BUAN 6356.501 - Business Analytics with R (Spring 2019) Problem Set 4

Question 1 <- hprice1

```
[1] 910.4328
           st_model1) # 925.2968
[1] 925.2968
  summary(best_model1)
lm(formula = price ~ assess + sqrft + colonial + assess:sqrft,
    data = hprice1)
Residuals:
                  10
                         Median
                                         3Q
-103.086 -20.747
                                   17.914 198.887
                         -2.724
Coefficients:
                  Estimate Std. Error t value Pr(>|t|)
(Intercept) 1.806e+02 5.907e+01 3.057 0.003009 **
                                             1.342 0.183236
                 2.793e-01 2.081e-01
assess
                                            1.342 0.183236
-2.885 0.004986 **
sqrft
                -7.932e-02 2.749e-02
colonial 2.161e+01 9.752e+00 2.216 0.029461 * assess:sqrft 2.483e-04 6.876e-05 3.611 0.000522 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
Residual standard error: 41.06 on 83 degrees of freedom
Multiple R-squared: 0.8475, Adjusted R-squared: 0.8402
F-statistic: 115.4 on 4 and 83 DF, p-value: < 2.2e-16
```

Question 2 <- gpa2

```
12) # 6590.858
[1] 6590.858
[1] 6679.446
  summary(best_model2)
call:
lm(formula = colgpa ~ sat + tothrs + hsize + hsrank + hsperc +
     female + black + sat:tothrs + sat:hsperc + tothrs:hsperc +
     hsize:hsrank + hsrank:hsperc, data = gpa2)
Residuals:
Min 1Q Median 3Q Max
-2.49445 -0.34247 0.01724 0.37326 2.06664
Coefficients:
                   Estimate Std. Error t value Pr(>|t|)
                  4.353e-01 1.502e-01 2.898 0.003781 **
2.314e-03 1.368e-04 16.913 < 2e-16 ***
(Intercept)
sat
                  9.961e-03 1.917e-03 5.195 2.14e-07 ***
3.031e-02 9.388e-03 3.229 0.001253 **
tothrs
                                               3.229 0.001253 **
hsize
                 -5.543e-03 7.103e-04 -7.803 7.59e-15 ***
hsrank
                                3.777e-03
1.740e-02
                  1.276e-02
                                              3.378 0.000738 ***
hsperc
                  1.452e-01
                                               8.346 < 2e-16 ***
female
                                             -8.329
black
                 -3.177e-01 3.814e-02
                                                       < 2e-16 ***
                                1.761e-06 -5.259 1.53e-07 ***
                 -9.260e-06
sat:tothrs
                 -2.483e-05 3.557e-06 -6.980 3.42e-12 ***
sat:hsperc
tothrs:hsperc 6.972e-05
                                              4.515 6.50e-06 ***
                                1.544e-05
hsize:hsrank 2.158e-04 7.241e-05 2.980 0.002897 **
hsrank:hsperc 5.236e-05 8.367e-06 6.258 4.29e-10 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 0.5357 on 4124 degrees of freedom
Multiple R-squared: 0.3404, Adjusted R-squared: 0.3385
F-statistic: 177.3 on 12 and 4124 DF, p-value: < 2.2e-16
```

Question 3 <- mlb1

Question 4 <- rental

1. The average rent in 1990 increased by 26% when compared to the average rent in 1980, $\beta_3 = 0.005$ For every 1 unit increase in *pctstu* (relative student size), there is nearly 0.5% increase in the rent.

- 2. The above standard errors are not valid because we did not use fixed-difference model.
- 3. We get $\beta_3 = 0.0112$. For 1 point increase in *pctstu*, there is nearly 1.12% increase in rent.

```
call:
plm(formula = log(rent) ~ y90 + log(pop) + log(avginc) + pctstu,
data = pdrental, model = "fd")

Balanced Panel: n = 64, T = 2, N = 128
Observations used in estimation: 64

Residuals:
Min. lst Qu. Median 3rd Qu. Max.
-0.186972 -0.062160 -0.014383 0.055183 0.237830

Coefficients:
Estimate Std. Error t-value Pr(>|t|)
(Intercept) 0.3855214 0.0368245 10.4692 3.661e-15 ***
log(pop) 0.0722457 0.0883426 0.8178 0.416713
log(avginc) 0.3099604 0.0664771 4.6627 1.788e-05 ***
pctstu 0.0112033 0.0041319 2.7114 0.008726 **
---
Signif. codes: 0 **** 0.001 *** 0.01 ** 0.05 *. 0.1 * 1

Total Sum of Squares: 0.7191
Residual Sum of Squares: 0.48736
R-Squared: 0.32226
Adj. R-Squared: 0.28837
F-statistic: 9.50992 on 3 and 60 DF, p-value: 3.1362e-05
```

4. Yes, we get same estimates and same errors as we got in fixed-difference model.

Question 5 <- murder

- 1. β_1 should be negative for deterrent effect. β_2 could be positive as unemployed might do crimes.
- 2. For 1990-93, $\beta_1 = 0.12773$ implying no deterrent effect but it is statistically insignificant.

3. $\beta_1 = -0.10384$ implying a deterrent effect. With every execution, murder rate drop by 10.38%

- 4. The robust standard error for exec is 0.164
- 5. Texas had 34 executions. Next highest is 11 implying Texas has a lead of 23 executions.
- 6. The usual and robust errors are close to each other when compare to pooled model.

7. For all three years model, $\beta_1 = -0.13832$ but the coefficients from both models are insignificant.

```
call:
plm(formula = mrdrte ~ as.factor(year) + exec + unem, data = pdmurder,
model = "within")

Balanced Panel: n = 51, T = 3, N = 153

Residuals:
    Min. 1st Qu. Median 3rd Qu. Max.
    -26.685751 -0.658371 -0.065721 0.674717 13.394112

Coefficients:
    as.factor(year)90 1.55621 0.74533 2.0880 0.03939 *
as.factor(year)91 1.73324 0.70044 2.4745 0.01506 *
exec -0.13832 0.17701 -0.7815 0.43642
unem 0.22132 0.29638 0.7467 0.45701
---
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1

Total Sum of Squares: 1311.5

Tesidual Sum of Squares: 1215.2
R-Squared: 0.073367
Adj, R-Squared: 0.43723
F-statistic: 1.93981 on 4 and 98 DF, p-value: 0.10984
```

Question 6 <- airfare

1. If $\Delta bmktshr = 0.10$ then fare increases by 3.6%

```
Carr.
plm(formula = log(fare) ~ as.factor(year) + bmktshr + log(dist) +
I(log(dist)^2), data = pdairfare, model = "pooling")
 Balanced Panel: n = 1149, T = 4, N = 4596
 Residuals:
                                   Median
                  1st Qu.
                                                  3rd Qu.
 Min. 1st Qu. Median 3rd Qu. Max.
-1.307955 -0.253740 -0.026729 0.247446 0.958113
 Coefficients:
                                  Estimate Std. Error t-value Pr(>|t|)
5.2092571  0.4206247 14.7620 < 2.2e-16 ***
0.0211244  0.0140419  1.5044  0.132553
0.0378496  0.0140413  2.6956  0.007052 **
                               6.2092571
0.0211244
as.factor(year)1998
as.factor(year)1999
 as.factor(year)2000
                                 0.0998700
                                                 0.0140432
                                                                   7.1116 1.324e-12 ***
                                                 0.0300691 11.9764 < 2.2e-16 ***
0.1282730 -7.0288 2.391e-12 ***
 bmktshr
                                 0.3601204
 log(dist)
                                -0.9016003
 I(log(dist)^2)
                                 0.1030196
                                                 0.0097255 10.5927 < 2.2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' '1
Total Sum of Squares: 875.09
Residual Sum of Squares: 519.64
                                      875.09
 R-Squared:
R-Squared: 0.40619
Adj. R-Squared: 0.40541
F-statistic: 523.175 on 6 and 4589 DF, p-value: < 2.22e-16
```

2. For β_1 , usual confidence interval is (0.301, 0.419) and robust confidence interval is (0.298, 0.423)

- 3. Coefficient of $[ln(dist)]^2$ shows increasing marginal effect. Relation between ln(fare) and dist becomes positive when the first derivative of dist with respect to ln(dist) equals zero and this happens when dist = 79.50877 which does not lie in our data range of (95,2724)
- 4. For fixed effects, coefficient estimate of $\beta_1 = 0.17$

- 5. Avg flights/route & Avg passengers/flight can be in α_i and might be correlated to *bmktshr*.
- 6. Yes, for both linear and pooled models the *bmktshr* coefficient estimate is positive.

Question 7 <- loanapp

1. For both logit and linear models, approval rate for whites is 90.84% and for nonwhites is 70.78%

```
glm(formula = approve ~ white, family = binomial(), data = loanapp)
Deviance Residuals:
   Min
             10
                  Median
                               3Q
                                       Max
-2.1864
          0.4384
                   0.4384
                           0.4384
                                    0.8314
Coefficients:
            Estimate Std. Error z value Pr(>|z|)
(Intercept)
             0.8847
                        0.1253 7.061 1.65e-12 ***
                                 9.325 < 2e-16 ***
             1.4094
                        0.1512
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '. ' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
    Null deviance: 1480.7 on 1988 degrees of freedom
Residual deviance: 1401.8 on 1987 degrees of freedom
AIC: 1405.8
Number of Fisher Scoring iterations: 5
```

2. Yes, there is significant evidence of discrimination against nonwhites.

```
glm(formula = approve ~ white + hrat + obrat + loanprc + unem +
    male + married + dep + sch + cosign + chist + pubrec + mortlat1 +
    mortlat2 + vr, family = binomial(), data = loanapp)
Deviance Residuals:
                  Median
    Min
             1Q
                                          Max
-2.9549
          0.2545
                    0.3458
                             0.4768
                                       2.0827
Coefficients:
             Estimate Std. Error z value Pr(>|z|)
(Intercept) 3.80171
                        0.59467
                                  6.393 1.63e-10 ***
                                   5.424 5.84e-08 ***
                         0.17290
white
             0.93776
                         0.01288
                                  1.030 0.30313
-4.702 2.58e-06 ***
             0.01326
hrat
obrat
             -0.05303
                         0.01128
                                   -4.138 3.51e-05 ***
loanprc
            -1.90495
                         0.46041
unem
            -0.06658
                         0.03281
                                  -2.029 0.04242 *
male
            -0.06639
                         0.20642
                                  -0.322 0.74776
                         0.17799
                                   2.828 0.00469 **
married
             0.50328
                                  -1.237 0.21598
0.231 0.81723
dep
             -0.09073
                         0.07333
sch
             0.04123
                         0.17840
                                   0.296 0.76720
cosign
             0.13206
                         0.44608
                                   6.230 4.67e-10 ***
chist
             1.06658
                         0.17121
pubrec
            -1.34067
                         0.21736
                                  -6.168 6.92e-10 ***
            -0.30988
                         0.46351
                                  -0.669 0.50378
mortlat1
                                  -1.574 0.11559
-2.276 0.02286 *
mortlat2
            -0.89468
                         0.56857
            -0.34983
vr
                         0.15372
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
Null deviance: 1476 on 1970 degrees of freedom
Residual deviance: 1201 on 1955 degrees of freedom
  (18 observations deleted due to missingness)
AIC: 1233
Number of Fisher Scoring iterations: 5
```

Question 8 <- alcohol

- 1. 89.82% of all people are employed and 9.92% of all people have abused alcohol.
- 2. Alcohol abuse lowers employability by 2.83% and it is significant at 5% which is as expected.

3. For logit model, the sign remains same, but the significance level improved from 5% to 1% Logit model suggests that alcohol abuse lowers employability by 28.3%, 10 times of linear model.

```
call:
glm(formula = employ ~ abuse, family = binomial(), data = alcohol)
Deviance Residuals:
Min
-2.1506
                       Median
           0.4566
                                 0.4566
                                            0.5219
                      0.4566
Coefficients:
              Estimate Std. Error z value Pr(>|z|)
              2.20832
-0.28337
(Intercept)
                            0.03559 62.046
0.10251 -2.764
                                                 0.0057 **
abuse
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
 (Dispersion parameter for binomial family taken to be 1)
Null deviance: 6463.8 on 9821 degrees of freedom
Residual deviance: 6456.6 on 9820 degrees of freedom
                                          degrees of freedom
Number of Fisher Scoring iterations: 4
```

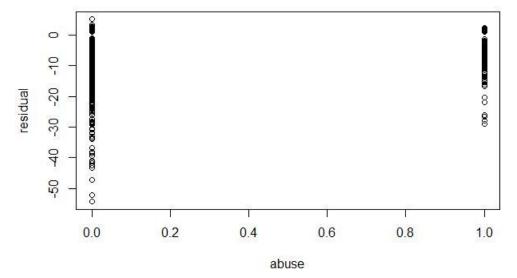
- 4. Fitted values are 0.901 for abuse = 0 and 0.873 for abuse = 1. They are same for both models.
- 5. Coefficient is almost is similar and it is still significant at 5% level.

```
term
               estimate std.error statistic p.value
(Intercept)
              0.179
                         0.0661
                                         2.71
                                               6.69
                         0.00990
abuse
                                                4.09
              0.0160
                                         5.63
age
                         0.00284
                                               1.90
I(age^2)
                         0.0000342
                                                  46
              0.0369
                         0.00540
                                         6.84
educ
                                                8.34
I(educ^2)
                         0.000210
                                                3.12
married
              0.0574
                         0.00884
                                         6.48
                                               9.33
              0.00299
famsize
                        0.00218
                                         1.37
                                                1.70
white
               0.0986
                         0.00866
                                        11.4
                         0.00917
northeast
              0.0166
                                         1.81
                                                7.02
              0.004\overline{71}
                         0.00864
                                         0.546
                                                5.85
midwest
                         0.00834
south
              0.0152
                                         1.82
                                                6.84
centcity
                         0.00829
                                                6.20
                         0.007<u>75</u>
0.008<u>30</u>
outercity
               0.0149
                                         1.92
                                                5.51
                                                2.43
art1
                         0.00832
                                                4.17
qrt2
                         0.00840
                                                8.
                                                  50
```

- 6. Marginal effect of abuse is still 23% (10 times of linear model) and its t-statistic is -2.14535
- 7. Considering their significance, it is obvious to include health related variables in our model.

```
mode [8d]
              estimate std.error statistic
term
                                              p. value
(Intercept)
                       0.0646
                                            2.38
exhealth
              0.574
                       0.0195
                                      29.4
                                            9.04
vghealth
              0.570
                       0.0196
                                      29.1
                                            3.85
goodhealth
              0.535
                       0.0197
                                            2.02
fairhealth
             0.393
                                             5.55
                       0.0221
                                      17.8
                       0.00945
abuse
                                            9.68
              0.0162
                       0.00270
                                       6.00 2.02
age
I(age^2)
                       0.0000326
                                            4.56
              0.0168
                       0.00519
                                       3.23
educ
                                            1.23e
I(educ^2)
                       0.000201
                                             7.96
```

8. As *abuse* goes from 0 to 1, *residuals* decrease implying that *abuse* and *residual* are correlated. *mothalc* & *fathalc* can't be used as instrument variables as they have low correlation with *abuse*.



Question 9 <- fertil1

1. Fertility dropped by 19.9% in the year 1982

```
call:
glm(formula = kids ~ educ + age + I(educ^2) + black + east +
     northcen + west + farm + othrural + town + smcity + y74 + y76 + y78 + y80 + y82 + y84, family = poisson(), data = fertill)
Deviance Residuals:
                         Median
 -2.83050 -0.68862
                       -0.04099
                                    0.55084
                                                2.77002
Coefficients:
               0.529391
0.073904
 (Intercept)
age
I(educ^2)
black
              0.007318
-0.004974
                            0.003131
0.001528
                                         2.337
                                                 0.01942
                                        -3.255
5.724
1.307
                                                 0.00114
               0.349381
0.069049
                            0.061034
                                               1.04e-08
                            0.052838
east
                                                 0.19128
northcen
               0.114356
                            0.047852
                                         2.390
                                                 0.01686
                            0.065857
                                         0.807
west
                                        -0.269
-0.702
farm
               -0.015461
                            0.057470
                            0.068889
0.048547
othrural
              -0.048372
               0.031044
                                         0.639
town
               0.078378
                            0.061528
smcity
               0.082107
                            0.062997
                                         1.303
               0.039072
                            0.067420
                            0.068552
                                        -0.434
                                                 0.66461
                            0.069034
                                                0.81893 0.00313
 y80
               -0.015803
                                        -0.229
y82
              -0.199045
                                        -2.955
              -0.222174
                            0.069405
                                        -3.201
                                                 0.00137 **
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for poisson family taken to be 1)
     Null deviance: 1331.1 on 1128 degrees of freedom
Residual deviance: 1185.9 on 1111 degrees of freedom
Number of Fisher Scoring iterations: 5
```

- 2. Estimated percentage difference in fertility for black woman nonblack woman is 34.94%
- 3. For poisson model, $R^2 = 0.11898$ and for linear model, $R^2 = 0.1248$ both of which are similar.