

## RUNNING INSTRUCTIONS

It was impossible for me to include one runnable text file with my program as I used separate compilation and a dependency manager in my development. As such, I've tried to alleviate this with including a zip file of my working directory wherein there is located a built binary file capable of being run on Linux systems (and hopefully Mac systems, I haven't tested it).

With the extracted zip file, there should appear a *puzzle-problem* directory. Navigate into it and the following command format should work:

```
./app/Main filePath heuristicFlag
```

filePath represents the input file path. For example: `./input/Input1.txt`

heuristicFlag represents the heuristic choice and can be either 0 or 1 with 0 representing a heuristic of only the sum of the manhattan distances and 1 representing the sum of manhattan distances + 2x linear conflicts.

An example running of the program with input `./input/Input1.txt` and heuristic 0 would be:

```
./app/Main ./input/Input1.txt 0
```

The output of which should be writing to the *output.txt* file in the *output* directory.

Another possible way to run this program is to install my dependency manager, stack, for which the instructions can be found on this page: [https://docs.haskellstack.org/en/stable/install\\_and\\_upgrade/](https://docs.haskellstack.org/en/stable/install_and_upgrade/)

Once installed, at least on a Linux system, one should be able to run my program, once again in the *puzzle-program* directory, you can type first:

```
slack build
```

To build the project and then you can type:

```
stack exec puzzle-problem-exe filePath heuristicFlag
```

Where filePath and heuristicFlag correspond to the previous usage of the command line arguments as described above for the running of the file with the binary

If this does not work, please contact me ([ggf221@nyu.edu](mailto:ggf221@nyu.edu)) and I can arrange a time to meet in person to show you the running of my program with any text file provided.

# OUTPUT

## **Output1\_A**

7 1 6

8 3 5

2 0 4

8 7 6

1 0 5

2 3 4

5

12

U U L D R

5 5 5 5 5

## **Output1\_B**

7 1 6

8 3 5

2 0 4

8 7 6

1 0 5

2 3 4

5

12

U U L D R

5 5 5 5 5

## **Output2\_A**

2 6 0

1 3 4

7 5 8

1 2 3

4 5 6

7 8 0

10

27

L D R U L L D R D R

10 10 10 10 10 10 10 10 10 10

## **Output2\_B**

2 6 0

1 3 4

7 5 8

1 2 3  
4 5 6  
7 8 0

10  
24  
L D R U L L D R D R  
10 10 10 10 10 10 10 10 10 10 10

### **Output3\_A**

5 4 3  
2 6 7  
1 8 0

1 2 3  
4 5 6  
7 8 0

22  
1921  
U L U L D D R U U L D D R R U L L D R U R D  
12 12 12 12 12 12 12 14 16 16 16 16 18 18 18 20 22 22 22 22 22 22 22

### **Output3\_B**

5 4 3  
2 6 7  
1 8 0

1 2 3  
4 5 6  
7 8 0

22  
1131  
U L U L D D R U U L D D R R U L L D R U R D  
12 14 14 14 14 14 14 16 18 18 18 18 18 18 18 20 22 22 22 22 22 22 22

### **Output4\_A**

8 7 3  
0 4 5  
6 2 1

1 2 3  
4 5 6  
7 8 0

23  
1164  
U R D D R U L D L U U R D R D L L U U R D R D

17 17 17 19 19 19 21 23 23 23 23 23 23 23 23 23 23 23 23 23 23

### **Output4\_B**

8 7 3

0 4 5

6 2 1

1 2 3

4 5 6

7 8 0

23

696

U R D D R U L D L U U R D R D L L U U R D R D

17 17 17 19 19 19 21 23 23 23 23 23 23 23 23 23 23 23 23 23 23

## **SOURCE CODE**

### **Board.hs**

module Board where

type Board = [Int]

boardWidth = 3 :: Int

### **Index.hs**

module Index where

import Data.List (elemIndex)

import Data.Tuple (swap)

import Board

toIndex :: (Int, Int) -> Int

toIndex (x,y) = x + (y \* boardWidth)

fromIndex :: Int -> (Int, Int)

fromIndex i = swap \$ divMod i boardWidth

-- validSingle checks if x or y val is on game board

validSingle :: Int -> Bool

validSingle x

  | x < 0 = False

  | x > boardLimit = False

  | otherwise = True

  where

    boardLimit = boardWidth - 1

-- validCoord checks if co-ord given is on game board

```

validCoord :: (Int, Int) -> Bool
validCoord (x,y)
  | not $ validSingle x = False
  | not $ validSingle y = False
  | otherwise = True

-- finds the starting index and the goal index for a value
findStartGoalIndexes :: Board -> Board -> Int -> Maybe (Int, Int)
findStartGoalIndexes current goal element =
  case elemIndex element current of
    Just currentIndex ->
      case elemIndex element goal of
        Just goalIndex -> (Just (currentIndex, goalIndex))
        Nothing -> Nothing
    Nothing -> Nothing

-- returns the sum of a list of Maybe Int
sumMaybeInt :: [Maybe Int] -> Maybe Int
sumMaybeInt = fmap sum . Sequence

```

### **Manhattan.hs**

```

module Manhattan where

import Data.List (elemIndex)
import Data.Functor (fmap)
import Control.Monad (sequence)

import Index
import Board

-- Get the distance between two x,y coords
coordDistance :: (Int, Int) -> (Int, Int) -> Int
coordDistance (x1,y1) (x2,y2) =
  xDistance + yDistance
  where
    xDistance = abs $ x1 - x2
    yDistance = abs $ y1 - y2

-- Get the manhattan distance given an element on the board
manhattanDistance :: Board -> Board -> Int -> Maybe Int
manhattanDistance current goal element =
  case findStartGoalIndexes current goal element of
    Just (currentIndex, goalIndex) ->
      (Just distance)
      where
        distance = coordDistance (fromIndex currentIndex) (fromIndex goalIndex)
    Nothing -> Nothing

-- Get the sum of all calculated manhattan distances on the board

```

```

manhattanSum :: Board -> Board -> Maybe Int
manhattanSum current goal =
    sumMaybeInt distanceList
  where
    distanceList = map (manhattanDistance current goal) [1..8]

```

## LinearConflict.hs

```

module LinearConflict where

```

```

import Index
import Board

```

```

-- listEquals checks if all elements in a list are the same

```

```

listEquals :: [Int] -> Bool

```

```

listEquals xs = and $ map (== head xs) (tail xs)

```

```

-- coordLinConflict returns if two vals (with start and goal coords known) are

```

```

-- in linear conflict. This function could use improvement. The nested ifs are

```

```

-- ugly.

```

```

coordLinConflict ::

```

```

    (Int, Int) -- startLeftCoord

```

```

-> (Int, Int) -- goalLeftCoord

```

```

-> (Int, Int) -- startRightCoord

```

```

-> (Int, Int) -- goalLeftCoord

```

```

-> Bool -- if linear conflict

```

```

coordLinConflict

```

```

    (leftStartX, leftStartY)

```

```

    (leftGoalX, leftGoalY)

```

```

    (rightStartX, rightStartY)

```

```

    (rightGoalX, rightGoalY) =

```

```

    -- are the coords in the same column?

```

```

    if listEquals $ leftStartX:leftGoalX:rightStartX:rightGoalX:[]

```

```

    then

```

```

        -- check whether they're in a linear conflict within the column

```

```

        if leftStartY < rightStartY

```

```

        then

```

```

            if leftGoalY > rightGoalY

```

```

            then True

```

```

            else False

```

```

        else if leftStartY > rightStartY

```

```

        then

```

```

            if leftGoalY < rightGoalY

```

```

            then True

```

```

            else False

```

```

        else False

```

```

    -- are the coords in the same row?

```

```

    else if listEquals $ leftStartY:leftGoalY:rightStartY:rightGoalY:[]

```

```

    then

```

```

        -- check if they're in a linear conflict within the row

```

```

if leftStartX < rightStartX
then
  if leftGoalX > rightGoalX
  then True
  else False
else if leftStartX > rightStartX
then
  if leftGoalX < rightGoalX
  then True
  else False
else False
else False

```

```

-- linConflict returns whether two squares on a start board are in linear conflict
-- with reference to the goal board

```

```

linConflict :: Board -> Board -> Int -> Int -> Maybe Bool

```

```

linConflict current goal left right =

```

```

  case findStartGoalIndexes current goal left of

```

```

    Just (startLeft, goalLeft) ->

```

```

      case findStartGoalIndexes current goal right of

```

```

        Just (startRight, goalRight) ->

```

```

          (Just conflict)

```

```

        where

```

```

          conflict = coordLinConflict (fromIndex startLeft) (fromIndex goalLeft) (fromIndex
startRight) (fromIndex goalRight)

```

```

          Nothing -> Nothing

```

```

          Nothing -> Nothing

```

```

-- conv maybe bool to maybe int

```

```

mBoolToInt :: Maybe Bool -> Maybe Int

```

```

mBoolToInt mbool =

```

```

  case mbool of

```

```

    Just val ->

```

```

      if val then (Just 1)

```

```

      else (Just 0)

```

```

    Nothing -> Nothing

```

```

mBoolToIntList :: [Maybe Bool] -> [Maybe Int]

```

```

mBoolToIntList = map mBoolToInt

```

```

-- returns the sum of a list of bools as an int

```

```

sumMaybeBool :: [Maybe Bool] -> Maybe Int

```

```

sumMaybeBool = sumMaybeInt . mBoolToIntList

```

```

-- for one value on the board, compute all its linear conflicts

```

```

linConflictSumVal :: Board -> Board -> Int -> Maybe Int

```

```

linConflictSumVal current goal val =

```

```

  sumMaybeBool conflicts

```

```

  where

```

```

    conflicts = map (linConflict current goal val) [1..8]

-- for all values on the board, compute the total linear conflicts
linConflictSum :: Board -> Board -> Maybe Int
linConflictSum current goal =
    sumMaybeInt conflictSums
    where
        conflictSums = map (linConflictSumVal current goal) [1..8]

```

### Heuristics.hs

```

module Heuristics where

```

```

import Board
import Index
import Manhattan
import LinearConflict

```

```

-- heuristic 1: only the manhattan distance
manhattanHeuristic :: Board -> Board -> Maybe Int
manhattanHeuristic current goal =
    manhattanSum current goal

-- heuristic 2: the sum of manhattan distance + 2x * linear conflicts
manhattanLinConflictHeuristic :: Board -> Board -> Maybe Int
manhattanLinConflictHeuristic current goal =
    sumMaybeInt $ manhattanResult:linConflictResult:[]
    where
        manhattanResult = manhattanSum current goal
        linConflictResult = linConflictSum current goal

```

### AStar.hs

```

module AStar where

```

```

import Board
import Index
import Data.List (elemIndex, minimumBy)
import Heuristics

```

```

data Move = L | R | U | D
    deriving (Eq)

```

```

moveSet = [L, R, U, D] :: [Move]

```

```

instance Show Move where
    show move =
        case move of
            L -> "L"
            R -> "R"
            U -> "U"

```



```
D -> "D"
```

```
-- type NodeSet = Map.Map NodeState Bool
type NodeSet = [NodeState]
```

```
data SearchState = SearchState {
  startBoard :: Board, -- holds the start board
  goalBoard :: Board, -- holds the goal board
  heuristic :: (Board -> Board -> Maybe Int), -- holds the heuristic function
  solutionDepth :: Int, -- holds the depth of the solution
  nodesGenerated :: NodeSet, -- holds the nodes that have been generated previously
  nodeQueue :: [NodeState], -- holds unexpanded nodes
  numNodesGenerated :: Int, -- holds number of generated nodes
  solutionMoves :: [Move], -- holds the moves to the solution
  solutionVals :: [Int] -- holds the f(n) values to the solution
}
```

```
data NodeState = NodeState {
  currentBoard :: Board, -- holds the current board
  fval :: Int, -- holds the f(n) value of the node
  depth :: Int, -- holds the depth of the node
  moves :: [Move], -- holds the moves from the ancestor nodes
  fvals :: [Int] -- holds the f(n) value of the ancestor nodes
}
```

```
instance Show NodeState where
  show (NodeState current fval depth moves fvals)
    = "\nCurrent Board: " ++ show current ++
      "\nF(n) value: " ++ show fval ++
      "\nDepth: " ++ show depth ++
      "\nMoves (newest first): " ++ show moves ++
      "\nF(n) values (newest first): " ++ show fvals ++
      "\n-----"
```

```
instance Eq NodeState where
  (==) (NodeState currentLeft _ _ _) (NodeState currentRight _ _ _) =
    currentLeft == currentRight
  (/=) x y =
    not ((==) x y)
```

```
compareNode :: NodeState -> NodeState -> Ordering
compareNode (NodeState _ leftFVal _ _ _) (NodeState _ rightFVal _ _ _)
  | leftFVal > rightFVal = GT
  | leftFVal < rightFVal = LT
  | otherwise = EQ
```

```
instance Ord NodeState where
  compare x y = compareNode x y
```

```

instance Show SearchState where
  show (SearchState startBoard goalBoard _ solutionDepth nodesGenerated nodeQueue
numNodesGenerated solutionMoves solutionVals)
    = "\nStart Board: " ++ show startBoard ++
      "\nGoal Board: " ++ show goalBoard ++
      "\nDepth: " ++ show solutionDepth ++
      -- "\nNodes Generated: " ++ show nodesGenerated ++
      -- "\nNode queue: " ++ show nodeQueue ++
      "\n# Nodes Generated: " ++ show (fromIntegral (length nodesGenerated)) ++
      "\nSolution Moves (newest first): " ++ show solutionMoves ++
      "\nSolution f(n)s (newest first): " ++ show solutionVals ++
      "\n-----"

-- swaps two elements in a list
swapTwo :: Int -> Int -> [a] -> [a]
swapTwo first second xs = zipWith (\x y ->
  if x == first then xs !! second
  else if x == second then xs !! first
  else y) [0..] xs

-- generates new coord based on move
moveCoord :: (Int, Int) -> Move -> (Int, Int)
moveCoord (x, y) move =
  case move of
    L -> (x-1, y)
    R -> (x+1, y)
    U -> (x, y-1)
    D -> (x, y+1)

-- generates all possible moves for coord
validMovesCoord :: (Int, Int) -> [Move]
validMovesCoord coord = [ move | move <- moveSet, validCoord $ moveCoord coord move ]

-- generates all possible moves for current board
allMoves :: Board -> Maybe [Move]
allMoves current =
  -- find the blank position
  case elemIndex 0 current of
    Just blankIndex -> (Just moves)
      where
        -- find the valid moves for the blank position
        moves = validMovesCoord $ fromIndex blankIndex
    Nothing -> Nothing

-- generates new board given current board and a move
moveBoard :: Board -> Move -> Maybe Board
moveBoard current move =
  -- find the blank position
  case elemIndex 0 current of

```

```
Just blankIndex -> (Just newBoard)
```

```
  where
```

```
    -- find the index of the blank tile once you move it accordingly
```

```
    moveIndex = toIndex $ moveCoord (fromIndex blankIndex) move
```

```
    -- generate the new board by swapping the blank with the tile its moving to
```

```
    newBoard = swapTwo blankIndex moveIndex current
```

```
  Nothing -> Nothing
```

```
-- bad code but running out of time
```

```
unsafeUnmaybe :: Maybe a -> a
```

```
unsafeUnmaybe maybe =
```

```
  case maybe of
```

```
    Just a -> a
```

```
    Nothing -> error "unsafeUnmaybe ran into some trouble"
```

```
nextNodeState :: Board -- Goal board
```

```
  -> (Board -> Board -> Int) -- f(n)
```

```
  -> NodeState -- Expanding node
```

```
  -> Move -- Current move
```

```
  -> NodeState -- New node
```

```
nextNodeState goal fn (NodeState current fval depth moves fvals) move =
```

```
  -- return newly generate node
```

```
  NodeState current' fval' depth' moves' fvals'
```

```
  where
```

```
    -- get the new current board
```

```
    current' = unsafeUnmaybe $ moveBoard current move
```

```
    -- get the new f(n) value
```

```
    fval' = fn current' goal
```

```
    -- increase depth counter by 1
```

```
    depth' = depth + 1
```

```
    -- add move to move list
```

```
    moves' = moves ++ move:[]
```

```
    -- add f(n) value to f(n) value list
```

```
    fvals' = fvals ++ fval':[]
```

```
possibleNodes :: Board -- Goal board
```

```
  -> (Board -> Board -> Maybe Int) -- Heuristic
```

```
  -> NodeState -- Expanding node
```

```
  -> [NodeState] -- List of new nodes
```

```
possibleNodes goal heuristic (NodeState current fval depth moves fvals) =
```

```
  -- generate all node states given new f(n) and valid moves
```

```
  map (nextNodeState goal fn (NodeState current fval depth moves fvals)) validMoves
```

```
  where
```

```
    -- generating new level, increasing depth (gn)
```

```
    gn = depth + 1
```

```
    -- generate new f(n)
```

```
    fn = constructFn gn heuristic
```

```
    -- get all valid moves given current board
```

```

validMoves = unsafeUnmaybe $ allMoves current

constructFn :: Int -> (Board -> Board -> Maybe Int) -> (Board -> Board -> Int)
constructFn gn hn =
  -- return a function that adds a given g(n) value with a heuristic function
  (\x y -> (+) gn (unsafeUnmaybe $ hn x y))

-- finds the node with the lowest f(n) value in a list of nodes
nextBestNode :: [NodeState] -> NodeState
nextBestNode = minimumBy compareNode

-- given a list of already generated nodes and a list of possible nodes, return
-- only the nodes that haven't already been generated
generateNewNodes :: NodeSet -> [NodeState] -> [NodeState]
generateNewNodes _ [] = []
generateNewNodes nodeset nodes =
  [node | node <- nodes, not $ elem node nodeset]

-- check if a node is a goal node
checkGoalNode :: Board -> NodeState -> Bool
checkGoalNode goal (NodeState current _ _ _) =
  goal == current

-- add a list of nodes to a list of already generated nodes
recordNewNodes :: NodeSet -> [NodeState] -> NodeSet
recordNewNodes nodeset nodes =
  nodeset ++ nodes

-- test data
testStartBoard = [2, 8, 3, 1, 6, 4, 7, 0, 5]
testGoalBoard = [1, 2, 3, 0, 8, 4, 7, 6, 5]
testFn = constructFn 0 manhattanHeuristic
testFval = testFn testStartBoard testGoalBoard
testNode = NodeState testStartBoard testFval 0 [] $ testFval:[]
testStartState = SearchState testStartBoard testGoalBoard manhattanHeuristic (-1) [] [] 0 [] []

-- run a recursive astar algorithm
runAStar :: SearchState -> SearchState
runAStar (SearchState startBoard goalBoard heuristic solutionDepth nodesGenerated nodeQueue
numNodesGenerated solutionMoves solutionVals) =
  -- check if the algorithm has started
  case null nodesGenerated of
    -- if it hasn't, generate the first node and call algorithm again
    True ->
      runAStar $ SearchState startBoard goalBoard heuristic solutionDepth nodesGenerated'
nodeQueue' numNodesGenerated' solutionMoves solutionVals
    where
      fn = constructFn 0 heuristic
      fval = fn startBoard goalBoard

```

```

    fvals = fval:[]
    node = NodeState startBoard fval 0 [] fvals
    nodesGenerated' = nodesGenerated ++ node:[]
    nodeQueue' = node:[]
    numNodesGenerated' = numNodesGenerated' + 1
-- if it has, find the next best move
False ->
    -- check if the next best move is the goal state
    case checkGoalNode goalBoard $ NodeState current fval depth moves fvals of
        -- if it is, return the goal state
        True ->
            SearchState startBoard goalBoard heuristic depth nodesGenerated nodeQueue'
numNodesGenerated moves fvals
        -- if it isn't, generate new nodes and record the data, before recursing again
        False ->
            runAStar newState
            where
                newNodes = generateNewNodes nodesGenerated $ possibleNodes goalBoard heuristic $
NodeState current fval depth moves fvals
                nodesGenerated' = recordNewNodes nodesGenerated newNodes
                nodeQueue'' = nodeQueue' ++ newNodes
                numNodesGenerated' = numNodesGenerated + length newNodes
                newState = SearchState startBoard goalBoard heuristic solutionDepth nodesGenerated'
nodeQueue'' numNodesGenerated' solutionMoves solutionVals
            where
                -- get next best node
                (NodeState current fval depth moves fvals) = nextBestNode nodeQueue
                -- remove best node from unexpanded node queue
                nodeQueue' = filter ((/=) $ NodeState current fval depth moves fvals) nodeQueue

```

## Lib.hs

```

module Lib where

```

```

import Data.List (lines)
import Data.List.Split (splitOn, chunksOf)

```

```

import Board
import Heuristics
import AStar

```

```

-- readBoards takes the data received from reading a test file and cleans it
-- into manageable data (a tuple of two Int arrays)
readBoards :: String -> (Board, Board)
readBoards content =
    -- construct a tuple from the generated array
    (flattenedBoards !! 0, flattenedBoards !! 1) :: (Board, Board)
    where
        -- split data into cleaned (no \r\n) lines
        fLines = map (filter (\x -> ((/=) '\r' x) && ((/=) '\n' x))) $ lines content

```

```

-- remove new line and split integer characters
splitFLines = map (splitOn " ") $ filter (/= "") fLines
-- convert strings to ints
cleanedContent = map (map (\x -> read x :: Int)) splitFLines
-- separate the big array of data into two boards
twoBoards = chunksOf 3 cleanedContent
-- flatten from two 2d array to two 1d arrays
flattenedBoards = map concat twoBoards

-- to2d takes a puzzle board and chunks it into a 2d list with elements of
-- length boardWidth for easier printing
to2d :: Board -> [[Int]]
to2d = chunksOf boardWidth

-- stringBoard "stringifies" a 2d-ified puzzle board
stringBoard :: [[Int]] -> String
stringBoard [] = ""
stringBoard (x:xs) = (show x) ++ "\n" ++ stringBoard xs

stringList :: Show a => [a] -> String
stringList [] = ""
stringList (x:xs) =
    (show x) ++ " " ++ stringList xs

string2dBoard :: [[Int]] -> String
string2dBoard [] = ""
string2dBoard (x:xs) =
    stringList x ++ "\n" ++ string2dBoard xs

-- ppBoard prints the a puzzle board in a pretty fashion
ppBoard :: Board -> String
ppBoard = string2dBoard . to2d

printSolution :: SearchState -> String
printSolution (SearchState startBoard goalBoard _ solutionDepth nodesGenerated _ _ solutionMoves
solutionVals)
    = ppBoard startBoard ++ "\n" ++
      ppBoard goalBoard ++ "\n" ++
      show solutionDepth ++ "\n" ++
      show (fromIntegral (length nodesGenerated)) ++ "\n" ++
      stringList solutionMoves ++ "\n" ++
      stringList solutionVals ++ "\n"

getSolution :: String -> Board -> Board -> String
getSolution hnChoice startBoard goalBoard =
    case hnChoice of
        "0" ->

```

```

    printSolution solution
  where
    solution = runAStar $ SearchState startBoard goalBoard manhattanHeuristic (-1) [] [] 0 [] []
"1" ->
  printSolution solution
  where
    solution = runAStar $ SearchState startBoard goalBoard manhattanLinConflictHeuristic (-1)
[] [] 0 [] []

```

## **Main.hs**

```

module Main where

```

```

import System.Environment (getArgs)

```

```

import Lib

```

```

main :: IO ()

```

```

main = do

```

```

  -- Get filepath and heuristic choice from command line args

```

```

  args <- getArgs

```

```

  case args of

```

```

    [] -> putStrLn "Missing filepath and heuristic choice"

```

```

    [inputFilePath] -> putStrLn "Missing heuristic choice - input 0 for manhattan distance heuristic or
1 for manhattan & 2x linear conflict heuristic"

```

```

    [inputFilePath, hnChoice] -> do

```

```

      -- Read the file into a string

```

```

      content <- readFile (inputFilePath)

```

```

      -- Process that string into two workable arrays

```

```

      let (startBoard, goalBoard) = readBoards content

```

```

        solution = getSolution hnChoice startBoard goalBoard

```

```

      -- Write the solution to an outfile

```

```

      writeFile "./output/output.txt" solution

```