

# Transient Dynamical Indicators of Critical Transitions

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## Abstract

Replace the text here with your abstract.

**Keywords:** tipping point, critical transition, critical slowing down, early warning signals, resilience, intensity of attraction

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# **1 Introduction**

## **1.1 Critical Transitions**

A tipping point or critical transition occurs in a dynamical system when a small perturbation to the system causes an abrupt qualitative shift in overall behavior. This informal concept is often understood as a local bifurcation, but may also correspond to a variety of other dynamical behaviors including global bifurcations, perturbations pushing a state variable across the boundary between two basins of attraction, and rate-induced tipping.

Empirically, critical transitions have been studied in contexts ranging from Earth's climate [2] to emerging infectious disease [1] to

In complex empirical systems, the conditions under which a critical transition occurs are generally extremely difficult to predict. In many cases, the underlying mechanisms driving such a system toward the brink may be impossible to fully understand or identify.

## **1.2 Motivation**

[? ]

# **2 Resilience Quantification**

## **2.1 Asymptotic Resilience**

## **2.2 Width of Basin of Attraction**

## **2.3 Reactivity**

## **2.4 Intensity of Attraction**

# **3 Critical Slowing Down**

## **3.1 Local Bifurcation**

## **3.2 Critical Slowing Down**

## **3.3 Early Warning Signals**

# **4 Transient Dynamical Indicators of Critical Transitions**

## **4.1 Indicators from Reactivity**

## **4.2 Possibility for Indicators from Intensity of Attraction**

# **5 Thesis Proposal**

## **5.1 Continuity of Intensity of Attraction**

## **5.2 Intensity through Critical Transitions**

## **5.3 Further Possibilities**

## References

- [1] Tobias S. Brett and Pejman Rohani. Dynamical footprints enable detection of disease emergence. *PLOS Biology*, 18(5):e3000697, May 2020. ISSN 1545-7885. doi:10.1371/journal.pbio.3000697.
- [2] Timothy M. Lenton. Early warning of climate tipping points. *Nature Climate Change*, 1(4):201–209, July 2011. ISSN 1758-6798. doi:10.1038/nclimate1143.