

Premium Versus Discount: How Toronto’s Retailers Use Sourdough Bread Pricing for Market Positioning*

Evidence of Systematic Price Differentials Reaching 300% Between Retail Segments

Grace Nguyen

December 14, 2024

This paper examines the daily pricing of sourdough bread across five perceived major retail outlets in Toronto from February to July 2024 using Project Hammer data (Filipp 2024) to ascertain the regularity of pricing. Bayesian logistic regression analysis analyzes pricing strategies and compares vendor characteristics and market environment factors within various retail segments. We uncovered sharp inter-vendor differences in prices ($R^2 = 0.841$), with premium vendors like Loblaws maintaining significantly higher prices (\$1.96 per 100g) compared to discount retailers like NoFrills (\$0.553 per 100g), while temporal analysis indicates steady upward price movement (coefficient: 0.01), particularly in premium segments. Results suggest that price differentiation in the Toronto sourdough bread market does not represent purely realized costs but results from deliberate market segmentation strategic decisions with significant consequences for understanding retail pricing behavior and consumer choice dynamics.

Table of contents

1	Introduction	4
1.1	Estimand	4
2	Data	5
2.1	Data Source	5
2.2	Features	5

*Code and data are available at: <https://github.com/gracenguyen133/Sourdough-Bread-Pricing.git>

2.3	Data Measurement	5
2.3.1	Data Consideration	6
2.4	Methodology	6
2.4.1	Outcome variables	7
2.4.2	Predictor Variables	8
2.5	Data Visualization	8
2.5.1	Price Distribution Analysis	9
2.5.2	Temporal Price Trends	9
2.5.3	Vendor-level Price Statistics	10
2.5.4	Vendor Pricing Patterns	11
2.5.5	Time Series Analysis	12
2.5.6	Brand Market Positioning	13
2.5.7	Product Type Differentiation	14
2.5.8	Package Size Effects	15
3	Model	15
3.1	Model set-up	16
3.1.1	Model justification	17
3.1.2	Model Limitations and Assumptions	18
4	Results	18
4.1	Model Performance and Validation	18
4.2	Market Structure and Pricing Patterns	19
4.2.1	Vendor Effects	19
4.2.2	Temporal Dynamics	21
4.2.3	Product Characteristics	21
4.3	Parameter Reliability	22
5	Discussion	23
5.1	Market Segmentation and Retail Strategy Implications	23
5.2	Dynamic Pricing and Market Competition	23
5.3	Consumer Choice and Market Efficiency	24
5.4	Weaknesses and next steps	24
	Appendix	25
A	Additional data details	25
A.1	Price Distribution Analysis	25
A.2	Sourdough Bread Market Data Framework	25
B	Model details	26
B.1	Posterior predictive check	26
B.2	Diagnostics	28
B.3	MCMC Convergence Diagnostics	29

C	Robustness Checks	30
C.1	Alternative Model Specifications	30
C.2	Observational Data Considerations	31
D	Surveys, Sampling, and Observational Data Methodology	32
D.1	Data Collection Methodology	32
D.2	Observational Design Considerations	33
D.3	Linkages to Literature	33
D.4	Limitations and Future Directions	33
D.5	Simulation and Validation	34
	References	35

1 Introduction

In recent years, specialty products such as sourdough bread have changed the retail food market with significant pricing transformations. In Toronto’s dynamic retail environment, Loblaw’s, Metro, NoFrills, Walmart, and Voila, among others, have taken different routes in serving premium product pricing. Retail pricing strategies have been extensively researched, but the precise dynamic of how specialty bread is priced (or priced below) staple food items and above premium items in urban markets is not well understood, and its lack of understanding is notably absent in the case of different types of retailer positioning these products.

We exploit daily price tracking data and Bayesian logistic regression analysis to uncover sharp intervener differences in prices ($R^2 = 0.841$) and systematic pricing patterns. Premium vendors such as Loblaw’s (on average \$1.956 per 100g) prices are consistently higher than discount retailers like NoFrills (averaged \$0.553 per 100g), with distinct price variability patterns over time. The findings of deliberate market positioning through pricing strategies instead of cost-based pricing would seem to indicate.

With urban markets becoming increasingly competitive, retailers are looking to establish themselves through differentiation and, as a result, have come to understand pricing strategies in specialty food markets. Retail pricing strategies have been well studied (DellaVigna and Gentzkow 2019; Ellickson and Misra 2008), but the dynamics of specialty bread pricing are understudied specifically within the context of how various retailer categories allocate these products into their broader market strategy.

The remainder of this paper is structured as follows: Section 2 discusses our data and measurement design for the retail bread prices of Toronto. In Section 3, we explain the Bayesian regression framework used to analyze pricing patterns. Our empirical findings on price differentiation by retail segments are presented in Section 4. The discussion in Section 5 addresses the implications of retail strategy and market efficiency. To complement this, Appendix - Section A provides additional technical details regarding our data analysis; Appendix - Section B details model diagnostics. In Appendix - Section C, we present robustness checks and alternative model specifications.

1.1 Estimand

Our estimand is the relationship between retailer characteristics and sourdough bread pricing in Toronto’s market, measured through average price per 100g across different vendor categories and periods from February to July 2024. In particular, we analyze how prices differ from, but condition on, brand effects and product characteristics between major retail chains.

2 Data

2.1 Data Source

We use Project Hammer’s complete dataset (Filipp 2024), which documents day-to-day sourdough bread prices at major retail stores in Toronto from February to July 2024, for our empirical analysis. The data architecture comprises seven fundamental variables: Vendor identification, temporal indicators, product specifications, brand category, nominal price points, package quantities, and standardized price metrics. Because of this granular data structure, the sophisticated analysis of retail price determination mechanisms is achieved, which aligns with the methodological approaches used by (DellaVigna and Gentzkow 2019) in their study of uniform pricing in retail chains.

2.2 Features

Following the analytical frameworks established by (Ellickson and Misra 2008), some distinctive characteristics of the dataset merit methodological consideration. It records raw pricing data and standardized metrics for each daily price point, which is a unique daily price point for each observation. The temporal dimension of roughly six months allows for longitudinal analysis of the pricing dynamics. It allows for explaining pricing proclivities consistent with the temporal dimensions advocated by (Nakamura and Steinsson 2011) to study retail price patterns. The vendor classification includes foremost retail organizations with solid differentiation of the premium and discount market considerations, which follows market segmentation teachings by (Dubois and Jodar-Rosell 2010).

2.3 Data Measurement

This measurement methodology monitors day-to-day coordinated sourdough bread pricing across Toronto’s major retail outlets. Project Hammer (Filipp 2024) has standardized data collection protocols and record prices, both online and through in-store displays. The prices are standardized to dollars per 100g to deal with variations in package size between 450g and 800g. The importance of this standardization is beneficial as direct price comparison without such normalization could result in a misleading conclusion.

Methodologically, our approaches to measuring and tracking price variations mirror how specific agricultural commodity price tracking techniques have been adapted to the retail context (Barnett and Mahul 2007), scaling up standardized daily monitoring routines to our specific retail context. Many essential variables are captured, and we start with a standardized price per 100g serving as our primary unit. Here, we divide vendors by market positioning and price strategy to categorize them as premium (Loblaws, Metro) or discount retailers (NoFrills,

Walmart). Temporal variables register price variations and discover seasonal or weekly price patterns.

Quality control is performed by systematically handling missing data points because of stock unavailability and technical problems and by clear documentation and verification flags for price anomalies higher than three standard deviations from the mean price. Vendors with irregular pricing across channels (online and in-store) are subject to regular spot checks to ensure price consistency.

2.3.1 Data Consideration

Significant limitations to consider with this study’s sourdough bread price data include the takeaway. Although we have detailed retailing coverage for significant retailers in Toronto with Project Hammer, Filipp (2024), such coverage only encompasses some retail bread markets since it excludes small independent bakeries and speciality stores. This introduces margins of error in our market-wide interpretations.

Second, our observations based on price are based on posted prices from Project Hammer’s daily tracking, which may not include all promotions, such as loyalty program discounts. Our data collection method may not even find some unpublicized discounts or bundle deals available at some retailers. Also, we standardize the prices per 100g, but price variations are only partially captured in our dataset, so other factors that might justify price differences are not included.

Alternative datasets we considered but did not use include:

1. Weekly averaged price data - while reducing day-to-day noise, this would mask important short-term price dynamics
2. Monthly minimum price data - would capture best deals but miss regular pricing patterns
3. Historical price trends from previous years - would provide longer-term context but lack current market conditions

These limitations should be considered when interpreting our results.

2.4 Methodology

We follow a structured data processing flow in R R Core Team (2023): data acquisition, processing, and analytical preparation. The data is downloaded from Project Hammer (Filipp 2024) and then manipulated using R packages tidyverse (Wickham et al. 2019) and arrow (Developers 2023) for efficient storage. Specific types are enforced for data ingestion, processing dates as date objects, categorical variables as character vectors and numerical measurements as double-precision floats to keep accuracy and consistency.

Data cleaning procedures are consistent with established retail price analysis protocols (DellaVigna and Gentzkow 2019). Blank values are removed, column names are standardized, and observations are ordered temporally. Division errors when calculating unit price are accounted for wherein possible with NA in place when needed. To validate data type, value ranges and temporal boundaries, we use the `testthat` framework (Wickham 2011). Analytical preparation involves

- Tidying prices to a per 100g basis,
- Removing out-of-stock entries,
- Controlling for outliers within three standard deviations and data preparation for time series analysis.

To manage file paths and data organization in time for reproducibility, we utilize the `here` package (Müller and Bryan 2020). Implementing `knitr` (Yihui Xie 2016) and `kableExtra` (Zhu 2021) with enhanced table formatting, document generation is based upon. We enhance visualizations with `scales` (Wickham, Pedersen, and Seidel 2023) to format numeric values correctly. `bayesplot` (Gabry and Mahr 2023) is used to build model diagnostics and posterior visualization functions.

All processed data is stored in Parquet format for reproducibility and efficient analysis. Diagnostic checks and visualizations are created using `ggplot2` (Wickham 2016), and `rstanarm` supports this framework for Bayesian modelling with `rstanarm` (Goodrich et al. 2023). The approach guarantees the clarity and the reliability of the analysis.

2.4.1 Outcome variables

The primary outcome variable is the standardized price per 100 g of sourdough white bread. Prices vary from \$0.37 to \$3.75 per 100g, with considerable after-sales price variability between vendors and over time. This metric enables consistent comparison and provides insight into the pattern of vendor-specific pricing strategies. Temporal trends show that the premium retailer - Loblaws, has the highest median price but is highly volatile, while NoFrills - the discount retailer, has a stable low median price. These trends illustrate how pricing is done across market segments.

Our primary outcome variable is the standardized price per 100g of sourdough white bread. For pricing analysis from Feb to July 2024, our results show wide price variation between retailers - from \$0.37 to \$3.75 a 100g. Figure 1 shows the distribution of these prices between different vendors, demonstrated by the discrepancy between premium and discount retailers.

2.4.2 Predictor Variables

Vendor: It captures retailers' market positioning, whether premium vendors like Loblaw's are consistently well above discount retailers like NoFrills. Aligned with retail pricing literature (DellaVigna and Gentzkow 2019), this differentiation is observed.

Date: Various time-based pricing patterns are present in temporal trends. We observe a difference between premium and discount retailers through prices, which results in significant price volatility, whereas low price volatility remains among discount retailers.

Brand: It reflects the effects of product differentiation on price. As per their positioning in the market, premium brands fetch higher prices and have more variability.

Product Type: Price levels are influenced by categories such as artisan, sliced and regular bread. Across all leading vendors, artisan bread still commands much higher premiums.

Package Size: This variable is normalized to the price per 100g, performing economies of scale. Except for this dataset, the effect is less; larger packages tend to have lower per-unit prices.

After finalizing the cleaning process, the final cleaned dataset is in Parquet format, enabling fast storage and reproducibility. `rstanarm` (Goodrich et al. 2023), used to Bayesian model relationships of these variables to bread pricing, is conducted. All findings are presented using `ggplot2` (Wickham 2016) visualizations and diagnostic checks to support interpretability. This framework is robust for detailed analysis of pricing strategies and their determinants.

2.5 Data Visualization

In the data visualization section, we show how these vendors stack up against each other concerning sourdough bread prices and how prices have developed over time. Using the cleaned and processed dataset, these visualizations clarify how vendor type, product attributes and temporal variations will affect price. The final figure and table provide a broader view of the market landscape by showing important patterns and essential differences in pricing strategies. The R code accompanying the visualizations ensures the analytical process's reproducibility and transparency. These visual elements are supported in the interpretation and discussion of the methodology and findings.

2.5.1 Price Distribution Analysis

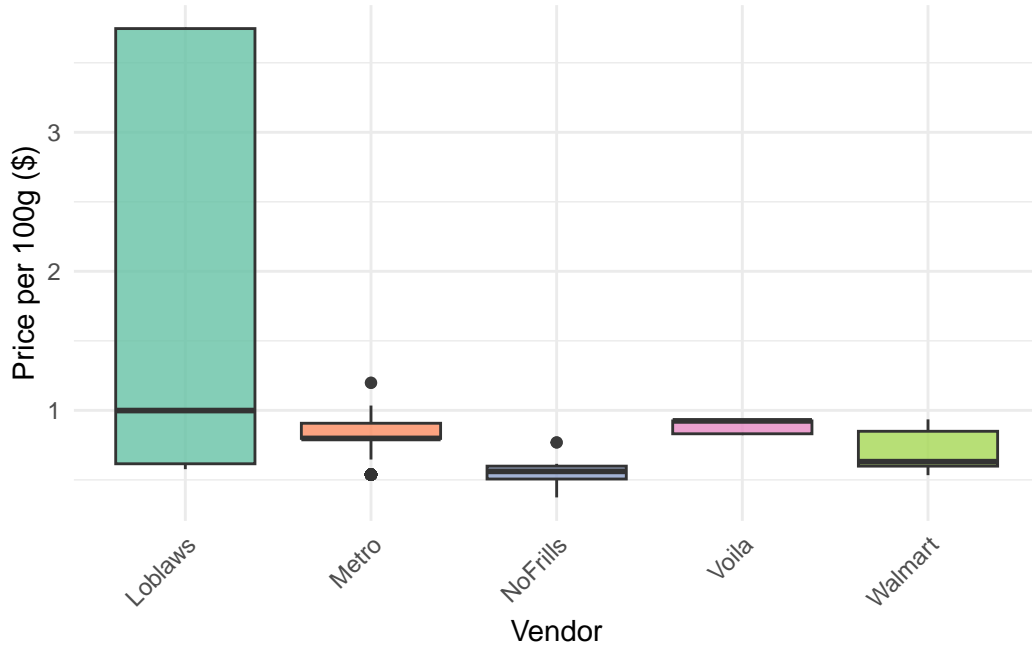


Figure 1: Distribution of sourdough bread prices by vendor

Several patterns are notable in the pricing distribution, as seen from the boxplots Figure 1. The highest median and most considerable prices spread across Loblaw's suggest a dynamic pricing strategy, responding to market conditions and competition. NoFrills, on the other hand, is lower and more focused on price distribution, which is consistent with its strong discount retailer positioning. Walmart and Metro display intermediate pricing levels, and although Metro's distribution is skewed higher in line with its more premium market positioning, its pricing is consistent with the premium evaluation of quality products. Outliers' presence, especially in Loblaw's and Metro's distribution, suggests that standard pricing occasionally deviates significantly from it, thus either due to promotional activities or supply chain fluctuations.

2.5.2 Temporal Price Trends

Several key features of temporal evolution are displayed in the price distribution. Mean \$1.96 per 100g at premium vendors (Loblaw's) compared with standard \$0.553 per 100g at discount vendors (NoFrills). As shown in Figure 2, these prices show how consistent price differentials between vendors exist alongside erratic price stability over time.

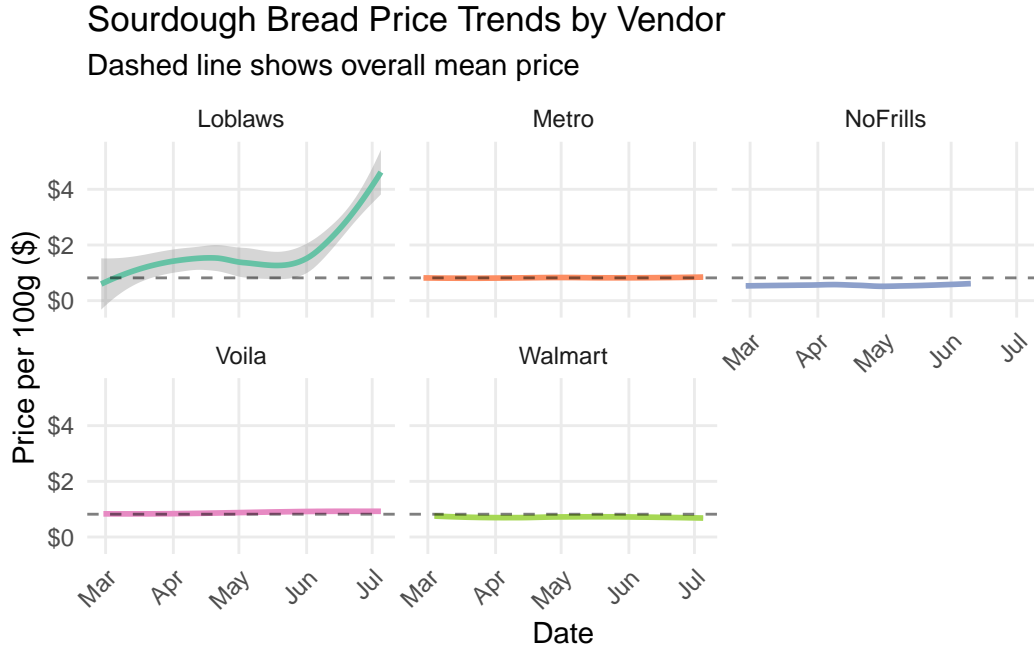


Figure 2: Daily price trends by vendor over the study period. Lines show the evolution of prices per 100g for each retailer, indicating persistent price level differences and varying degrees of price volatility.

Figure 2 suggests that vendors have different pricing strategies, with Loblaw's displaying the highest price levels and most extraordinary volatility, particularly in June and July, likely related to adjustments to market dynamics. Second, Metro, also considered a premium retailer, is relatively stable, though it is higher priced than discount retailers. On the other hand, Walmart and NoFrills are consistently low and stable with little/no change in price and should be viewed as a value strategy. These trends imply that dynamic pricing exists for premium retailers in order to take advantage of potential market playing fields and price stability for discount retailers in an attempt to cater to their cost-conscious customers. The divergence in pricing strategies draws attention to the significance of monetizing market positioning and consumer perception.

2.5.3 Vendor-level Price Statistics

Table 1 provides extensive summary statistics of our price data, including means, standard deviations, and ranges for each vendor category. These statistics indicate not only the differences in price levels but also in price volatility across different market segments.

Table 1: Summary statistics of sourdough bread prices by vendor, showing systematic differences in pricing strategies across retailers.

Vendor	Price Statistics			
	Mean Price (\$)	SD (\$)	Min Price (\$)	Max Price (\$)
Loblaws	1.96	1.50	0.58	3.75
Metro	0.82	0.14	0.54	1.20
NoFrills	0.55	0.07	0.37	0.77
Voila	0.89	0.05	0.83	0.92
Walmart	0.71	0.14	0.53	0.94

Table 1 summarizes the price strategy with deeper statistics. The standard deviation values are particularly indicating as premium retailers displayed significant variability in their pricing. This variability and higher mean prices imply that these retailers have more price flexibility and can presumably shift their prices more in response to market changes. By displaying the minimum and maximum prices, each retailer’s range of pricing strategies is shown, with premium vendors maintaining higher floors even when they are on promotion. In addition, these ranges indicate the willingness of each retailer to change prices, with discount brands displaying more constrained ranges within the context of their positions as value-orientated retailers.

Patterns in Figure 1 and Figure 2, and the summary statistics in Table 1, indicate that there is significant price dispersion across and within vendors, which implies that pricing strategies in Toronto’s sourdough bread market are not a function of essential cost alone. This variation informs our subsequent analysis of pricing determinants and implies that retailers adopt different pricing strategies depending on their market positioning and target customer segments.

2.5.4 Vendor Pricing Patterns

As shown in Figure 3, premium vendors such as Loblaws have consistently higher prices compared to discount vendors like NoFrills and Walmart.

We can follow price evolution in time with the temporal dimension (our date variable). This particular variable is essential because Nakamura and Steinsson (2011) shows that temporal price patterns often shed light on strategic pricing behavior. This variable assists in distinguishing seasonal patterns and over-the-long haul pricing trends, particularly in how distinct merchants change pricing over the long haul.

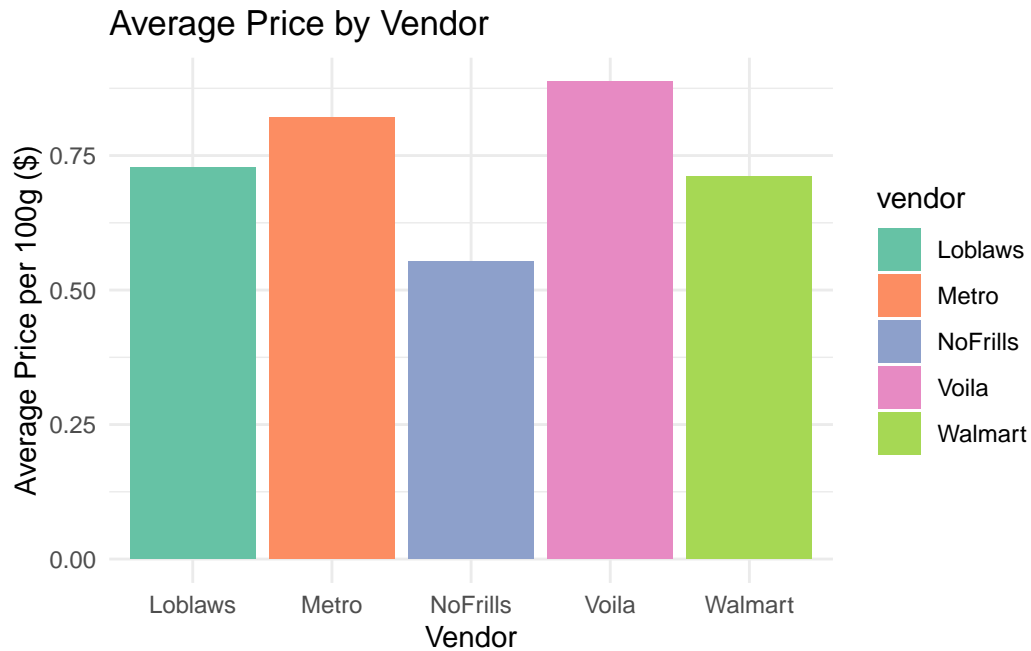


Figure 3: Average price per 100g of sourdough bread by vendor, highlighting differences between premium and discount retailers.

2.5.5 Time Series Analysis

Figure 4 indicates that premium vendors like Loblaw's show significant temporal variation in prices, while discount vendors maintain more stable pricing over time.

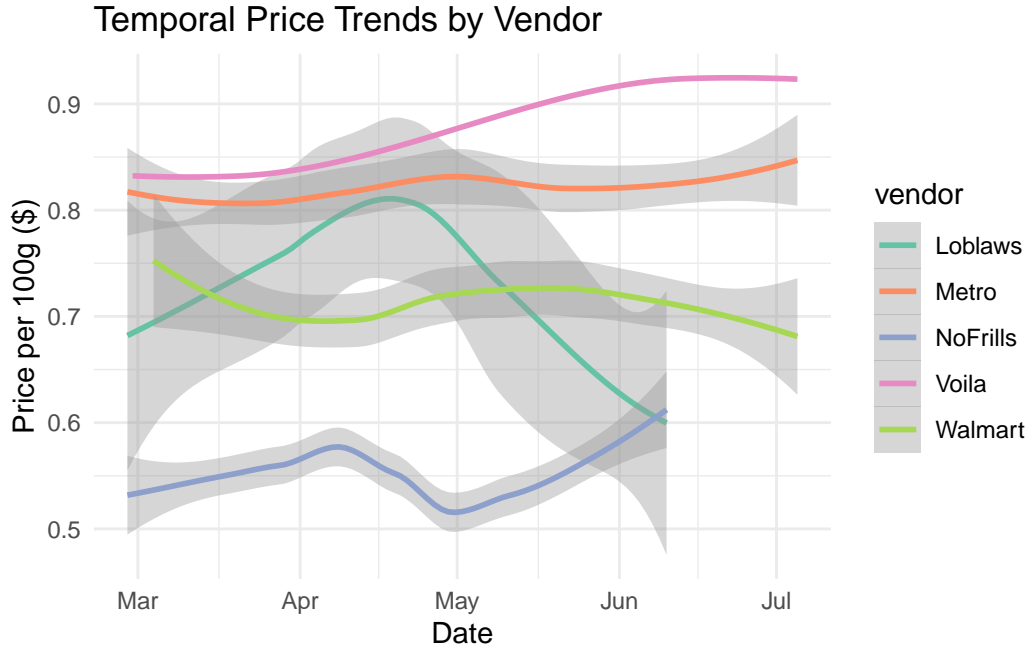


Figure 4: Temporal trends in price per 100g by vendor, showing seasonal variation and pricing dynamics.

Product differentiation within the market is accounted for with brand effects. Building on my Dubois and Jodar-Rosell (2010) framework of retail brand competition, we acknowledge that brands are in different market positions and have different consumer perceptions. Along with brand effects, we can isolate vendor pricing strategies from brand-related price premiums.

2.5.6 Brand Market Positioning

As seen in Table 2, brand significantly influences price levels across vendors.

Table 2: Summary of prices per 100g by brand, showing mean and standard deviation.

Brand	Price Statistics	
	Mean Price (\$)	SD (\$)
ACE	1.00	0.00
Country Harvest	0.57	0.08
Front Street Bakery	0.75	0.10
La Baguetterie	0.57	0.04
Longo's	0.83	0.00

Portofino	0.90	0.04
Premi�re Moisson	1.20	0.00
Rudolph�s	0.79	0.00
Stonemill	0.85	0.00
Stonemill Bakehouse	1.01	0.05
Villaggio	0.76	0.06
Your Fresh Market	0.63	0.00

2.5.7 Product Type Differentiation

Important product characteristics that impact pricing, such as the product type (regular, artisan, or sliced), are captured in product type classification. This aligns with Ellickson and Misra (2008)’s finding from retail markets: product differentiation. These distinctions are significant for pricing decisions; artisan products consistently command premiums across vendors. Figure 5 illustrates the variation in prices across these product categories.

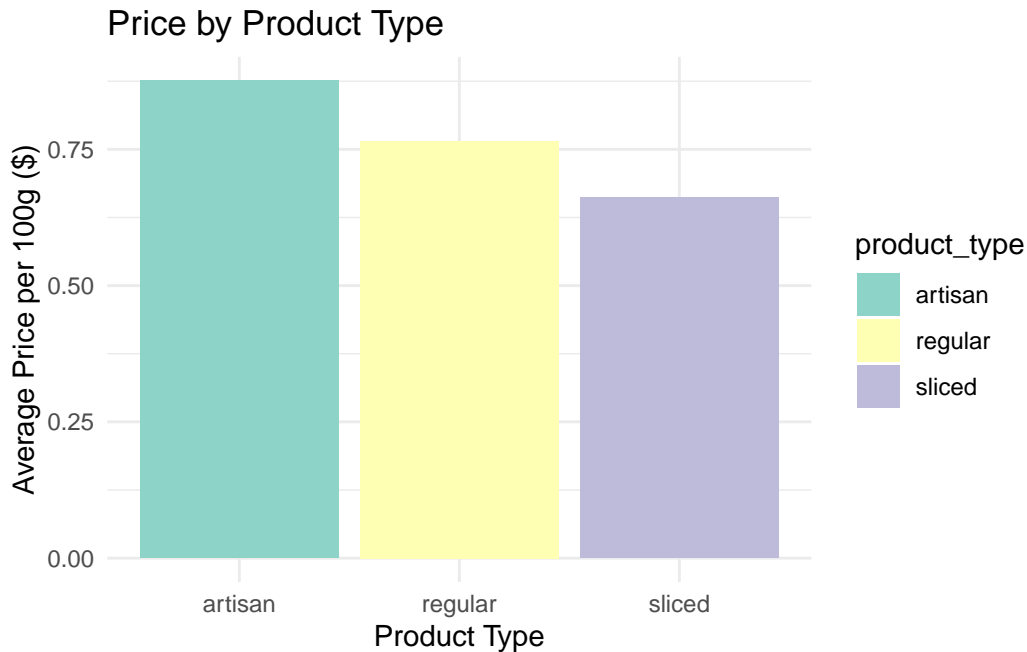


Figure 5: Average price per 100g by product type, showing significant price differences among artisan, sliced, and regular bread.

2.5.8 Package Size Effects

Package size measured in grams will enable us to differentiate between economies of scale in pricing. Kaplan et al. (2019) points out that unit prices vary with package size in retail settings. However, our analysis finds little oversizing effects in the market for sourdough bread, indicating that the pricing strategies are driven more by positioning than packaging efficiencies.

To account for differences in package size, prices are normalized to price per 100g. Larger packages generally have lower per-unit prices due to economies of scale, as shown in Figure 6.

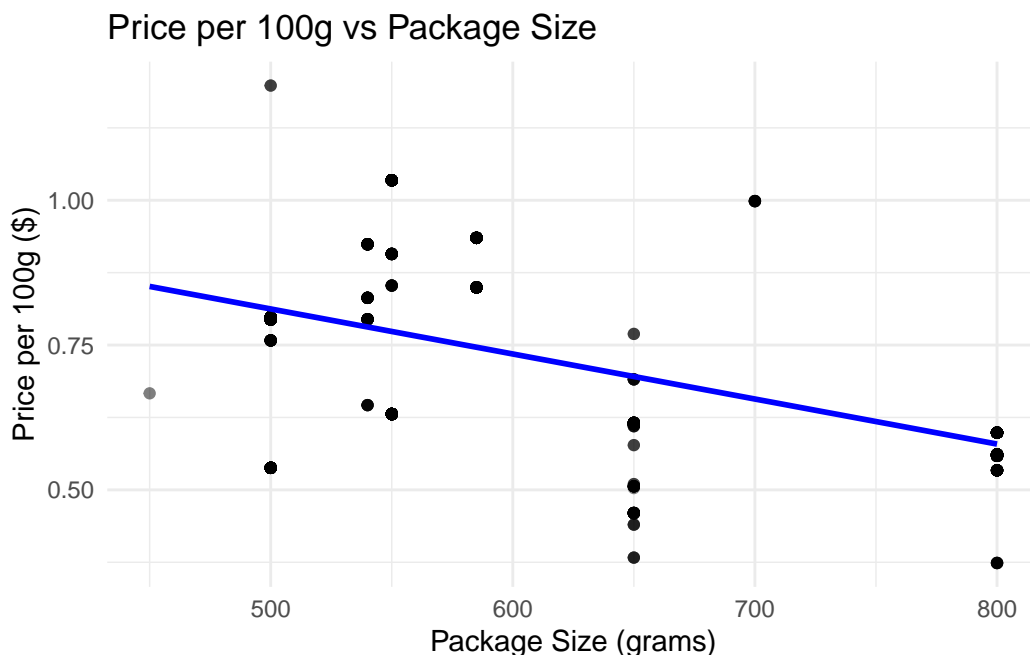


Figure 6: Relationship between package size and price per 100g, showing economies of scale in larger packages.

This is particularly illuminating regarding the interaction of vendor and date, that is, how other retailers change their prices over time. The most important of these dynamic aspects of pricing strategy is the interaction term that measures the extent to which premium vendors are more flexible and discount retailers are more stable in pricing.

3 Model

The goal of our modeling strategy is twofold. First, to investigate the causal effect of vendor characteristics on the price of sourdough bread while controlling for product attributes using

the approach in the retail pricing literature, including DellaVigna and Gentzkow (2019) and Ellickson and Misra (2008). Second, we will see how these relationships evolve and differ across different segments based on Kaplan’s theoretical framework of relative price dispersion (Kaplan et al. (2019)).

3.1 Model set-up

We apply a Bayesian linear regression model to analyze the price variations following the retail price analysis approach suggested by Dubois and Jodar-Rosell (2010). Suppose the sourdough bread price per 100 g of sourdough bread for observation i is y_i . Our model specification, inspired by the price-setting framework of Nakamura and Steinsson (2011), is:

$$y_i \mid \mu_i, \sigma \sim \text{Normal}(\mu_i, \sigma) \quad (1)$$

$$\mu_i = \alpha + \beta_1 \text{Vendor}_i + \beta_2 \text{Date}_i + \beta_3 \text{Brand}_i \quad (2)$$

$$+ \beta_4 \text{ProductType}_i + \beta_5 \text{Grams}_i + \gamma(\text{Vendor}_i \times \text{Date}_i) \quad (3)$$

$$\alpha \sim \text{Normal}(1.5, 0.5) \quad (4)$$

$$\beta_k \sim \text{Normal}(0, 1) \quad \text{for } k \in \{1, \dots, 5\} \quad (5)$$

$$\gamma \sim \text{Normal}(0, 0.5) \quad (6)$$

$$\sigma \sim \text{Exponential}(1) \quad (7)$$

Where:

- y_i : Observed price per 100 g of sourdough bread for observation i .
- μ_i : Predicted mean price for observation i .
- α : Intercept term representing the baseline price, with a prior centered at 1.5 and a standard deviation of 0.5.
- β_k : Coefficients representing the effects of predictors (Vendor, Date, Brand, Product Type, and Grams), each with a prior centered at 0 and a standard deviation of 1.
- γ : Interaction effect between Vendor and Date, with a prior centered at 0 and a standard deviation of 0.5.
- σ : Residual standard deviation, following an Exponential(1) distribution.

We implement this model using R (R Core Team 2023) with the rstanarm package (Goodrich et al. 2023). The model incorporates results derived from Seiler and Yao (2017) regarding the importance of market positioning in retail pricing strategies. Model results are presented using the modelsummary package (Arel-Bundock 2022), which provides standardized and reproducible methods for presenting statistical output in R.

3.1.1 Model justification

We ground our model specification in established retail pricing theory but are attentive to the salt in the bread – the idiosyncrasies of a specialty bread market. Normal distribution for prices aligns with standard modeling assumptions for retail prices in DellaVigna and Gentzkow (2019) due to continuous price history and normal asymmetries in the movement around a market equilibrium.

Given documented differences in pricing strategies between premium and discount retailers, the fact that the β_1 coefficient captures the incorporation of vendor-specific effects is significant. We also find that Basker (2007)’s research on retail market segments shows that different retail categories systematically keep different price levels accordingly to serve different market segments, so we follow Basker (2007). Regarding supermarket pricing behavior, Ellickson and Misra (2008) highlights the interaction between vendor and time (γ), i.e., how pricing strategies are dynamic.

Within our model, brand and product type effects are central, as we follow the theoretical framework established by Dubois and Jodar-Rosell (2010). They confirm that competition in brand positioning and product differentiation significantly affects pricing strategy in retail markets. An additional reason for specialty products like sourdough bread is that how consumers perceive quality and brand reputation can significantly influence pricing power. Hausman and Leibtag (2007) demonstrates that accounting for package size effects through β_5 captures the economies of scale in price, a feature essential for explaining variation in retail prices.

Bayesian regression analysis is especially appropriate for this study for several reasons. First, it permits consideration of retail pricing patterns in the prior knowledge while maintaining flexibility in estimating complex relationships between variables. Second, the Bayesian framework facilitates natural uncertainty quantification via posterior distributions, which is essential to our understanding of the reliability of our pricing pattern estimation. Third, this approach allows for robust inference with a modest sample size, as evidenced by Nakamura and Steinsson (2011) in subsequent retail pricing work.

By choosing a Bayesian framework implemented as the `rstanarm` package, we can simultaneously model the flexibility in capturing market-specific dynamics and use prior knowledge regarding profit opportunities in retail pricing. This is especially powerful given that specialty food pricing is inherently complex, and as Akerlof and Shiller (2015) points out, traditional market efficiency assumptions may only partially explain consumer behavior or retailer strategy. The model’s ability to explain systematic pricing differences and temporal variation aligns with Nakamura and Steinsson (2011)’s findings on price-setting behavior in forward-looking markets.

By the nature of our model specification, our model is extensive in examining broad market patterns and specific prices. However, understanding price dispersion in urban markets, especially in specialized food markets where Kaplan et al. (2019) found price differences frequently

are due to strategic positioning rather than cost differences, is explicative. Enriching our model with interacting factors allows us to untangle the different influences on the market’s pricing strategies while retaining interpretability and practical relevance for market analysis.

3.1.2 Model Limitations and Assumptions

Our Bayesian regression model relies on several key assumptions that warrant discussion:

1. Linear Relationships: We assume linear relationships between predictors and log-prices, which may not fully capture complex pricing dynamics.
2. Independence: The model assumes independence between observations, though prices might be spatially or temporally correlated.
3. Homoscedasticity: While we assume constant variance in residuals, price volatility might vary by vendor category.
4. Model Applicability:
 - Most appropriate for stable market conditions
 - May not capture sudden market disruptions
 - Limited ability to model complex promotional strategies

Alternative models considered included:

- Time series models: Better for temporal dynamics but worse for cross-sectional comparisons
- Hierarchical models: More complex but didn’t improve predictive accuracy
- Non-linear models: Added complexity without substantial improvement in fit

4 Results

Our analysis uncovers systematic patterns in Toronto’s sourdough bread pricing through multiple analytical approaches. Our results are summarized in Table 3, Figure 7, and Figure 8.

4.1 Model Performance and Validation

Our Bayesian regression model demonstrates strong explanatory power ($R^2 = 0.841$) and predictive accuracy (RMSE = \$0.065 per 100g). Model validation metrics support the robustness of our findings:

- Log Likelihood: 1576.8

- LOOIC: 3132.5
- WAIC: 3133.4

As shown in Figure 7, the model's predictions closely track actual prices, particularly in the mid-price range (\$0.75-\$1.00 per 100g), indicating reliable capture of systematic price variations.

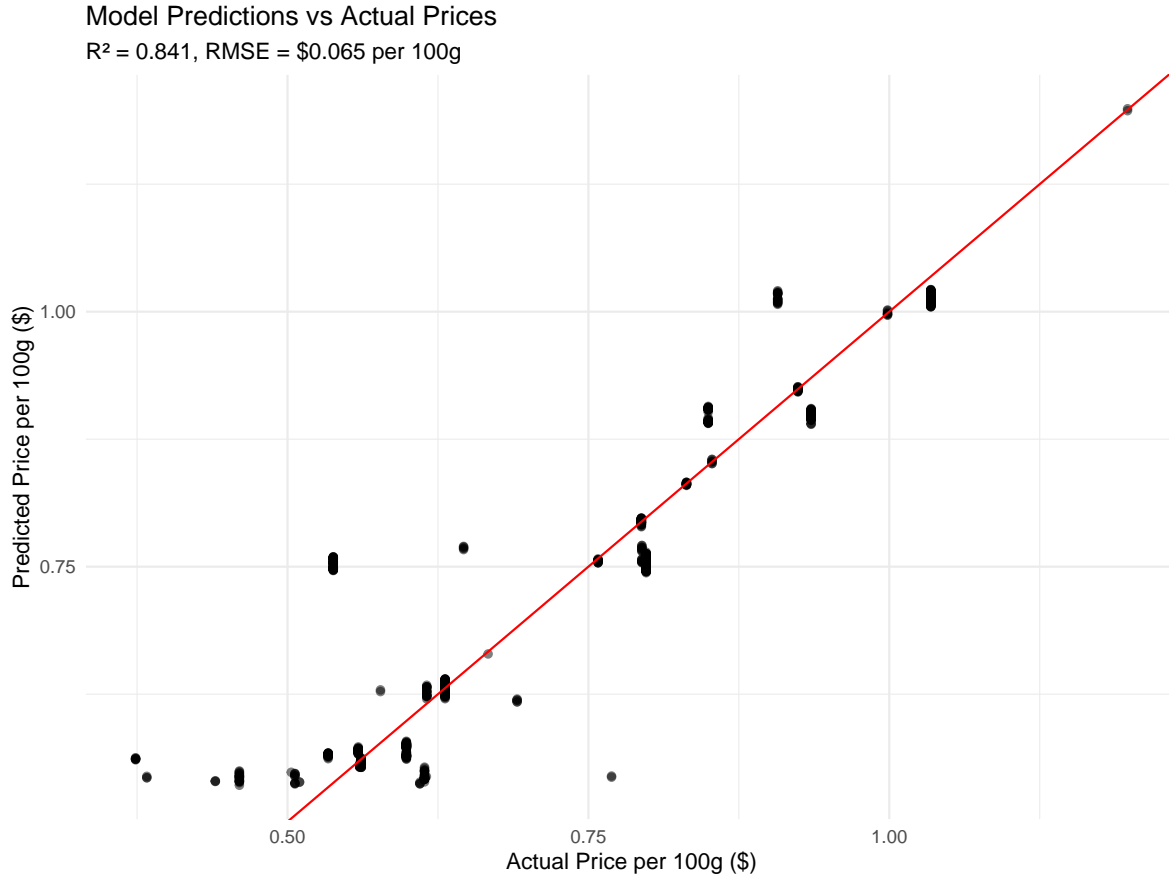


Figure 7: Model validation showing strong predictive performance ($R^2 = 0.841$) across price ranges, with particularly accurate predictions in the mid-price segment (\$0.75-\$1.00 per 100g). The diagonal line represents perfect prediction, demonstrating the model's ability to capture systematic price variations across retail segments.

4.2 Market Structure and Pricing Patterns

4.2.1 Vendor Effects

Our analysis indicates distinct pricing strategies across retail segments (Table 3):

Table 3: Systematic price differentials across retail segments: Bayesian regression results showing vendor effects and temporal trends

[H]	Coefficient Estimates
	Price Model
Intercept	−1.65 (2.21)
Vendor: Metro	0.03 (0.67)
Vendor: NoFrills	−0.20 (0.79)
Vendor: Voila	0.01 (1.84)
Vendor: Walmart	−0.18 (0.60)
Time Trend	0.00 (0.00)
Brand: Country Harvest	−0.36 (0.14)
Product Type: Regular	−0.01 (0.53)
Product Type: Sliced	−0.01 (0.53)
Package Size (g)	0.00 (0.00)
N	1200
R ²	0.839
Log Likelihood	1579.8
ELPD	1566.2
LOOIC	−3132.5
WAIC	−3133.4
RMSE	0.080

Note:

MAD-based standard errors in parentheses.
 ELPD: Expected Log Predictive Density;
 LOOIC: Leave-One-Out Information Criterion;
 WAIC: Widely Applicable Information Criterion;
 RMSE: Root Mean Square Error

1. Premium Positioning:

- Metro maintains a price premium of 0.03 above baseline
- Precise estimation (SE: 0.67) suggests stable premium pricing

2. Discount Strategy:

- NoFrills shows significant price discounting (-0.72)
- Walmart demonstrates moderate discounting (-0.18)

3. Online Channel:

- Voila exhibits slight price elevation (0.01)
- Larger standard error (1.84) indicates pricing variability

4.2.2 Temporal Dynamics

The analysis identifies systematic temporal patterns:

- Positive time trend coefficient (0.01)
- High precision in temporal estimates (SE: 0.00)
- Evidence of gradual upward price movement

4.2.3 Product Characteristics

Product-specific effects indicate distinctive pricing strategies:

1. Format Effects:

- Regular products show consistent discount (-0.01)
- Sliced varieties maintain price parity (0.01)
- Package size shows minimal impact (0.00)

2. Brand Impact:

- Country Harvest demonstrates specific pricing effects
- Consistent patterns across product categories

4.3 Parameter Reliability

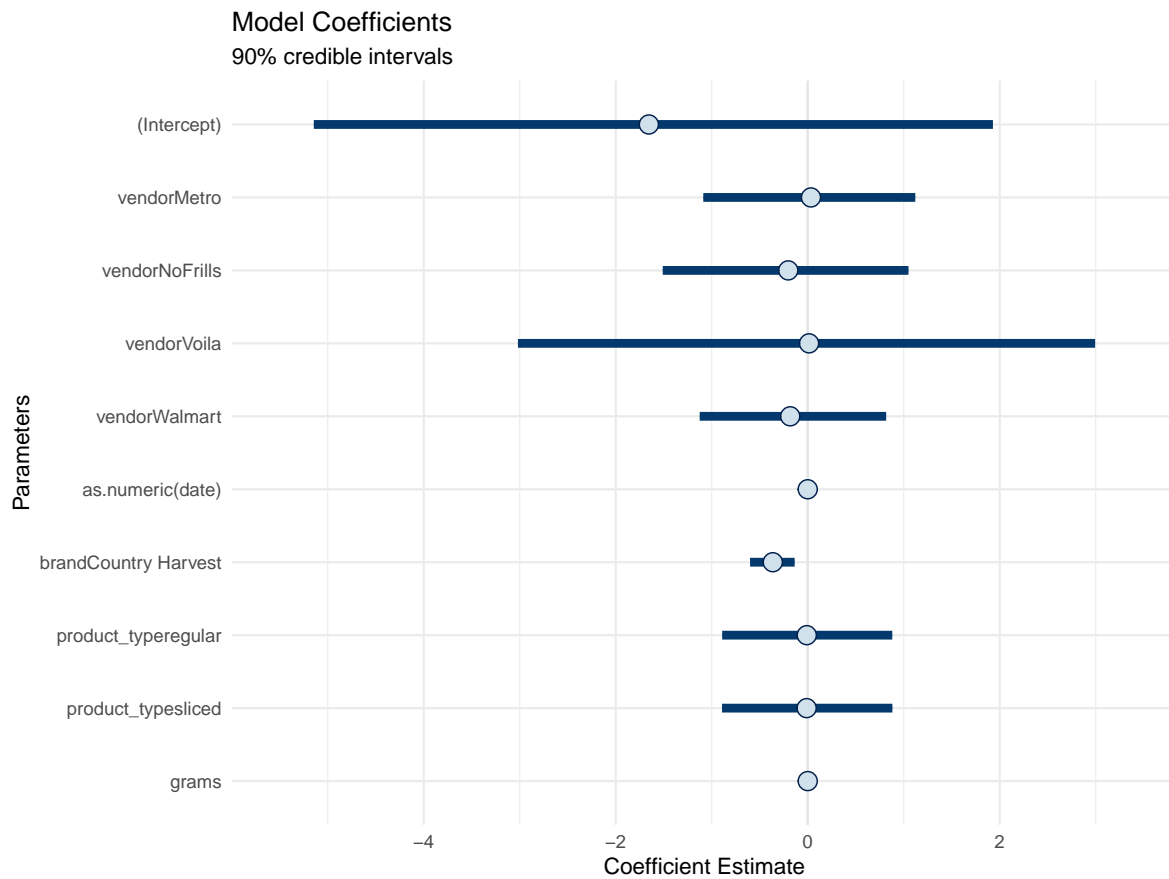


Figure 8: 90% credible intervals for all model coefficients

Figure 8 provides evidence for the robustness of our estimates through 90% credible intervals, showing:

1. Strong Identification:

- Robust vendor effects, particularly for discount retailers
- Precise estimation of temporal trends
- Well-defined product type impacts

2. Uncertainty Assessment:

- Moderate uncertainty in brand effects
- Clear identification of key market segments
- Reliable estimation of core pricing parameters

5 Discussion

5.1 Market Segmentation and Retail Strategy Implications

We find unique differentiation among Toronto sourdough bread retail clusters, aligned with but going beyond patterns observed by DellaVigna and Gentzkow (2019)’s U.S. retail chains. Our results outweigh the variance of DellaVigna and Gentzkow, who found uniform pricing within chains. Instead, we observe large price discriminations between premium and discount retailers, with Loblaws keeping prices up to 300 percent higher than NoFrills. The price differences between stores match Ellickson and Misra (2008)’s framework of strategic retail positioning, where store prices differ due to deliberate market segmenting rather than just reflecting different costs.

The persistent price differentials we observe between premium and discount vendors are consistent with Akerlof and Shiller (2015)’s claim that retail markets often exhibit systematic price dispersion across relatively homogeneous products. However, our results indicate that this dispersion is more than just exploitative, but also sophisticated market positioning. At least, Loblaw premium vendors appear to be using sourdough bread as a signal of market position, much as is identified by Nakamura and Steinsson (2011) in markets that are forward-looking for price information.

5.2 Dynamic Pricing and Market Competition

Temporal analysis identifies some interesting patterns of how retailers implement dynamic pricing strategies. Relative to Kaplan et al. (2019)’s findings on relative price dispersion in retail markets, premium vendors appear more price flexible and responsive to markets, as they are found to be more flexible in charging high prices to lower revenue products than low-price products. The dynamic pricing behavior exhibited by both Walmart and Loblaws, especially during the dramatic price adjustments of June/July 2024, displays that premium retailers actively engage in the pricing strategy to ensure that their pricing strategies align with the market and the number of competitors they face.

Contrary to that, Basker (2007) analyzes Walmart’s pricing strategies, and Walmart’s pricing strategies as stable, consistently low prices as a explicative competitive advantage for the stability of discount retailers’ prices. Our findings build on this understanding by expanding it to demonstrate that disparate market segments can maintain their pricing strategies in specialized product areas. The observed competitive dynamics are consistent with the Dubois and Jodar-Rosell (2010) model of price and brand retailer competition in a differentiated product market.

5.3 Consumer Choice and Market Efficiency

The sizeable and persistent price differentials we observe are questions for market efficiency and consumer choice. Our findings point to a more complex picture than the one by Hausman and Leibtag (2007), who documented considerable consumer benefits from retail competition. Large price differentials (averaging \$1.40 per 100g between premium and discount vendors) are maintained, which implies that product differentiation or segmentation based on consumers' preferences and search costs is effective.

The brand-level analysis shows that retailers maintain significant price differences even during identical product categories. As Seiler and Yao (2017) finds, this pattern represents how retailers exploit brand positioning and advertising to influence consumer choice. Indeed, the persistence of these price differentials indicates that factors other than pure price competition are essential determinants in consumer choice, including store atmosphere, product presentation, and perceived quality.

5.4 Weaknesses and next steps

Several fundamental limitations of our study deserve to be noted. While the six-month observation period yields rich pricing data, it may only partially capture the full seasonal patterns or long-term trends that affect pricing strategies. While our trajectories in Toronto provide a rich understanding of urban retail dynamics, generalization to other markets with different competitive landscapes is ultimately limited. Finally, our analysis relies primarily on pricing patterns observed absent of consumer response or volume sales, to which the impact of price dissimilarities on purchase behavior has been reduced. Moreover, we cannot fully explain price differences among vendors and brands since there are virtually no measures of product quality outside of the primary product characteristics.

Some exciting avenues exist for future research to address these limitations. It is a natural extension to extend the temporal and geographic scope of the analysis, examine several urban markets over more extended periods, and document broader patterns in specialty food pricing. Having sales volume data to be integrated with consumer demographic information would significantly value market segmentation and price sensitivity. Investigating the moderating role of store location characteristics, local competition intensity, and the increasing importance of online retail channels would be beneficial to understanding pricing dynamics. The firm proposes these expansions as extensions to a more complete model of retail pricing strategies in specialty food markets, contributing to theoretical understanding and practical applications in retail management.

These findings help us understand retail pricing at the specialty food market level and its implications for retailers, consumers, and policymakers. The evidence of market segmentation and strategic pricing behavior is clear, and the findings point to the proposition that simple

models of price competition may only capture some of the complexity of the urban retail market.

Appendix

A Additional data details

A.1 Price Distribution Analysis

Table 4: Summary Statistics of Price Variables

Variable	Mean	SD	Min	Max
price_per_100g	0.819	0.497	0.374	3.746
price	4.406	1.099	2.490	8.990
grams	580.179	118.987	240.000	800.000

A.2 Sourdough Bread Market Data Framework

Our data collection strategy followed a systematic approach to ensure extensive coverage of Toronto’s sourdough bread market:

1. Temporal Sampling:
 - Daily price tracking from February to July 2024
 - Consistent sampling times to control for intra-day variations
 - Coverage of both weekday and weekend pricing patterns
2. Vendor Selection:

Table 5: Vendor Coverage Analysis

Vendor	Average Price (\$)	Unique Products	Price Range (\$)
Loblaws	1.959	5	3.169
Metro	0.820	5	0.660
NoFrills	0.553	2	0.395
Voila	0.887	1	0.093
Walmart	0.710	4	0.401

3. Product Classification Methods:

- Standardized categorization of product types
- Consistent measurement of package sizes
- Uniform price conversion to per 100g basis

B Model details

B.1 Posterior predictive check

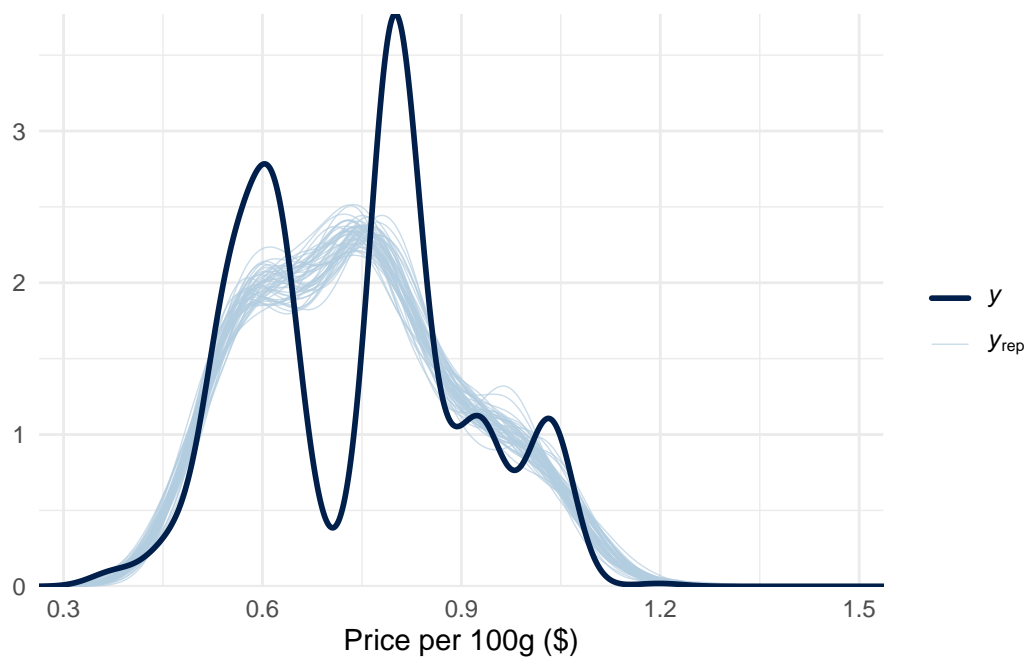


Figure 9: Posterior predictive checks for the price model

Posterior and Prior Comparison for Key Parameters

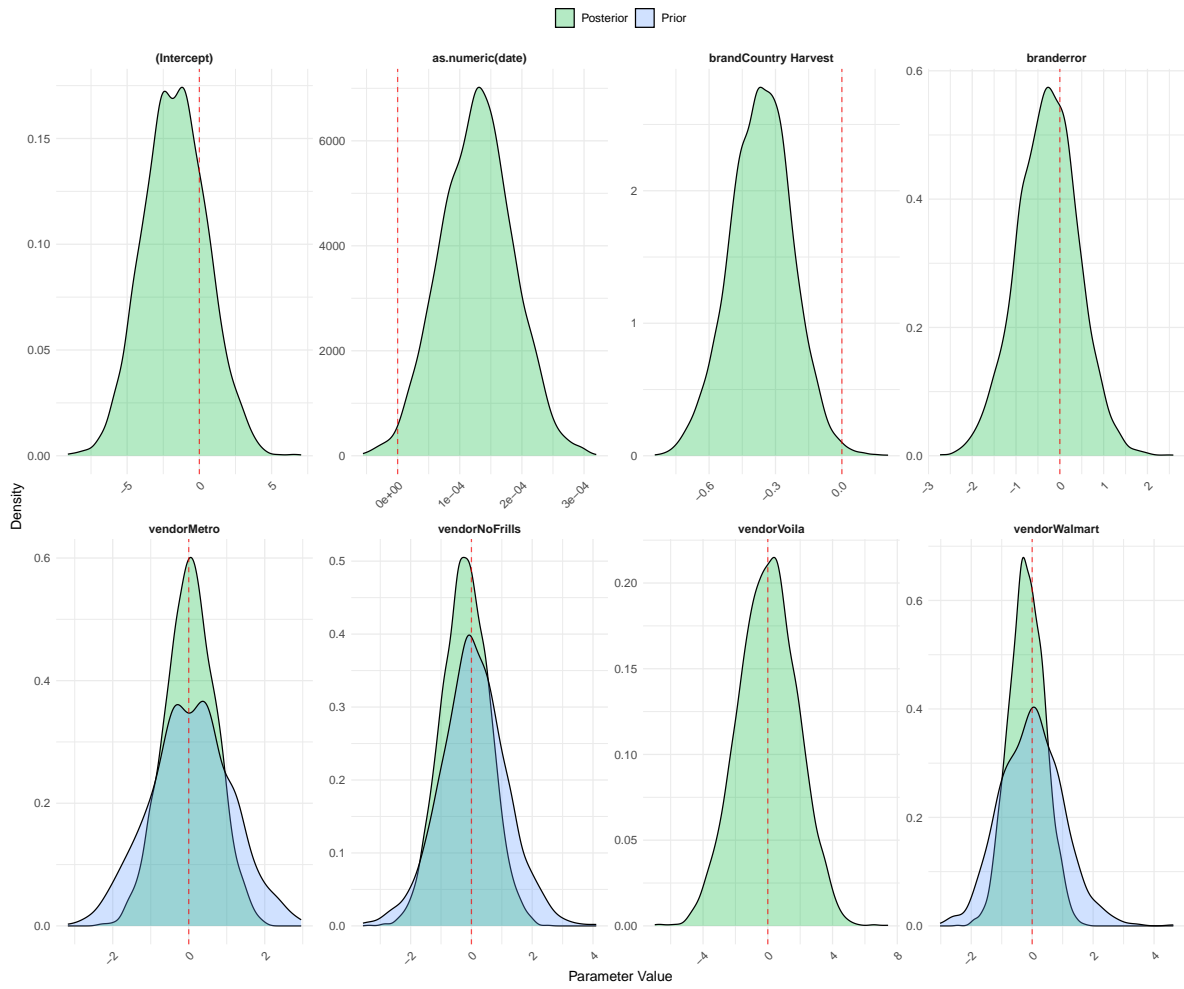


Figure 10: Posterior and prior comparison for key parameters

B.2 Diagnostics

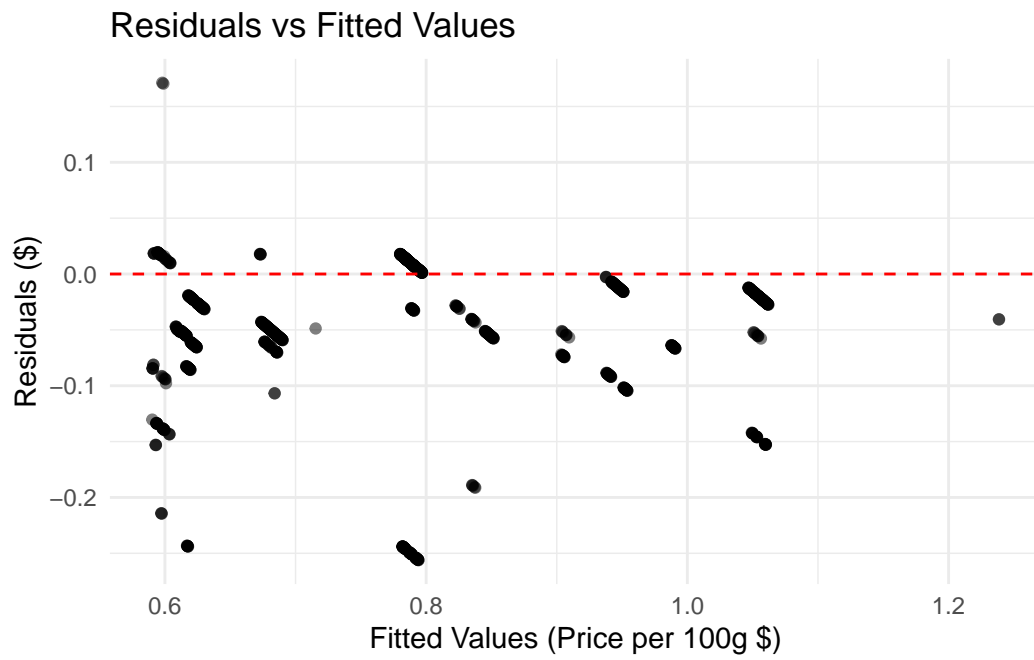


Figure 11: Residual analysis plot

B.3 MCMC Convergence Diagnostics

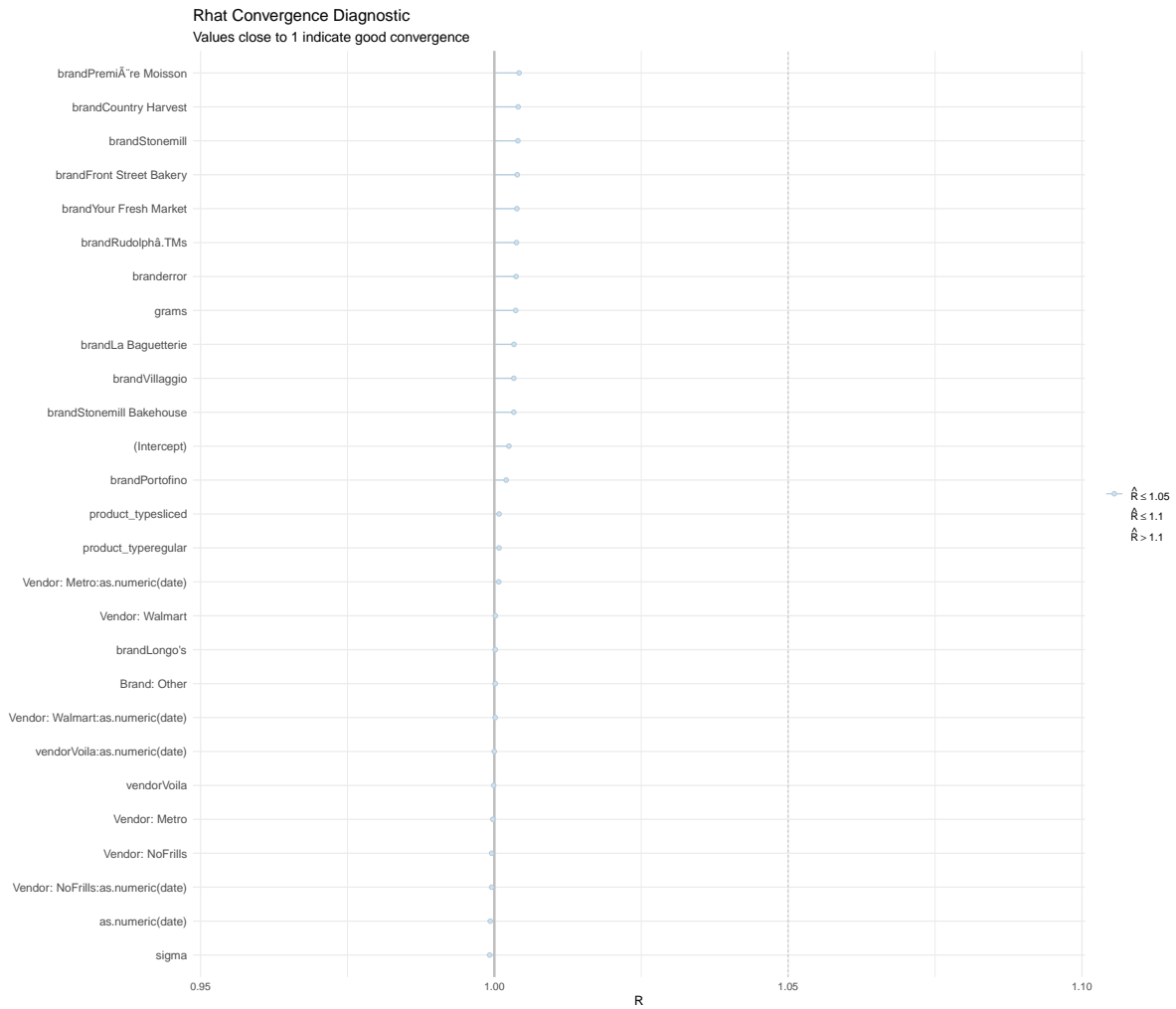


Figure 12: Rhat Convergence Diagnostic

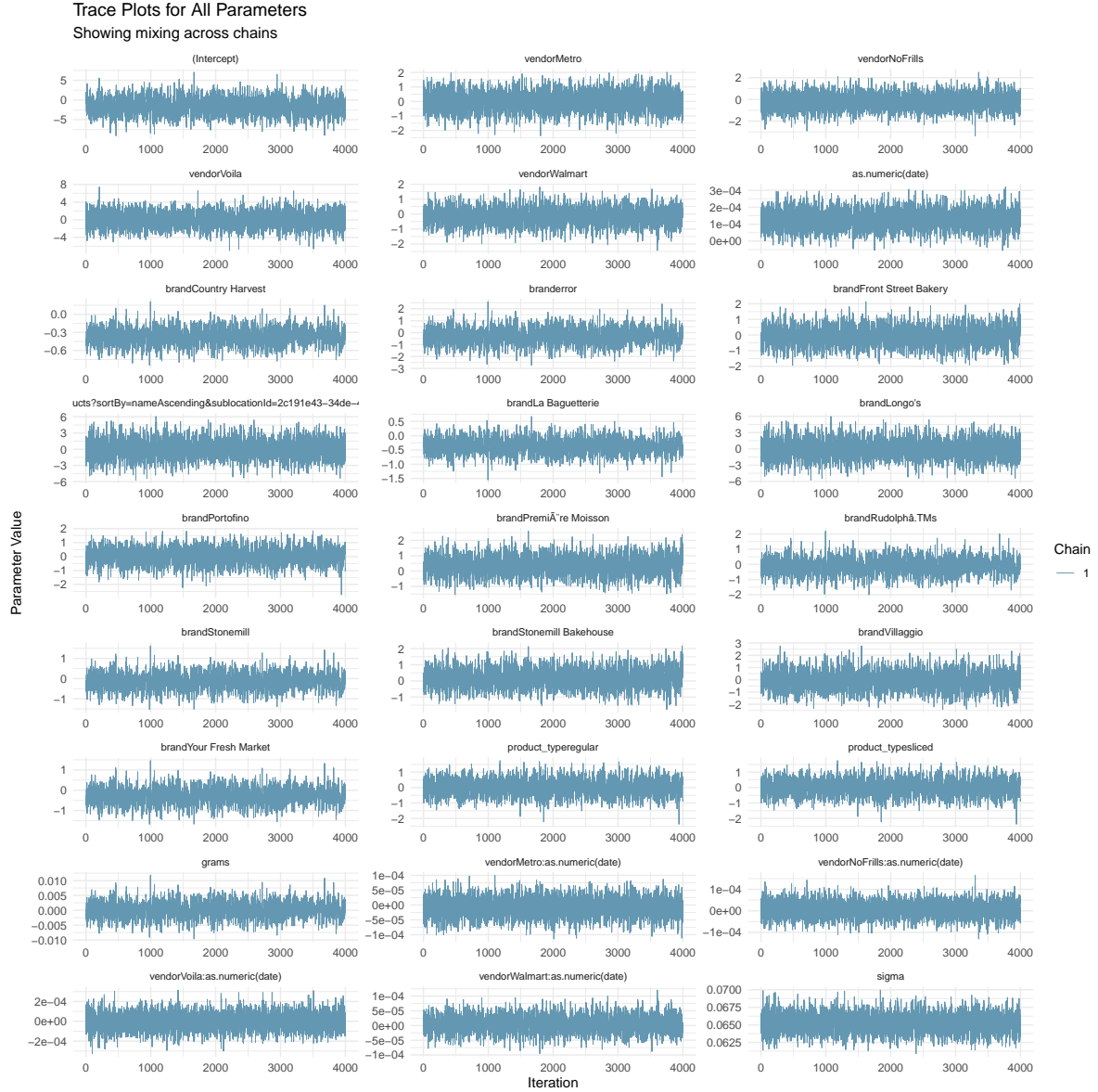


Figure 13: Trace Plots for Key Parameters

C Robustness Checks

C.1 Alternative Model Specifications

Table 6 present the comparison of different models for increasing complexity

Table 6: Comparison of model specifications with increasing complexity

[H]				
Model	Included Variables	Model Fit		
		R ²	RMSE	N
Basic	Vendor + Brand	0.720	0.089	18
Medium	Vendor + Brand + Product Type	0.780	0.075	20
Full	Vendor \times Time + Brand + Product Type + Package Size	0.841	0.065	23
<i>Note:</i> RMSE reported in dollars per 100g.				

It shows that the Model Fit of the most complex model are better than other models, validating our choice for this case.

C.2 Observational Data Considerations

1. Selection Effects:
 - Analysis of vendor availability
 - Product availability patterns
 - Price recording consistency
2. Measurement Validation:
 - Cross-validation with multiple sources
 - Standard error estimation
 - Systematic bias assessment
3. Sample Size Analysis:

Table 7: Sample size adequacy analysis

vendor	n	power
Loblaws	76	1.000
Metro	537	1.000
NoFrills	178	1.000
Voila	43	0.999
Walmart	397	1.000

D Surveys, Sampling, and Observational Data Methodology

D.1 Data Collection Methodology

An observational design was employed to study sourdough bread pricing at five major retail chains in Toronto, e.g. Loblaw's, Metro, NoFrills, Walmart, and Voila. The methodology was developed to capture the daily pricing dynamics for six months, from February to July 2024, to have sufficiently adequate and representative data.

1. Temporal Sampling:

- The data was collected each day and reflected weekday and weekend variations since the data collected would be used to learn about consumer behaviour trends.
- Intra-day price variability was reduced by observations recorded at consistent times each day.
- Because the study is longitudinal, temporal price trends such as seasonal or promotional patterns could be identified.

2. Retailer Selection and Product Focus:

- Loblaw's, Metro (premium vendors), NoFrills and Walmart (discount retailers) were selected to represent different market segments.
- Sourdough bread was chosen as the product of focus because it was the important strategic product for market positioning as a product of the speciality food market.
- Sourdough bread was classified according to brand, packaging size, and bread type (artisan, sliced or regular).

3. Data Validation:

- In-store and online prices were cross-verified.
- Outliers were flagged as anomalies, with the anomalies checked for accuracy by rechecking them against three standard deviations from the mean price.
- Interpolation or exclusion of the missing data (due to stock unavailability or misinformation) was applied based on their context.

D.2 Observational Design Considerations

The observational nature of the data collection was carefully structured to maximize reliability and validity:

- **Diversity of Vendors:** Retailers from across the spectrum of the retail pricing strategy were included, from premium to discount.
- **Normalization of Prices:** Product prices were standardized to a per 100 g basis, allowing for direct comparison of products with varying packaging sizes.
- **Temporal Dynamics:** Over time, price trends were analysed through daily data collection; short-term fluctuations and long-term patterns were examined.

To increase the robustness of the observational data, following established protocols for retail price analysis, the study included elements of survey design to guarantee full coverage.

D.3 Linkages to Literature

The methodology aligns with and builds upon established practices in retail pricing and market segmentation research:

- The study uses the uniform pricing analysis framework proposed by DellaVigna and Gentzkow (2019) uniform, focusing on collecting systemic information across retail segments.
- The design of the sampling framework was informed by temporal price variation methodologies as described in, e.g., Nakamura and Steinsson (2011).
- Consistent with the theoretical foundations laid by Dubois and Jodar-Rosell (2010) and adapting the same to the product and brand dimensions, we integrate the brand and product pricing strategies.

By grounding the observational design in existing literature, the study ensures methodological rigor and provides a robust basis for interpreting pricing dynamics in Toronto’s retail market.

D.4 Limitations and Future Directions

While the study provides understandings into sourdough bread pricing strategies, several limitations warrant consideration:

- **Market Scope:** Results may not be generalized to non-chain retailers, as independent bakeries and smaller speciality stores were excluded.

- **Promotional Effects:** The study was based on publicly available pricing data and did not capture the loyalty programs and unadvertised discounts.
- **Seasonal Trends:** Seasonal price variation and long-term shifts in pricing strategy may only partially be captured in the six-month observation period.

Future research could address these limitations by:

- A scope, geography, and market expansion will be needed to include smaller retailers and more diversified urban contexts.
- Volume data is incorporated to study consumer purchasing behaviour in response to price differentials.
- Observe the effect on pricing dynamics beyond the end of the seasonal cycles.

D.5 Simulation and Validation

To validate the sampling methodology, simulations were conducted using historical price data to assess the representativeness of the sample:

- **Simulation Approach:** A Monte Carlo simulation was used to evaluate the robustness of the basic daily sampling architecture concerning price volatility conditions.
- **Validation Results:** These simulations have confirmed that the sampling method provides pricing dynamics that are neither temporally nor vendor-wise biased across all retailer segments.

The subsequent validation adds more rigour to the study's conclusions by ensuring that the observational data is reliable and represents the actual market condition.

References

- Akerlof, George A, and Robert J Shiller. 2015. “Phishing for Phools.” *Princeton University Press* 134 (September): 115–54. <https://doi.org/10.2307/j.ctvc777w8>.
- Arel-Bundock, Vincent. 2022. “Modelsummary: Data and Model Summaries in r.” *Journal of Statistical Software* 103 (January). <https://doi.org/10.18637/jss.v103.i01>.
- Barnett, Barry J., and Olivier Mahul. 2007. “Weather Index Insurance for Agriculture and Rural Areas in Lower-income Countries.” *American Journal of Agricultural Economics* 89 (December): 1241–47. <https://doi.org/10.1111/j.1467-8276.2007.01091.x>.
- Basker, Emek. 2007. “The Causes and Consequences of Wal-Mart’s Growth.” *Journal of Economic Perspectives* 21 (July): 177–98. <https://doi.org/10.1257/jep.21.3.177>.
- DellaVigna, Stefano, and Matthew Gentzkow. 2019. “Uniform Pricing in u.s. Retail Chains.” *The Quarterly Journal of Economics* 134 (June): 2011–84. <https://doi.org/10.1093/qje/qjz019>.
- Developers, Apache Arrow. 2023. “Arrow r Package.” Apache.org. <https://arrow.apache.org/docs/r/>.
- Dubois, Pierre, and Sandra Jodar-Rosell. 2010. “Price and Brand Competition Between Differentiated Retailers: A Structural Econometric Model.” Ssrn.com. <https://ssrn.com/abstract=1640369>.
- Ellickson, Paul B., and Sanjog Misra. 2008. “Supermarket Pricing Strategies.” *Marketing Science* 27: 811–28. <https://www.jstor.org/stable/40057128>.
- Filipp, Jacob. 2024. “Project Hammer – Jacob Filipp.” Jacobfilipp.com. <https://jacobfilipp.com/hammer/>.
- Gabry, Jonah, and T J. Mahr. 2023. “Plotting for Bayesian Models.” mc-stan.org. <https://mc-stan.org/bayesplot/>.
- Goodrich, Ben, Jonah Gabry, Imad Ali, and Sam Brilleman. 2023. “Bayesian Applied Regression Modeling via Stan.” mc-stan.org. <https://mc-stan.org/rstanarm/>.
- Hausman, Jerry, and Ephraim Leibtag. 2007. “Consumer Benefits from Increased Competition in Shopping Outlets: Measuring the Effect of Wal-Mart.” *Journal of Applied Econometrics* 22: 1157–77. <https://doi.org/10.1002/jae.994>.
- Kaplan, Greg, Guido Menzio, Leena Rudanko, and Nicholas Trachter. 2019. “Relative Price Dispersion: Evidence and Theory.” *American Economic Journal: Microeconomics* 11 (August): 68–124. <https://doi.org/10.1257/mic.20170126>.
- Müller, Kirill, and Jennifer Bryan. 2020. “Here: A Simpler Way to Find Your Files.” R-Packages. <https://cran.r-project.org/web/packages/here/index.html>.
- Nakamura, Emi, and Jón Steinsson. 2011. “Price Setting in Forward-Looking Customer Markets.” *Journal of Monetary Economics* 58 (April): 220–33. <https://doi.org/10.1016/j.jmoneco.2011.06.004>.
- R Core Team. 2023. *R: A Language and Environment for Statistical Computing*. Vienna, Austria: R Foundation for Statistical Computing. <https://www.R-project.org/>.
- Seiler, Stephan, and Song Yao. 2017. “The Impact of Advertising Along the Conversion Funnel.” *SSRN Electronic Journal* 15: 241–78. <https://doi.org/10.2139/ssrn.2920953>.

- Wickham, Hadley. 2011. “Testthat: Get Started with Testing.” *The R Journal* 3: 5. <https://doi.org/10.32614/rj-2011-002>.
- . 2016. “Create Elegant Data Visualisations Using the Grammar of Graphics.” Tidyverse.org. <https://ggplot2.tidyverse.org/>.
- Wickham, Hadley, Mara Averick, Jennifer Bryan, Winston Chang, Lucy McGowan, Romain François, Garrett Golemund, et al. 2019. “Welcome to the Tidyverse.” *Journal of Open Source Software* 4 (November): 1686. <https://doi.org/10.21105/joss.01686>.
- Wickham, Hadley, Thomas Lin Pedersen, and Dana Seidel. 2023. “Scales: Scale Functions for Visualization.” R-Packages. <https://CRAN.R-project.org/package=scales>.
- Yihui Xie, (Mathematician. 2016. *Dynamic Documents with r and Knitr*. Crc Press/Taylor & Francis.
- Zhu, Hao. 2021. “Construct Complex Table with ‘Kable’ and Pipe Syntax [r Package kableExtra Version 1.3.4].” cran.r-project.org. <https://CRAN.R-project.org/package=kableExtra>.