

# Announcements

- Office hours
  - Tue March 5, 4-5pm in room 3234
  - Thu March 7:
    - online, 5.30-7pm:
    - write me an email for appointment: [gquer@ucsd.edu](mailto:gquer@ucsd.edu)
- Thu March 7: NO LECTURE
- **Readings: 09\_ABtesting/readings.md due on Friday 3/8 at 6PM**

# A/B test: binary outcomes

- Email 1:  $n_1 = 605$ , clicks:  $c_1 = 351$
- Email 2:  $n_2 = 585$ , clicks:  $c_2 = 123$
- Click per email:  $p_1 = 0.58$  ,  $p_2 = 0.21$
- Is there **enough evidence** that Email 1 is better than email 2?
- Numbers are large ( $>100$ ) so we can approximate with a Gaussian
- The null hypothesis is  $p_1 = p_2$  , we can calculate
- $p = (c_1 + c_2) / (n_1 + n_2)$  : the mean click rate in the null hypothesis
- $\sigma^2 = p(1-p)$  : the variance of the outcome
- 
- If  $t > 1.96$ , they are actually different  
(with 95% confidence)



$$t = \frac{\hat{p}_1 - \hat{p}_2}{\sqrt{\sigma^2 \left( \frac{1}{n_1} + \frac{1}{n_2} \right)}}$$

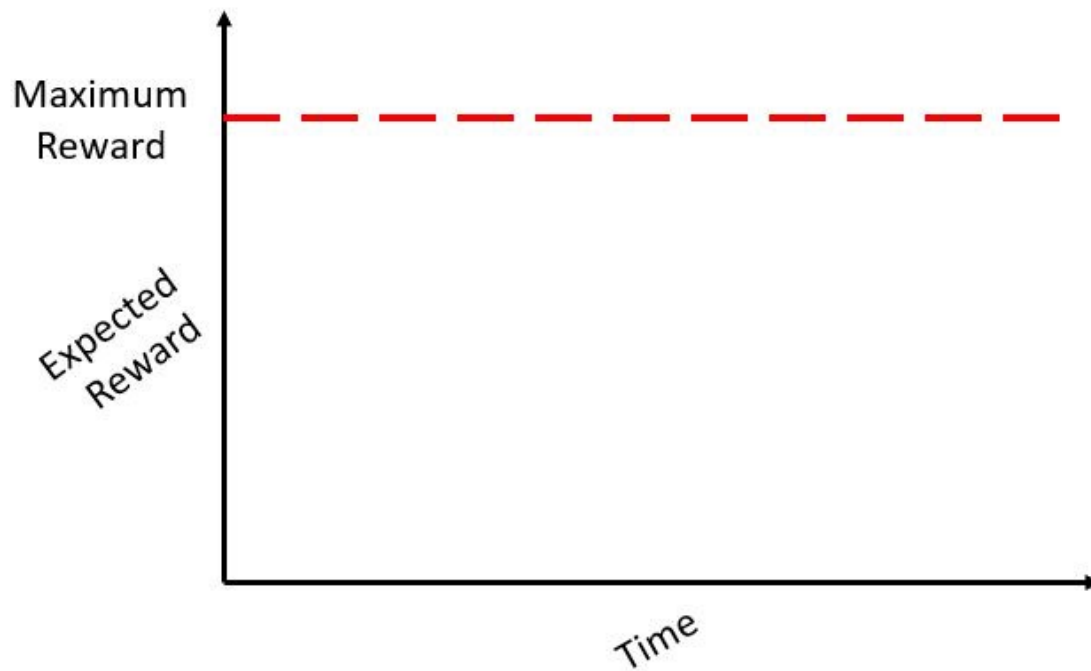
# Common Pitfalls of A/B Tests

1. Optimizing for the wrong metric
2. Failing to correctly randomize
3. Stopping early
4. Unethical testing
5. Non-stationary problem

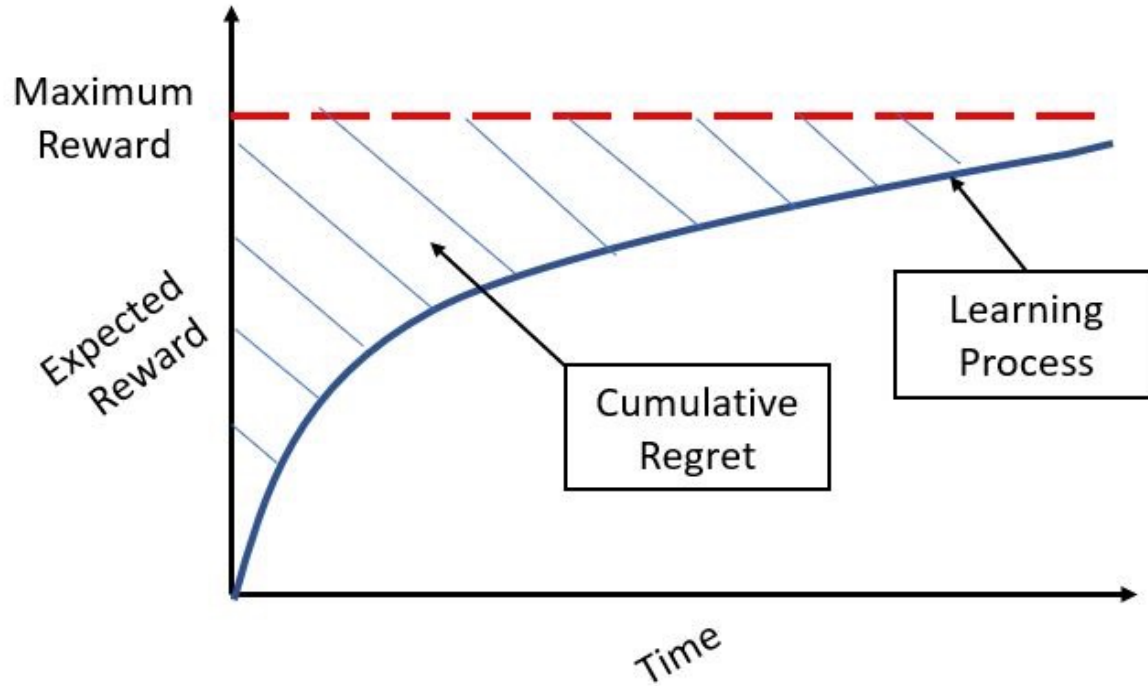
# Multi-Armed Bandits



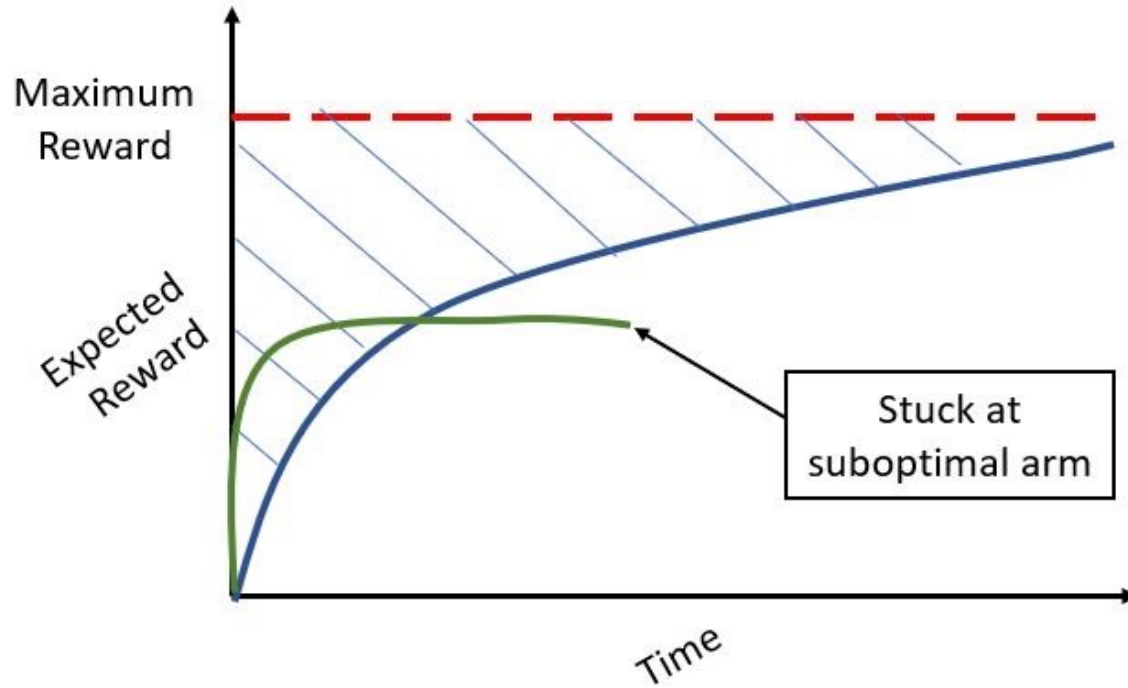
# Perfect Knowledge



# Exploring causes regret



# Not exploring enough causes more regret



# Explore then greedy

Hypothesis testing approach:

1. Run each experiment  $N$  times.
2. Choose a winner, and use that forever.

How to determine  $N$ ?

What might go wrong with this approach?

- $N$  too small and you might choose the wrong winner
- $N$  too large and you spend too long experimenting



# Upper Confidence Bound

$j=1,\dots,K$  possible actions

Each action has a stationary random reward between 0 and 1

Choose the action that maximizes:

$$m_j + \sqrt{\frac{2 \ln N}{N_j}}$$

- $m_j$  = the current average reward of arm  $j$
- $N$  = the number of pulls, and
- $N_j$  = the number of pulls on lever  $j$

# Other Approaches

- Epsilon Greedy
- Softmax Exploration
- Decayed Epsilon Greedy
- Thompson Sampling