

# MATH 748: Weekly Report

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Nayeong Kim (nkim10@sfsu.edu)

## 9 Multi-Class Classification

### 9.7 Regularized Discriminant Analysis

(1) Friedman(1989)

A compromise between QDA and LDA. Set  $\hat{\Sigma}_k(\alpha) = \alpha\hat{\Sigma}_k + (1 - \alpha)\hat{\Sigma}$  for  $\alpha \in [0, 1]$ .  $\alpha$  can be chosen by hyper-parameter-adjusting(e.g. cross-validation).

- $\alpha = 0 \Rightarrow$  LDA
- $\alpha = 1 \Rightarrow$  QDA

(2) Regularized LDA:  $\hat{\Sigma}(r) = r\hat{\Sigma} + (1 - r)\hat{\sigma}^2 I$

(3) Regularized QDA:  $\hat{\Sigma}_k(\alpha, \gamma) = \alpha\hat{\Sigma}_k + (1 - \alpha)\gamma\hat{\Sigma} + (1 - \alpha)(1 - \gamma)\hat{\sigma}^2 I$

We can choose  $\alpha, \gamma$  by cross-validation.

- $\alpha = \gamma = 1 \Rightarrow$  QDA
- $\alpha = 0, \gamma = 1 \Rightarrow$  LDA

### 9.8 More flexible, more complex decision boundaries

This is mentioned in *Chapter 12*

(1) FDA (Flexible Discriminant Analysis)

(2) PDA (Penalized Discriminant Analysis)

(3) MDA (Mixture Discriminant Analysis)

While LDA sets  $X|Y = k \sim \text{MVN}(\mu_k, \Sigma)$ , MDA sets  $X|Y = k \sim \pi_1 \text{MVN}(\mu_{k,1}, \Sigma) + (1 - \pi_1) \text{MVN}(\mu_{k,2}, \Sigma)$

## 10 Remedies for Severe Class Imbalance

### Introduction

(1) What is imbalanced data?

*Imbalanced data* is a classification problem where the classes are not represented equally. (e.g. fraud transaction, online advertising, disease screening, job application, credit card application)

(2) Why is this a problem?

Hard to predict the minority class.

(3) How to resolve this problem.

Resampling

- Under-sampling  
idea  
benefit  
problem: loss of info
- Over-sampling  
idea: replication  
benefit: No loss of information  
problem: Might lead to overfitting

Synthetic Data Generation

Reading: SMOTE

- ROC Curve: Tell you both the type1, type2 error. x axis: type I error rate  
y axis: type II error rate  
area under the curve = area below the curve  $\leq 1$  Each corner : extreme cases  
Ideal curve:

### 10.1 ddd

## 11 Feature Selection

### 11.1 Motivation

### 11.2 Feature Selection

It is a process of selection subset of predictors.

(1) Advantages

(2) Applications

(3) 3 types of Feature Selection Methods

- Filter: Give rankings to the data and take top
- Wrapper:
- Embedded:

### 11.3 Filter

It is independent of classifier (1) Univariate Filter e.g.  $Y, X_1 \rightarrow P_1$   
 $Y \text{ vs } Y_p \rightarrow P_p$  smallest p-value ranks the original use correlation

- Pearson's correlation
- ANOVA test
- A lot of tests

(2) Multivariate Filter Evaluate an entire feature subset Slower

### 11.4 Wrapper

Interacting with the classifier. Wrapper is guided by the performance of the classifier on the subset. Classifier dependent. 3 Highs: cost, chance of overfitting, success 2 major search schemes

- Sequential  
Not guaranteed. Only look at the moment
- Randomized alg.

### 11.5 Filter vs Wrapper

- Interaction with the classifier
- Speed
- Performance

### 11.6 Subset Selection

(1) Best subset selection  $k$  predictors  $\rightarrow Y = \beta_0 + \beta_1 X + \beta_k$  Select a single best model from among the  $p + 1$  models.  $2^p$  very large It is computationally expensive How to decide? Smallest RSS or largest  $R^2$   
Credit data: e.g. from ISL book

## References

[1] Wikipedia: Hamming Distance