

$$\begin{aligned} 1. \text{ Eval } \sin\left(\frac{\pi}{2}\right) \cot\left(\frac{5\pi}{3}\right) + \sec\left(\frac{5\pi}{4}\right) \\ &= (1) \cdot \frac{1}{\tan\left(\frac{5\pi}{3}\right)} + \frac{1}{\cos\left(\frac{5\pi}{4}\right)} \\ &= 1 \cdot \left(1 \div -\frac{\sqrt{3}}{1}\right) + \left(1 \div -\frac{1}{\sqrt{2}}\right) \\ &= 1 \cdot \left(-\frac{1}{\sqrt{3}}\right) + (-\sqrt{2}) \\ &= -\frac{1}{\sqrt{3}} + -\sqrt{2} \\ &= \frac{-1 - \sqrt{6}}{\sqrt{3}} \end{aligned}$$

$$\begin{aligned} 2. \text{ Evaluate } \sin\left(\frac{13\pi}{12}\right) \\ &= \sin\left(\frac{9\pi}{12} + \frac{4\pi}{12}\right) = \sin\left(\frac{3\pi}{4} + \frac{\pi}{3}\right) \\ &= \sin\left(\frac{3\pi}{4}\right) \cos\left(\frac{\pi}{3}\right) + \cos\left(\frac{3\pi}{4}\right) \sin\left(\frac{\pi}{3}\right) \\ &= \left(\frac{1}{\sqrt{2}}\right)\left(\frac{1}{2}\right) + \left(-\frac{1}{\sqrt{2}}\right)\left(\frac{\sqrt{3}}{2}\right) \\ &= \frac{1}{2\sqrt{2}} + \left(-\frac{\sqrt{3}}{2\sqrt{2}}\right) \\ &= \frac{1 - \sqrt{3}}{2\sqrt{2}} \end{aligned}$$

$$\begin{aligned} 3. \text{ Express } f(x) &= \frac{1}{\sqrt{2}} \cos(x) + \frac{1}{\sqrt{2}} \sin(x) \text{ as cosine function w/ hor-translation} \\ &= \cos\left(\frac{\pi}{4}\right) \cos(x) + \sin\left(\frac{\pi}{4}\right) \sin(x) \\ &= \cos\left(\frac{\pi}{4} - x\right) \\ &= \cos\left(-(x - \frac{\pi}{4})\right) \end{aligned}$$

$$\frac{1}{\sqrt{2}} = \cos\left(\frac{\pi}{4}\right) \text{ or } \sin\left(\frac{\pi}{4}\right)$$

$\therefore$  is a cosine function with a horizontal translation of  $\frac{\pi}{4}$  right

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4. Sketch  $f(x) = -2\sin(4x - \frac{\pi}{6}) + 5$   
 $= -2\sin(4(x - \frac{\pi}{24})) + 5$

amp: 2

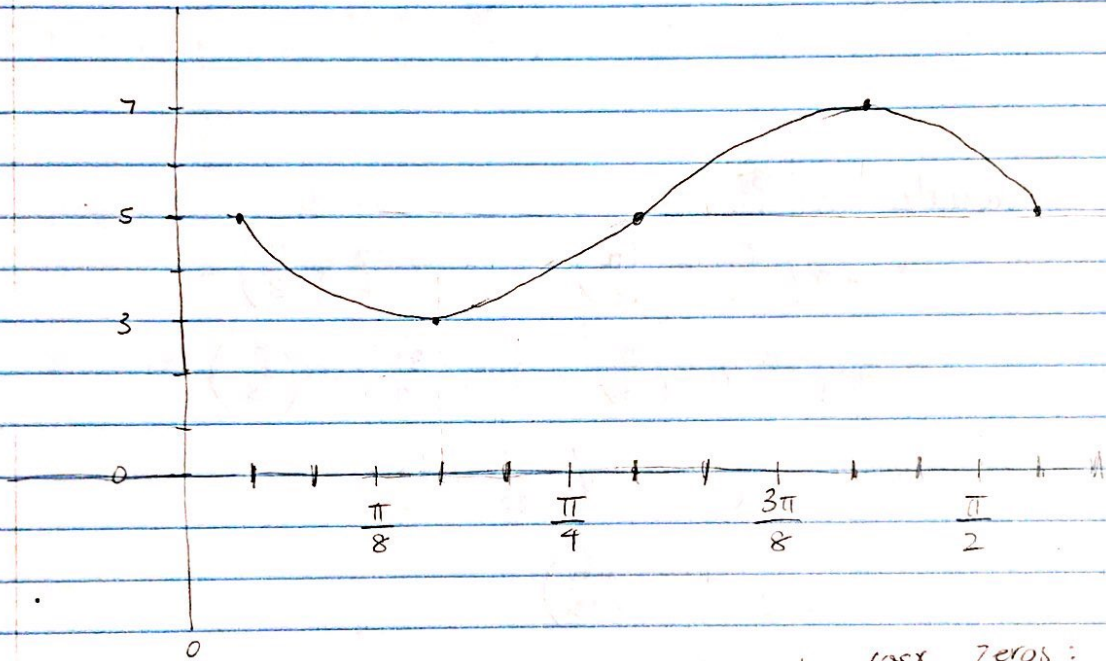
axis:  $y = 5$

reflection along  $x$ -axis!

$\frac{1}{4}$  per:  $\frac{1}{8}$

period =  $\frac{2\pi}{k} = \frac{2\pi}{4} = \frac{\pi}{2}$

translation  $\frac{\pi}{24}$  right



amp: 2

axis:  $y = 1$

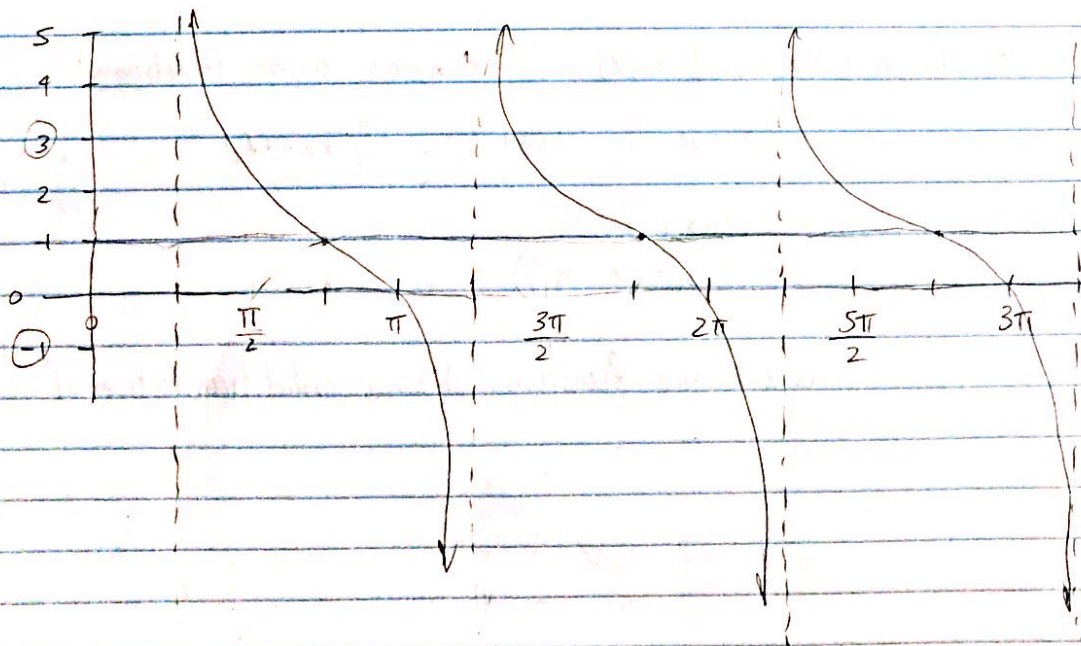
5. Sketch  $f(x) = 2\cot(x - \frac{\pi}{4}) + 1$

period =  $2\pi$

translation hor:

$\frac{\pi}{4}$  right

$\cot = \frac{\cos x}{\sin x}$  Zeros:  $(4n+1)\frac{\pi}{4}$   
 asymp:  $(4n+1)\frac{\pi}{4}$





6. Determine one sine equation and one cosine equation for the following graph

sine :

amp : 2      period  $\frac{2\pi}{k} = \frac{\pi}{2}$        $\frac{\pi k}{2} = 2\pi$        $k = 4$

axis :  $y = 1$       horz translation :  $\frac{5\pi}{24}$  right

$$\textcircled{1} f(x) = 2 \sin\left(4\left(x - \frac{5\pi}{24}\right)\right) + 1$$

cos :

amp 2      period = 4

axis :  $y = 1$       horz translation :  $\frac{\pi}{3}$  right

$$\textcircled{2} f(x) = 2 \cos\left(4\left(x - \frac{\pi}{3}\right)\right) + 1$$

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