SAS Output from Method 1

CATMOD PROCEDURE

Response: A*B*C	Response Levels (R)= 8
Weight Variable: None	Populations (S)= 1
Data Set: A	Total Frequency (N)= 46
	Observations (Obs)= 46

Sample	Function Number	Response Function	DESI	GN MATRIX	3
1	1	0.60870	1	0	0
	2	0.60870	0	1	0
	3	0.34783	0	0	1

ANALYSIS OF VARIANCE TABLE

Source	DF	Chi-Square	Prob
MODEL: MEAN	2	6.58	0.0372
RESIDUAL	0		

ANALYSIS OF WEIGHTED-LEAST-SQUARES ESTIMATES

Effect	Parameter	Estimate	Standard Error		Prob
MODEL	1		0.0720		
	2	0.6087	0.0720	71.56	0.0000
	3	0.3478	0.0702	24.53	0.0000

Contrast	DF	Chi-Square	Prob
A=B=C	2	6.58	0.0372
A=B	1	0.00	1.0000
A=C	1	5.79	0.0161
B=C	1	5.79	0.0161

SAS Output from Method 2

CATMOD PROCEDURE

Response: A*B*C	Response Levels (R)= 8
Weight Variable: None	Populations (S)= 1
Data Set: A	Total Frequency (N) = 46
	Observations (Obs)= 46

Sample	Function Number	Response Function	DESI 1	GN MATRI	Х З
1	1	0.60870	1	1	0
	2	0.60870	1	0	1
	3	0.34783	1	-1	-1

ANALYSIS OF VARIANCE TABLE

Source	DF	Chi-Square	Prob
INTERCEPT	1	146.84	0.0000
DRUG	2	6.58	0.0372
RESIDUAL	0		

ANALYSIS OF WEIGHTED-LEAST-SQUARES ESTIMATES

Effect	Parameter	Estimate	Standard Error	Chi- Square	Prob
INTERCEPT	1	0.5217	0.0431	146.84	0.0000
DRUG	2	0.0870	0.0507	2.95	0.0861
	3	0.0870	0.0507	2.95	0.0861

Contrast	DF	Chi-Square	Prob
A=B	1	0.00	1.0000
A=C	1	5.79	0.0161
B=C	1	5.79	0.0161

SAS Output from Method 3

CATMOD PROCEDURE

Response: A*B*C	Response Levels (R)=	8
Weight Variable: None	Populations (S)=	1
Data Set: A	Total Frequency (N)=	46
	Observations (Obs)=	46

Sample	Function Number	Response Function	DESIGN MATRIX
1	1	0.60870	1
	2	0.60870	1
	3	0.34783	1

ANALYSIS OF VARIANCE TABLE

Source	DF	Chi-Square	Prob
MODEL: MEAN	0*		
RESIDUAL	2	6.58	0.0372

NOTE: Effects marked with * contained 1 or more singularities (i.e., redundant parameters).

ANALYSIS OF WEIGHTED-LEAST-SQUARES ESTIMATES

			Standard	Chi-	
Effect	Parameter	Estimate	Error	Square	Prob
MODEL	1	0.4930	0.0416	140.62	0.0000

• Since the model consists only of an intercept, there are no degrees of freedom for the default effect labelled MODEL: MEAN in the ANOVA table

SAS Output from the Reduced Model

CATMOD PROCEDURE

Response: A*B*C	Response Levels	(R)=	8
Weight Variable: None	Populations	(S)=	1
Data Set: A	Total Frequency	(N) = 4	46
	Observations (Ob	os)= 4	46

			DESIG	N
	Function	Response	MATRI	X
Sample	Number	Function	1	2
1	1	0.60870	1	0
	2	0.60870	1	0
	3	0.34783	1	1

ANALYSIS OF VARIANCE TABLE

Source	DF	Chi-Square	Prob	
_				
Intercept	1	98.54	0.0000	
Drug C Effect	1	6.58	0.0103	
RESIDUAL	1	0.00	1.0000	

ANALYSIS OF WEIGHTED-LEAST-SQUARES ESTIMATES

Effect	Parameter	Estimate	Standard Error	Prob
MODEL	_	0.6087 -0.2609	0.0613 0.1017	 0.0000

- \bullet The reduced model fits very well (perfectly, since $p_A=p_B)$
- \bullet Drug C is significantly different from Drugs A and B (Wald statistic=6.58, $p{=}0.01)$

${f SAS}$ Output from Model 1

CATMOD PROCEDURE

Response: W9*W10*W11*W12	Response Levels (R)=	16
Weight Variable: COUNT	Populations (S)=	1
Data Set: A	Total Frequency (N) =	1019
	Observations (Obs)=	16

	Function	Response		DESIGN M	ATRIX	
Sample	Number	Function	1	2	3	4
1	1	0.26006	1	1	0	0
	2	0.25025	1	0	1	0
	3	0.23553	1	0	0	1
	4	0.21197	1	-1	-1	-1

ANALYSIS OF VARIANCE TABLE

Source	DF	Chi-Square	Prob
INTERCEPT AGE	1 3	523.63 12.85	0.0000
RESTDUAL	0		

ANALYSIS OF WEIGHTED-LEAST-SQUARES ESTIMATES

			Standard	Chi-	
Effect	Parameter	Estimate	Error	Square	Prob
INTERCEPT	1	0.2395	0.0105	523.63	0.0000
AGE	2	0.0206	0.00876	5.53	0.0187
	3	0.0108	0.00809	1.78	0.1822
	4	-0.00393	0.00807	0.24	0.6266

• We reject H_0 : $\Pi_9 = \Pi_{10} = \Pi_{11} = \Pi_{12} \ (W_C = 12.85, \, \mathrm{df} = 3, \, p = .005)$

SAS Output from Model 2

CATMOD PROCEDURE

Response: W9*W10*W11*W12	Response Levels (R) =	16
Weight Variable: COUNT	Populations (S)=	1
Data Set: A	Total Frequency (N) =	1019
	Observations (Obs)=	16

	Function	Response		DESIGN M	ATRIX	
Sample	Number	Function	1	2	3	4
1	1	0.26006	1	-3	1	-1
	2	0.25025	1	-1	-1	3
	3	0.23553	1	1	-1	-3
	4	0.21197	1	3	1	1

ANALYSIS OF VARIANCE TABLE

Source	DF	Chi-Square	Prob
Intercept	1	523.63	0.0000
Age	3	12.85	0.0050
Linear	1	11.88	0.0006
Quadratic	1	0.53	0.4666
Cubic	1	0.01	0.9219
Nonlinear	2	0.54	0.7620
RESTDUAL	0		

ANALYSIS OF WEIGHTED-LEAST-SQUARES ESTIMATES

Effect	Parameter	Estimate	Standard Error	Chi- Square	Prob
MODEL	1	0.2395	0.0105	523.63	0.0000
	2	-0.00795	0.00231	11.88	0.0006
	3	-0.00343	0.00472	0.53	0.4666
	4	-0.0002	0.00200	0.01	0.9219

• The nonlinear age effects are jointly nonsignificant ($W_C=0.54,\,\mathrm{df}=2,\,p=0.762$)

SAS Output from Model 3

CATMOD PROCEDURE

Response: W9*W10*W11*W12	Response Levels	(R) =	16
Weight Variable: COUNT	Populations	(S)=	1
Data Set: A	Total Frequency	(N) =	1019

			DESIG	ŀN
	Function	Response	MATRI	X
Sample	Number	Function	1	2
1	1	0.26006	1	0
	2	0.25025	1	1
	3	0.23553	1	2
	4	0.21197	1	3

ANALYSIS OF VARIANCE TABLE

Source	DF	Chi-Square	Prob
Intercept	1	418.51	0.0000
Linear Age	1	12.31	0.0005
RESIDUAL	2	0.54	0.7620

ANALYSIS OF WEIGHTED-LEAST-SQUARES ESTIMATES

Effect	Parameter	Estimate	Standard Error	 Prob
MODEL	_		0.0129 0.00460	

	Observed		Pred				
		Function		Standard		Standard	
Sample Number		Number	Function	Error	Function	Error	Residual
	1	1	0.26005888	0.01374192	0.26320937	0.01286614	-0.0031505
		2	0.25024534	0.01356924	0.24708501	0.01083431	0.00316033
		3	0.23552502	0.0132927	0.23096065	0.01055764	0.00456437
		4	0.21197252	0.01280334	0.2148363	0.01215658	-0.0028638

SAS Output from Logit Model

CATMOD PROCEDURE

Response: W9*W10*W11*W12	Response Levels (R) =	16
Weight Variable: COUNT	Populations $(S)=$	1
Data Set: A	Total Frequency (N) =	1019
	Observations (Obs)=	16

Sample	Function Number	Response Function	DESIG MATRI 1	
1	1	-1.04566	1	0
	2	-1.09730	1	1
	3	-1.17737	1	2
	4	-1.31308	1	3

ANALYSIS OF VARIANCE TABLE

Source	DF	Chi-Square	Prob
Intercept Linear Age	1 1	235.78 11.77	0.0000
RESIDUAL	2	0.67	0.7167

ANALYSIS OF WEIGHTED-LEAST-SQUARES ESTIMATES

Effect	Parameter	Estimate	Standard Error	 Prob
MODEL	_		0.0669	

		Observed		Pred			
		Function		Standard		Standard	
Sample Number		Number	Function	Error	Error Function		Residual
	1	1	-1.0456625	0.0714132	-1.0275926	0.0669218	-0.0180699
		2	-1.0973042	0.07232198	-1.1154682	0.05812335	0.01816398
		3	-1.1773721	0.07382658	-1.2033438	0.05992065	0.02597167
		4	-1.3130763	0.07664829	-1.2912194	0.0715193	-0.0218569

SAS Output from Model 1 (Analysis of Marginal Proportions)

CATMOD PROCEDURE

Response: NO*N3*N6	Response Levels	(R) =	27
Weight Variable: COUNT	Populations	(S)=	1
Data Set: A	Total Frequency	(N) =	1926

	Function	Response			DESIGN MA	ATRIX		
Sample	Number	Function	1	2	3	4	5	6
1	1	0.19626	1	 -1	1	0	0	0
	2	0.23780	0	0	0	1	-1	1
	3	0.12201	1	0	-2	0	0	0
	4	0.22949	0	0	0	1	0	-2
	5	0.08411	1	1	1	0	0	0
	6	0.18120	0	0	0	1	1	1

ANALYSIS OF VARIANCE TABLE

Source		DF	Chi-Square	Prob
Pr(0):	Intercept	1	656.31	0.0000
	Linear	1	122.85	0.0000
	Quadratic	1	4.99	0.0255
	Overall	2	123.10	0.0000
Pr(1-2):	Intercept	1	1213.98	0.0000
	Linear	1	21.26	0.0000
	Quadratic	1	3.69	0.0547
	Overall	2	26.77	0.0000
Both:	Linear	2	181.00	0.0000
	Quadratic	2	6.68	0.0354
Homogeneity		4	184.23	0.0000
RESIDUAL		0		

ANALYSIS OF WEIGHTED-LEAST-SQUARES ESTIMATES

Effect	Parameter	Estimate	Standard Error	Chi- Square	Prob
MODEL	 1	0.1341	0.00524	656.31	0.0000
	2	-0.0561	0.00506	122.85	0.0000
	3	0.00606	0.00271	4.99	0.0255
	4	0.2162	0.00620	1213.98	0.0000
	5	-0.0283	0.00614	21.26	0.0000
	6	-0.00666	0.00347	3.69	0.0547

SAS Output from Alternate Form of Model 1 (Analysis of Marginal Proportions)

	Function	Response			DESIGN M	ATRIX		
Sample	Number	Function	1	2	3	4	5	6
1	1	0.19626	1	0	1	0	0	0
	2	0.23780	0	1	0	1	0	0
	3	0.12201	1	0	0	0	1	0
	4	0.22949	0	1	0	0	0	1
	5	0.08411	1	0	-1	0	-1	0
	6	0.18120	0	1	0	-1	0	-1

ANALYSIS OF VARIANCE TABLE

Source	DF	Chi-Square	Prob
INTERCEPT	2 4	2168.84 184.23	0.0000
RESTRIAL	0	104.25	0.0000

ANALYSIS OF WEIGHTED-LEAST-SQUARES ESTIMATES

Effect	Parameter	Estimate	Standard Error	Chi- Square	Prob
INTERCEPT	1	0.1341	0.00524	656.31	0.0000
	2	0.2162	0.00620	1213.98	0.0000
TIME	3	0.0621	0.00610	103.60	0.0000
	4	0.0216	0.00732	8.74	0.0031
	5	-0.0121	0.00542	4.99	0.0255
	6	0.0133	0.00694	3.69	0.0547

Contrast	DF	Chi-Square	Prob	
0: L	1	122.85	0.0000	
Q	1	4.99	0.0255	
L&Q	2	123.10	0.0000	
1-2: L	1	21.26	0.0000	
Q	1	3.69	0.0547	
L&Q	2	26.77	0.0000	
Both: L	2	181.00	0.0000	
Q	2	6.68	0.0354	

SAS Output from Model 2 (Analysis of Mean Scores)

CATMOD PROCEDURE

Response: NO*N3*N6	Response Levels (R) =	27
Weight Variable: COUNT	Populations (S)=	1
Data Set: A	Total Frequency (N) =	1926
	Observations (Obs)=	27

Sample	Function Number	Response Function	DESI 1	GN MATRI	X 3
1	1	2.62046	1	1	0
	2	2.93821	1	0	1
	3	3.21054	1	-1	-1

ANALYSIS OF VARIANCE TABLE

Source	DF	Chi-Square	Prob
INTERCEPT TIME	1 2	14567.09 178.47	0.0000
RESIDUAL	0		

ANALYSIS OF WEIGHTED-LEAST-SQUARES ESTIMATES

Effect	Parameter	Estimate	Standard Error	~	Prob
INTERCEPT TIME	_	2.9231 -0.3026		14567.09 134.40	
	3	0.0151	0.0233	0.42	0.5149

Contrast	DF	Chi-Square	Prob
Linear	1	177.80	0.0000
Quadratic	1	0.42	0.5149

SAS Output from Model 3 (Reduced Mean Score Model)

CATMOD PROCEDURE

Response: S0*S3*S6	Response Levels (R) =	27
Weight Variable: COUNT	Populations $(S)=$	1
Data Set: A	Total Frequency (N) =	1926
	Observations (Obs)=	27

			DESIG	N
	Function	Response	MATRI	X
Sample	Number	Function	1	2
1	1	2.62046	1	0
	2	2.93821	1	3
	3	3.21054	1	6

ANALYSIS OF VARIANCE TABLE

Source	DF	Chi-Square	Prob
Intercept	1	5560.85	0.0000
Linear Time	1	178.04	0.0000
RESIDUAL	1	0.42	0.5149

ANALYSIS OF WEIGHTED-LEAST-SQUARES ESTIMATES

Effect	Parameter	Estimate	Standard Error	 Prob
MODEL	1 2	2.6290 0.0978	0.0353 0.00733	

		Observed		Pred		
	Function Standard					
Sample	Number	Function	Error	Function	Error	Residual
1	1	2.62045691	0.03760267	2.62897392	0.03525458	-0.008517
	2	2.93821391	0.03424882	2.92243207	0.02419897	0.01578185
	3	3.21053998	0.03103507	3.21589022	0.02992769	-0.0053502

SAS Output from Model 1 (Saturated Marginal Probability Model) Complete Data Only

Response: ATTENDO*ATTEND3*ATTEND6	Response Levels (R) =	8
Weight Variable: COUNT	Populations (S)=	2
Data Set: COMPLETE	Total Frequency (N)=	1973
Frequency Missing: 0	Observations (Obs)=	16

	Function	Response						
Sample	Number	Function	1	2	3	4	5	6
1	1	0.81465	1	-1	1	0	0	0
	2	0.79863	1	0	-2	0	0	0
	3	0.75667	1	1	1	0	0	0
2	1	0.70242	0	0	0	1	-1	1
	2	0.69940	0	0	0	1	0	-2
	3	0.65861	0	0	0	1	1	1

ANALYSIS-OF-VARIANCE TABLE

Source		DF	Chi-Square	Prob
Females:	Intercept	1	6613.87	0.0000
	Linear	1	29.23	0.0000
	Quadratic	1	2.97	0.0848
	Lin & Quad	2	30.46	0.0000
Males:	Intercept	1	1814.09	0.0000
	Linear	1	8.97	0.0027
	Quadratic	1	2.76	0.0964
	Lin & Quad	2	11.00	0.0041
Both:	Linear	2	38.20	0.0000
	Quadratic	2	5.74	0.0568
	Lin & Quad	4	41.45	0.0000
RESIDUAL		0	•	

ANALYSIS OF WEIGHTED-LEAST-SQUARES ESTIMATES

Effect	Parameter	Estimate	Standard Error	Chi- Square	Prob
MODEL	1 2 3 4 5	0.7900 -0.0290 -0.00432 0.6868 -0.0219 -0.00629	0.00971 0.00536 0.00251 0.0161 0.00731 0.00379	2.97	0.0000 0.0000 0.0848 0.0000 0.0027 0.0964

Contrast	DF	Chi-Square	Prob
Sex Eq.	3	31.50	0.0000
Int Eq.	1	30.04	0.0000
Lin Eq.	1	0.61	0.4347
Quad Eq	1	0.19	0.6641

SAS Output from Model 2 (Reduced Marginal Probability Model) Complete Data Only

	Function	Response		DESIGN MA		
Sample	Number	Function	1 	2 	3 	4
1	1	0.81465	1	0	-1	1
	2	0.79863	1	0	0	-2
	3	0.75667	1	0	1	1
2	1	0.70242	0	1	-1	1
	2	0.69940	0	1	0	-2
	3	0.65861	0	1	1	1

ANALYSIS-OF-VARIANCE TABLE

Source	DF	Chi-Square	Prob
Intercept: Females	1	6645.60	0.0000
Males	1	1813.45	0.0000
Linear Time	1	37.67	0.0000
Quadratic Time	1	5.47	0.0193
RESIDUAL	2	0.87	0.6476

ANALYSIS OF WEIGHTED-LEAST-SQUARES ESTIMATES

Effect	Parameter	Estimate	Standard Error	Chi- Square	Prob
MODEL	1	0.7905	0.00970	6645.60	0.0000
	2	0.6865	0.0161	1813.45	0.0000
	3	-0.0265	0.00432	37.67	0.0000
	4	-0.00489	0.00209	5.47	0.0193

ANALYSIS OF CONTRASTS

Contrast		Chi-Square	Prob	
Intercept Equality	1	30.63	0.0000	

		Obse	rved	Pred		
	Function		Standard		Standard	
Sample	Number	Function	Error	Function	Error	Residual
1	1	0.81464531	0.0107321	0.81215206	0.01038477	0.00249325
	2	0.798627	0.0110757	0.80028283	0.01066748	-0.0016558
	3	0.75667429	0.01185079	0.75908383	0.01113785	-0.0024095
2	1	0.70241692	0.01776939	0.70810761	0.01668638	-0.0056907
	2	0.69939577	0.01782092	0.69623837	0.01665332	0.0031574
	3	0.65861027	0.01842937	0.65503938	0.01695246	0.0035709

SAS Output from Model 3 (Reparameterized Reduced Marginal Probability Model) Complete Data Only

	Function	Response		DESIGN MA	ATRIX	
Sample	Number	Function	1	2	3	4
1	1	0.81465	1	0	0	0
	2	0.79863	1	0	3	9
	3	0.75667	1	0	6	36
2	1	0.70242	0	1	0	0
	2	0.69940	0	1	3	9
	3	0.65861	0	1	6	36

ANALYSIS-OF-VARIANCE TABLE

Source	DF	Chi-Square	Prob
Intercept: Females	1	6116.18	0.0000
Males	1	1800.84	0.0000
Linear Time	1	0.05	0.8275
Quadratic Time	1	5.47	0.0193
RESIDUAL	2	0.87	0.6476

ANALYSIS OF WEIGHTED-LEAST-SQUARES ESTIMATES

Effect	Parameter	Estimate	2 2 411 441 41	Chi- Square	Prob
MODEL	1	0.8122	0.0104	6116.18	0.0000
	2	0.7081	0.0167	1800.84	0.0000
	3	0.000932	0.00428	0.05	0.8275
	4	-0.00163	0.000697	5.47	0.0193

ANALYSIS OF CONTRASTS

Contrast	DF	Chi-Square	Prob	
Intercept Equality	1	30.63	0.0000	

		Obse	rved	Pred	icted	
	Function		Standard		Standard	
Sample	Number	Function	Error	Function	Error	Residual
1	1	0.81464531	0.0107321	0.81215206	0.01038477	0.00249325
	2	0.798627	0.0110757	0.80028283	0.01066748	-0.0016558
	3	0.75667429	0.01185079	0.75908383	0.01113785	-0.0024095
2	1	0.70241692	0.01776939	0.70810761	0.01668638	-0.0056907
	2	0.69939577	0.01782092	0.69623837	0.01665332	0.0031574
	3	0.65861027	0.01842937	0.65503938	0.01695246	0.0035709

SAS Output from Saturated Marginal Logit Model Complete Data Only

	Function	Response			DESIGN M	ATRIX		
Sample	Number	Function	1	2	3	4	5	6
1	1	1.48048	1	-1	1	0	0	0
	2	1.37774	1	0	-2	0	0	0
	3	1.13453	1	1	1	0	0	0
2	1	0.85883	0	0	0	1	-1	1
	2	0.84442	0	0	0	1	0	-2
	3	0.65711	0	0	0	1	1	1

ANALYSIS OF VARIANCE TABLE

Source		DF	Chi-Square	Prob
Females:	Intercept	1	508.53	0.0000
	Linear	1	28.94	0.0000
	Quadratic	1	2.32	0.1281
	Homogeneity	2	31.08	0.0000
Males:	Intercept	1	109.56	0.0000
	Linear	1	8.94	0.0028
	Quadratic	1	2.62	0.1058
	Homogeneity	2	11.17	0.0038
Both:	Linear	2	37.88	0.0000
	Quadratic	2	4.93	0.0849
	Homogeneity	4	42.25	0.0000
RESIDUAL		0		

ANALYSIS OF WEIGHTED-LEAST-SQUARES ESTIMATES

Effect	Parameter	Estimate	S.E.	Chi-Sq	Prob
MODEL	1 2	1.3309 -0.1730	0.0590 0.0322	508.53 28.94	0.0000
	3	-0.0234	0.0154	2.32	0.1281
	4	0.7868	0.0752	109.56	0.0000
	5	-0.1009	0.0337	8.94	0.0028
	6	-0.0288	0.0178	2.62	0.1058

Contrast	DF	Chi-Square	Prob
Gender	3	33.92	0.0000
I. Eq.	1	32.42	0.0000
L. Eq.	1	2.39	0.1217
Q. Eq.	1	0.05	0.8183
Paral.	2	2.47	0.2909

SAS Output from Reduced Marginal Logit Model Complete Data Only

CATMOD PROCEDURE

Response: A0*A3*A6	Response Levels (R)=	8
Weight Variable: COUNT	Populations $(S)=$	2
Data Set: B	Total Frequency (N)= 1	1973
	Observations (Obs)=	16

	Function	Response		DESIGN M	ATRIX	
Sample	Number	Function	1	2	3 	4
1	1	1.48048	1	0	-1	1
	2	1.37774	1	0	0	-2
	3	1.13453	1	0	1	1
2	1	0.85883	0	1	-1	1
	2	0.84442	0	1	0	-2
	3	0 65711	0	1	1	1

ANALYSIS OF VARIANCE TABLE

Source	DF	Chi-Square	Prob
Intercept: Females	1	508.42	0.0000
Males	1	111.12	0.0000
Linear Time	1	35.44	0.0000
Quad. Time	1	4.98	0.0257
Time	2	39.78	0.0000
RESIDUAL	2	2.47	0.2909

ANALYSIS OF WEIGHTED-LEAST-SQUARES ESTIMATES

Effect	Parameter	Estimate	Standard Error	Chi- Square	Prob
MODEL	1	1.3241	0.0587	508.42	0.0000
	2	0.7911	0.0750	111.12	0.0000
	3	-0.1385	0.0233	35.44	0.0000
	4	-0.0260	0.0116	4.98	0.0257

Contrast	DF	Chi-Square	Prob
Int. Eq.	1	31.45	0.0000

SAS Output: Analysis of All Data

CATMOD PROCEDURE

Response: 077*079*081	Response Levels (R) =	26
Weight Variable: COUNT	Populations (S)=	1
Data Set: A	Total Frequency (N) =	522
	Observations (Obs)=	26

			DESIG	N
	Function	Response	MATRI	X
Sample	Number	Function	1	2
1	1	0.18820	1	0
	2	0.20533	1	2
	3	0.23684	1	4

ANALYSIS OF VARIANCE TABLE

Source	DF	Chi-Square	Prob
Intercept Linear Age	1	85.66 3.83	0.0000 0.0503
RESIDUAL	1	0.15	0.6998

ANALYSIS OF WEIGHTED-LEAST-SQUARES ESTIMATES

Effect	Parameter	Estimate	Standard Error	 Prob
MODEL	1 2		0.0201 0.00613	 0.0000

		ubse	rvea	Pred	ictea	
	Function		Standard		Standard	
Sample	Number	Function	Error	Function	Error	Residual
1	1	0.18820225	0.02071626	0.18631702	0.02013121	0.00188522
	2	0.20533333	0.02085963	0.21031118	0.01638623	-0.0049779
	3	0.23684211	0.02180946	0.23430535	0.0207938	0.00253676

SAS Output: Analysis of Complete Data

$\bullet\,$ Model with linear age effect

Response: 077*079*081	Response Levels (R)=	8
Weight Variable: COUNT	Populations $(S)=$	1
Data Set: B	Total Frequency (N) =	225
Frequency Missing: 0	Observations (Obs)=	8

			DESIG	N
	Function	Response	MATRI	X
Sample	Number	Function	1	2
1	1	0.19556	1	0
	2	0.19111	1	2
	3	0.23111	1	4

ANALYSIS-OF-VARIANCE TABLE

Source	DF	Chi-Square	Prob
Intercept	1	55.03	0.0000
Linear Age	1	1.49	0.2223
RESIDUAL	1	0.95	0.3304

ANALYSIS OF WEIGHTED-LEAST-SQUARES ESTIMATES

Effect	Parameter	Estimate	S.E.	Chi-Sq	Prob
MODEL	1	0.1884	0.0254	55.03	0.0000
	2	0.00829	0.00680	1.49	0.2223

• Model with only an intercept

Sample	Function Number	Response Function	
1	1	0.19556	1
	2	0.19111	1
	3	0.23111	1

ANALYSIS-OF-VARIANCE TABLE

Source	DF	Chi-Square	Prob	
Intercept	1	85.96	0.0000	
RESIDUAL	2	2.44	0.2957	

ANALYSIS OF WEIGHTED-LEAST-SQUARES ESTIMATES

Effect	Parameter	Estimate	S.E.	Chi-Sq	Prob
MODEL	1	0.2039	0.0220	85.96	0.0000

SAS Output from Model 1 (Saturated Marginal Probability Model) All Data

Response: ATTENDO*ATTEND3*ATTEND6	Response Levels (R)=	23
Weight Variable: COUNT	Populations (S)=	2
Data Set: CHURCH	Total Frequency (N) =	3085
Frequency Missing: 0	Observations (Obs)=	44

	Function	Response			DESIGN M	ATRIX		
Sample	Number	Function	1	2	3	4	5	6
1	1	0.76999	1	 -1	1	0	0	0
	2	0.77043	1	0	-2	0	0	0
	3	0.75204	1	1	1	0	0	0
2	1	0.63485	0	0	0	1	-1	1
	2	0.65389	0	0	0	1	0	-2
	3	0.65689	0	0	0	1	1	1

ANALYSIS-OF-VARIANCE TABLE

Source		DF	Chi-Square	Prob
Females:	Intercept	1	7595.57	0.0000
	Linear	1	2.44	0.1183
	Quadratic	1	1.36	0.2442
	Lin & Quad	2	3.28	0.1943
Males:	Intercept	1	2259.45	0.0000
	Linear	1	1.75	0.1860
	Quadratic	1	0.47	0.4932
	Lin & Quad	2	2.73	0.2558
Both:	Linear	2	4.19	0.1232
	Quadratic	2	1.83	0.4014
	Lin & Quad	4	6.00	0.1989
RESTDUAL.		0		

ANALYSIS OF WEIGHTED-LEAST-SQUARES ESTIMATES

Effect	Parameter	Estimate	Standard Error	Chi- Square	Prob
MODEL	1	0.7642	0.00877	7595.57	0.0000
	2	-0.00898	0.00575	2.44	0.1183
	3	-0.00314	0.00270	1.36	0.2442
	4	0.6485	0.0136	2259.45	0.0000
	5	0.0110	0.00833	1.75	0.1860
	6	-0.00267	0.00390	0.47	0.4932

SAS Output from Model 2 (Reduced Marginal Probability Model) All Data

CATMOD PROCEDURE

Response: ATTENDO*ATTEND3*ATTEND6	Response Levels (R)=	23
Weight Variable: COUNT	Populations (S)=	2
Data Set: CHURCH	Total Frequency (N)= 30	85
Frequency Missing: 0	Observations (Obs)=	44

Sample	Function Number	Response Function	MATRI 1	
1	1	0.76999	1	0
	2	0.77043	1	0
	3	0.75204	1	0
0	4	0 63495	0	4
2	1	0.63485	U	1
	2	0.65389	0	1
	3	0.65689	0	1

ANALYSIS-OF-VARIANCE TABLE

Source		DF	Chi-Square	Prob
	Intercept Intercept	1 1	7926.90 2355.15	0.0000
RESIDUAL		4	6.00	0.1989

ANALYSIS OF WEIGHTED-LEAST-SQUARES ESTIMATES

Effect	Parameter	Estimate	Standard Error	V	Prob
MODEL	1 2		0.00860 0.0133		

Contrast	DF	Chi-Square	Prob
Int. Equality	1	60.12	0.0000

SAS Output from Model 1 (Saturated Marginal Probability Model) Separate Analyses of Complete and Incomplete Data within the Same Model

Sample	Function e Number	Respor		1	DESIGN 1	MATRIX 3	4	5
2	1 2 3 4 5 6 1 2 3 4 5 6	0.814 0.798 0.756 0.674 0.600 0.702 0.699 0.658 0.542 0.600	363 367 480 384 000 242 940 361 167	1 1 1 0 0 0 0 0 0 0 0	-1 0 1 0 0 0 0 0 0 0	1 -2 1 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 1 1 1 0 0	0 0 0 0 0 0 0 -1 0 1 0
Sample	Function Number	6	7	DESI 8	GN MATRIX 9	10	11	12
1	1 2 3 4 5	0 0 0 0 0	0 0 0 1 1	0 0 0 -1 0	0 0 0 0 1 -2 1	0 0 0 0 0	0 0 0 0 0	0 0 0 0 0
2	1 2 3 4 5 6	1 -2 1 0 0	0 0 0 0 0	0 0 0 0 0	0 0 0 0 0	0 0 0 1 1	0 0 0 -1 0 1	0 0 1 -2 1
	Source	ANALY	YSIS-OF	-VARIANO DF C	E TABLE Chi-Square	I	Prob	
	C: F-Int Lin Qua M-Int Lin Qua IC: F-Int Lin Qua M-Int Lin Qua RESIDUAL	1. ad 5. 1. ad 6. 1. ad 6. 1. ad		1 1 1 1 1 1 1 1 1 1 1 1 1	6613.87 29.23 2.97 1814.09 8.97 2.76 454.68 0.94 0.02 179.95 0.29 0.68	0.0 0.0 0.0 0.0 0.0 0.3 0.8	0000 0000 0848 0000 0027 0964 0000 3315 3912 0000 5932	
	Contrast	ANA	ALYSIS	OF CONTR DF	RASTS Chi-Squa	re	Prob	
	C=IC C=IC: Int. C=IC: L & C)		6 2 4	82. 31. 1.	76 (0.0000 0.0000 0.8132	

SAS Output from Model 2 (Reduced Marginal Probability Model) Separate Analyses of Complete and Incomplete Data within the Same Model

	Function	Response	DESIGN MATRIX							
Sample	Number	Function	1	2	3	4	5	6	7	8
1	1	0.81465	1	0	 -1	1	0	0	0	0
	2	0.79863	1	0	0	-2	0	0	0	0
	3	0.75667	1	0	1	1	0	0	0	0
	4	0.67480	0	1	-1	1	0	0	0	0
	5	0.64384	0	1	0	-2	0	0	0	0
	6	0.60000	0	1	1	1	0	0	0	0
2	1	0.70242	0	0	0	0	1	0	-1	1
	2	0.69940	0	0	0	0	1	0	0	-2
	3	0.65861	0	0	0	0	1	0	1	1
	4	0.54167	0	0	0	0	0	1	-1	1
	5	0.52000	0	0	0	0	0	1	0	-2
	6	0.60000	0	0	0	0	0	1	1	1

ANALYSIS-OF-VARIANCE TABLE

Source	DF	Chi-Square	Prob	
F: C Int.	1	6616.83	0.0000	
IC Int.	1	1211.19	0.0000	
Linear	1	31.99	0.0000	
Quadratic	1	2.70	0.1002	
M: C Int.	1	1814.16	0.0000	
IC Int.	1	518.87	0.0000	
Linear	1	9.51	0.0020	
Quadratic	1	2.36	0.1245	
RESIDUAL	4	1.58	0.8132	

Contrast	DF	Chi-Square	Prob
C=IC: Int.	 2	81.11	0.0000
F Int.	1	47.73	0.0000
M Int.	1	33.39	0.0000
M=F: L & Q	2	1.01	0.6041
Lin.	1	0.77	0.3813
Quad.	1	0.12	0.7320
Int.: M=F	2	46.27	0.7320
C Int.: M=F	1	29.96	0.0000
IC Int.: M=F	1	16.83	0.0000

SAS Output from Model 3 (Further Reduced Marginal Probability Model) Separate Analyses of Complete and Incomplete Data within the Same Model

	Function	Response			DESIGN MA	ATRIX		
Sample	Number	Function	1	2	3	4	5	6
1	1	0.81465	1	0	0	0	-1	1
	2	0.79863	1	0	0	0	0	-2
	3	0.75667	1	0	0	0	1	1
	4	0.67480	0	1	0	0	-1	1
	5	0.64384	0	1	0	0	0	-2
	6	0.60000	0	1	0	0	1	1
2	1	0.70242	0	0	1	0	-1	1
	2	0.69940	0	0	1	0	0	-2
	3	0.65861	0	0	1	0	1	1
	4	0.54167	0	0	0	1	-1	1
	5	0.52000	0	0	0	1	0	-2
	6	0.60000	0	0	0	1	1	1

ANALYSIS-OF-VARIANCE TABLE

Source	DF	Chi-Square	Prob
F: C Int.	1	6647.83	0.0000
IC Int.	1	1239.44	0.0000
M: C Int.	1	1813.32	0.0000
IC Int.	1	531.98	0.0000
Linear Time	1	40.70	0.0000
Quadratic Time	1	4.92	0.0266
RESIDUAL	6	2.58	0.8590

ANALYSIS OF WEIGHTED-LEAST-SQUARES ESTIMATES

			Standard	Chi-	
Effect	Parameter	Estimate	Error	Square	Prob
MODEL	1	0.7904	0.00969	6647.83	0.0000
	2	0.6485	0.0184	1239.44	0.0000
	3	0.6864	0.0161	1813.32	0.0000
	4	0.5202	0.0226	531.98	0.0000
	5	-0.0269	0.00421	40.70	0.0000
	6	-0.00445	0.00200	4.92	0.0266

DF	Chi-Square	Prob
3	150.89	0.0000
2	50.53	0.0000
1	30.57	0.0000
1	19.95	0.0000
2	81.91	0.0000
1	46.94	0.0000
1	36.06	0.0000
1	122.20	0.0000
1	2.40	0.1211
	3 2 1 1 2 1	3 150.89 2 50.53 1 30.57 1 19.95 2 81.91 1 46.94 1 36.06 1 122.20

SAS Output from Model 4 (Reparameterized Reduced Marginal Probability Model) Separate Analyses of Complete and Incomplete Data within the Same Model

	Function	Response]	DESIGN MA	ATRIX		
Sample	Number	Function	1	2	3	4	5	6
1	1	0.81465	1	0	0	0	0	0
	2	0.79863	1	0	0	0	3	9
	3	0.75667	1	0	0	0	6	36
	4	0.67480	0	1	0	0	0	0
	5	0.64384	0	1	0	0	3	9
	6	0.60000	0	1	0	0	6	36
2	1	0.70242	0	0	1	0	0	0
	2	0.69940	0	0	1	0	3	9
	3	0.65861	0	0	1	0	6	36
	4	0.54167	0	0	0	1	0	0
	5	0.52000	0	0	0	1	3	9
	6	0.60000	0	0	0	1	6	36

ANALYSIS-OF-VARIANCE TABLE

Source	DF	Chi-Square	Prob
F: C Int.	1	6210.65	0.0000
IC Int.	1	1359.51	0.0000
M: C Int.	1	1817.35	0.0000
IC Int.	1	591.57	0.0000
Linear Time	1	0.00	0.9863
Quadratic Time	1	4.92	0.0266
RESIDUAL	6	2.58	0.8590

ANALYSIS OF WEIGHTED-LEAST-SQUARES ESTIMATES

			Standard	Chi-	
Effect	Parameter	Estimate	Error	Square	Prob
MODEL		0.0100	0.0102	CO10 CE	0 0000
MODEL	1	0.8128	0.0103	6210.65	0.0000
	2	0.6710	0.0182	1359.51	0.0000
	3	0.7089	0.0166	1817.35	0.0000
	4	0.5426	0.0223	591.57	0.0000
	5	-0.00007	0.00403	0.00	0.9863
	6	-0.00148	0.000668	4.92	0.0266

Contrast	DF	Chi-Square	Prob
Int.: Equal.	 3	150.89	0.0000
F=M	2	50.53	0.0000
F=M:C	1	30.57	0.0000
IC	1	19.95	0.0000
C=IC	2	81.91	0.0000
C=IC:F	1	46.94	0.0000
M	1	36.06	0.0000
C F=IC M	1	122.20	0.0000
IC F=C M	1	2.40	0.1211