



TP de Especificación

Sudoku

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Algoritmos y Estructuras de Datos I

Grupo 17

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1. Problemas

```
proc sudoku_esTableroValido (in t: seq⟨seq⟨ℤ⟩⟩, out result: Bool) {
  Pre {True}
  Post {result = esTableroValido(t)}
}

proc sudoku_esCeldaVacía (in t: seq⟨seq⟨ℤ⟩⟩, in f: ℤ, in c: ℤ, out result: Bool) {
  Pre {esTableroValido(t) ∧L 0 ≤ f, c < |t|}
  Post {result = (t[f][c] = 0)}
}

proc sudoku_nroDeCeldasVacías (in t: seq⟨seq⟨ℤ⟩⟩, out result: ℤ) {
  Pre {esTableroValido(t)}
  Post {∑i=0|t|-1 ( ∑j=0|t|-1 if t[i][j] = 0 then 1 else 0 fi)}
}

proc sudoku_primeraCeldaVacíaFila (in t: seq⟨seq⟨ℤ⟩⟩, out result: ℤ) {
  Pre {esTableroValido(t)}
  Post {if (∃i : ℤ)(0 ≤ i < |t| ∧L filaTieneCeldaVacía(t[i]) ∧L (∀j : ℤ)
    (0 ≤ j < i →L ¬filaTieneCeldaVacía(t[j])))
    then result = i
    else result = -1 fi}
}

proc sudoku_primeraCeldaVacíaColumna (in t: seq⟨seq⟨ℤ⟩⟩, out result: ℤ) {
  Pre {esTableroValido(t)}
  Post {if (∃i : ℤ)(0 ≤ i < |t| ∧L filaTieneCeldaVacía(t[i]) ∧L (∀j : ℤ)(0 ≤ j < i →L ¬filaTieneCeldaVacía(t[j])))
    then result = indicePrimeraCeldaVacíaEnFila(t[i])
    else result = -1 fi}
}

proc sudoku_valorEnCelda (in t: seq⟨seq⟨ℤ⟩⟩, in f: ℤ, in c: ℤ, out result: ℤ) {
  Pre {esTableroValido(t) ∧L 0 ≤ f, c ≤ 8 ∧L t[i][j] ≠ 0}
  Post {result = t[f][c]}
}

proc sudoku_llenarCelda (inout t: seq⟨seq⟨ℤ⟩⟩, in f: ℤ, in c: ℤ, in value: ℤ) {
  Pre {esTableroValido(t) ∧L 0 ≤ f, c ≤ 8 ∧L t[i][j] = 0 ∧L 1 ≤ value ≤ 9 ∧L t = t0}
  Post {t[f][c] = value ∧L (∀i : ℤ)(∀j : ℤ)(0 ≤ i, j < |t| ∧L (i ≠ f ∨ j ≠ c)) →L t[i][j] = t0[i][j]}
}

proc sudoku_vaciarCelda (inout t: seq⟨seq⟨ℤ⟩⟩, in f: ℤ, in c: ℤ) {
  Pre {esTableroValido(t) ∧L 0 ≤ f, c ≤ 8 ∧L t[i][j] ≠ 0 ∧L t = t0}
  Post {t[f][c] = 0 ∧L (∀i : ℤ)(∀j : ℤ)((0 ≤ i, j < |t| ∧L (i ≠ f ∨ j ≠ c)) →L t[i][j] = t0[i][j])}
}

proc sudoku_esTableroParcialmenteResuelto (in t: seq⟨seq⟨ℤ⟩⟩, out result: Bool) {
  Pre {True}
  Post {result = esTableroParcialmenteResuelto(t)}
}
```

```

proc sudoku_esTableroTotalmenteResuelto (in t: seq⟨seq⟨ℤ⟩⟩, out result: Bool) {
  Pre {true}
  Post {esParcialmenteResuelto(t) ∧L ∀i : ℤ)(0 ≤ i < |t| →L ¬filaTieneCeldaVacía(t[i]))}
}

proc sudoku_esTablero (in t0, t1 : seq⟨seq⟨ℤ⟩⟩, out result : Bool){
  Pre {true}
  Post {esSubtablero(t0, t1) = result}
}

proc sudoku_esSubTablero (in t0, t1 : seq⟨seq⟨ℤ⟩⟩, out result : Bool){
  Pre {true}
  Post {esSubtablero(t0, t1) = result}
}

```

2. Predicados y Auxiliares generales

```

pred esMatriz (t: seq⟨seq⟨ℤ⟩⟩) {
  (∀i : ℤ)(∀j : ℤ)(0 ≤ i, j < |t| →L | t[i] | = | t[j] |)}

fun cantidadFilas (t: seq⟨seq⟨ℤ⟩⟩) : ℤ = |t|;

fun cantidadColumnas (t: seq⟨seq⟨ℤ⟩⟩) : ℤ = if cantidadFilas(t) > 0 then |t[0]| else 0 fi;

pred esMatrizCuadrada (t: seq⟨seq⟨ℤ⟩⟩) {
  esMatriz(t) ∧ ( cantidadFilas(t) = cantidadColumnas(t) )}

pred esTableroValido (t: seq⟨seq⟨ℤ⟩⟩) {esMatrizCuadrada(t) ∧L |t|=9 ∧L
  (∀i : ℤ)(∀j : ℤ)(0 ≤ i, j < |t| →L 0 ≤ t[i][j] ≤ 9)}

pred filaTieneCeldaVacía (f: seq⟨ℤ⟩) {
  (∃i : ℤ)(0 ≤ i < |f| ∧L f[i] = 0)}

fun indicePrimeraCeldaVacíaEnFila (s: seq⟨ℤ⟩) : ℤ = if ((∃ i : ℤ)(0 ≤ i < |s| ∧L s[i] = 0 ∧L
  (∀j : ℤ)(0 ≤ j < i →L s[j] ≠ 0))) then i else -1 fi;

pred noHayRepetidosEnRegion (s: seq⟨ℤ⟩) {(∀i : ℤ)(∀j : ℤ)(∀k : ℤ)(∀l : ℤ)
  (0 ≤ i, j, k, l < 9 ∧L (i div 3 = k div 3) ∧L (j div 3 = l div 3) ∧L (i ≠ k ∨ j ≠ l) →L t[i][j] ≠ t[k][l])}

pred noHayRepetidosEnFila (s: ℤ) {(∀i : ℤ)(∀j : ℤ)(0 ≤ i, j < |s| ∧L j ≠ i →L s[i] ≠ s[j])}

pred noHayRepetidosEnColumna (t: ℤ) {(∀j : ℤ)(0 ≤ j < |t| →L (∀l : ℤ)(∀k : ℤ)
  (0 ≤ l, k < |t| ∧L l ≠ k →L t[i][j] ≠ t[k][j]))}

pred esTableroParcialmenteResuelto (t: ℤ) {esTableroValido(t) ∧L (∀i : ℤ)(0 ≤ i < |t| →L
  (noHayRepetidosEnFila(t[i]) ∧L noHayRepetidosEnColumna(t) ∧L noHayRepetidosEnRegion(t)))}

pred esSubTablero (t0, t1 : seq⟨seq⟨ℤ⟩⟩){
  ( esTableroValido(t0) ∧L esTableroValido(t1)) ∧L ((∀i : ℤ)(∀j : ℤ)
  (0 ≤ i < |t| ∧L t0[i][j] ≠ 0) →L (t0[i][j] = t1[i][j]))}

```

3. Decisiones tomadas