

Statistical Methods for Discrete Response, Time Series, and Panel Data (W271): Lab 4

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Description of the Lab

In this lab, you are asked to answer the question “Do changes in traffic laws affect traffic fatalities?” To do so, you will conduct the tasks specified below using the data set *driving.Rdata*, which includes 25 years of data that cover changes in various state drunk driving, seat belt, and speed limit laws.

```
load("~/git/main-2019-summer/labs/lab4/driving.RData")
head(data,5)
```

```
##   year state sl55 sl65 sl70 sl75 slnone seatbelt minage zerotol gdl bac10
## 1 1980     1    1    0    0    0      0      0     18      0    0     1
## 2 1981     1    1    0    0    0      0      0     18      0    0     1
## 3 1982     1    1    0    0    0      0      0     18      0    0     1
## 4 1983     1    1    0    0    0      0      0     18      0    0     1
## 5 1984     1    1    0    0    0      0      0     18      0    0     1
##   bac08 perse totfat nghtfat wkndfat totfatpvm nghtfatpvm wkndfatpvm
## 1     0     0   940    422    236      3.20      1.437      0.803
## 2     0     0   933    434    248      3.35      1.558      0.890
## 3     0     0   839    376    224      2.81      1.259      0.750
## 4     0     0   930    397    223      3.00      1.281      0.719
## 5     0     0   932    421    237      2.83      1.278      0.720
##   statepop totfatrte nghtfatrte wkndfatrte vehicmiles unem perc14_24
## 1 3893888   24.14    10.84      6.06   29.37500  8.8    18.9
## 2 3918520   24.07    11.08      6.33   27.85200 10.7    18.7
## 3 3925218   21.37     9.58      5.71   29.85765 14.4    18.4
## 4 3934109   23.64    10.09      5.67   31.00000 13.7    18.0
## 5 3951834   23.58    10.65      6.00   32.93286 11.1    17.6
##   sl70plus sbprim sbsecon d80 d81 d82 d83 d84 d85 d86 d87 d88 d89 d90 d91
## 1      0      0      0    1    0    0    0    0    0    0    0    0    0    0    0
## 2      0      0      0    0    1    0    0    0    0    0    0    0    0    0    0
## 3      0      0      0    0    0    1    0    0    0    0    0    0    0    0    0
## 4      0      0      0    0    0    0    1    0    0    0    0    0    0    0    0
## 5      0      0      0    0    0    0    0    1    0    0    0    0    0    0    0
##   d92 d93 d94 d95 d96 d97 d98 d99 d00 d01 d02 d03 d04 vehicmilespc
## 1  0  0  0  0  0  0  0  0  0  0  0  0  0    7543.874
## 2  0  0  0  0  0  0  0  0  0  0  0  0  0    7107.785
## 3  0  0  0  0  0  0  0  0  0  0  0  0  0    7606.622
## 4  0  0  0  0  0  0  0  0  0  0  0  0  0    7879.802
## 5  0  0  0  0  0  0  0  0  0  0  0  0  0    8333.562
```

```
library(dplyr)
```

```
##
## Attaching package: 'dplyr'
##
## The following objects are masked from 'package:stats':
##
##   filter, lag
```

```
## The following objects are masked from 'package:base':
##
## intersect, setdiff, setequal, union
```

```
library(plm)
```

```
##
## Attaching package: 'plm'
## The following objects are masked from 'package:dplyr':
##
## between, lag, lead
```

```
str(data)
```

```
## 'data.frame':    1200 obs. of  56 variables:
## $ year          : int  1980 1981 1982 1983 1984 1985 1986 1987 1988 1989 ...
## $ state         : int  1 1 1 1 1 1 1 1 1 1 ...
## $ sl55          : num  1 1 1 1 1 ...
## $ sl65          : num  0 0 0 0 0 ...
## $ sl70          : num  0 0 0 0 0 0 0 0 0 0 ...
## $ sl75          : num  0 0 0 0 0 0 0 0 0 0 ...
## $ slnone        : num  0 0 0 0 0 0 0 0 0 0 ...
## $ seatbelt      : int  0 0 0 0 0 0 0 0 0 0 ...
## $ minage        : num  18 18 18 18 18 20 21 21 21 21 ...
## $ zerotol       : num  0 0 0 0 0 0 0 0 0 0 ...
## $ gdl           : num  0 0 0 0 0 0 0 0 0 0 ...
## $ bac10         : num  1 1 1 1 1 1 1 1 1 1 ...
## $ bac08         : num  0 0 0 0 0 0 0 0 0 0 ...
## $ perse         : num  0 0 0 0 0 0 0 0 0 0 ...
## $ totfat        : int  940 933 839 930 932 882 1080 1111 1024 1029 ...
## $ nghtfat       : int  422 434 376 397 421 358 500 499 423 418 ...
## $ wkndfat       : int  236 248 224 223 237 224 279 300 226 247 ...
## $ totfatpvm     : num  3.2 3.35 2.81 3 2.83 ...
## $ nghtfatpvm    : num  1.44 1.56 1.26 1.28 1.28 ...
## $ wkndfatpvm    : num  0.803 0.89 0.75 0.719 0.72 ...
## $ statepop      : int  3893888 3918520 3925218 3934109 3951834 3972527 3991569 4015261 402388 ...
## $ totfatrte     : num  24.1 24.1 21.4 23.6 23.6 ...
## $ nghtfatrte    : num  10.84 11.08 9.58 10.09 10.65 ...
## $ wkndfatrte    : num  6.06 6.33 5.71 5.67 6 ...
## $ vehicmiles    : num  29.4 27.9 29.9 31 32.9 ...
## $ unem          : num  8.8 10.7 14.4 13.7 11.1 ...
## $ perc14_24     : num  18.9 18.7 18.4 18 17.6 ...
## $ sl70plus      : num  0 0 0 0 0 0 0 0 0 0 ...
## $ sbprim        : int  0 0 0 0 0 0 0 0 0 0 ...
## $ sbsecon       : int  0 0 0 0 0 0 0 0 0 0 ...
## $ d80           : int  1 0 0 0 0 0 0 0 0 0 ...
## $ d81           : int  0 1 0 0 0 0 0 0 0 0 ...
## $ d82           : int  0 0 1 0 0 0 0 0 0 0 ...
## $ d83           : int  0 0 0 1 0 0 0 0 0 0 ...
```

```
## $ d84      : int  0 0 0 0 1 0 0 0 0 0 ...
## $ d85      : int  0 0 0 0 0 1 0 0 0 0 ...
## $ d86      : int  0 0 0 0 0 0 1 0 0 0 ...
## $ d87      : int  0 0 0 0 0 0 0 1 0 0 ...
## $ d88      : int  0 0 0 0 0 0 0 0 1 0 ...
## $ d89      : int  0 0 0 0 0 0 0 0 0 1 ...
## $ d90      : int  0 0 0 0 0 0 0 0 0 0 ...
## $ d91      : int  0 0 0 0 0 0 0 0 0 0 ...
## $ d92      : int  0 0 0 0 0 0 0 0 0 0 ...
## $ d93      : int  0 0 0 0 0 0 0 0 0 0 ...
## $ d94      : int  0 0 0 0 0 0 0 0 0 0 ...
## $ d95      : int  0 0 0 0 0 0 0 0 0 0 ...
## $ d96      : int  0 0 0 0 0 0 0 0 0 0 ...
## $ d97      : int  0 0 0 0 0 0 0 0 0 0 ...
## $ d98      : int  0 0 0 0 0 0 0 0 0 0 ...
## $ d99      : int  0 0 0 0 0 0 0 0 0 0 ...
## $ d00      : int  0 0 0 0 0 0 0 0 0 0 ...
## $ d01      : int  0 0 0 0 0 0 0 0 0 0 ...
## $ d02      : int  0 0 0 0 0 0 0 0 0 0 ...
## $ d03      : int  0 0 0 0 0 0 0 0 0 0 ...
## $ d04      : int  0 0 0 0 0 0 0 0 0 0 ...
## $ vehicmilespc: num  7544 7108 7607 7880 8334 ...
## - attr(*, "datalabel")= chr ""
## - attr(*, "time.stamp")= chr "22 Jan 2013 14:09"
## - attr(*, "formats")= chr  "%8.0g" "%8.0g" "%9.0g" "%9.0g" ...
## - attr(*, "types")= int   252 251 254 254 254 254 251 254 254 ...
## - attr(*, "val.labels")= chr  "" "" "" "" ...
## - attr(*, "var.labels")= chr  "1980 through 2004" "48 continental states, alphabetical" "s"
## - attr(*, "version")= int 12
```

```
summary(data)
```

```
##      year      state      sl55      sl65
## Min.   :1980   Min.   : 1.00   Min.   :0.0000   Min.   :0.0000
## 1st Qu.:1986   1st Qu.:15.75   1st Qu.:0.0000   1st Qu.:0.0000
## Median :1992   Median :27.50   Median :0.0000   Median :0.0000
## Mean   :1992   Mean   :27.15   Mean    :0.3533   Mean    :0.4399
## 3rd Qu.:1998   3rd Qu.:39.25   3rd Qu.:1.0000   3rd Qu.:1.0000
## Max.    :2004   Max.    :51.00   Max.    :1.0000   Max.    :1.0000
##      sl70      sl75      slnone      seatbelt
## Min.   :0.000   Min.   :0.00000   Min.   :0.000000   Min.   :0.000
## 1st Qu.:0.000   1st Qu.:0.00000   1st Qu.:0.000000   1st Qu.:0.000
## Median :0.000   Median :0.00000   Median :0.000000   Median :1.000
## Mean   :0.119   Mean   :0.08024   Mean    :0.007569   Mean    :1.116
## 3rd Qu.:0.000   3rd Qu.:0.00000   3rd Qu.:0.000000   3rd Qu.:2.000
## Max.    :1.000   Max.    :1.00000   Max.    :1.000000   Max.    :2.000
##      minage      zerotol      gdl      bac10
## Min.   :18.0   Min.   :0.0000   Min.   :0.0000   Min.   :0.0000
```

##	1st Qu.:	21.0	1st Qu.:	0.0000	1st Qu.:	0.0000	1st Qu.:	0.0000
##	Median :	21.0	Median :	0.0000	Median :	0.0000	Median :	1.0000
##	Mean :	20.6	Mean :	0.4519	Mean :	0.1741	Mean :	0.6231
##	3rd Qu.:	21.0	3rd Qu.:	1.0000	3rd Qu.:	0.0000	3rd Qu.:	1.0000
##	Max. :	21.0	Max. :	1.0000	Max. :	1.0000	Max. :	1.0000
##	bac08		perse		totfat		nghtfat	
##	Min. :	0.0000	Min. :	0.0000	Min. :	63.0	Min. :	26.0
##	1st Qu.:	0.0000	1st Qu.:	0.0000	1st Qu.:	310.0	1st Qu.:	139.8
##	Median :	0.0000	Median :	1.0000	Median :	676.0	Median :	316.0
##	Mean :	0.2135	Mean :	0.5471	Mean :	900.7	Mean :	427.3
##	3rd Qu.:	0.0000	3rd Qu.:	1.0000	3rd Qu.:	1099.5	3rd Qu.:	518.2
##	Max. :	1.0000	Max. :	1.0000	Max. :	5504.0	Max. :	2918.0
##	wkndfat		totfatpvm		nghtfatpvm		wkndfatpvm	
##	Min. :	10.0	Min. :	0.780	Min. :	0.2700	Min. :	0.1140
##	1st Qu.:	70.0	1st Qu.:	1.577	1st Qu.:	0.6847	1st Qu.:	0.3410
##	Median :	163.0	Median :	2.020	Median :	0.9130	Median :	0.4770
##	Mean :	222.3	Mean :	2.122	Mean :	0.9990	Mean :	0.5255
##	3rd Qu.:	277.0	3rd Qu.:	2.500	3rd Qu.:	1.2110	3rd Qu.:	0.6420
##	Max. :	1499.0	Max. :	5.700	Max. :	3.0030	Max. :	1.6750
##	statepop		totfatrte		nghtfatrte		wkndfatrte	
##	Min. :	453401	Min. :	6.20	Min. :	2.660	Min. :	1.180
##	1st Qu.:	1641938	1st Qu.:	14.38	1st Qu.:	6.338	1st Qu.:	3.240
##	Median :	3700425	Median :	18.43	Median :	8.420	Median :	4.390
##	Mean :	5329896	Mean :	18.92	Mean :	8.796	Mean :	4.606
##	3rd Qu.:	6069563	3rd Qu.:	22.77	3rd Qu.:	10.650	3rd Qu.:	5.680
##	Max. :	35894000	Max. :	53.32	Max. :	29.600	Max. :	14.430
##	vehicmiles		unem		perc14_24		sl70plus	
##	Min. :	3.703	Min. :	2.200	Min. :	11.70	Min. :	0.0000
##	1st Qu.:	14.574	1st Qu.:	4.500	1st Qu.:	13.90	1st Qu.:	0.0000
##	Median :	33.863	Median :	5.600	Median :	14.90	Median :	0.0000
##	Mean :	46.323	Mean :	5.951	Mean :	15.33	Mean :	0.2068
##	3rd Qu.:	58.639	3rd Qu.:	7.000	3rd Qu.:	16.60	3rd Qu.:	0.0000
##	Max. :	329.600	Max. :	18.000	Max. :	20.30	Max. :	1.0000
##	sbprim		sbsecon		d80		d81	
##	Min. :	0.0000	Min. :	0.0000	Min. :	0.00	Min. :	0.00
##	1st Qu.:	0.0000	1st Qu.:	0.0000	1st Qu.:	0.00	1st Qu.:	0.00
##	Median :	0.0000	Median :	0.0000	Median :	0.00	Median :	0.00
##	Mean :	0.1792	Mean :	0.4683	Mean :	0.04	Mean :	0.04
##	3rd Qu.:	0.0000	3rd Qu.:	1.0000	3rd Qu.:	0.00	3rd Qu.:	0.00
##	Max. :	1.0000	Max. :	1.0000	Max. :	1.00	Max. :	1.00
##	d82		d83		d84		d85	
##	Min. :	0.00	Min. :	0.00	Min. :	0.00	Min. :	0.00
##	1st Qu.:	0.00	1st Qu.:	0.00	1st Qu.:	0.00	1st Qu.:	0.00
##	Median :	0.00	Median :	0.00	Median :	0.00	Median :	0.00
##	Mean :	0.04	Mean :	0.04	Mean :	0.04	Mean :	0.04
##	3rd Qu.:	0.00	3rd Qu.:	0.00	3rd Qu.:	0.00	3rd Qu.:	0.00
##	Max. :	1.00	Max. :	1.00	Max. :	1.00	Max. :	1.00
##	d86		d87		d88		d89	

```
## Min. :0.00 Min. :0.00 Min. :0.00 Min. :0.00
## 1st Qu.:0.00 1st Qu.:0.00 1st Qu.:0.00 1st Qu.:0.00
## Median :0.00 Median :0.00 Median :0.00 Median :0.00
## Mean :0.04 Mean :0.04 Mean :0.04 Mean :0.04
## 3rd Qu.:0.00 3rd Qu.:0.00 3rd Qu.:0.00 3rd Qu.:0.00
## Max. :1.00 Max. :1.00 Max. :1.00 Max. :1.00
## d90 d91 d92 d93
## Min. :0.00 Min. :0.00 Min. :0.00 Min. :0.00
## 1st Qu.:0.00 1st Qu.:0.00 1st Qu.:0.00 1st Qu.:0.00
## Median :0.00 Median :0.00 Median :0.00 Median :0.00
## Mean :0.04 Mean :0.04 Mean :0.04 Mean :0.04
## 3rd Qu.:0.00 3rd Qu.:0.00 3rd Qu.:0.00 3rd Qu.:0.00
## Max. :1.00 Max. :1.00 Max. :1.00 Max. :1.00
## d94 d95 d96 d97
## Min. :0.00 Min. :0.00 Min. :0.00 Min. :0.00
## 1st Qu.:0.00 1st Qu.:0.00 1st Qu.:0.00 1st Qu.:0.00
## Median :0.00 Median :0.00 Median :0.00 Median :0.00
## Mean :0.04 Mean :0.04 Mean :0.04 Mean :0.04
## 3rd Qu.:0.00 3rd Qu.:0.00 3rd Qu.:0.00 3rd Qu.:0.00
## Max. :1.00 Max. :1.00 Max. :1.00 Max. :1.00
## d98 d99 d00 d01
## Min. :0.00 Min. :0.00 Min. :0.00 Min. :0.00
## 1st Qu.:0.00 1st Qu.:0.00 1st Qu.:0.00 1st Qu.:0.00
## Median :0.00 Median :0.00 Median :0.00 Median :0.00
## Mean :0.04 Mean :0.04 Mean :0.04 Mean :0.04
## 3rd Qu.:0.00 3rd Qu.:0.00 3rd Qu.:0.00 3rd Qu.:0.00
## Max. :1.00 Max. :1.00 Max. :1.00 Max. :1.00
## d02 d03 d04 vehicmilespc
## Min. :0.00 Min. :0.00 Min. :0.00 Min. : 4372
## 1st Qu.:0.00 1st Qu.:0.00 1st Qu.:0.00 1st Qu.: 7788
## Median :0.00 Median :0.00 Median :0.00 Median : 9013
## Mean :0.04 Mean :0.04 Mean :0.04 Mean : 9129
## 3rd Qu.:0.00 3rd Qu.:0.00 3rd Qu.:0.00 3rd Qu.:10327
## Max. :1.00 Max. :1.00 Max. :1.00 Max. :18390
```

```
#hist(data$year,col='lightblue',breaks=40)
#hist(data$state,col='lightblue',breaks=40)
```

```
#ggplot(gather(subset(data, select=c("year","state"))),
# aes(value)) +
# geom_histogram(bins = 100) +
# facet_wrap(~ key, scales = 'free')
```

```
E <- pdata.frame(data, index=c("state","year"))
```

```
table(E$state)
```

```
##
```

```
## 1 3 4 5 6 7 8 10 11 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28
## 25 25 25 25 25 25 25 25 25 25 25 25 25 25 25 25 25 25 25 25 25 25 25
## 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51
## 25 25 25 25 25 25 25 25 25 25 25 25 25 25 25 25 25 25 25 25 25
```

```
table(E$year)
```

```
##
## 1980 1981 1982 1983 1984 1985 1986 1987 1988 1989 1990 1991 1992 1993 1994
## 48 48 48 48 48 48 48 48 48 48 48 48 48 48 48
## 1995 1996 1997 1998 1999 2000 2001 2002 2003 2004
## 48 48 48 48 48 48 48 48 48 48
```

```
library(ggplot2)
```

```
## Registered S3 methods overwritten by 'ggplot2':
```

```
## method from
## [.quosures rlang
## c.quosures rlang
## print.quosures rlang
```

```
library(tidyr)
```

```
library(lattice)
```

```
# Let's organize the 29 terms
```

```
speed_limit_terms = c("sl55", "sl65", "sl70", "sl75", "slnone", "sl70plus")
```

```
drunk_driving_terms = c("minage", "bac10", "bac08")
```

```
admin_law_terms = c("seatbelt", "perse", "zerotol", "gdl", "sbprim", "sbsecon")
```

```
pop_metric_terms = c("unem", "perc14_24", "statepop")
```

```
vehicle_miles_terms = c("vehicmilespc", "vehicmiles")
```

```
fatality_terms = c("totfat", "nghtfat", "wkndfat", "totfatpvm", "nghtfatpvm",
                    "wkndfatpvm", "totfatrte", "nghtfatrte", "wkndfatrte")
```

```
date_terms = c("d80", "d81", "d82", "d83", "d84", "d85", "d86", "d87", "d88", "d89",
                "d90", "d91", "d92", "d93", "d94", "d95", "d96", "d97", "d98", "d99",
                "d00", "d01", "d02", "d03", "d04")
```

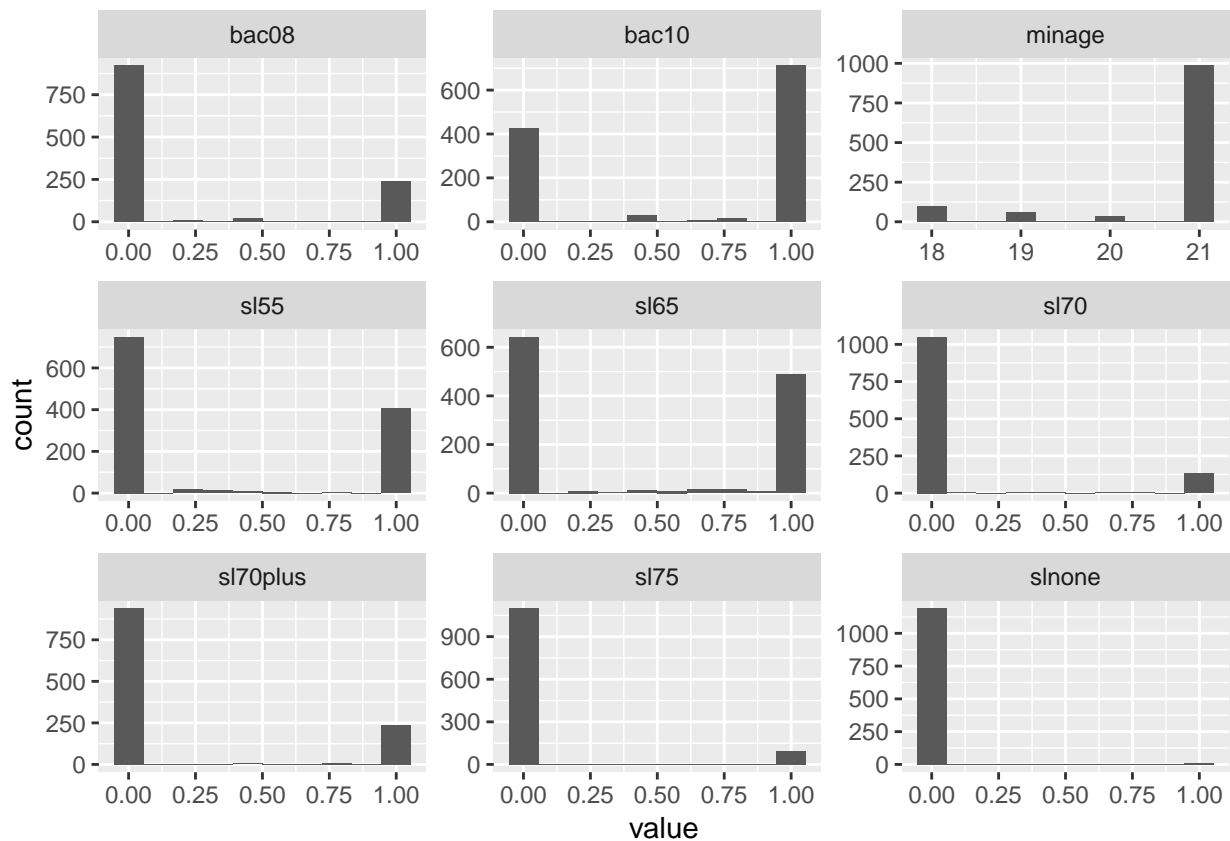
```
all_terms = cbind(speed_limit_terms, drunk_driving_terms, admin_law_terms, vehicle_miles_terms,
                  pop_metric_terms, fatality_terms)
```

```
## Warning in cbind(speed_limit_terms, drunk_driving_terms, admin_law_terms, :
```

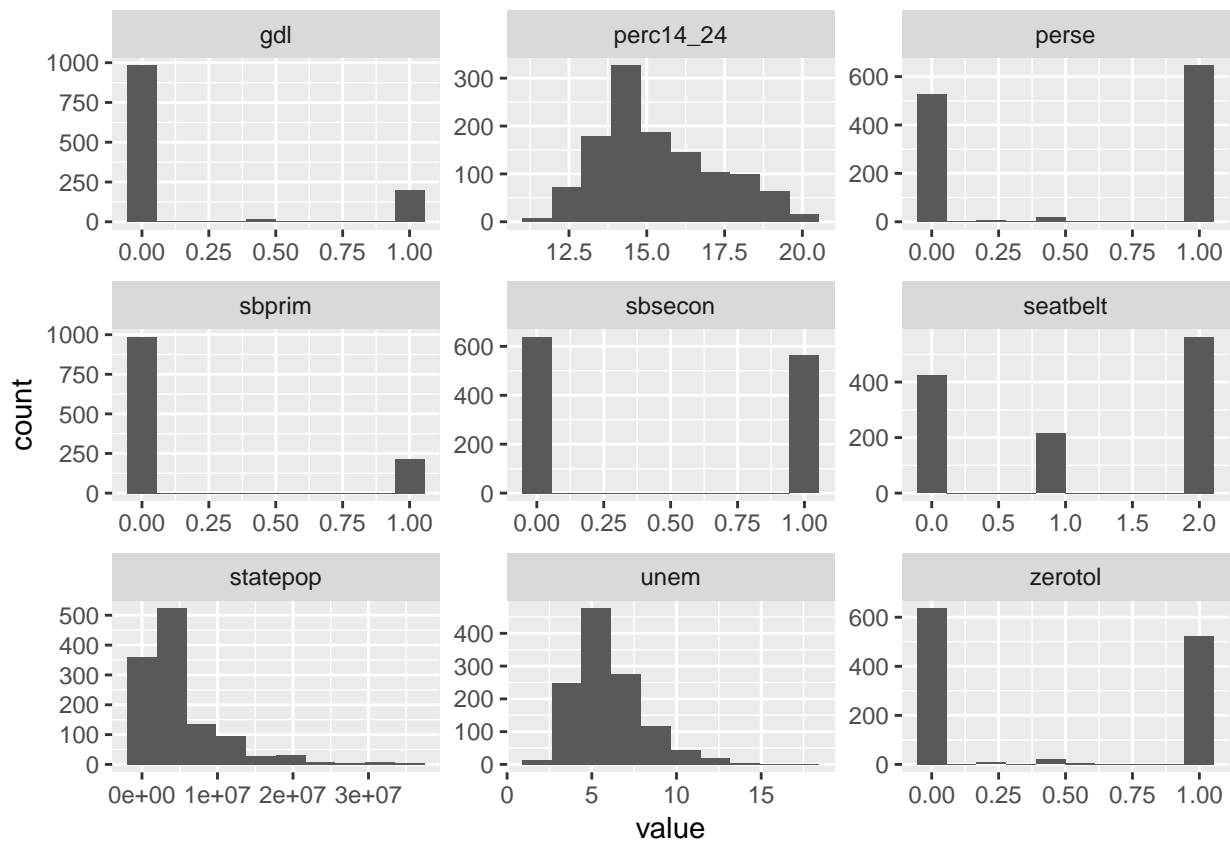
```
## number of rows of result is not a multiple of vector length (arg 1)
```

```
# speed_limit_terms + drunk_driving_terms
```

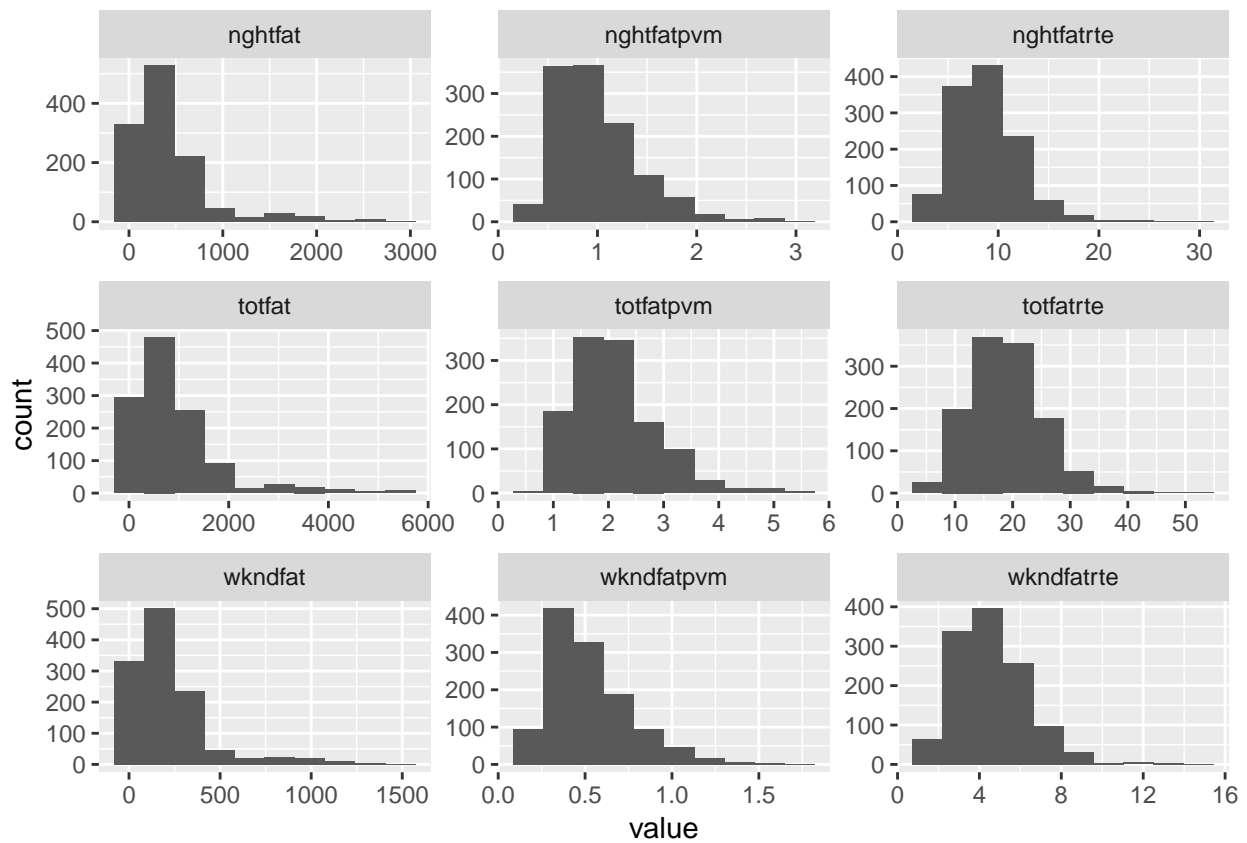
```
ggplot(gather(subset(data, select=c(speed_limit_terms, drunk_driving_terms))),
  aes(value)) +
  geom_histogram(bins = 10) +
  facet_wrap(~ key, scales = 'free', ncol = 3)
```



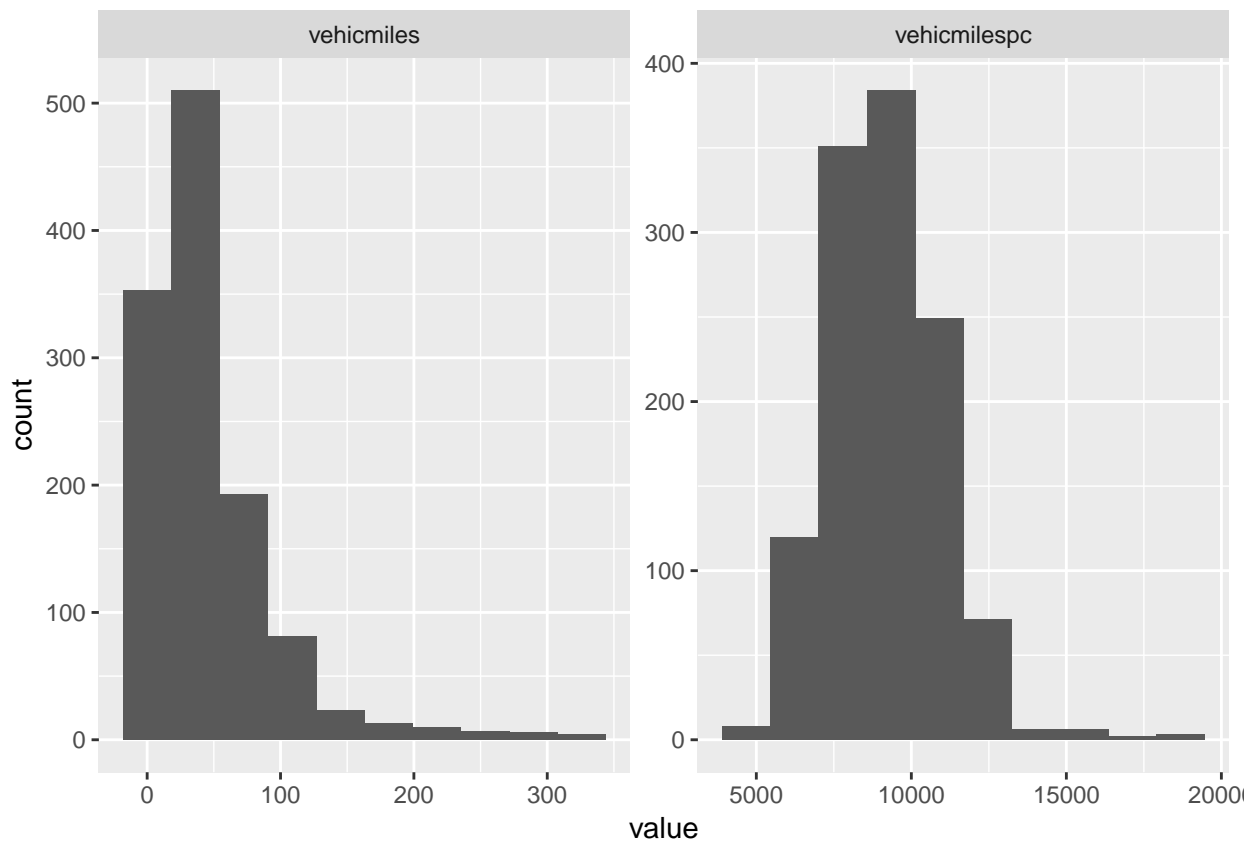
```
# adminLawTerms + popMetricsTerms
ggplot(gather(subset(data, select=c(adminLawTerms,popMetricTerms))),
  aes(value)) +
  geom_histogram(bins = 10) +
  facet_wrap(~ key, scales = 'free',ncol = 3)
```

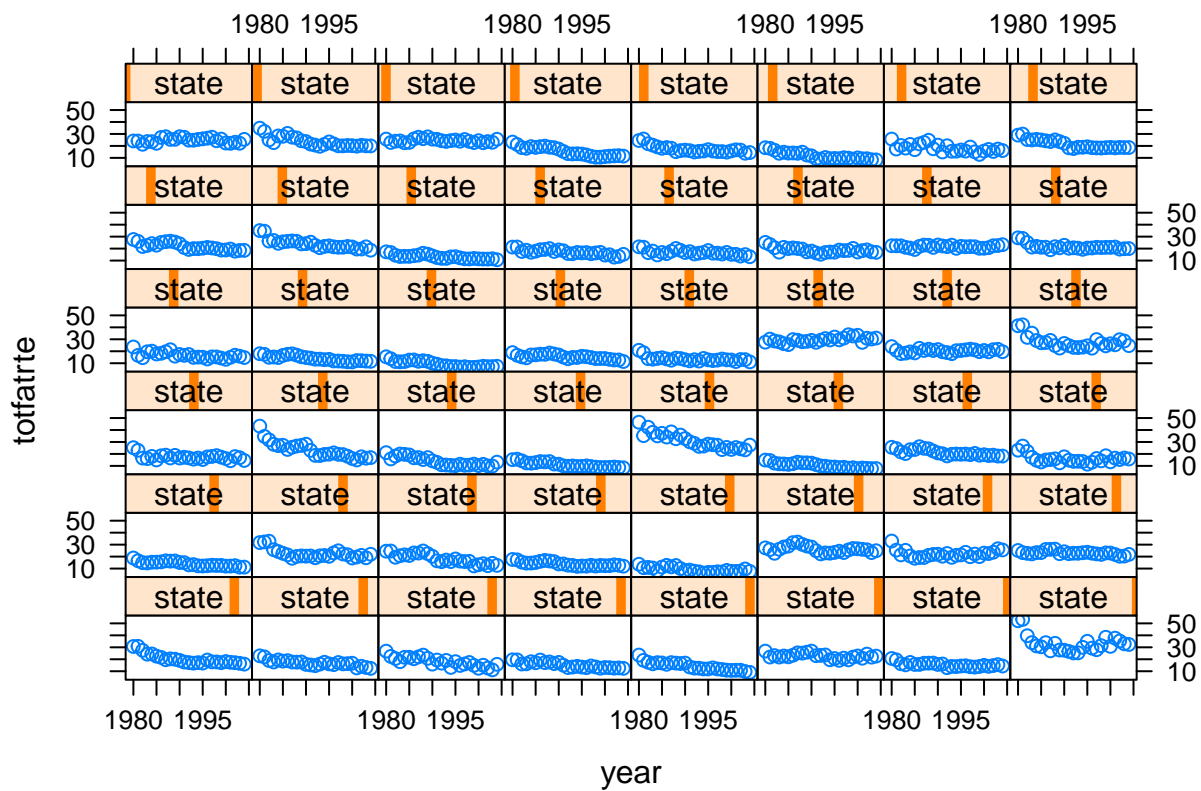
```
# fatality_terms
ggplot(gather(subset(data, select=c(fatality_terms))),
  aes(value)) +
  geom_histogram(bins = 10) +
  facet_wrap(~ key, scales = 'free', ncol = 3)
```



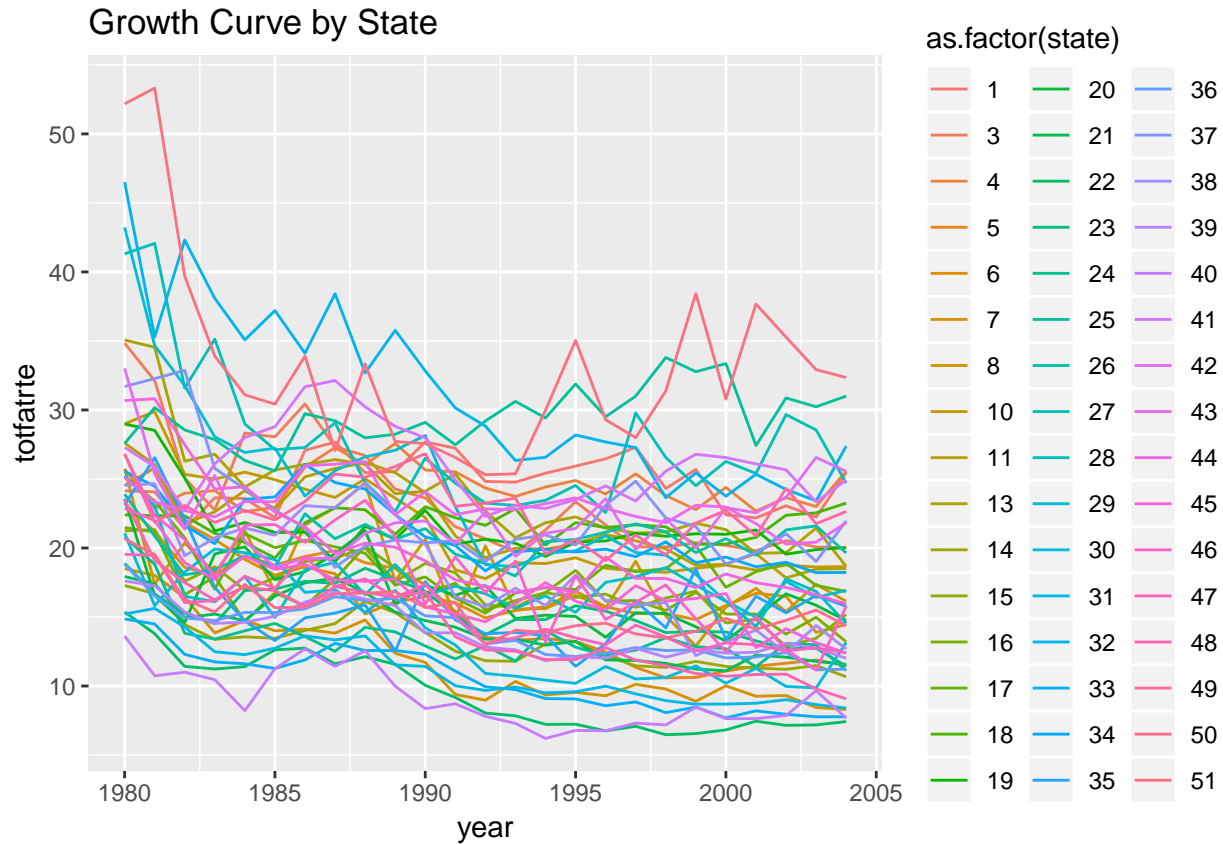
```
# vehicle_miles_terms
ggplot(gather(subset(data, select=c(vehicle_miles_terms))),
  aes(value)) +
  geom_histogram(bins = 10) +
  facet_wrap(~ key, scales = 'free', ncol = 2)
```



```
xyplot(totfatrte ~ year | state, data=data, as.table=T)
```



```
ggplot(data, aes(year, totfatrte, colour = as.factor(state))) +  
  geom_line() + ggtitle("Growth Curve by State")
```



Specifically, this data set contains data for the 48 continental U.S. states from 1980 through 2004. Various driving laws are indicated in the data set, such as the alcohol level at which drivers are considered legally intoxicated. There are also indicators for “per se” laws—where licenses can be revoked without a trial—and seat belt laws. A few economics and demographic variables are also included. The description of the each of the variables in the dataset is come with the dataste.

Exercises:

Question 1

1. Load the data. Provide a description of the basic structure of the dataset, as we have done throughout the semester. Conduct a very thorough EDA, which should include both graphical and tabular techniques, on the dataset, including both the dependent variable *totfatrte* and the potential explanatory variables. You need to write a detailed narrative of your observations of your EDA. *Reminder: giving an “output dump” (i.e. providing a bunch of graphs and tables without description and hoping your audience will interpret them) will receive a zero in this exercise.*

Question 2

2. How is the our dependent variable of interest *totfatrte* defined? What is the average of this variable in each of the years in the time period covered in this dataset? Estimate a linear regression model of *totfatrte* on a set of dummy variables for the years 1981 through 2004. What does this model explain? Describe what you find in this model. Did driving become safer over this period? Please provide a detailed explanation.

totfatrte is defined as $totfatrte = totfat * 100,000 / statepop$

```
data %>%
  group_by(year) %>%
  summarise(mean_totfatrte = mean(totfatrte))

## # A tibble: 25 x 2
##   year mean_totfatrte
##   <int>         <dbl>
## 1  1980          25.5
## 2  1981          23.7
## 3  1982          20.9
## 4  1983          20.2
## 5  1984          20.3
## 6  1985          19.9
## 7  1986          20.8
## 8  1987          20.8
## 9  1988          20.9
## 10 1989          19.8
## # ... with 15 more rows

data1 <- data %>% select(c("totfatrte", date_terms))
lm_fit1 = lm(totfatrte ~ ., data=data1)
summary(lm_fit1)
```

```
##
## Call:
## lm(formula = totfatrte ~ ., data = data1)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -12.9302  -4.3468  -0.7305   3.7488  29.6498
##
## Coefficients: (1 not defined because of singularities)
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 16.72896    0.86712  19.293 < 2e-16 ***
## d80          8.76563    1.22629   7.148 1.54e-12 ***
## d81          6.94125    1.22629   5.660 1.90e-08 ***
## d82          4.21354    1.22629   3.436 0.000611 ***
## d83          3.42396    1.22629   2.792 0.005321 **
## d84          3.53854    1.22629   2.886 0.003979 **
## d85          3.12250    1.22629   2.546 0.011014 *
```

```
## d86          4.07146      1.22629      3.320 0.000927 ***
## d87          4.04583      1.22629      3.299 0.000999 ***
## d88          4.16271      1.22629      3.395 0.000710 ***
## d89          3.04333      1.22629      2.482 0.013213 *
## d90          2.77625      1.22629      2.264 0.023759 *
## d91          1.36583      1.22629      1.114 0.265596
## d92          0.42896      1.22629      0.350 0.726550
## d93          0.39875      1.22629      0.325 0.745112
## d94          0.42625      1.22629      0.348 0.728208
## d95          0.93958      1.22629      0.766 0.443712
## d96          0.64042      1.22629      0.522 0.601603
## d97          0.88167      1.22629      0.719 0.472302
## d98          0.53646      1.22629      0.437 0.661855
## d99          0.52146      1.22629      0.425 0.670745
## d00          0.09667      1.22629      0.079 0.937183
## d01          0.06375      1.22629      0.052 0.958549
## d02          0.30062      1.22629      0.245 0.806383
## d03          0.03458      1.22629      0.028 0.977506
## d04          NA          NA          NA      NA
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 6.008 on 1175 degrees of freedom
## Multiple R-squared:  0.1276, Adjusted R-squared:  0.1098
## F-statistic: 7.164 on 24 and 1175 DF,  p-value: < 2.2e-16
```

```
library(grid)
library(gridExtra)
```

```
##
## Attaching package: 'gridExtra'
```

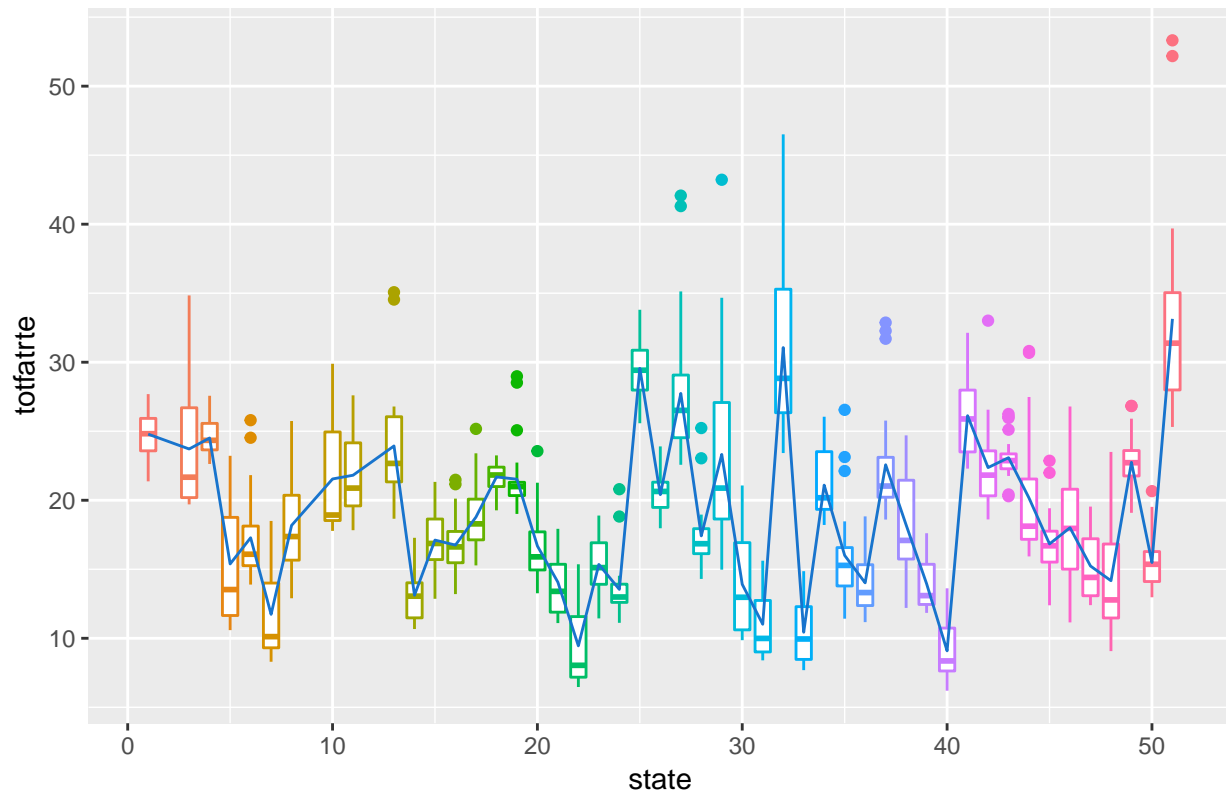
```
## The following object is masked from 'package:dplyr':
##
##      combine
```

```
data1 <- data %>% group_by(state) %>% summarise(totfatrte_mean = mean(totfatrte))
```

```
# Plot boxplot of totfatrte for each state along
# with mean values.
```

```
ggplot(data, aes(y = totfatrte, x = state,
                 group = state,color=as.factor(state))) +
  geom_boxplot() +
  ggtitle("totfatrte : Heterogeneity across states") +
  geom_line(color='dodgerblue3',data = data1, aes(group = 1, x=state, y=totfatrte_mean)) +
  theme(legend.position = "none")
```

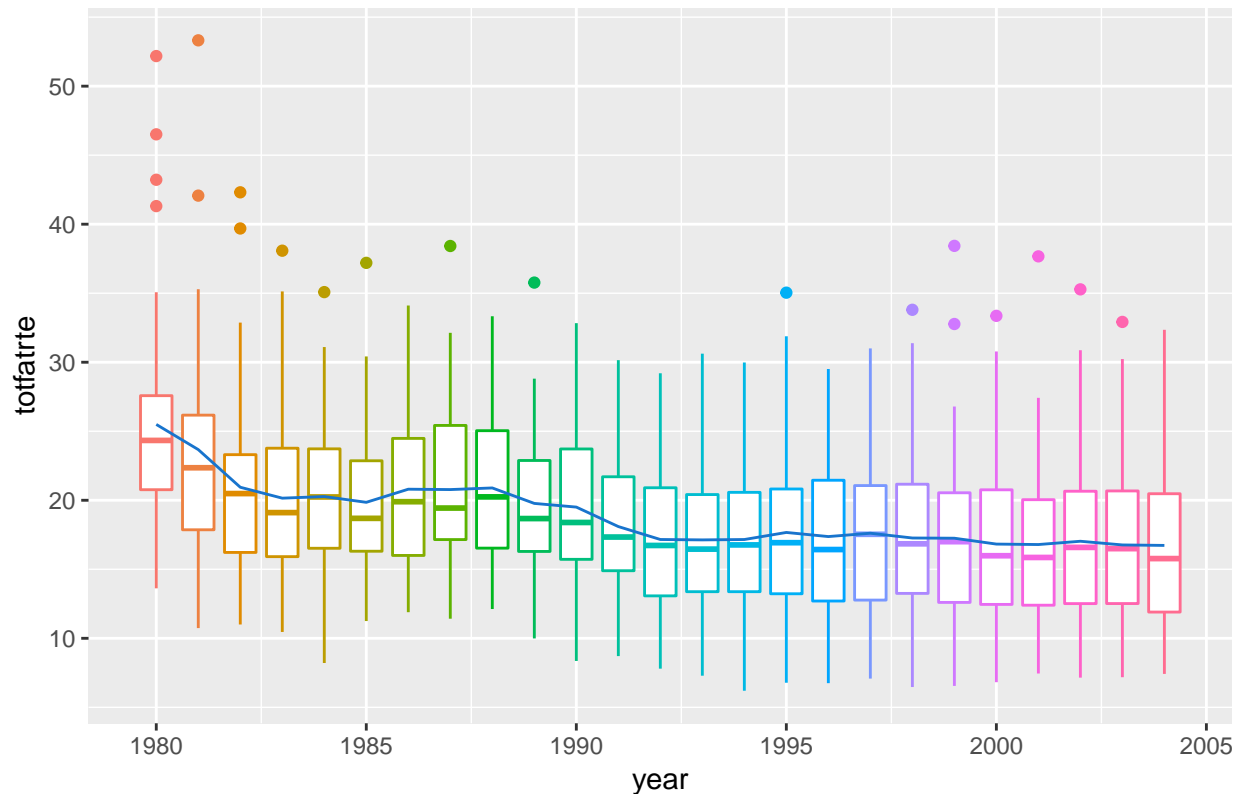
totfatrte : Heterogeneity across states



```
data2 <- data %>% group_by(year) %>% summarise(totfatrte_mean = mean(totfatrte))

# Plot boxplot of totfatrte for each year along
# with mean values.
ggplot(data, aes(y = totfatrte, x = year,
                  group = year,color=as.factor(year))) +
  geom_boxplot() +
  ggtitle("totfatrte : Heterogeneity across years") +
  geom_line(color='dodgerblue3',data = data2, aes(group = 1, x=year, y=totfatrte_mean)) +
  theme(legend.position = "none")
```

totfatrte : Heterogeneity across years



```
#grid.arrange(p1, p2, nrow = 1, ncol = 1)
```

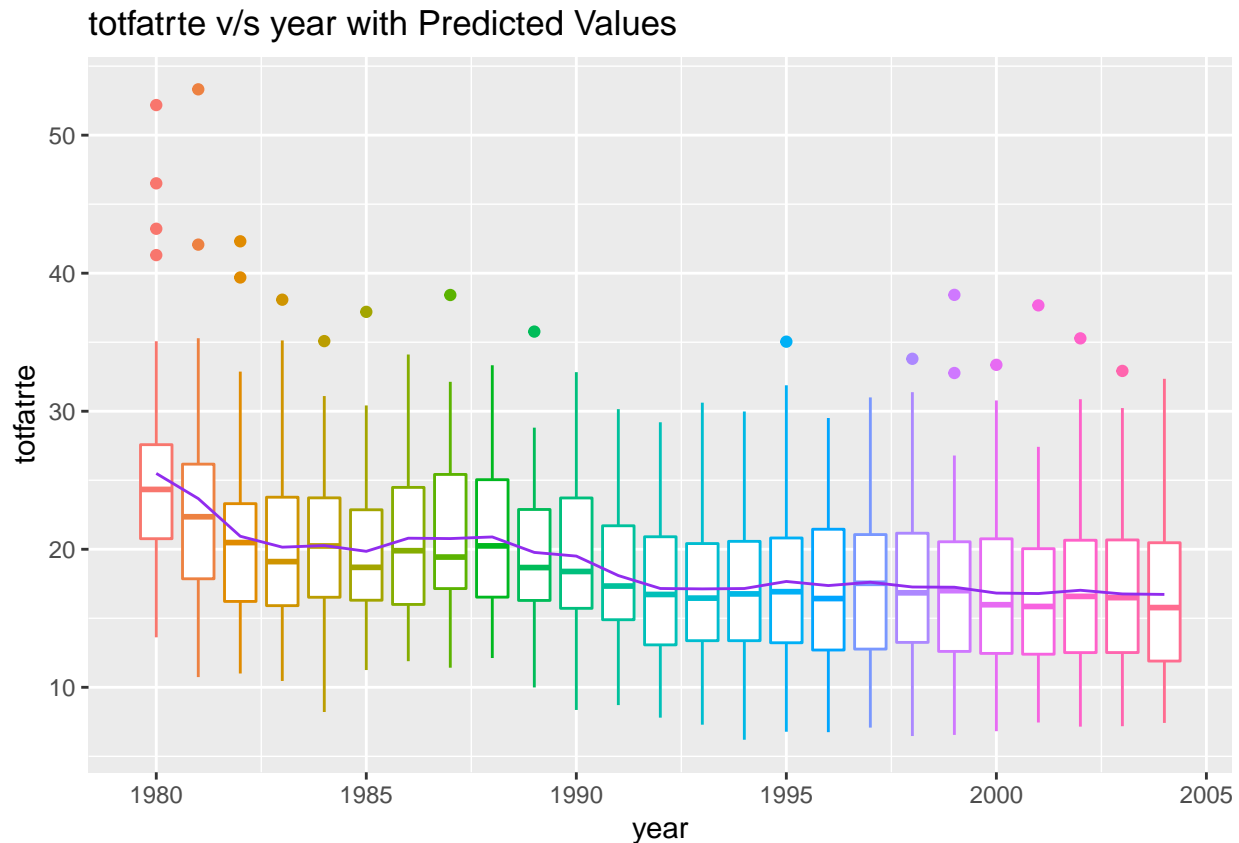
```
# get predicted values
```

```
data$predicted_value=predict(lm_fit1)
```

```
# Plot boxplot of totfatrte for each year along
```

```
# with predicted values.
```

```
ggplot(data, aes(y = totfatrte, x = year,
                  group = year,color=as.factor(year))) +
  geom_boxplot() +
  ggtitle("totfatrte v/s year with Predicted Values") +
  geom_line(color='purple2',data = data, aes(group = 1, x=year, y=predicted_value)) +
  #geom_line(color='dodgerblue3',data = data2, aes(group = 1, x=year, y=totfatrte_mean)) +
  theme(legend.position = "none")
```

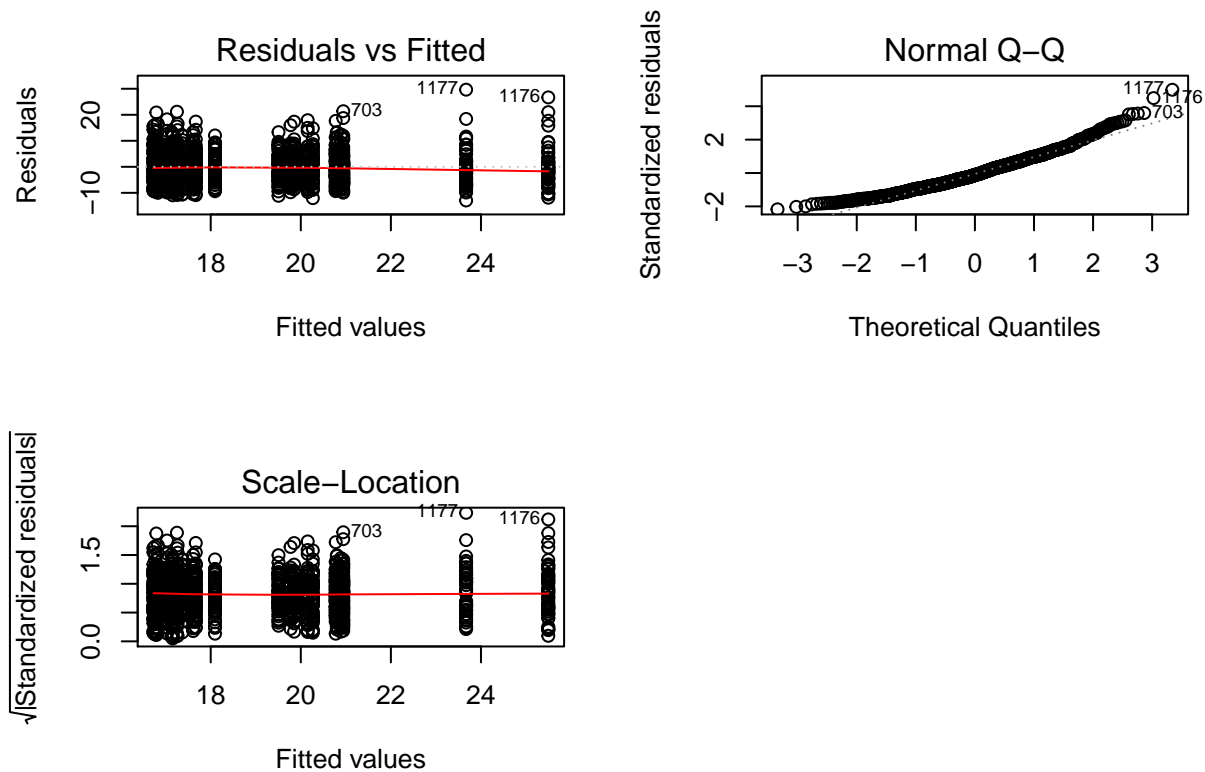



Looking at the significance of the date terms to *totfatrte* in the linear regression model, we observe that the early years 1980 - 1990 have the most significance. The later years after 1990 have the least contribution. From this we can conclude that driving did become safer over the years.

The predicted values from the regression model overlaid on the box plot of the *totfatrte* values over the years confirms the same i.e. *totfatrte* decreased over the years.

```
par(mfrow=c(2,2))
plot(lm_fit1)
```

```
## hat values (leverages) are all = 0.02083333
## and there are no factor predictors; no plot no. 5
```

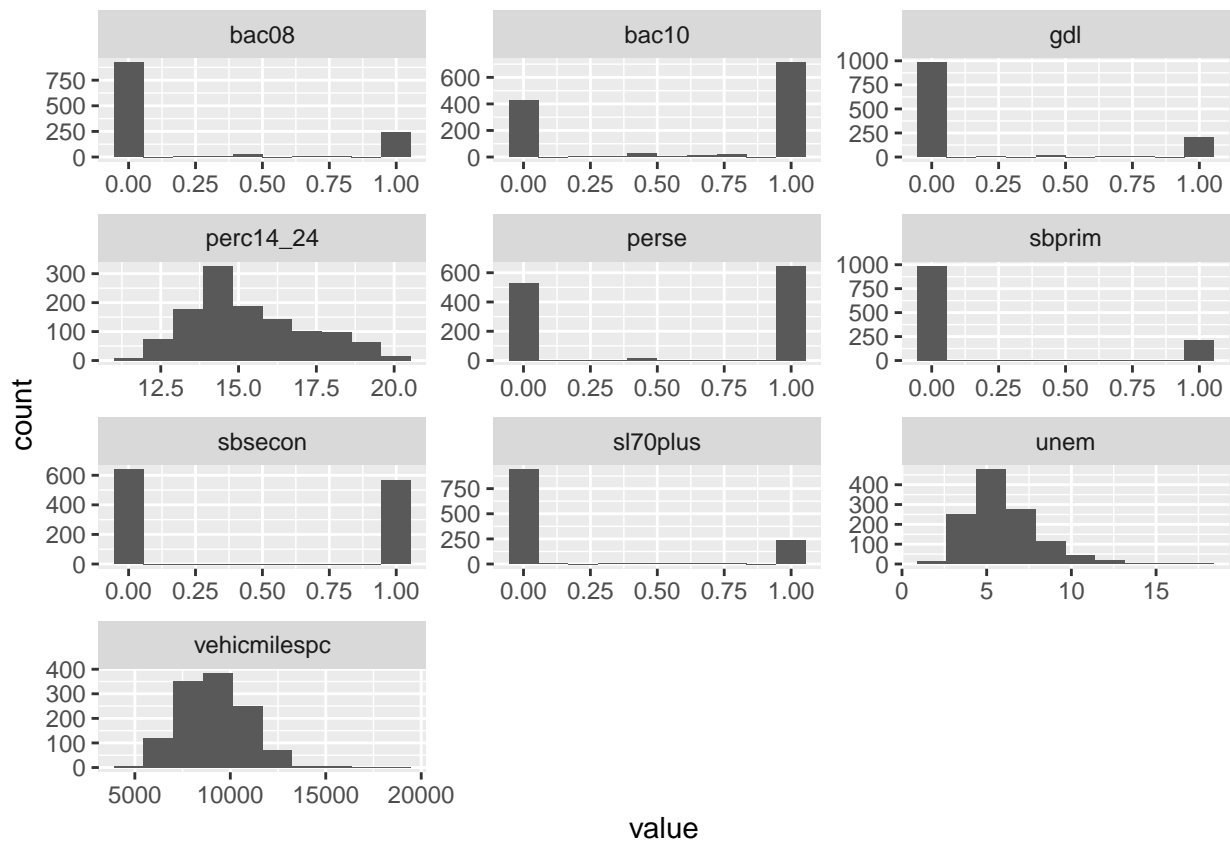


Question 3

- Expand your model in *Exercise 2* by adding variables *bac08*, *bac10*, *perse*, *sbprim*, *sbsecon*, *sl70plus*, *gdl*, *perc14_24*, *unem*, *vehicmilespc*, and perhaps *transformations of some or all of these variables*. Please explain carefully your rationale, which should be based on your EDA, behind any transformation you made. If no transformation is made, explain why transformation is not needed. How are the variables *bac8* and *bac10* defined? Interpret the coefficients on *bac8* and *bac10*. Do *per se laws* have a negative effect on the fatality rate? What about having a primary seat belt law? (Note that if a law was enacted sometime within a year the fraction of the year is recorded in place of the zero-one indicator.)

```
regression_terms = c("bac08", "bac10", "perse", "sbprim", "sbsecon",
                     "sl70plus", "gdl", "perc14_24", "unem", "vehicmilespc")

ggplot(gather(subset(data, select=c(regression_terms))),
       aes(value)) +
  geom_histogram(bins = 10) +
  facet_wrap(~ key, scales = 'free', ncol = 3)
```



```
data %>% select(c(regression_terms)) %>% head()
```

```
##   bac08 bac10 perse sbprim sbsecon sl70plus gdl perc14_24 unem
## 1     0     1     0     0       0         0  0      18.9   8.8
## 2     0     1     0     0       0         0  0      18.7  10.7
## 3     0     1     0     0       0         0  0      18.4  14.4
## 4     0     1     0     0       0         0  0      18.0  13.7
## 5     0     1     0     0       0         0  0      17.6  11.1
## 6     0     1     0     0       0         0  0      17.3   8.9
##   vehicmilespc
## 1      7543.874
## 2      7107.785
## 3      7606.622
## 4      7879.802
## 5      8333.562
## 6      8845.614
```

```
minmax <- function(x){(x-min(x))/(max(x)-min(x))}
```

```
data$vehicmilespclog <- log(data$vehicmilespc)
```

```
data$unemlog <- log(data$unem)
```

```
data$perc14_24log <- log(data$perc14_24)
```

```
data$vehicmilespcscaled <- minmax(data$vehicmilespc)
```

```
data$unemscaled <- minmax(data$unem)
```

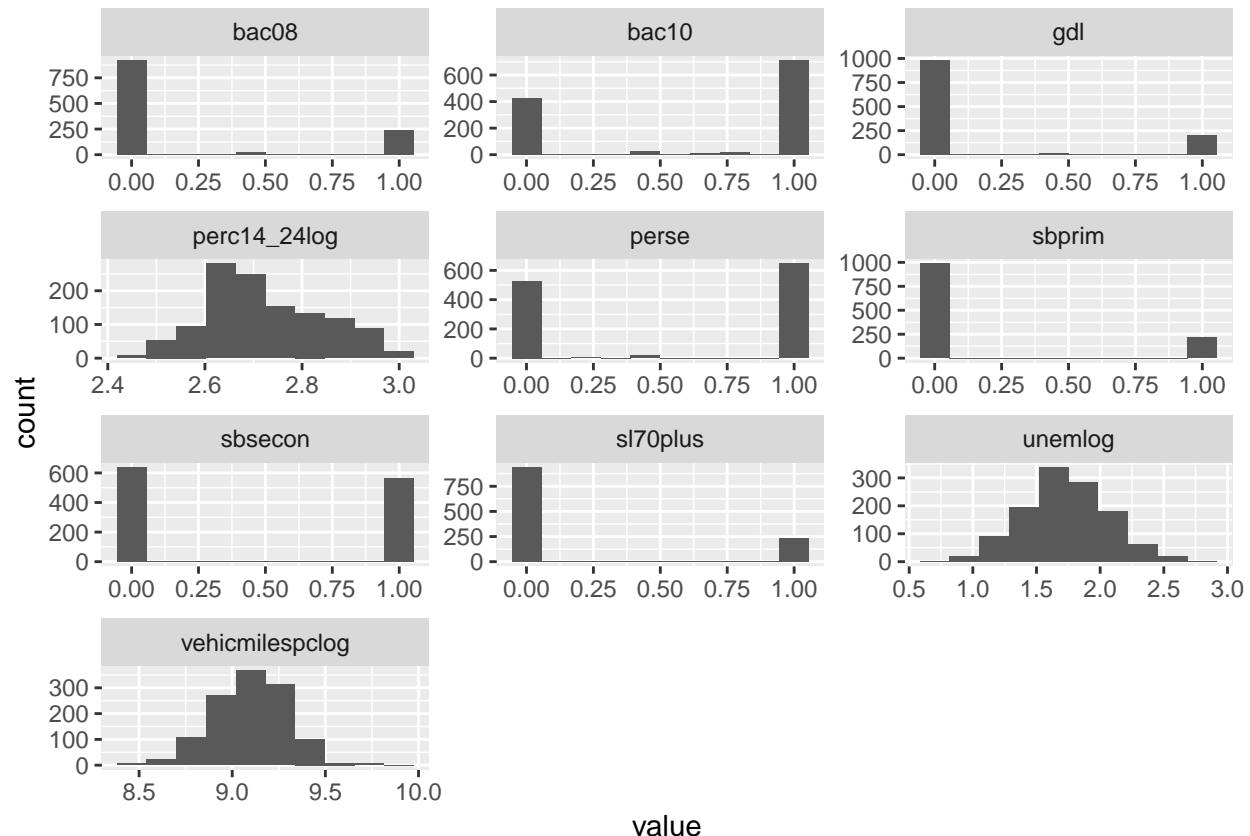
```

data$perc14_24scaled <- minmax(data$perc14_24)

regression_terms = c("bac08", "bac10", "perse", "sbprim", "sbsecon",
                     "sl70plus", "gdl", "perc14_24log", "unemlog", "vehicmileslog")

ggplot(gather(subset(data, select=c(regression_terms))),
       aes(value)) +
  geom_histogram(bins = 10) +
  facet_wrap(~ key, scales = 'free', ncol = 3)

```



```

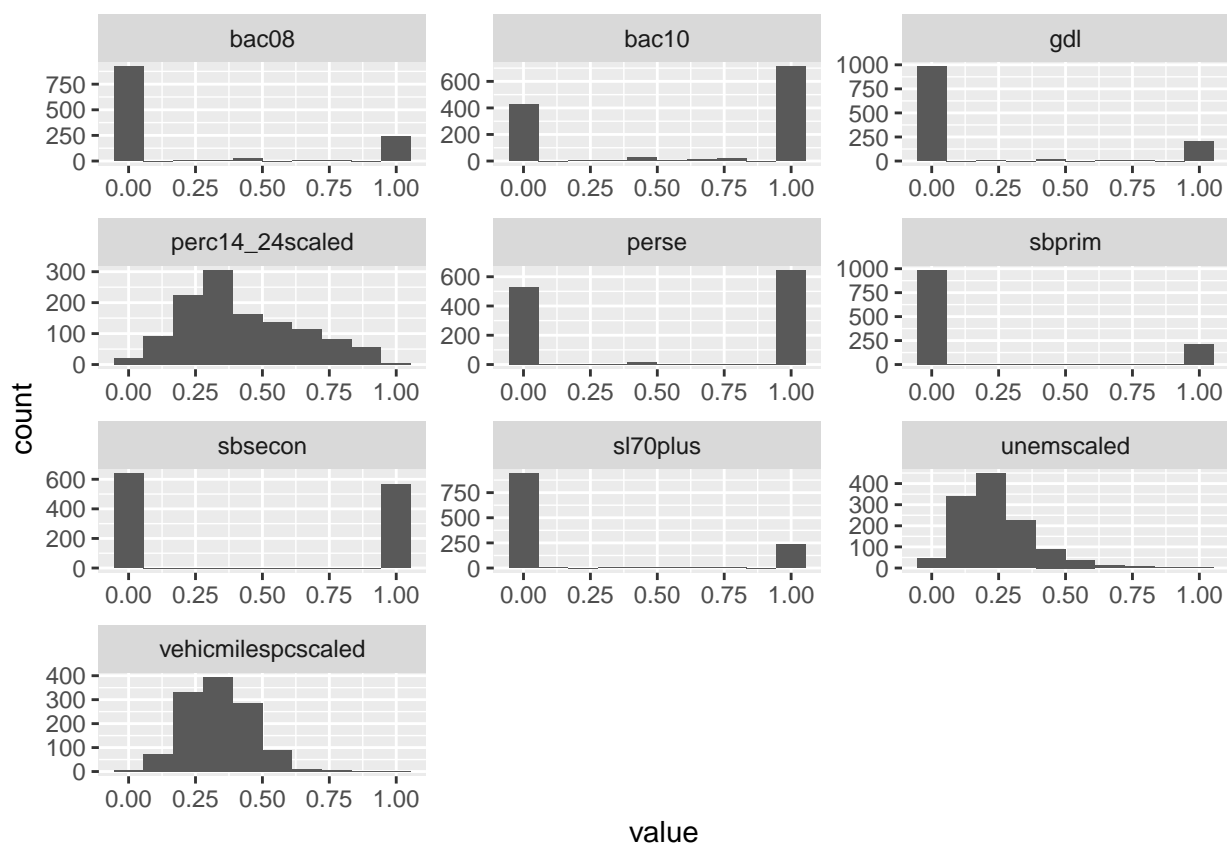
minmax <- function(x){(x-min(x))/(max(x)-min(x))}

data$vehicmilespscscled <- minmax(data$vehicmilespsc)
data$unemscled <- minmax(data$unem)
data$perc14_24scaled <- minmax(data$perc14_24)

regression_terms = c("bac08", "bac10", "perse", "sbprim", "sbsecon",
                     "sl70plus", "gdl", "perc14_24scaled", "unemscled", "vehicmilespscscled")

ggplot(gather(subset(data, select=c(regression_terms))),
       aes(value)) +
  geom_histogram(bins = 10) +
  facet_wrap(~ key, scales = 'free', ncol = 3)

```



```
data3 <- data %>% select(c("totfatrte",c(regression_terms,date_terms)))
lm_fit3 = lm(totfatrte ~ ., data=data3)
summary(lm_fit3)
```

```
##
## Call:
## lm(formula = totfatrte ~ ., data = data3)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -14.9160  -2.7384  -0.2778   2.2859  21.4203
##
## Coefficients: (1 not defined because of singularities)
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   -3.31516    1.21135  -2.737 0.006299 **
## bac08         -2.49848    0.53751  -4.648 3.73e-06 ***
## bac10         -1.41757    0.39633  -3.577 0.000362 ***
## perse         -0.62011    0.29820  -2.079 0.037791 *
## sbprim        -0.07533    0.49078  -0.153 0.878032
## sbsecon        0.06728    0.42930   0.157 0.875492
## sl70plus       3.34791    0.44517   7.521 1.09e-13 ***
## gdl           -0.42691    0.52691  -0.810 0.417978
## perc14_24scaled  1.21768    1.05504   1.154 0.248675
## unemscaled    11.96144    1.23091   9.718 < 2e-16 ***
```

```
## vehicmilespscscald 41.00853      1.33126  30.804 < 2e-16 ***
## d80                  16.71127      1.38697  12.049 < 2e-16 ***
## d81                  14.53579      1.36963  10.613 < 2e-16 ***
## d82                  10.11530      1.36766   7.396 2.67e-13 ***
## d83                   9.31458      1.32894   7.009 4.05e-12 ***
## d84                  10.86088      1.26403   8.592 < 2e-16 ***
## d85                  10.22802      1.22683   8.337 < 2e-16 ***
## d86                  10.85848      1.16023   9.359 < 2e-16 ***
## d87                  10.34388      1.12027   9.233 < 2e-16 ***
## d88                  10.11969      1.08537   9.324 < 2e-16 ***
## d89                   8.64031      1.06449   8.117 1.21e-15 ***
## d90                   7.75260      1.05368   7.358 3.52e-13 ***
## d91                   5.64272      1.04916   5.378 9.08e-08 ***
## d92                   3.83288      1.04551   3.666 0.000257 ***
## d93                   3.98055      1.03708   3.838 0.000131 ***
## d94                   4.34644      1.01967   4.263 2.18e-05 ***
## d95                   4.75872      1.01399   4.693 3.01e-06 ***
## d96                   2.83490      0.98023   2.892 0.003898 **
## d97                   2.45289      0.96149   2.551 0.010864 *
## d98                   1.66960      0.93502   1.786 0.074420 .
## d99                   1.62073      0.89626   1.808 0.070813 .
## d00                   1.26733      0.87920   1.441 0.149724
## d01                   0.52756      0.85108   0.620 0.535463
## d02                  -0.01308      0.83829  -0.016 0.987557
## d03                  -0.31004      0.83130  -0.373 0.709252
## d04                   NA          NA      NA      NA
```

```
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
```

```
## Residual standard error: 4.046 on 1165 degrees of freedom
## Multiple R-squared:  0.6078, Adjusted R-squared:  0.5963
## F-statistic: 53.1 on 34 and 1165 DF, p-value: < 2.2e-16
```

```
data4 <- data %>% select(c("totfatrte",c(regression_terms,"year","state")))
plm_data <- pdata.frame(data4, index=c("state","year"))
```

```
plm_fit1 <- plm(totfatrte~year+bac08+bac10+perse+sbprim+sbsecon+
               sl70plus+gdl+perc14_24scaled+unemscaled+vehicmilespscscald, data = plm_data,
               summary(plm_fit1))
```

```
## Pooling Model
```

```
##
```

```
## Call:
```

```
## plm(formula = totfatrte ~ year + bac08 + bac10 + perse + sbprim +
##       sbsecon + sl70plus + gdl + perc14_24scaled + unemscaled +
##       vehicmilespscscald, data = plm_data, effect = "individual",
##       model = "pooling")
##
```

```

## Balanced Panel: n = 48, T = 25, N = 1200
##
## Residuals:
##      Min.      1st Qu.      Median      3rd Qu.      Max.
## -14.91602  -2.73839   -0.27779    2.28591   21.42027
##
## Coefficients:
##              Estimate Std. Error t-value Pr(>|t|)
## (Intercept)    13.396109   1.145957  11.6899 < 2.2e-16 ***
## year1981       -2.175479   0.827611  -2.6286 0.0086859 **
## year1982       -6.595970   0.853403  -7.7290 2.330e-14 ***
## year1983       -7.396690   0.869019  -8.5115 < 2.2e-16 ***
## year1984       -5.850394   0.876336  -6.6760 3.792e-11 ***
## year1985       -6.483252   0.894798  -7.2455 7.820e-13 ***
## year1986       -5.852796   0.930669  -6.2888 4.516e-10 ***
## year1987       -6.367393   0.966960  -6.5850 6.869e-11 ***
## year1988       -6.591578   1.013708  -6.5024 1.170e-10 ***
## year1989       -8.070967   1.052622  -7.6675 3.684e-14 ***
## year1990       -8.958670   1.076953  -8.3185 2.463e-16 ***
## year1991      -11.068552   1.101162 -10.0517 < 2.2e-16 ***
## year1992      -12.878398   1.122518 -11.4728 < 2.2e-16 ***
## year1993      -12.730718   1.136283 -11.2038 < 2.2e-16 ***
## year1994      -12.364833   1.157223 -10.6849 < 2.2e-16 ***
## year1995      -11.952549   1.183602 -10.0985 < 2.2e-16 ***
## year1996      -13.876377   1.223339 -11.3430 < 2.2e-16 ***
## year1997      -14.258378   1.249804 -11.4085 < 2.2e-16 ***
## year1998      -15.041676   1.265488 -11.8861 < 2.2e-16 ***
## year1999      -15.090547   1.284308 -11.7499 < 2.2e-16 ***
## year2000      -15.443946   1.305337 -11.8314 < 2.2e-16 ***
## year2001      -16.183715   1.334040 -12.1314 < 2.2e-16 ***
## year2002      -16.724350   1.348033 -12.4065 < 2.2e-16 ***
## year2003      -17.021308   1.359468 -12.5206 < 2.2e-16 ***
## year2004      -16.711273   1.386970 -12.0488 < 2.2e-16 ***
## bac08          -2.498483   0.537505  -4.6483 3.729e-06 ***
## bac10          -1.417565   0.396328  -3.5768 0.0003622 ***
## perse          -0.620108   0.298202  -2.0795 0.0377907 *
## sbprim         -0.075335   0.490785  -0.1535 0.8780318
## sbsecon         0.067280   0.429300   0.1567 0.8754918
## sl70plus        3.347914   0.445170   7.5205 1.086e-13 ***
## gdl            -0.426911   0.526906  -0.8102 0.4179781
## perc14_24scaled  1.217677   1.055042   1.1542 0.2486752
## unemscaled      11.961436   1.230911   9.7176 < 2.2e-16 ***
## vehicmilespscaled 41.008531   1.331262  30.8042 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Total Sum of Squares:    48612
## Residual Sum of Squares: 19067

```

```
## R-Squared:      0.60778
## Adj. R-Squared: 0.59633
## F-statistic: 53.0957 on 34 and 1165 DF, p-value: < 2.22e-16

data2 <- data %>% select(c("totfatrte",c(regression_terms,date_terms)))
lm_fit2 = lm(totfatrte ~ ., data=data2)
summary(lm_fit2)

##
## Call:
## lm(formula = totfatrte ~ ., data = data2)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -14.9160  -2.7384  -0.2778   2.2859  21.4203
##
## Coefficients: (1 not defined because of singularities)
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   -3.31516     1.21135  -2.737 0.006299 **
## bac08         -2.49848     0.53751  -4.648 3.73e-06 ***
## bac10         -1.41757     0.39633  -3.577 0.000362 ***
## perse         -0.62011     0.29820  -2.079 0.037791 *
## sbprim        -0.07533     0.49078  -0.153 0.878032
## sbsecon         0.06728     0.42930   0.157 0.875492
## sl70plus        3.34791     0.44517   7.521 1.09e-13 ***
## gdl           -0.42691     0.52691  -0.810 0.417978
## perc14_24scaled  1.21768     1.05504   1.154 0.248675
## unemscaled     11.96144     1.23091   9.718 < 2e-16 ***
## vehicmilespscaled 41.00853     1.33126  30.804 < 2e-16 ***
## d80            16.71127     1.38697  12.049 < 2e-16 ***
## d81            14.53579     1.36963  10.613 < 2e-16 ***
## d82            10.11530     1.36766   7.396 2.67e-13 ***
## d83             9.31458     1.32894   7.009 4.05e-12 ***
## d84            10.86088     1.26403   8.592 < 2e-16 ***
## d85            10.22802     1.22683   8.337 < 2e-16 ***
## d86            10.85848     1.16023   9.359 < 2e-16 ***
## d87            10.34388     1.12027   9.233 < 2e-16 ***
## d88            10.11969     1.08537   9.324 < 2e-16 ***
## d89             8.64031     1.06449   8.117 1.21e-15 ***
## d90             7.75260     1.05368   7.358 3.52e-13 ***
## d91             5.64272     1.04916   5.378 9.08e-08 ***
## d92             3.83288     1.04551   3.666 0.000257 ***
## d93             3.98055     1.03708   3.838 0.000131 ***
## d94             4.34644     1.01967   4.263 2.18e-05 ***
## d95             4.75872     1.01399   4.693 3.01e-06 ***
## d96             2.83490     0.98023   2.892 0.003898 **
## d97             2.45289     0.96149   2.551 0.010864 *
## d98             1.66960     0.93502   1.786 0.074420 .
```



```
## d99          1.62073    0.89626    1.808 0.070813 .
## d00          1.26733    0.87920    1.441 0.149724
## d01          0.52756    0.85108    0.620 0.535463
## d02         -0.01308    0.83829   -0.016 0.987557
## d03         -0.31004    0.83130   -0.373 0.709252
## d04          NA        NA        NA        NA
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4.046 on 1165 degrees of freedom
## Multiple R-squared:  0.6078, Adjusted R-squared:  0.5963
## F-statistic:  53.1 on 34 and 1165 DF,  p-value: < 2.2e-16
```

Question 4

- Reestimate the model from *Exercise 3* using a fixed effects (at the state level) model. How do the coefficients on *bac08*, *bac10*, *perse*, and *sbprim* compare with the pooled OLS estimates? Which set of estimates do you think is more reliable? What assumptions are needed in each of these models? Are these assumptions reasonable in the current context?

```
plm_fit1 <- plm(totfatrte~year+bac08+bac10+perse+sbprim+sbsecon+
               sl70plus+gdl+perc14_24scaled+unemscaled+vehicmilespscscalled, data = plm_data,
               summary(plm_fit1))
```

```
## Oneway (individual) effect Within Model
##
## Call:
## plm(formula = totfatrte ~ year + bac08 + bac10 + perse + sbprim +
##       sbsecon + sl70plus + gdl + perc14_24scaled + unemscaled +
##       vehicmilespscscalled, data = plm_data, model = "within", index = c("year"))
##
## Balanced Panel: n = 48, T = 25, N = 1200
##
## Residuals:
##      Min.      1st Qu.      Median      3rd Qu.      Max.
## -8.4273592 -1.0258600 -0.0029547  0.9572345 14.8109310
##
## Coefficients:
##              Estimate Std. Error t-value Pr(>|t|)
## year1981      -1.511071   0.413215  -3.6569 0.0002672 ***
## year1982      -3.025496   0.442431  -6.8383 1.316e-11 ***
## year1983      -3.503601   0.456577  -7.6736 3.628e-14 ***
## year1984      -4.259361   0.464943  -9.1610 < 2.2e-16 ***
## year1985      -4.726793   0.485470  -9.7365 < 2.2e-16 ***
## year1986      -3.661185   0.517698  -7.0721 2.686e-12 ***
## year1987      -4.305788   0.555329  -7.7536 2.001e-14 ***
## year1988      -4.767121   0.601556  -7.9246 5.501e-15 ***
## year1989      -6.129973   0.640191  -9.5752 < 2.2e-16 ***
```

```
## year1990      -6.229738    0.664851   -9.3701 < 2.2e-16 ***
## year1991      -6.917140    0.681954  -10.1431 < 2.2e-16 ***
## year1992      -7.774172    0.702886  -11.0604 < 2.2e-16 ***
## year1993      -8.094109    0.715947  -11.3055 < 2.2e-16 ***
## year1994      -8.504217    0.734109  -11.5844 < 2.2e-16 ***
## year1995      -8.255402    0.756236  -10.9164 < 2.2e-16 ***
## year1996      -8.606619    0.795950  -10.8130 < 2.2e-16 ***
## year1997      -8.707817    0.819757  -10.6224 < 2.2e-16 ***
## year1998      -9.349240    0.833735  -11.2137 < 2.2e-16 ***
## year1999      -9.474891    0.843991  -11.2263 < 2.2e-16 ***
## year2000      -9.991860    0.856064  -11.6719 < 2.2e-16 ***
## year2001      -9.631217    0.872554  -11.0380 < 2.2e-16 ***
## year2002      -8.906730    0.882053  -10.0977 < 2.2e-16 ***
## year2003      -8.936503    0.889947  -10.0416 < 2.2e-16 ***
## year2004      -9.339361    0.911070  -10.2510 < 2.2e-16 ***
## bac08         -1.437221    0.394212   -3.6458 0.0002788 ***
## bac10         -1.062668    0.268838   -3.9528 8.208e-05 ***
## perse         -1.151617    0.233987   -4.9217 9.867e-07 ***
## sbprim        -1.227400    0.342715   -3.5814 0.0003564 ***
## sbsecon       -0.349708    0.252171   -1.3868 0.1657826
## sl70plus      -0.062533    0.269311   -0.2322 0.8164283
## gdl           -0.411776    0.292574   -1.4074 0.1595790
## perc14_24scaled 1.609246    0.817857    1.9676 0.0493567 *
## unemscaled    -9.035071    0.957141   -9.4397 < 2.2e-16 ***
## vehicmilespscald 13.177679    1.556613    8.4656 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Total Sum of Squares:    12134
## Residual Sum of Squares: 4535.3
## R-Squared:    0.62624
## Adj. R-Squared: 0.59916
## F-statistic: 55.0943 on 34 and 1118 DF, p-value: < 2.22e-16
```

- FE removes the effect of those time-invariant characteristics so we can assess the net effect of the predictors on the outcome variable.
- Those time-invariant characteristics are unique to the individual and should not be correlated with other individual characteristics.

Question 5

5. Would you prefer to use a random effects model instead of the fixed effects model you built in *Exercise 4*? Please explain.

```
plm_fit2 <- plm(totfatrte~year+bac08+bac10+perse+sbprim+sbsecon+
               sl70plus+gdl+perc14_24scaled+unemscaled+vehicmilespscald, data = plm_data,
               summary(plm_fit2))
```

```

## Oneway (individual) effect Random Effect Model
##   (Swamy-Arora's transformation)
##
## Call:
## plm(formula = totfatrte ~ year + bac08 + bac10 + perse + sbprim +
##       sbsecon + sl70plus + gdl + perc14_24scaled + unemscaled +
##       vehicmilespscscald, data = plm_data, model = "random", index = c("state",
##       "year"))
##
## Balanced Panel: n = 48, T = 25, N = 1200
##
## Effects:
##               var std.dev share
## idiosyncratic 4.057   2.014 0.328
## individual    8.294   2.880 0.672
## theta: 0.8615
##
## Residuals:
##      Min.   1st Qu.   Median   3rd Qu.    Max.
## -8.25582 -1.15221 -0.15787  0.93086 16.45691
##
## Coefficients:
##               Estimate Std. Error z-value Pr(>|z|)
## (Intercept)    23.505008   0.982620  23.9207 < 2.2e-16 ***
## year1981       -1.548874   0.428297  -3.6164 0.0002988 ***
## year1982       -3.243321   0.457724  -7.0858 1.383e-12 ***
## year1983       -3.744747   0.472120  -7.9318 2.161e-15 ***
## year1984       -4.372875   0.480638  -9.0981 < 2.2e-16 ***
## year1985       -4.860931   0.501363  -9.6954 < 2.2e-16 ***
## year1986       -3.829544   0.534160  -7.1693 7.539e-13 ***
## year1987       -4.501403   0.572131  -7.8678 3.610e-15 ***
## year1988       -4.981938   0.618874  -8.0500 8.279e-16 ***
## year1989       -6.371318   0.657971  -9.6833 < 2.2e-16 ***
## year1990       -6.535657   0.682788  -9.5720 < 2.2e-16 ***
## year1991       -7.302698   0.700302 -10.4279 < 2.2e-16 ***
## year1992       -8.238956   0.721261 -11.4230 < 2.2e-16 ***
## year1993       -8.541762   0.734487 -11.6296 < 2.2e-16 ***
## year1994       -8.918308   0.752970 -11.8442 < 2.2e-16 ***
## year1995       -8.676932   0.775406 -11.1902 < 2.2e-16 ***
## year1996       -9.096863   0.815728 -11.1518 < 2.2e-16 ***
## year1997       -9.220296   0.839844 -10.9786 < 2.2e-16 ***
## year1998       -9.892173   0.853804 -11.5860 < 2.2e-16 ***
## year1999      -10.031557   0.864259 -11.6071 < 2.2e-16 ***
## year2000      -10.549021   0.876674 -12.0330 < 2.2e-16 ***
## year2001      -10.273651   0.893359 -11.5000 < 2.2e-16 ***
## year2002       -9.637586   0.902780 -10.6755 < 2.2e-16 ***
## year2003       -9.682820   0.910895 -10.6300 < 2.2e-16 ***
## year2004      -10.054258   0.932541 -10.7816 < 2.2e-16 ***

```

```
## bac08          -1.569317    0.403835   -3.8860 0.0001019 ***
## bac10          -1.138042    0.276041   -4.1227 3.744e-05 ***
## perse         -1.093281    0.238852   -4.5772 4.712e-06 ***
## sbprim        -1.176078    0.351436   -3.3465 0.0008184 ***
## sbsecon       -0.347578    0.260245   -1.3356 0.1816862
## sl70plus       0.029969    0.277721    0.1079 0.9140655
## gdl           -0.385244    0.302487   -1.2736 0.2028095
## perc14_24scaled 1.693737    0.836030    2.0259 0.0427722 *
## unemscaled    -7.779559    0.977059   -7.9622 1.690e-15 ***
## vehicmilespscald 16.463335    1.539593   10.6933 < 2.2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Total Sum of Squares:    12834
## Residual Sum of Squares: 5078.6
## R-Squared:    0.60429
## Adj. R-Squared: 0.59274
## Chisq: 1779.05 on 34 DF, p-value: < 2.22e-16
```

```
plm_fit2 <- plm(totfatrte~year+bac08+bac10+perse+sbprim+sbsecon+
               sl70plus+gdl+perc14_24scaled+unemscaled+vehicmilespscald, data = plm_data,
               summary(plm_fit2))
```

```
## Oneway (individual) effect Random Effect Model
##   (Swamy-Arora's transformation)
##
## Call:
## plm(formula = totfatrte ~ year + bac08 + bac10 + perse + sbprim +
##       sbsecon + sl70plus + gdl + perc14_24scaled + unemscaled +
##       vehicmilespscald, data = plm_data, model = "random", index = c("state"))
##
## Balanced Panel: n = 48, T = 25, N = 1200
##
## Effects:
##               var std.dev share
## idiosyncratic 4.057    2.014 0.328
## individual    8.294    2.880 0.672
## theta: 0.8615
##
## Residuals:
##      Min.   1st Qu.   Median   3rd Qu.    Max.
## -8.25582 -1.15221 -0.15787  0.93086 16.45691
##
## Coefficients:
##               Estimate Std. Error z-value Pr(>|z|)
## (Intercept)    23.505008   0.982620  23.9207 < 2.2e-16 ***
## year1981       -1.548874   0.428297  -3.6164 0.0002988 ***
## year1982       -3.243321   0.457724  -7.0858 1.383e-12 ***
```

```

## year1983      -3.744747    0.472120   -7.9318  2.161e-15 ***
## year1984      -4.372875    0.480638   -9.0981 < 2.2e-16 ***
## year1985      -4.860931    0.501363   -9.6954 < 2.2e-16 ***
## year1986      -3.829544    0.534160   -7.1693  7.539e-13 ***
## year1987      -4.501403    0.572131   -7.8678  3.610e-15 ***
## year1988      -4.981938    0.618874   -8.0500  8.279e-16 ***
## year1989      -6.371318    0.657971   -9.6833 < 2.2e-16 ***
## year1990      -6.535657    0.682788   -9.5720 < 2.2e-16 ***
## year1991      -7.302698    0.700302  -10.4279 < 2.2e-16 ***
## year1992      -8.238956    0.721261  -11.4230 < 2.2e-16 ***
## year1993      -8.541762    0.734487  -11.6296 < 2.2e-16 ***
## year1994      -8.918308    0.752970  -11.8442 < 2.2e-16 ***
## year1995      -8.676932    0.775406  -11.1902 < 2.2e-16 ***
## year1996      -9.096863    0.815728  -11.1518 < 2.2e-16 ***
## year1997      -9.220296    0.839844  -10.9786 < 2.2e-16 ***
## year1998      -9.892173    0.853804  -11.5860 < 2.2e-16 ***
## year1999     -10.031557    0.864259  -11.6071 < 2.2e-16 ***
## year2000     -10.549021    0.876674  -12.0330 < 2.2e-16 ***
## year2001     -10.273651    0.893359  -11.5000 < 2.2e-16 ***
## year2002      -9.637586    0.902780  -10.6755 < 2.2e-16 ***
## year2003      -9.682820    0.910895  -10.6300 < 2.2e-16 ***
## year2004     -10.054258    0.932541  -10.7816 < 2.2e-16 ***
## bac08         -1.569317    0.403835   -3.8860  0.0001019 ***
## bac10         -1.138042    0.276041   -4.1227  3.744e-05 ***
## perse         -1.093281    0.238852   -4.5772  4.712e-06 ***
## sbprim        -1.176078    0.351436   -3.3465  0.0008184 ***
## sbsecon       -0.347578    0.260245   -1.3356  0.1816862
## sl70plus      0.029969    0.277721    0.1079  0.9140655
## gdl           -0.385244    0.302487   -1.2736  0.2028095
## perc14_24scaled 1.693737    0.836030    2.0259  0.0427722 *
## unemscaled    -7.779559    0.977059   -7.9622  1.690e-15 ***
## vehicmilespscald 16.463335    1.539593   10.6933 < 2.2e-16 ***
## ---

```

```
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
##
```

```
## Total Sum of Squares:    12834
```

```
## Residual Sum of Squares: 5078.6
```

```
## R-Squared:      0.60429
```

```
## Adj. R-Squared: 0.59274
```

```
## Chisq: 1779.05 on 34 DF, p-value: < 2.22e-16
```

```
phptest(plm_fit1,plm_fit2)
```

```
##
```

```
## Hausman Test
```

```
##
```

```
## data: totfatrte ~ year + bac08 + bac10 + perse + sbprim + sbsecon + ...
```

```
## chisq = 148.69, df = 34, p-value = 2.727e-16
```

```
## alternative hypothesis: one model is inconsistent
```

Let's run the Hausman test where the null hypothesis is that the preferred model is random effects vs. the alternative the fixed effects. A small p-value (typically ≤ 0.05) indicates strong evidence against the null hypothesis hence we can conclude that the fixed effects model is a better fit.

Question 6

6. Suppose that *vehicmiles*, the number of miles driven per capita, increases by 1,000. Using the FE estimates, what is the estimated effect on *totfatrt*? Please interpret the estimate.

```
min_vehicmilespc <- min(data$vehicmilespc)
max_vehicmilespc <- max(data$vehicmilespc)

totfatrt_change = (1000*13.177679)/(max_vehicmilespc-min_vehicmilespc)
totfatrt_change

## [1] 0.9400519

total_pop <- data %>% summarise(sum_state_pop = sum(statepop[year==2004])) %>% pull(sum_state_pop)
total_pop * totfatrt_change / 100000

## [1] 2737.487
```

Thus, a 1,000 increase in *vehicmiles* would increase *totfatrt* by 0.94. A more intuitive way to express this would be that for the next year i.e. 2005, if the *vehicmiles* driven would increase by 1,000, then the total fatalities is projected to increase by 2737.487.

Question 7

7. If there is serial correlation or heteroskedasticity in the idiosyncratic errors of the model, what would be the consequences on the estimators and their standard errors?

```
library(lmtest)

## Loading required package: zoo
##
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
##      as.Date, as.Date.numeric

bptest(plm_fit1)

##
## studentized Breusch-Pagan test
##
## data: plm_fit1
## BP = 150.07, df = 34, p-value < 2.2e-16
```

The null hypothesis of the Breusch-Pagan test is homoscedasticity i.e. variance does not depend on auxiliary regressors. In this case, the null hypothesis is rejected as the p-value is small.