

From complex values to objects

A database perspective

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A very first example

- Class book
 - title
 - set of authors
 - publisher
 - set of keywords
- Easy to model in any programming language
- Tricky in relational database!

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Basic proposal

- Either we ignore the normalization...

Title	Author	Publisher	Keyword
FoD	S. Abiteboul	Addison-Wesley	Database
FoD	R. Hull	Addison-Wesley	Database
FoD	V. Vianu	Addison-Wesley	Database
FoD	S. Abiteboul	Addison-Wesley	Logic
FoD	R. Hull	Addison-Wesley	Logic
FoD	V. Vianu	Addison-Wesley	Logic
TCB	J.D. Ullman	Pearson	Database
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- Key: (Title, Author, Keyword)
- Not in 2NF since Title → Publisher

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Intermediate state

- ... Or we go to 3NF, BCNF

		Title	Author	Keyword			
<table><tr><th>Title</th><th>Publisher</th></tr><tr><td>FoD</td><td>Addison-Wesley</td></tr></table>	Title	Publisher	FoD	Addison-Wesley	FoD	S. Abiteboul	Database
	Title	Publisher					
	FoD	Addison-Wesley					
	FoD	R. Hull	Database				
	FoD	V. Vianu	Database				
	FoD	S. Abiteboul	Logic				
FoD	R. Hull	Logic					
FoD	V. Vianu	Logic					

- But we still ignore the multivalued dependencies...
- Title \twoheadrightarrow Author and Title \twoheadrightarrow Keyword

About MVD's and 4NF

- MVD: full constraint on relation

Definition (Multi-Valued Dependency)

Let R be a relation of schema $\{X, Y, Z\}$; $X \twoheadrightarrow Y$ holds whenever (x, y, z) and (x, t, u) exist in R implies that (x, y, u) and (x, t, z) should also exist in R

Example

- Analysis: Department {Building} {Employee {Telephone}}
- MVD's = {Department \twoheadrightarrow Building, Employee \twoheadrightarrow Telephone}

About MVD's and 4NF (cont'd)

MVD Properties in $R(X, Y, Z)$

- $X \twoheadrightarrow Y \Rightarrow X \twoheadrightarrow Z$
- $X \rightarrow Y \Rightarrow X \twoheadrightarrow Y$
- $X \twoheadrightarrow R - X$ always holds (trivial MVD)

Definition (4NF)

For every non trivial MVD $X \twoheadrightarrow Y$ in R , then X is a superkey

Lossesless-join decomposition

A decomposition of R into (X, Y) and (X, Z) is a **lossesless-join decomposition** iff $X \twoheadrightarrow Y$ holds in R

The ultimate schema

- ... Or we go to 4NF

Title	Publisher	Title	Author
FoD	Addison-Wesley	FoD	S. Abiteboul
		FoD	R. Hull
		FoD	V. Vianu
Title	Keyword		
FoD	Database		
FoD	Logic		

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Pros & Cons

- 4NF design
 - requires many joins in queries (performance pitfall)
 - and loses the big picture of entities
- 1NF relational view
 - eliminates the need for users to perform joins
 - but loses the one-to-one correspondence between tuples and objects
 - has a large amount of redundancy
 - and could yield to insertion, deletion, update anomalies

Contents

Complex Values

Nested Tables

eNF² Data Model

Identifiers & References

Features of OO-DBMS

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Preamble

Alice: Complex values?

Riccardo: We could have used a different title: nested relations, complex objects, structured objects. . .

Vittorio: . . . N1NF, NFNF, NF2, NF², V-relation. . . I have seen all these names and others as well.

Sergio: In a nutshell, relations are nested within relations; something like Matriochka relations.

Alice: Oh, yes. I love Matriochkas.

FoD: chap. 20, p. 508

Beyond the Relational Model

- Theoretical extensions of the RM
 - Nested relations: NF²
 - Type constructors and free combination: eNF²
- New Requirements
 - Operations as extension to relational algebra
 - Normal form to provide consistency
- Today, part of SQL3 and commercial systems

The NF² Database Model

NF² = NFNF = Non First Normal Form

Principle

NF² relations permit **complex values** whenever we encounter atomic, i.e. indivisible, values

- Violates first normal form
- Allows more intuitive—let say *conceptual*—modeling for applications with complex data
- Preserves mathematical foundations of relational model

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From Flatland to Lineland¹...

- Relation schema in 1NF: τ

$$\tau := \langle A_1 : \text{dom}, \dots, A_k : \text{dom} \rangle$$

- Sort constructors: **tuple** and—finite—**set**
- Construction pattern: $\text{set}(\text{tuple}(\text{dom}^*))$
- $\neg 1\text{NF}$: much more combinations

$$\tau := \text{dom} \mid \langle A_1 : \tau, \dots, A_k : \tau \rangle \mid \{\tau\}$$

- We denote by $\llbracket \tau \rrbracket$ the set of complex values of sort τ

¹Flatland, a Romance of Many Dimensions. Edwin A. Abbott (1884).

Examples

Sort	Complex value
dom	a
$\{\text{dom}\}$	$\{a, b, c\}$
$\{\{\text{dom}\}\}$	$\{\{a, b\}, \{a\}, \{\}\}$
$\langle A:\text{dom}, B:\text{dom} \rangle$	$\langle A:a, B:b \rangle$
$\langle A:\langle B:\text{dom} \rangle \rangle$	$\langle A:\langle B:b \rangle \rangle$
$\{\langle A:\text{dom}, B:\text{dom} \rangle\}$	$\{\langle A:a, B:b \rangle, \langle A:a, B:b \rangle\}$
$\langle A:\{\langle B:\text{dom} \rangle\} \rangle$	$\langle A:\{\langle B:b \rangle, \langle B:c \rangle\} \rangle$

Complex value as **table**

A	B	C						
a b		<div style="border: 1px solid black; padding: 10px; text-align: center;"><table style="margin: auto;"><tr><th style="text-align: center;">A</th><th style="text-align: center;">E</th></tr><tr><td style="text-align: center;">c</td><td style="text-align: center;"><input type="text"/></td></tr><tr><td style="text-align: center;">d</td><td style="text-align: center;"><input type="text"/></td></tr></table></div>	A	E	c	<input type="text"/>	d	<input type="text"/>
A	E							
c	<input type="text"/>							
d	<input type="text"/>							
e f		<div style="border: 1px solid black; padding: 10px; text-align: center;"><table style="margin: auto;"><tr><th style="text-align: center;">A</th><th style="text-align: center;">E</th></tr><tr><td colspan="2" style="height: 40px;"></td></tr></table></div>	A	E				
A	E							

Side note: also of sort $\langle A, B, C: \{ \langle A, E: \{ \emptyset \} \} \rangle$

Database instance

Definition (NF² Schema)

A schema $R:\tau$ is a relation name R with $\text{sort}(R) = \tau$

- Extend to database schema \mathcal{R} as a set of relation schemes

Definition (NF² Relation)

A relation $I(R)$ of schema $R:\tau$ is a finite set of values of sort τ

Definition (NF² Database instance)

A database instance I over schema \mathcal{R} is a mapping

$$\begin{aligned} I : \mathcal{R} &\longrightarrow \mathcal{P}[\![\text{sort}(\mathcal{R})]\!] \\ R:\tau &\longmapsto I(R) \end{aligned}$$

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Running example

Abuse of notation

- R stands either for schema or instance of a relation, wherever it is unambiguous
- X is a shorthand for $X:\text{dom}$ wherever it is applicable

Database

Instance J of schema $\mathcal{R} = \{R_1, R_2, R_3\}$ with

$$\text{sort}(R_1) = \text{sort}(R_3) = \langle A, B: \{ \langle A_1, A_2 \rangle \} \rangle$$

$$\text{sort}(R_2) = \langle A, A_1, A_2 \rangle$$

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Running example (cont'd)

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<i>A</i> ₁	<i>A</i> ₂						
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J(R₁)

<i>A</i>	<i>A</i> ₁	<i>A</i> ₂
<i>d</i> ₁	<i>d</i> ₁	<i>d</i> ₂
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<i>d</i> ₂	<i>d</i> ₁	<i>d</i> ₃
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J(R₂)

<i>A</i>	<i>B</i>								
<i>d</i> ₁	<table><tr><th><i>A</i>₁</th><th><i>A</i>₂</th></tr><tr><td><i>d</i>₁</td><td><i>d</i>₂</td></tr><tr><td><i>d</i>₃</td><td><i>d</i>₄</td></tr><tr><td><i>d</i>₅</td><td><i>d</i>₆</td></tr></table>	<i>A</i> ₁	<i>A</i> ₂	<i>d</i> ₁	<i>d</i> ₂	<i>d</i> ₃	<i>d</i> ₄	<i>d</i> ₅	<i>d</i> ₆
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Exercises 1/2

1. Definitions

MVD, 4NF, NF², Complex value, NF² Schema, NF² Relation, NF² Db instance

2. True or False?

- i) FD's are MVD's.
- ii) 4NF generalizes BCNF.
- iii) Relation $R \subseteq \{\vartheta \mid \vartheta \vdash \tau\}$ is of sort $\{\tau\}$.
- iv) Set vertex in a sort tree may have many children.
- v) Set vertex in a CV tree may have many children.
- vi) Type inference from CV yields one single sort.

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Exercises 2/2

3. Sorts and complex values

Draw the tree of each sort and complex value from the *Examples* slide.

4. Problem

Consider a (flat) relation R of sort $\langle \text{email}, \text{location}, \text{post}, \text{friend_email}, \text{friend_location} \rangle$ and the MVD $\text{email location} \twoheadrightarrow \text{post}$. Prove that the same information can be stored in a complex value relation of sort

$\langle \text{email}, \text{location}, \text{posts} : \{ \text{dom} \}, \text{friends} : \{ \langle \text{friend_email}, \text{friend_location} \rangle \} \rangle$

Discuss pros of this alternative representation (w.r.t. size and update anomalies).

Overview

Chapter Nested Tables

1. From NF² to Nested Tables
2. SQL3 Transcription of NF²
3. Design and Normalization of Nested Tables

A popular restriction

Definition (Nested relation)

A nested relation is a NF² relation where **set** and **tuple** constructors are required to **alternate**

Examples

$$\begin{array}{ll}
 \tau_1 = \langle A, B, C : \{ \langle D, E : \{ \langle F, G \rangle \} \} \rangle & \text{Ok} \\
 \tau_2 = \langle A, B, C : \{ \langle E : \{ \langle F, G \rangle \} \} \rangle & \text{Ok} \\
 \tau_3 = \langle A, B, C : \langle D, E : \{ \langle F, G \rangle \} \rangle & \text{No!} \\
 \tau_4 = \langle A, B, C : \{ \{ \langle F, G \rangle \} \} \rangle & \text{No!}
 \end{array}$$

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One more *real-life* example to take away

Relation Dpts of sort

$\langle \text{Dpt}, \text{Emps} : \{ \langle \text{SSN}, \text{Name}, \text{Tels} : \{ \langle \text{Tel} \rangle \}, \text{Salary} \rangle \} \rangle$

Department	Employees			
	SSN	Name	Telephones	Salary
			Tel	
Computer Science	4711	Todd	038203-12230 0381-498-3401	6,000
	5588	Whitman	0391-334677 0391-5592-3452	6,000
	7754	Miller		550
	8832	Kowalski		2,800
Mathematics	6834	Wheat	0345-56923	750


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About nested relations

Nested relations vs. N1NF-relations

Cosmetic restriction only

Size of nested relations

$\mathcal{O}(2^{2^{\dots 2^n}})$ with n being the size of the active domain of R and *the tower of 2* equals depth of R (nested levels)

Reminder: Size of flat relations is polynomial

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Languages for nested relations

Logic

Mainly extend RC to **variables denoting sets**

$$\{t.\text{Dpt} \mid \text{Dpts}(t) \wedge \forall X, u : (t.\text{Emps} = X \wedge u \in X \rightarrow u.\text{Salary} \leq 5,000)\}$$

With queries as terms:

$$\{t.\text{Dpt} \mid \text{Dpts}(t) \wedge t.\text{Emps} \subseteq \{u \mid u.\text{Salary} \leq 5,000\}\}$$

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Operations on nested relations

The usual way

$$\sigma_{A=d_1}(R_1) \quad \text{and} \quad \pi_A(R_1)$$

$$R_1 \bowtie R_2$$

$$R_1 - R_3 \quad \text{and} \quad R_1 \cup R_3$$

Straightforward extensions

$$\sigma_{B=C}(R_1 \bowtie \rho_{B \rightarrow C}(R_3))$$

$$\sigma_{B \subset C}(R_1 \bowtie \rho_{B \rightarrow C}(R_3))$$

$$\pi_{B.A_1}(R_1)$$

$$\sigma_{A \in B.A_1}(R_1)$$

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Nested relational algebra

- $\cup - \pi \bowtie$ nearly as in relational algebra
- σ : condition extended to support
 - **Relations as operands** (instead of constants in dom)
 - **Set operations** like $\theta \in \{\in, \subseteq, \subset, \supset, \supseteq\}$
- **Recursively structured** operation parameters, e.g.
 - π : nested projection attribute lists
 - σ : selection conditions on nested relations

Nested relational algebra (cont'd)

- Additional operations: Nest (ν) and Unnest (μ)
 - $\mu_{\$k}(I(R))$: remove nesting from k^{th} column of $I(R)$
 - $\nu_{\$1,\dots,\$k}(I(R))$: nest columns $1, \dots, k$ of $I(R)$
 - There exists an equivalent named flavor
- A curiosity: The **Powerset** operator

$$\Omega(I(R)) = \{\vartheta \mid \vartheta \subseteq I(R)\}$$

- Ω extends algebra up to **reachability** (eq. Datalog)

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Unnest operator

- Suppose schema $\mathcal{R} = \{R, S\}$ with sorts:

$$\text{sort}(R) = \langle A_1:\tau_1, \dots, A_k:\tau_k, B:\{\langle A_{k+1}:\tau_{k+1}, \dots, A_n:\tau_n \rangle\} \rangle$$

$$\text{sort}(S) = \langle A_1:\tau_1, \dots, A_k:\tau_k, A_{k+1}:\tau_{k+1}, \dots, A_n:\tau_n \rangle$$

- The unnest operator is defined as follows:

$$\begin{aligned} \mu_B(I(R)) = & \{ \langle A_1:x_1, \dots, A_n:x_n \rangle \mid \\ & \exists y : \langle A_1:x_1, \dots, A_k:x_k, B:y \rangle \in I(R) \wedge \\ & \langle A_{k+1}:x_{k+1}, \dots, A_n:x_n \rangle \in y \} \end{aligned}$$

- Example: $\mu_B(R_1) = R_2$

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Nest operator

$$\begin{aligned} \nu_{B=(A_{k+1}, \dots, A_n)}(I(S)) = & \{ \langle A_1 : x_1, \dots, A_k : x_k, B : y \rangle \mid \\ & y = \{ \langle A_{k+1} : x_{k+1}, \dots, A_n : x_n \rangle \mid \\ & \quad \langle A_1 : x_1, \dots, A_n : x_n \rangle \in I(S) \} \wedge \\ & y \neq \emptyset \} \end{aligned}$$

- Example: $\nu_{B=(A_1, A_2)}(R_2) = R_3$


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About duality of Nest & Unnest

- The following statement holds:

$$\mu_B(\nu_{B=(A_1A_2)}(R_2)) = R_2$$

- However

$$\nu_{B=(A_1A_2)}(\mu_B(R_1)) \neq R_1$$

- Unnest is the **right inverse** of nest: $\mu_A \circ \nu_{A=\alpha} \equiv \text{Id}$
- Unnest is **not information preserving** (one-to-one) and so has no right inverse

About duality of Nest & Unnest (cont'd)

Unnesting not generally reversible

A	D	
	B	C
1	2	7
	3	6
1	4	5
2	1	1

$$\xrightarrow{\mu_D(R)}$$

A	B	C
1	2	7
1	3	6
1	4	5
2	1	1

$$\nu_{D=(B,C)}(S)$$

A	D	
	B	C
1	2	7
	3	6
	4	5
2	1	1

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Nesting in queries

Flat-Flat Theorem

Let Q be a nested relational algebra expression;

- Q takes a non-nested relation as input
- Q produces a non-nested relation as output

Then, Q can be rewritten as a **regular relational algebra expression** (i.e., w/o nesting)

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Nesting in queries (cont'd)

Result is actually stronger for query Q

Nested Query Theorem

Assume a d_1 -nested relation as input and a d_2 -nested relation as output; there is no need for intermediate results having depth greater than $\max(d_1, d_2)$

What for?

- Can be used by query optimizers
- No need to introduce intermediate nesting
- Standard techniques for query evaluation

NF² concepts in SQL3

- SQL:1999 introduced **tuple type constructor ROW**
- Only few changes to type system in SQL:2003
 - **Bag type constructor MULTISSET**
 - XML data types
- Implementations in commercial DBMS most often do NOT comply with standard!

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ROW type constructor

- ROW implements **tuple** type constructor

Example

```

CREATE ROW TYPE AddressType (
    Street  VARCHAR(30),
    City    VARCHAR(30),
    Zip     VARCHAR(10) );

CREATE ROW TYPE CustomerType (
    Name     VARCHAR(40),
    Address  AddressType );

CREATE TABLE Customer OF TYPE CustomerType
    ( PRIMARY KEY Name );

```

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ROW type constructor (cont'd)

- Insertion of records requires call to **row constructor**

```

INSERT INTO Customer
VALUES( 'Doe', ROW( '50 Otages', 'Nantes', '44000' ) );

```

- Component access by usual dot '.' notation with field parenthesis (\neq table prefix)

```

SELECT C.Name, (C.Address).City FROM Customer C;

```

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MULTISET type constructor

- SQL:2003 MULTISET implements set/bag type constructor
- Can be combined with ROW type constructors
- Allows creation of nested tables (NF²)

```

CREATE TABLE Department (
    Name VARCHAR(40),
    Buildings INTEGER MULTISET,
    Employees ROW( Firstname VARCHAR(30),
                    Lastname  VARCHAR(30),
                    Office    INTEGER ) MULTISET );

```

MULTISET type constructor (cont'd)

Operations

- MULTISET constructor
- UNNEST implements μ
- COLLECT: special aggregate function to implement ν
- FUSION: special aggregate function to build union of aggregated multisets
- MULTISET UNION|INTERSECT|EXCEPT
- CARDINALITY for size
- SET eliminates duplicates
- ELEMENT converts singleton to a tuple (row) expression

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MULTISET type constructor (cont'd)

Predicates

- MEMBER: $x \in E$
- SUBMULTISET multiset containment: $S \subseteq E$
- IS [NOT] A SET test whether there are duplicates or not

```

SELECT D.Name FROM Department D
WHERE CARDINALITY(D.Buildings) >= 2 AND
       D.Employees IS A SET;

```

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MULTISET type constructor (cont'd)

Insert and Update statements

```

INSERT INTO Department
VALUES( 'Computer Science',
      MULTISET[29,30],
      MULTISET( ROW( ... ) ) );

```

```

INSERT INTO Department
VALUES( 'Computer Science',
      MULTISET[28],
      MULTISET( SELECT ... FROM ... );

```

```

UPDATE Department
SET Buildings=Buildings MULTISET UNION MULTISET[17]
WHERE Name='Computer Science';

```

MULTISET type constructor (cont'd)

- **Unnesting** of a multiset

```
SELECT D.Name, Emp.LastName
FROM Department D,
      UNNEST( D.Employees ) Emp;
```

- **Nesting** using the COLLECT aggregation function

```
SELECT P.Name, COLLECT( S.hobby ) AS hobbies
FROM Person P NATURAL JOIN SpareTime S
GROUP BY P.Name;
```

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Partitioned Normal Form

Definition (PNF)

Let $R(X, Y)$ be a n -ary relation where X is the set of atomic attributes and Y is the set of relation-valued attributes; R is in partitioned normal form (PNF) iff

1. $X \rightarrow X, Y$ (X is a super-key)
2. Recursively, $\forall r \in Y$ and $\forall I(r) \in \pi_r(R)$, $I(r)$ is in PNF

- If $X = \emptyset$, then $\emptyset \rightarrow Y$ must hold
- If $Y = \emptyset$, then $X \rightarrow X$ holds trivially

Thus a **1NF relation is in PNF**

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Properties of PNF

1. A flat (1NF) relation is always in PNF
2. PNF relations are **closed** under unnesting
3. Nesting and unnesting operations **commute** for PNF relations
4. Size of PNF relations remains polynomial

Strong theoretical results and many practical applications

4NF counter-part of PNF

PNF relation and equivalent unnested relation

A	E		F
	B	C	D
1	2	3	1
	4	2	
2	1	1	2
	4	1	3
3	1	1	2

$$\mu_E \circ \mu_F \longrightarrow$$

A	B	C	D
1	2	3	1
1	4	2	1
2	1	1	2
2	4	1	2
2	1	1	3
2	4	1	3
3	1	1	2

- $S = \mu_E \circ \mu_F(R)$ and $A \twoheadrightarrow BC$ holds in S
- PNF mimics 4NF for nested relations (A superkey)

PNF and MVD's and scheme tree

Preliminary statement

A **scheme tree** captures the logical structure of a nested relation schema and explicitly represents the **set of MVD's**

One more property of PNF relations

A nested relation R is in PNF iff the scheme of R follows a scheme tree with respect to the given set of MVD's

MVD's by example

- Book db: {Title \rightarrow Author}
- Class db: Student, Major, Class, Exam, Project
{Student \twoheadrightarrow Major, Class \rightarrow Exam}

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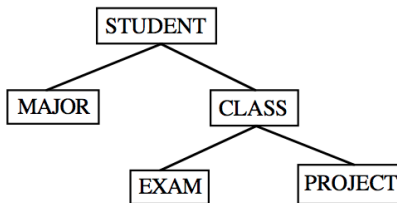
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Scheme—or schema—Tree

A tool for nested relation design

Definition (Scheme Tree)

A scheme tree is a tree containing at least one node and whose nodes are labelled with nonempty sets of attributes that form a disjoint partition of a set U of atomic attributes



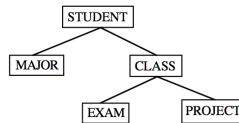
Design by MVD's

Pattern

Ancestors-and-self → Child-and-descendants

Example (cont'd)

- STUDENT \rightarrow MAJOR
- STUDENT \rightarrow CLASS EXAM PROJECT
- STUDENT CLASS \rightarrow EXAM
- STUDENT CLASS \rightarrow PROJECT



Nested Relation Schema

Definition (NRS)

A nested relation scheme (NRS) for a scheme tree T , denoted by \mathcal{T} , is a set defined recursively by:

1. If T is empty, i.e. T is defined over an empty set of attributes, then $\mathcal{T} = \emptyset$;
2. If T is a leaf node X , then $\mathcal{T} = \langle X \rangle$;
3. If A is the root of T and T_1, \dots, T_n , $n \geq 1$, are the principal subtrees of T then $\mathcal{T} = \langle A, B_1: \{\mathcal{T}_1\}, \dots, B_n: \{\mathcal{T}_n\} \rangle$

Example (cont'd)

$\langle \text{STUDENT}, \text{Majors}: \{ \langle \text{MAJOR} \rangle \},$
 $\text{Classes}: \{ \langle \text{CLASS}, \text{Exams}: \{ \langle \text{EXAM} \rangle \}, \text{Projects}: \{ \langle \text{PROJECT} \rangle \} \} \rangle$

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Nested relation over \mathcal{T}

Student	{Major}	{Class}	{Exam}	{Project}}
Anna	Maths Computing	CS100	mid-year final	Project A Project B Project C
Bill	Physics Chemistry	P100	final	Pract Test 1 Prac Test 2
		CH200	test A test B test C	Exp 1 Exp 2 Exp 3

Exercises 1/2

1. Definitions

Nested relation, Nest, Unnest, Powerset, Flat-flat theorem, Scheme tree, NRS, PNF

2. True or False?

- i) Nested algebra dominates RA.
- ii) Nested relations is a restriction from NF².
- iii) Nesting and unnesting are out of the scope of SQL.
- iv) Nest is the right inverse of unnest for PNF relations.
- v) Nesting a PNF relation produces a PNF relation.
- vi) Any scheme tree encodes a set of MVD's.

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Exercises 2/2

3. Nested relational queries

1. Give result of each query example from Slide 6.
2. Give NRS from the following *serialized* schema tree:

$$(ab(c(de)(f))(gh(i(j))(kl))(m(n)))$$

4. Problem

Given a PNF relation R of sort $\langle A, B: \{\langle C, D \rangle\} \rangle$; (a) prove that the size of any instance $I(R)$ is bounded by a polynomial in $\text{adom}(I(R))$; (b) Show how to encode the same information within 2 flat tables.

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Overview

Chapter eNF²

1. Extending NF²
2. Object Structure
3. Class Hierarchy


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The eNF² data model

eNF² = Extended NF² Model

- Extend NF² model by introducing
 - various **type constructors** and
 - allowing their **free combination**
- Type constructors:
 - set $\{.\}$: create a set type of nested type
 - tuple $\langle.\rangle$: tuple type of nested type
 - list $(.)$: list type of nested type
 - bag $\{[.]\}$: bag—multi-set—type of nested type
 - array $[.]_n$: array type of nested type
 - map $[./.]$: key/value dictionary type of nested types
- First two are already available in RM and NF²

The eNF² data model (cont'd)

The Evolution of Data Models

b.t.w. of sort comparison

- Relational Model $\tau := \langle A_1:\text{dom}, \dots, A_k:\text{dom} \rangle$
- NF² $\tau := \text{dom} \mid \langle A_1:\tau, \dots, A_k:\tau \rangle \mid \{\tau\}$
- eNF²

$$\tau := \text{dom} \mid \langle A_1:\tau, \dots, A_k:\tau \rangle \mid \{\tau\} \mid (\tau) \mid [\tau]_n \mid \{\{\tau\}\} \mid [\tau/\tau]$$

Flavors by **restrictions**, such like nested relations for NF²

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Type constructors

- $\langle . \rangle$ $\{ . \}$ $(.)$ $[.]_n$ $\{ . \}$ $[. / .]$ a.k.a. **Parametrizable Data Types**
- Construction based on '.', the **input data type**
- Define **own operations** for access and modification
- Similar to pre-defined parametrizable data types of programming languages
 - Generics in Java `java.util`
 - Templates in C++ STL
 - Type inference in OCaml

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Comparison of type constructors

Type	Dupl.	Bounded	Order	Access by	Composite
Set {.}	✗	✗	✗	Iterator	✗
Bag { .}	✓	✗	✗	Iterator	✗
Map [./.]	✓	✗	✗	Key	✗
List (.)	✓	✗	✓	Position/Iter.	✗
Array [.] _n	✓	✓	✓	Index	✗
Tuple ⟨.⟩	✓	✓	✓	Name	✓

- All but tuple type constructors are **collection data types**
- Tuple type constructor is a **composite data type**

SQL ARRAY type constructor

- Introduced within SQL:1999

```
CREATE TABLE Contacts(
    Name          VARCHAR(40),
    PhoneNumbers  VARCHAR(20) ARRAY[4],
    Addresses     AddressType ARRAY[3] );
```

SQL ARRAY type constructor (cont'd)

- Array type constructor for record insertion
- Access to elements by **explicit position** [*k*]

```
INSERT INTO Contacts
VALUES( 'Doe',
      ARRAY['1234','5678'],
      ARRAY[ROW( '50 0tages', 'Nantes', '44000' )] );
```

```
UPDATE Contacts
  SET PhoneNumbers[3]='91011'
  WHERE Name='Doe';
```

SQL ARRAY type constructor (cont'd)

- Alternative access to element by **unnesting of collection**

```
SELECT Name, Tel.*
FROM Contacts,
      UNNEST( Contacts.PhoneNumbers ) WITH ORDINALITY
      AS Tel(PHONE, Position)
WHERE Name='Doe';
```

- Further operations:
 - size CARDINALITY()
 - concatenation ||

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Object structure

- Complex value—state—conforms to object structure
- Type constructors are building blocks: tuple, set, list, array, bag, dictionary
- eNF² as the reference model
- Implementation within SQL3


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Yet another popular restriction

- **Class** of sort τ following

$$\tau := \langle A_1:\varrho, \dots, A_k:\varrho \rangle$$

$$\varrho := \text{dom} \mid \langle A_1:\varrho, \dots, A_k:\varrho \rangle \mid \{\varrho\} \mid (\varrho) \mid [\varrho]_n \mid \{\!\!\{\varrho\}\!\!\} \mid [\varrho/\varrho]$$

- Objects are **instances** of classes, a.k.a. class members
- An object o satisfies sort τ of its class c
- Essentially struct in C Programming Language

User-Defined Type in SQL3

UDT's occur at two levels:

- Columns of relations
- Tuples of relations

```
CREATE TYPE AddressType AS ( Street CHAR(50),
                             City   CHAR(50),
                             Zip    CHAR(5) );
```

```
CREATE TYPE BarType      AS ( Name   CHAR(20),
                             Addr   AddressType );
```

```
CREATE TABLE Bars OF BarType ( PRIMARY KEY (Name) );
```

```

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Encapsulated object vs. row

- Bars is unary: tuples are objects with 2 components
- Grant **access privilege** to components
- **Type constructor**

```

INSERT INTO Bars
VALUES BarType( 'Le Flesselles',
                AddressType( '50 Otages',
                              'Nantes',
                              '44000' ) );

```

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Encapsulated object vs. row (cont'd)

- **Observer** $A()$ and **Mutator** $A(v)$ for each attribute A
- Calls to implicit *getters* and *setters*, **redefinition** allowed

UPDATE Bars

SET Bars.Addr.Street('Allée Flesselles')

WHERE Bars.Name = 'Le Flesselles';

SELECT B.Name, B.Addr FROM Bars B;

Excerpt of the result set:

```

BarType( 'Le Flesselles',
        AddressType( 'Allée Flesselles', 'Nantes', '44000' ) )

```

Object behavior

Method := signature + body

Operation that apply to objects of a type

- $f(x)$ is invoked by sending a message to object o : $o.f(3)$
- Method
 - returns single value (may be a collection)
 - is typically written in general-purpose PL
 - could have unexpectable **side-effect**
- Implementation within ODL and SQL3

Disclaimer

Insight into object behavior is out of the scope of this series of slides

Corollary: main focus is the **structural part**

A word on eNF² in Oracle

- Supports **majority** of standard features as part of its object-relational extension—since 8i
 - **Multi-set** type constructor as NESTED TABLE type
 - **Array** type constructor as VARRAY type
 - **Object** (and **Tuple**) type constructor as OBJECT type
- Uses different syntax than ANSI/ISO SQL standard...

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Alternative languages

Definition of object structures

- DDL part of SQL3 OR-Databases
- DDL part of [your favorite or-dbms] OR-Databases
- Entity/Relationship (E/R) Model Relational Databases
- Object Description Language (ODL) OO-Databases
- Unified Modeling Language (UML) OO-PL
- ...

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ODMG ODL

Example

```
class Bar {
    attribute string                name;
    attribute struct addr {string street,
                               string city,
                               int    zip}    address;
    attribute enum lic {full, beer, none} license;
    attribute set< string >        drinks;
}
```

- Primitive types: int, real, char, string, bool, and *enumeration*
- Composite type: *structure*
- Collection types: set, array, bag, list, and dictionary

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Class hierarchy

- Reuse of class definition
- A subclass is a refinement of its superclass

Definition (Class hierarchy)

A class hierarchy $(\mathcal{C}, \sigma, \prec)$ has 3 components:

1. a set \mathcal{C} of class names
2. types τ 's associated with these classes: $\sigma(c) = \tau$
3. specification of the is-a relationship \prec between classes

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Subtyping relationship

A subtype **inherits** value—and behavior—of a predefined type

Definition (Subtyping)

Let $(\mathcal{C}, \sigma, \prec)$ be a class hierarchy; subtyping relationship is the smallest partial order \leq over types σ satisfying:

1. $\text{dom} \leq \text{dom}$
2. if $\tau_i \leq \tau'_i$, $1 \leq i \leq n$, then
 $\langle A_1:\tau_1, \dots, A_n:\tau_n, \dots, A_{n+k}:\tau_{n+k} \rangle \leq \langle A_1:\tau'_1, \dots, A_n:\tau'_n \rangle$
3. if $\tau_1 \leq \tau_2$, then $\{\tau_1\} \leq \{\tau_2\}$, $(\tau_1) \leq (\tau_2)$, $\{\tau_1\} \leq \{\tau_2\}$ and $[\tau_1]_n \leq [\tau_2]_n$
4. if $\tau_1 \leq \tau_3$ and $\tau_2 \leq \tau_4$, then $[\tau_1/\tau_2] \leq [\tau_3/\tau_4]$
5. for each τ , $\tau \leq \text{ANY}$ (i.e. ANY is the top of the hierarchy)

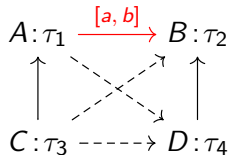
Covariance and contravariance

Subtyping follows from wider to narrower: **covariance** only

Definition (Covariance)

Typing rules preserve the ordering on \leq

About the map type constructor



- **Contravariance** reverses the ordering: type safety in PL

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Well-formed class hierarchy

Property

A class hierarchy $(\mathcal{C}, \sigma, \prec)$ is **well-formed** iff for each pair c_1, c_2 of classes, $c_1 \prec c_2$ implies $\sigma(c_1) \leq \sigma(c_2)$

Example

- $\sigma(\text{Person}) = \langle \text{name} \rangle$
- $\sigma(\text{Teacher}) = \langle \text{name}, \text{dpts} : \{ \langle \text{id} \rangle \} \rangle$
- $\sigma(\text{Student}) = \langle \text{name}, \text{major}, \text{enrol} : \{ \text{dom} \} \rangle$
- $\sigma(\text{Lecturer}) = \langle \text{name}, \text{dpts} : \{ \langle \text{id}, \text{office} \rangle \}, \text{contacts} : [\text{dom}]_3 \rangle$
- $\sigma(\text{Tutor}) = \langle \text{name}, \text{dpts} : \{ \langle \text{id} \rangle \}, \text{labs} : \{ \langle \text{day}, \text{room} \rangle \} \rangle$

$\{\text{Student}, \text{Teacher}\} \prec \text{Person}$, and $\{\text{Lecturer}, \text{Tutor}\} \prec \text{Teacher}$

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Subtyping within SQL

UNDER clause with NOT FINAL statement in the base type

```

CREATE TYPE PersonType AS (
    Name          VARCHAR(20)    NOT NULL,
    DateOfBirth   DATE,
    Gender        CHAR)
NOT FINAL;

CREATE TYPE StudentType UNDER PersonType AS (
    StudentID     VARCHAR(10),
    Major         VARCHAR(20)
);

CREATE TABLE Student OF StudentType;

```

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Multiple Inheritance

- **More than one superclass** vs. single inheritance
- The is-a relationship forms a directed acyclic graph (DAG)
- A subclass inherits state and behavior from **all** its superclasses
- Potential for ambiguity, e.g., fields with the same name
- The “*diamond problem*”: $D \prec \{B, C\} \prec A$
- SQL does not support multiple inheritance of UDT's

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Inheritance within ODL

```

class Person {
    attribute string    name;
    attribute character gender; }

class Teacher extends Person {...}
class Student extends Person {...}

class TeachingFellow extends Teacher, Student {
    attribute string    degree; }

```

- How many names and genders for a single TF ?!

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Membership in a class hierarchy

Definition (Object assignment)

A function π mapping each name in \mathcal{C} to a finite set of objets

- Proper extension of c : $\pi(c)$
- Set of database objects: $O = \{\pi(c) \mid c \in \mathcal{C}\}$
- **Extension** of c : $\pi^*(c) = \bigcup \{\pi(x) \mid x \in \mathcal{C} \wedge x \prec c\}$
- $\pi^*(c_1) \subseteq \pi^*(c_2)$ whenever $c_1 \prec c_2$

Definition (Substitutability principle)

Value of type S can be substituted to value of its supertype T


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Alternative memberships

Properties

- **Complete** assignment: $\pi^*(c) \neq \emptyset \rightarrow \pi(c) = \emptyset$
- **Disjoint** assignment: $\pi(c_1) \cap \pi(c_2) \neq \emptyset \rightarrow (c_1 \prec c_2 \vee c_2 \prec c_1)$

Each class may have direct subclasses with:

- complete vs. partial assignment
- disjoint vs. overlapping assignment

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Extension in ODL

- **Extent** declaration: *named* set of objects of the same type
 - Class \sim Schema of a relation
 - Extent \sim Instance of a relation
- Optional **Key** declaration: unicity constraint

```

class Course ( extent Courses
                keys   id, (dept, title), (classroom, time) )
{...};

```

```

SELECT c.id, c.title FROM Courses c
WHERE c.dept='Computer Science';

```

- Object Query Language (OQL): SQL-like for pure object db's
- Alias for extent (c) is mandatory: typical class member

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“Subtabling” within SQL

No native extension for types in SQL: create table for each UDT

Table inheritance!

```

CREATE TABLE Person OF PersonType;
CREATE TABLE Student OF StudentType UNDER Person;

```

- A Person row matches at most one Student row
- A Student row matches exactly one Person row
- Inherited columns are inserted only into Person table
- Delete Student row deletes matching Person row

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“Subtabling” within SQL (cont'd)

- Default: retrieve the extension $\pi^*(\text{Person})$ with all subtable rows

```
SELECT P.Name FROM Person P;
```

- ONLY clause: retrieve the proper extension $\pi(\text{Person})$

```
SELECT P.Name FROM ONLY (Person) P;
```

Open issues

Multiple-table inheritance ? Propagation of referential integrity constraints ? Index ? ...

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Basics of relational mapping

- Classes are all distinct tables
- Keys must be defined
- The three ways to cope with class hierarchy:
 1. E/R-style: one partial table by subclass with key+specific fields
 2. OO-style: one full table by subclass
 3. Null-style: all subclasses embedded within one single base table

Example

Person(name, gender)

Teacher(name, dpt)

Student(name, major)

Person(name, gender)

Teacher(name, gender, dpt)

Student(name, gender, major)

Person(name, gender, dpt, major)

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Exercises 1/2

1. Definitions

eNF², Class, Class member, UDT, Observer, Mutator, Method, ODL, Class hierarchy, Subtyping, Covariance, Diamond problem, Substitutability principle, Extension, OQL

2. True or False?

- i) eNF² dominates NF².
- ii) Map is a composite type constructor.
- iii) SQL implements eNF².
- iv) Subtyping rules are covariant only.
- v) $\pi(c) = \emptyset$ except for the leaves, is a full complete assignment.
- vi) SQL Subtabling implements relational mapping in E/R-style.

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Exercises 2/2

3. Misc

1. Exhibit a class hierarchy that is not well formed.
2. Give in ODL the Person class hierarchy of the example slide.

4. Problem

How many relations are required, using the OO-style mapping, if there is a 3-level hierarchy with out-degree 4, and that hierarchy is: (a) disjoint and complete at each level, (b) disjoint and partial at each level, and (c) overlapping and partial.

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Overview

Chapter ID's and Refs

1. OID's and References
2. Relationships
3. Graph Databases

Object identity

- Persistent objects are given an **Object Identifier** (OID)
- Used to manage *inter-object references*
- OID's are
 - **unique** among the set of objects stored in the DB
 - **immutable** even on update of the object value
 - **permanent** all along the object lifecycle
- OID's are not based on physical representation/storage of object (i.e., \neq ROWID or TID, \neq @object)

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Ultimate object representation

Definition (Object)

An object is a pair (o, ϑ) , with o being the OID and ϑ is the value

- Object identity is given by the OID
- Object value is not required to be unique

Values by example

- In the *class-oriented* restriction of eNF², values ϑ are
 - tuple-based complex values:
 - $(o_1, \langle \text{title} : \text{'cs123'}, \text{desc} : \text{'...'} \rangle)$
 - $(o_2, \langle \text{title} : \text{'cs987'}, \text{desc} : \text{'...'} \rangle)$
 - $(o_3, \langle \text{name} : \text{'Doe'}, \text{major} : \text{'cs'}, \text{year} : \text{'junior'}, \text{enrol} : \{o_1, o_2\} \rangle)$
 - OID to achieve aliasing: (o_4, o_3)
 - *nil* for nullable reference: (o_5, nil)

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Composition graph

Structural representation of an object as a labeled directed graph

$$\text{struct}(o) := G(V, E)$$

where

- Vertices $V \subset O \cup \text{dom}$ are OID's and atomic values
- Edges $E \subseteq V \times \mathcal{A} \times V$ are labeled with symbols from \mathcal{A} , the set of field names
- Draw an edge (o_i, x) whenever $x \in \{o_j, a\}$ occurs in the value of o_i , a being an atomic value in dom

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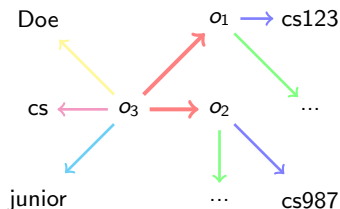
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Composition graph (cont'd)

Example for object o_3



name	major	year
title	desc	enrol

Extend to a—cyclic—graph: *teacher* → *dpt* → *employees*

Statement

Object db is essentially **a huge persistent relational graph**

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Equality

- **Identity** ($==$) is checked by means of OID's comparison
- Composition graph allows to compare two objects for equality
 - **Shallow equality** ($=$): graphs must be identical, including OID's
 - **Deep equality** ($=_*$): isomorphic graphs with different OID's but atomic values are equal

Properties

$$o_i == o_j \longrightarrow o_i = o_j$$

$$o_i = o_j \longrightarrow o_i =_* o_j$$


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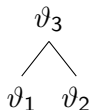
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Object expansion

Definition (Expansion)

Expansion of an object o , denoted $\text{expand}(o)$, is the—possibly infinite—tree obtained by replacing each object by its value recursively

Example of $\text{expand}(o_3)$



- Infinite expansion: cycle in the composition graph
- Deep equality can be checked from expansion traversal

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Object persistence

- In OO-PL, objects are **transient**
- Persistence is orthogonal to object types—classes
- Many policies to come up with **persistent** objects:
 - Object creation and explicit declaration
 - Homogeneous collection by **extension**
 - **Reachability**: declare persistent objects by name, and the system makes persistent all reachable objects at any level of the composition graph


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Reachability vs. extension

Names

1. Extension: all class members are designated by the name of a single collection
2. Reachability: objects are linked to the name of their **root of persistence**

On delete

1. Extension: must detect an orphan (?) and retrieve the object from its collection name
2. Reachability: garbage collecting when an object has a null in-degree

Types revisited

The family of *types* τ over the set \mathcal{C} of class names is as follows:

$$\tau := \langle A_1 : \varrho, \dots, A_k : \varrho \rangle$$

$$\varrho := \text{dom} \mid c \mid \langle A_1 : \varrho, \dots, A_k : \varrho \rangle \mid \{\varrho\} \mid (\varrho) \mid [\varrho]_n \mid \{\varrho\} \mid [\varrho/\varrho]$$

- dom may be refined into primitive types of the language
- c is any class name in \mathcal{C}

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Types revisited (cont')

- Object assignment π is basically OID assignment
- $\text{ANY} \in \mathcal{C}$ is a—singular—type such that $\text{dom}(\text{ANY}) = \llbracket O \rrbracket$
- Subtyping relationship is extended to:
 6. if $c_1 \prec c_2$, then $c_1 \leq c_2$
- Semantics of a class c is $\text{dom}(c) = \pi^*(c) \cup \{\text{nil}\}$

SQL3 References

Principle

If τ is a type, then $\text{REF}(\tau)$ is a **type of references** to τ

- Weak translation of OID's into SQL world
- Unlike OID's, a REF is **visible** although it is gibberish

```
CREATE TYPE SellType AS (
  bar    REF(BarType)  SCOPE Bar,
  beer   REF(BeerType) SCOPE Beer,
  price  FLOAT );
```

Following REF's and dereferencing

```
CREATE TABLE Sell OF SellType (
  REF IS sellID SYSTEM GENERATED,
  PRIMARY KEY (bar, beer) );
```

```
SELECT Deref(s.beer) AS beer
FROM Sells s
WHERE s.bar->name = 'Le Flesselles';
```

- It would have required a join or nested query otherwise

Relationships

- Operate at the type system—class definition—level
- Connect entities/classes/types one with each other
- Binary relationships as **partial multi-valued functions**
- Decide for a direction: contains or isIncluded or both
- Prevent from redundancy: computed relationships
- Multiway relationships simulated by *connecting* classes

ODL example

```
class Sell {
  attribute    real price;
  relationship Bar  theBar;
  relationship Beer theBeer;
}
```

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Multiplicity of relationships

- For binary relationships
 - One-one: class/class
 - Many-one: set²/class
 - Many-many: set/set
- 'One' means **at most one**
- Many-one variants: **aggregation** and **composition** (1..1)
- Weak class: id depends on master class id's (\neq OLD's)

```

class Employee (key (name, affiliated_to)) { // weak class
  attribute      string      name;
  relationship Department    affiliated_to; // one-one
  relationship set<Task>      assigned_to;   // many-one
  relationship list<Project> participates_in; // many-many
}

```

²or any collection type constructor.

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Basic properties of partial multi-valued functions

- A function $f : X \rightarrow Y$ can be
 - **total**: domain of f is X
 - **injective**: for all a, b in domain of f , if $f(a) = f(b)$ then $a = b$
 - **surjective**: range (or codomain) of f is Y
 - **bijective**: both injective and surjective
- The **inverse** function $f^{-1} : Y \rightarrow X$ satisfies $f^{-1} \circ f = \text{Id}$, with
 - extended to sets of values

Comments

- Impact on design choices and further encoding
- Problems arise especially when mixed with inheritance

Implementation of the inverse function

- Two relationships are right inverses by means of
 - Both ways of the same link in graphical languages
 - inverse statement in ODL
 - Not supported in SQL3

Example in ODL

```
class Employee { ...
    relationship list<Project> participates_in
                        inverse      Project::members; }
class Project { ...
    relationship set<Employee> members
                        inverse      Employee::participates_in; }

```

Relational mapping

- Relationships are essentially all distinct tables
- Key fields both parts come into play
- Exceptions:
 - Supporting relationship of a weak class does not require a separate table
 - Inlining of aggregations and compositions
- Discussion about inlining each *-one relationship
- Implement relationships one way only

OQL features

- Query can include **path expressions** rather than joins:

```
SELECT s.beer.name, s.price
FROM Sell
WHERE s.bar.name='Le Flesselles';
```

- Alternative query

```
SELECT s.beer.name, s.price
FROM Bar b, b.beerSold s
WHERE b.name='Le Flesselles';
```

- Collections cannot be further extended by dot notation
- Collections can be part of the FROM clause

OQL features (cont'd)

- Result type is basically $\{\langle.\rangle\}$
- Complex result type can be constructed in query

```
SELECT DISTINCT struct( e.name,
                        projects:(
  SELECT p.projectId
  FROM e.participates_in AS p) )
FROM Employees AS e;
```

- Result type:

$$\{\langle\text{name:string, projects:}\{\{\text{int}\}\}\rangle\}$$

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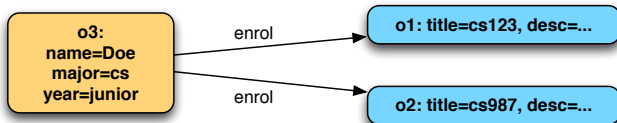
```

Relationship as first-class citizen

Reminder

- Object db as a (multi-)relational graph
- Can be further simplified to a vertex-attributed relational graph where atomic key/value pairs are an extended part of the object node itself

Example of o_3



Claim

Object db's are graph db's

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Requirements for graph databases

The 3D graph data model [Angles et al., ACM CS 2008]

1. Data structure

- data and schema are (separate) **graphs**
- standard abstractions: is-a is-type-of is-part-of is-composed-by is-member-of is-associated-to

2. Update and query language

- graph transformations
- primitives on paths, neighborhoods, subgraphs, graph patterns, connectivity and graph statistics (diameter, centrality, etc.)
- multi-relational graph algorithms

3. Integrity constraints

- schema-instance consistency, identity, referential integrity and functional and inclusion dependencies

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Requirements for graph databases (cont'd)

Definition (Graph database (tentative of))

Any storage system that provides index-free adjacency

- Each vertex has direct references to its adjacent vertices
 - act as a **mini-index**
- $\mathcal{O}(1)$ to move from a vertex to its neighbors
- $\mathcal{O}(\log n)$ b.t.w. of an index in non-graph db's

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Dominant and alternative models of db's

Data model

An (attributed) multi-relational labeled digraph $G(V, E)$ where

- V is a finite set of distinct node labels (id's)
- $E \subseteq V \times \Sigma \times V$, Σ being a finite alphabet of directed edge—**relationship**—symbols
- optional attributes—**properties**—may apply to both vertices and edges as a set of key/value pairs

Extension to

- hypernode: nested graphs where nodes are graphs themselves
- hypergraph: with hyperedges, i.e., sets of nodes
- multigraph: multiple single-relational edges


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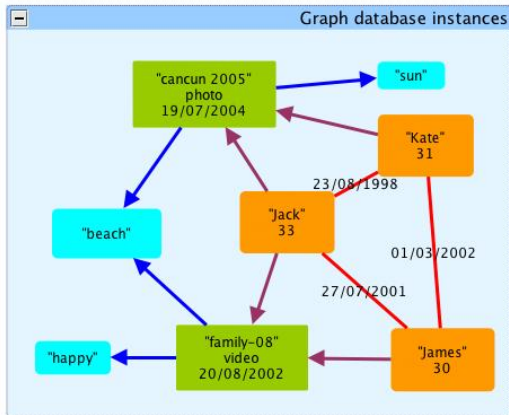
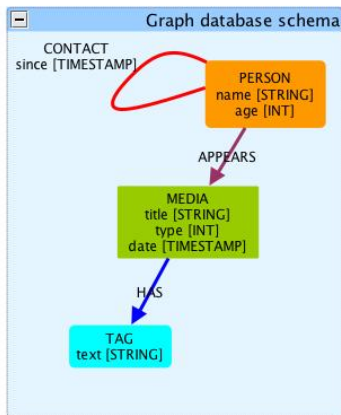
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Graph db example



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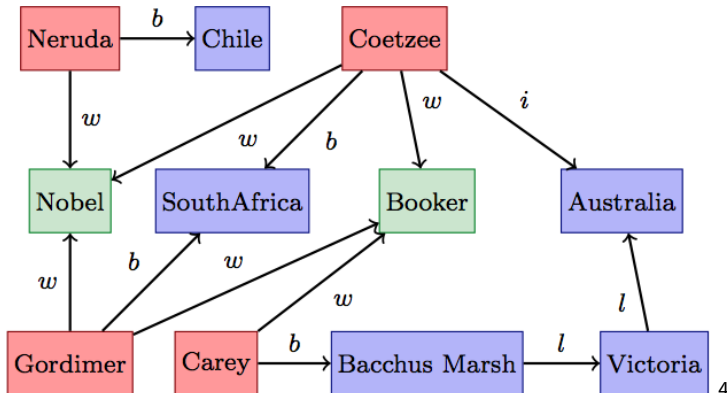
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Another graph db example



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b:bornIn *w*:hasWon *i*:livesIn *l*:locatedIn

⁴Source: (P.T. Wood, SIGMOD Record 2012)

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Conjunctive Queries

Implements **subgraph matching**

Definition (Graph CQ's)

$$\text{ans}(\vec{z}) \leftarrow \bigwedge_{1 \leq i \leq m} (x_i, a_i, y_i)$$

where x_i, y_i are node variables or constants, each z_j is x_i, y_i or any constant, and $a_i \in \Sigma$

Example

$$\begin{aligned} \text{ans}(x) \leftarrow & (x, \text{hasWon}, \text{Nobel}), (x, \text{hasWon}, \text{Booker}), \\ & (x, \text{bornIn}, \text{SouthAfrica}) \end{aligned}$$

Conjunctive Regular Path Queries

Implements **reachability** by path expressions

Definition (Graph CRPQ's)

$$\text{ans}(\vec{z}) \leftarrow \bigwedge_{1 \leq i \leq m} (x_i, r_i, y_i)$$

Extend CQ's to r_i as a **regular expression** over Σ

Example

$$\begin{aligned} \text{ans}(x) &\leftarrow (x, \text{hasWon}, \text{Booker}), (x, r, \text{Australia}) \\ r &:= \text{citizenOf} \mid ((\text{bornIn} \mid \text{livesIn}).\text{locatedIn}^*) \end{aligned}$$

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Extended CRPQ's

Paths may

- occur in the output by means of **free path variables**
- be compared within a **regular relation**

Examples

Retrieve every path between nodes r and s that go through node e :

$$\text{ans}(\pi_1, \pi_2) \leftarrow (r, \pi_1, e), (e, \pi_2, s)$$

Retrieve all pairs (x, y) connected by paths following pattern $a^n.b^n$:

$$\text{ans}(x, y) \leftarrow (x, \pi_1, z), (z, \pi_2, y), a^*(\pi_1), b^*(\pi_2), \left(\bigcup_{a, b \in \Sigma} (a, b) \right)^*(\pi_1, \pi_2)$$

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Extended CRPQ's (cont'd)

Definition (Graph ECRPQ's)

$$\text{ans}(\vec{z}, \vec{\chi}) \leftarrow \bigwedge_{1 \leq i \leq m} (x_i, \pi_i, y_i), \bigwedge_{1 \leq j \leq p} R_j^{k_j}(\vec{\omega}_j)$$

where χ_ℓ , π_i , ω_{jt} are path variables, and $R_j^{k_j}$ is a regular expression that defines a regular relation over Σ

Extension to approximate matching and ranking

- Define an **edit distance** $d_e(x, y)$ on Σ^*
- Operate with a regular expression over triples of the form (a, k, b) , $a, b \in \Sigma \cup \{\epsilon\}$, k the cost of substitution

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Aggregation and arithmetic predicates

count sum min max + − * / for computing:

- degree, eccentricity of a node
- distance between two nodes
- diameter of the graph
- *etc.*

Example

Length of the *shortest path* between each pair of nodes

```

len(x, x, x, 0)    ←  dist(x, y, ℓ)
len(x, x, x, 0)    ←  dist(y, x, ℓ)
len(x, z, y, d)    ←  sp(x, z, s), dist(z, y, ℓ), d = s + ℓ
sp(x, y, min(d))   ←  len(x, z, y, d)

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Node creation

Skolem function

- remove existential quantifiers within FO formula: basically, $\exists x.P(x)$ becomes $P(a)$ with a a constant
- substitute to free variables to create new nodes in queries

Example

From a people-centric network to a city-centric network

$\text{ans}(f(c), \text{is-a}, \text{city})$	$\leftarrow \Delta(p, c)$
$\text{ans}(f(c), \text{name}, c)$	$\leftarrow \Delta(p, c)$
$\text{ans}(f(c), \text{population}, \text{count}(p))$	$\leftarrow \Delta(p, c)$
$\Delta(p, c)$	$\leftarrow (p, \text{is-a}, \text{person}), (p, \text{livesIn}, c)$


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The Web of Data

- Resource Description Framework (RDF) for the Semantic Web
- RDF statement: (subject, predicate, object)
- **Triple store** is a restriction of graph db

RDF Data Model

Vertex set is split into URIs (U), literals (L), and blank/anonymous nodes (B), such that:

$$G \subseteq ((U \times B) \times U \times (U \times B \times L))$$

- Extension to **named graphs** as $ng = (n, g)$ with $n \in U$ and $g \in \mathcal{G}$, the family of RDF graphs

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The Web of Data (cont'd)

SPARQL

Graph pattern-based SQL-like query language for RDF triple stores

```

PREFIX foaf: <http://xmlns.com/foaf/0.1/>
SELECT ?name ?email
WHERE {
    ?person a foaf:Person.
    ?person foaf:name ?name.
    ?person foaf:mbox ?email.
}

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Semi-structured data

eXtended Markup Language (XML)

- Tree-like structures: **rooted digraphs!**
- Labeled unbounded ordered trees: restricted type of graph
- Referencing mechanism: simulation of arbitrary graphs
- Self-describing: hierarchical structure within the document
- Implicit *composition* relation only

XML query languages

- **XPath**: path expressions
- **XQuery**: SQL-like query language for XML db's

Object db's vs. Graph db's

At a glance:

- Structural part is essentially the same
- Querying capabilities may converge

Main differences:

- Graph db's are schema-less
- Object db's equip objects with operations

Small variants:

- Graph db's handle properties on edges
- Graph db's emphasize interconnections and their properties
- Object db's emphasize dynamic state and behavior of objects

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Exercises 1/2

1. Definitions

OID, Composition graph, Shallow equality, Deep equality, Expansion, Persistence by reachability, Partial multi-valued function, Graph database, Graph CQ, Graph CRPQ, Graph ECRPQ, RDF data model

2. True or False?

- i) OID's are kind of primary keys.
- ii) Given $=$ and $=_*$ are resp. $=_0$ and $=_\infty$, then $=_{k+1}$ refines $=_k$.
- iii) One-one relationships are injective functions.
- iv) Graph db's cannot implement class hierarchies.
- v) Subgraph matching is basic requirement for graph db querying.
- vi) RDF triple stores are graph db's.

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Exercises 2/2

3. ODL relationships

1. Give an ODL design with all the inverse relationships for the Person class to represent a genealogy.
2. What makes a relationships its own inverse ?

4. Problem

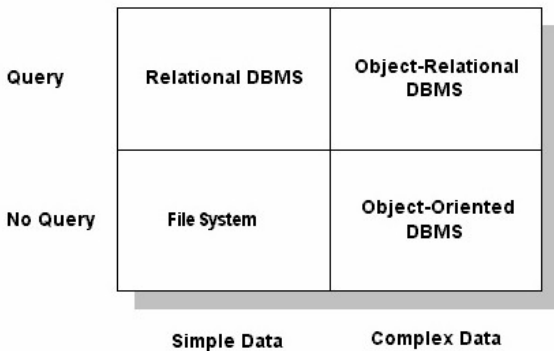
Prove that $\text{expand}(o)$ is a regular tree, i.e., it has a finite number of distinct subtrees.

From Lineland to Spaceland

Object-Oriented paradigm brings to the—relational—data world

- Mashup of:
 1. Databases
 2. OO Programming Languages
 3. Conceptual/Semantic Modeling
- Practical approaches to contemporary issues
- Lack of strong mathematical foundations

The Matrix



M. Stonebraker: *Object-Relational DBMS: The Next Great Wave*, MK, 1998
15 years later, OO-DBMS in South-East quadrant is questionable

Impedance Mismatch revisited

Find a sunset picture taken within a coastal zone by a professional photographer

```
SELECT p.id
FROM slides p, area a, a.landmarks l
WHERE sunset (p.picture) AND
      p.owner.occupation = 'photographer' AND
      a.type = 'coastal' AND
      contains (p.caption, l.name) ;
```

- User-defined functions: sunset() contains()
- Path expression: P.owner.occupation
- Collection as table: area.landmarks

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The First Manifesto

M. Atkinson, F. Bancilhon, D. DeWitt, K. Dittrich, D. Maier, and S. Zdonik.
The Object-Oriented Database System Manifesto. In *Proceedings of the First International Conference on Deductive and Object-Oriented Databases*, pages 223-240, Kyoto, Japan, December 1989

13 must-have features of OO-DBMS

- 8 from **Object-Oriented Programming Languages**
 complex objects, object identity, encapsulation, types and classes, inheritance, polymorphism, completeness, extensibility
- 5 from **Databases**
 persistence, secondary storage management, concurrency, recovery, *ad hoc* query facility

ODMG Standard

- Object Database Management Group
 - **1991** ODMG was created by R. Cattell of Sun Microsystems
 - **2000** Latest standard: ODMG 3.0
 - **2001** ODMG disbanded to focus on Java Data Object (JDO)
 - **2006** OMG Object Database Technology (ODBT) Working Group for the 4th generation of OO-DBMS standard
- Four components
 1. Object Model
 2. Object Definition Language (ODL)
 3. Object Query Language (OQL)
 4. Language Binding for C++, Java, Smalltalk

Object Query Language (OQL)

- Extension of the SQL-92 standard: object-oriented notions, like complex objects, object identity, path expressions, operation invocation etc.
- High level constructs to deal with sets of objects and primitives for structures, list, arrays etc.
- Functional language where operators can freely be composed, as long as the operands respect the type system
- OQL does not provide explicit **update** operators but rather invokes operations defined on objects for that purpose

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OO-DBMS vs. OR-DBMS vs. O/R Mapping

Relation as first-class citizen?

- Yes: SQL3
 - PostgreSQL, IBM DB2, Oracle, Microsoft SQL Server, Sybase
- No: ODMG ODL+OQL
 - db4o, Versant, ObjectStore, ObjectDB, Native Queries, LINQ
- Don't care: PL coupled with (R-)DBMS Mapping Framework
 - Hibernate, JPA, JDO, CodeIgniter, Symfony, Django, EF