience department
- Default rule: *Students* in the *ComputerScience* department take classes in their department

Initial Reasoning

- Since Alice is a Student in ComputerScience, by default Students take CS101
- Conclusion: Alice takesCourse CS101

New Information

 Alice is an exchange student who does not meet the prerequisites for CS101

Revised Reasoning

New conclusion: Alice does not takeCourse CS101

Common Sense Reasoning

- Common sense reasoning is the ability to make assumptions, draw conclusions based on everyday knowledge about the world
 - Involves typical, unstated knowledge that humans take for granted, e.g.,
 - "If you drop a glass, it will likely break"
 - Knowing that "people eat food when they are hungry" without being explicitly told

Characteristics

- Deals with incomplete, uncertain, or ambiguous information
- Relies on defaults, heuristics, and typical patterns rather than strict logical proofs
- Often flexible and tolerant of exceptions

Challenges

- Common sense knowledge is vast, informal, and often not precisely defined
- Difficult to encode all of it explicitly in a machine-readable form
- Handling exceptions and contradictions is complex

Techniques

- Knowledge graphs
- Non-monotonic logic
- Probabilistic reasoning
- Machine learning models trained on large, diverse data

Common Sense Reasoning: University Example

Initial facts

- Alice is a Student
- Bob is a Student
- CS101 is a Course offered by the ComputerScience department

Common sense knowledge

- Students typically enroll in courses offered by their department
- Students usually attend classes they are enrolled in
- Professors usually teach the courses they are assigned

Reasoning steps

- Alice belongs to the ComputerScience department
- CS101 is offered by the ComputerScience department
- Common sense suggests Alice is likely enrolled in CS101, even if enrollment is not explicitly stated
- Therefore, it is reasonable to assume: Alice takesCourse CS101

New information

- Alice is pursuing research only and not taking courses
- The assumption that *Alice takesCourse CS*101 must be revised

Open World vs Closed World Assumptions

Closed World Assumption (CWA)

- Missing information is false, e.g.,
 - Fact: "Alice takes CS101" is known
 - Nothing is said about Bob
 - Under CWA: Conclude Bob does not take CS101
- Common in databases and logic programming

Open World Assumption (OWA)

- Missing information is unknown, not false, e.g.,
 - Fact: "Alice takes CS101" is known
 - Nothing is said about Bob
 - Under OWA: Cannot conclude if Bob takes CS101: it is unknown
- Common in Semantic Web, RDF, ontologies

Applications

- OWA
 - Semantic Web (RDF, OWL)
 - Knowledge representation with incomplete or growing data
- CWA
 - Traditional relational databases (SQL)
 - Business rules and systems requiring complete data

Inductive Logic Programming

Inductive Logic Programming

- Learns logical rules from examples and common sense knowledge
- Given positive and negative examples, and background facts, infer logical rules that explain the examples

Example

- Background: "Birds have wings"
- Positive example: "Tweety can fly"
- Negative example: "Penguin cannot fly"
- Learned rule: "Birds can fly unless they are penguins"

Features

- Produces human-readable logical rules
- Integrates learning with symbolic reasoning
- Supports background knowledge integration

Challenges

- Computational complexity with large datasets
- Handling noisy, incomplete, or ambiguous data

- Knowledge Representation
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 - Intro
 - Description Logics
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Description Logic

- Description Logic
 - Represents structured knowledge about a domain
 - Balances expressivity and computational efficiency
 - More expressive than propositional logic, less than first-order logic
- Core building blocks:
 - Concepts / classes: abstract groups
 - E.g., Person, Animal
 - Roles / properties: binary relations between individuals
 - E.g., hasChild, ownsPet
 - Individuals / instances: specific objects
 - E.g., GP, Nuvolo
- Supports reasoning tasks such as:
 - Concept subsumption: "is A a subset of B?"
 - Instance checking: "does a belong to A?"
- Syntax often combines:
 - Atomic concepts and roles
 - Logical constructors $(\sqcap, \sqcup, \neg, \forall, \exists)$
 - E.g.,
 - Father ≡ Man □ ∃hasChild.Person
- Widely used in ontologies, e.g., OWL (Web Ontology Language)

ALC

- Attributive Concept Language with Complements (ALC) is a basic but expressive description logic
 - Concepts can be combined using logical operators, e.g.,
 - □ means "and"
 - □ means "or"
 - ¬ means "not"
 - Allows for existential and universal quantification, e.g., $\exists R.C, \forall R.C$
- Interpretation is set-theoretic
 - Concepts as sets, roles as binary relations
- Example:
 - "All students take some course": Student

 ∃takes.Course
 - "A mother is a woman who has at least one child"
 Mother ≡ Woman □ ∃hasChild. □
- ALC:
 - Is decidable
 - balances expressiveness and computational complexity
 - Is basis for more complex logics used in OWL
 - Practical for moderate-sized ontologies

SHOIN

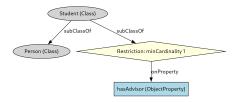
- SHOIN is a description logic more expressive than ALC
- Components:
 - S: Allows transitive properties
 - E.g., ancestorOf is transitive
 - \mathcal{H} : Supports role hierarchies
 - E.g., hasSon

 hasChild
 - O: Introduces specific individuals
 - E.g., John is a nominal class
 - ullet \mathcal{I} : Enables roles to be navigated backward
 - E.g., isChildOf is inverse of hasChild
 - \mathcal{N} : Sets cardinality constraints
 - E.g., "has exactly 1 passport"
- E.g.,:
 - "Exactly two children" Person \sqsubseteq (= 2 hasChild. \top)
- Characteristics
 - More powerful but reasoning is harder (exponential complexity)
 - Model richer real-world scenarios
 - Foundation for OWL DL reasoning capabilities

OWL

- OWL = Web Ontology Language
 - Semantic web language designed to represent complex knowledge about things and their relationships
 - Enables rich knowledge representation on the web (based on SHOIN)
 - "OWL" easier to pronounce than "WOL"
 - Supports formal semantics for machine reasoning
 - Key constructs:
 - Classes, properties, individuals, axioms
- Example:
- OWL variants:
 - OWL Lite: simpler, for classification hierarchies
 - OWL DL: full expressiveness with decidable reasoning
 - OWL Full: maximum expressiveness, but undecidable
- Applications
 - Semantic search
 - Biomedical data

Example of OWL in RDF



RDF (Resource Description Framework)

- RDF is a standard model for data interchange on the web
 - Represent structured information in a machine-readable way
- Basic building block is a triple (Subject, Predicate, Object)
 - Subject: the entity being described, e.g., Nuvolo
 - Predicate: the property or relationship, e.g., isA
 - Object: the value or another entity, e.g., Dog
- Key Features:
 - Statements are directed graphs of nodes and edges
 - Components of the triple are URIs (Uniform Resource Identifiers) to ensure global uniqueness or literals (e.g., strings, numbers), e.g., http://example.org/Nuvolo
- Use Cases:
 - Building knowledge graphs
 - Enabling semantic search
 - Supporting ontologies (e.g., OWL)

Book123 hasAuthor Author456 Author456 hasName "F. Scott Fitzgera Book123 publishedYear "1925"	Subject	Predicate	Object
Book123 belongsToGenre "Fiction"	Book123 Author456 Book123	hasAuthor hasName publishedYear	"F. Scott Fitzgerald" "1925"

SPARQL

- SPARQL is the query language for RDF data
 - Allows users to retrieve and manipulate data stored in RDF format
- Key Concepts:
 - Triple Patterns: Query fragments that match triples in an RDF graph
 - Basic Graph Pattern: A set of triple patterns combined
 - Variables: Stand in for unknown parts of the triples (e.g., ?person, ?animal)
- Main Query Types:
 - SELECT: Retrieve specific variables from the data
 - CONSTRUCT: Create new RDF triples based on query results
 - ASK: Return a boolean indicating whether a pattern exists
 - DESCRIBE: Return an RDF graph describing resources
- Example:
 - "Find all resources that are of type Bird"
 SELECT ?animal WHERE { ?animal rdf:type ex:Bird }

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Semantic Web

- The Semantic Web extends the current Web by enabling machines to understand and interpret data
 - HTML is human-readable but lacks semantic structure for computers
 - The Semantic Web adds meaning / semantics to data
 - Allow better data integration, automation, and discovery across sites

Key Technologies

- RDF (Resource Description Framework): base data model
- SPARQL: query language for RDF data
- OWL (Web Ontology Language): define rich ontologies

Current Status

- Some core ideas (e.g., structured data and ontologies) are widely adopted
- Full vision remains only partially realized

Challenges

- Complexity of widespread adoption
- · Issues around privacy, data ownership, and feasibility
- Need for standardization and tools

Criticism

- Skepticism about practicality and scalability
- Concerns about centralization and censorship

WikiData

- WikiData is a free, open, collaborative knowledge base
 - Stores structured data for Wikipedia
 - Accessible via APIs using SPARQL queries
- Graph-based data model
 - Item: represents an entity or concept, e.g.,
 - Q42 → Douglas Adams
 - Property: describes a relationship or attribute, e.g.,
 - P31 (instance of), P27 (country of citizenship)
 - Value: specific data linked to an item via a property, e.g.,
 - Q42 (Douglas Adams) o P31 (instance of) o Q5 (human)
 - Q42 \rightarrow P106 (occupation) \rightarrow Q36180 (science fiction writer)
 - Reference: supports a claim by citing a source, e.g.,
 - Stating Douglas Adams's citizenship with a reference to a biography
 - Qualifier: adds context or additional information to a statement
 Q90 (Paris) → P1082 (population) → "2,165,423"
 - With qualifier: P585 (point in time) → "2021"

- Meaning: "The population of Paris was 2,165,423 in the year 2021"
- Applications:
 - Knowledge graph
 - Semantic search
 - Al reasoning
 - Data enrichment

DBPedia

- DBpedia extracts structured content from Wikipedia
 - Creates a large-scale, multilingual knowledge graph for querying
 - Data is extracted as RDF triples (subject-predicate-object), e.g.,
 - "Berlin" entity linked with properties like dbo:country Germany, dbo:populationTotal 3.7M
 - Enables semantic queries over Wikipedia data via SPARQL endpoints
- Applications
 - Semantic Web research
 - Enhancing AI models with real-world knowledge

Semantic Networks

- Semantic Networks represent knowledge as graphs of concepts and relations
 - Nodes represent concepts
 - Edges represent relations (e.g., "is-a", "part-of")
 - E.g., if a Dog is an Animal, it inherits Animal traits
 - Examples: WordNet, ConceptNet
- Pros
 - Easy to visualize and traverse
 - Support reasoning
 - Common in early AI systems and current KG applications

WordNet

- WordNet is a large lexical database of English words
 - Designed to model the semantic relationships between words
 - Groups words into sets of synonyms
 - Manually curated, ensuring high-quality semantic relations
 - Can be incomplete for domain-specific language
- Key Components:
 - Synsets: Sets of synonyms expressing a distinct concepts
 - E.g., {car, automobile} share the same synset
 - Relations between synsets:
 - Is-a relationships (e.g., Dog is a type of Animal)
 - Part-whole relationships (e.g., Wheel is a part of Car)
 - Opposite meanings
- Structure:
 - Semantic network where nodes are synsets and edges are relations
 - Organized hierarchically, especially for nouns and verbs
- Applications:
 - Word sense disambiguation: choose the correct meaning of a word in context
 - Semantic similarity measures: how close two concepts are
 - Information retrieval and question answering systems

ConceptNet

- ConceptNet is a large knowledge graph
 - Connects words and phrases with labeled semantic relationships
 - Represents commonsense knowledge about the world
- Key Characteristics:
 - Designed to capture knowledge that people generally assume but often leave unstated
 - Focuses on making AI systems more human-like in their understanding
- Structure:
 - Nodes: concepts (words or phrases)
 - Edges: semantic relationships between concepts, e.g.,
 - IsA: (dog, animal)
 - PartOf: (wheel, car)
 - UsedFor: (knife, cutting)
 - CapableOf: (bird, fly)
 - Causes: (fire, smoke)
- Example Triple:
 - (bicycle, UsedFor, transportation)
- Applications:
 - Natural language understanding
 - Question answering and chatbots
 - Commonsense reasoning in AI
 - Semantic search and recommendation systems

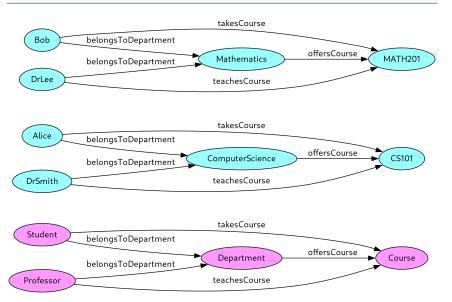
Frame-Based Representations

- Frame-based systems represent structured knowledge about objects, events, or situations
- Key Concepts:
 - Frame: A data structure for a concept or entity
 - E.g., a frame for Dog might include properties like hasLegs, hasFur, barks
 - Slots: attributes or relationships associated with the frame
 - E.g., slot hasLegs with value 4
 - Slot fillers: values or links to other frames that fill the slots
 - E.g., slot eats might link to another frame Meat
- Example:
 - Frame: Dog
 - Slots:
 - isA: Animal
 - hasLegs: 4
 - sound: Bark
 - canDo: [Run, Fetch]
- Features:
 - Inheritance: frames can inherit slots and slot values from more general frames. e.g..

Knowledge Graphs (KGs)

- KGs represent entities and their relationships as a graph structure
 - Nodes = entities
 - Edges = relations
 - E.g., "Paris \rightarrow isCapitalOf \rightarrow France"
- Query languages like SPARQL allow expressive information retrieval
- KGs support reasoning via path traversal and schema inference
- Applications:
 - Question answering
 - Recommendation
 - Semantic search
- Widely used by Google, Facebook, and academic search engines

Knowledge Graph: University Example



Technologies

- TransE (Translation Embedding)
 - Embedding model for knowledge graph completion
 - Represents relationships as translations in vector space: $h + r \approx t$
 - Good for 1-to-1 relations, less effective with complex patterns

RotatE

- Embeds entities in complex space
- Models relations as rotations: $t = h \circ r$ where \circ is complex multiplication
- Captures symmetry, antisymmetry, inversion, and composition

DeepProbLog

- Combines ProbLog (probabilistic logic) with deep learning
- Supports neural predicates in logic programs
- · Learns probabilistic facts and neural components jointly

PyMLN

- Python-based Markov Logic Network (MLN) system
- MLNs combine first-order logic with probabilistic graphical models
- Allows reasoning with weighted logical rules

ProbLog

- Probabilistic logic programming language
- Extends Prolog by attaching probabilities to facts
- Computes success probabilities of queries

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