

# Graeme Wilkin - Curriculum Vitae

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<b>Position</b>	Lecturer	<b>Citizenship</b>	Australian
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		<b>Google</b>	<a href="#">Google Scholar Profile</a>

## Personal Profile

I use a range of techniques from differential geometry, geometric analysis and algebraic geometry to study moduli spaces in gauge theory, with particular emphasis on moduli spaces of Higgs bundles and quiver varieties. I have proved new results in Morse theory with a view to computing topological invariants of these moduli spaces, as well as understanding the algebraic structures that arise on the associated Morse complex. In my work I have shown that these structures have a number of surprising connections with Nakajima's constructions in Geometric Representation Theory.

## Employment History

- Aug 2019 - present** - [University of York](#) *Lecturer*
- Jul 2011 - Jun 2019** - [National University of Singapore](#) *Assistant Professor*
- Aug 2009 - Jun 2011** - [University of Colorado](#) *Burnett Meyer Postdoctoral Instructor*
- Jul 2006 - Jun 2009** - [Johns Hopkins University](#) *J.J. Sylvester Assistant Professor*

## Education

- 2001-2006** PhD in Mathematics - [Brown University](#)  
**Thesis title** An analytic stratification of the space of Higgs bundles  
**Thesis Advisor** Georgios Daskalopoulos
- 1994-1999** B.Sc. (Hons) / B. Eng. (Hons) - [University of Melbourne](#)  
*First class honours in Mathematics*  
*First class honours in Electrical Engineering*

## Publications

1. G. Wilkin, *Morse theory for the space of Higgs bundles*, **Communications in Analysis and Geometry**, Vol. 16, No. 2 (2008), pp283-332.  
DOI: [dx.doi.org/10.4310/CAG.2008.v16.n2.a2](https://doi.org/10.4310/CAG.2008.v16.n2.a2), Arxiv: [0611113](https://arxiv.org/abs/0611113)
2. G. Wilkin, *Homotopy groups of moduli spaces of stable quiver representations*, **International Journal of Mathematics**, Vol. 21, No. 9 (2010), pp1219-1238.  
DOI: [doi.org/10.1142/S0129167X1000646X](https://doi.org/10.1142/S0129167X1000646X), Arxiv: [0901.4156](https://arxiv.org/abs/0901.4156)
3. G. Daskalopoulos, R. Wentworth, G. Wilkin, *Cohomology of  $SL(2, \mathbb{C})$  character varieties and the action of the Torelli group*, **Asian Journal of Mathematics**, Vol. 14, No. 3 (2010), pp359-384.  
DOI: [dx.doi.org/10.4310/AJM.2010.v14.n3.a5](https://doi.org/10.4310/AJM.2010.v14.n3.a5), Arxiv: [0808.0131](https://arxiv.org/abs/0808.0131)
4. I. Biswas, G. Wilkin, *Morse theory for the space of Higgs  $G$ -bundles*, **Geometriae Dedicata**, Vol. 149, No. 1 (2010), pp189-203.  
DOI: [doi.org/10.1007/s10711-010-9476-9](https://doi.org/10.1007/s10711-010-9476-9), Arxiv: [1002.1108](https://arxiv.org/abs/1002.1108)
5. G. Daskalopoulos, J. Weitsman, R. Wentworth, G. Wilkin, *Morse theory and hyperkähler Kirwan surjectivity for Higgs bundles*, **Journal of Differential Geometry**, Vol. 87, No. 1 (2011), pp81-116.  
DOI: [doi.org/10.4310/jdg/1303219773](https://doi.org/10.4310/jdg/1303219773), Arxiv: [0701560](https://arxiv.org/abs/0701560)
6. M. Harada, G. Wilkin, *Morse theory of the moment map for representations of quivers*, **Geometriae Dedicata**, Vol. 150, No. 1 (2011), pp307-353.  
DOI: [doi.org/10.1007/s10711-010-9508-5](https://doi.org/10.1007/s10711-010-9508-5), Arxiv: [0807.4734](https://arxiv.org/abs/0807.4734)
7. R. Wentworth, G. Wilkin, *Morse theory and stable pairs*, **Variational Problems in Differential Geometry**, pp142-181, London Math. Soc. Lecture Note Ser., 394, Cambridge Univ. Press, Cambridge, 2012.  
DOI: [doi.org/10.1017/CBO9780511863219.009](https://doi.org/10.1017/CBO9780511863219.009), Arxiv: [1002.3124](https://arxiv.org/abs/1002.3124)
8. S. Bradlow, G. Wilkin, *Morse theory, Higgs fields and Yang-Mills-Higgs functionals*, **Journal of Fixed Point Theory and Applications**, Vol. 11, No. 1 (2012), pp1-41.  
DOI: [doi.org/10.1007/s11784-012-0073-4](https://doi.org/10.1007/s11784-012-0073-4), Arxiv: [1308.1460](https://arxiv.org/abs/1308.1460)
9. R. Wentworth, G. Wilkin, *Cohomology of  $U(2, 1)$  representation varieties of surface groups*, **Proceedings of the London Mathematical Society**, Vol. 106, No. 2 (2013), pp445-476.  
DOI: [doi.org/10.1112/plms/pds048](https://doi.org/10.1112/plms/pds048), Arxiv: [1109.0197](https://arxiv.org/abs/1109.0197)
10. I. Biswas, G. Wilkin, *Anti-holomorphic isometries of hyperkähler manifolds and branes*, **Journal of Geometry and Physics**, Vol. 88 (2015), pp52-55.  
DOI: [doi.org/10.1016/j.geomphys.2014.11.001](https://doi.org/10.1016/j.geomphys.2014.11.001), Arxiv: [1410.6616](https://arxiv.org/abs/1410.6616)
11. G. Wilkin, *Moment map flows and the Hecke correspondence for quivers*, **Advances in Mathematics**, Vol. 320 (2017), pp730-794.  
DOI: [doi.org/10.1016/j.aim.2017.09.011](https://doi.org/10.1016/j.aim.2017.09.011), Arxiv: [1307.3728](https://arxiv.org/abs/1307.3728)
12. G. Daskalopoulos, C. Mese, G. Wilkin, *Higgs bundles over cell complexes and representations of finitely presented groups*, **Pacific Journal of Mathematics**, Vol. 296-1 (2018), pp31-55.  
DOI: [doi.org/10.2140/pjm.2018.296.31](https://doi.org/10.2140/pjm.2018.296.31), Arxiv: [1605.04625](https://arxiv.org/abs/1605.04625)
13. S. Kim, G. Wilkin, *Analytic convergence of harmonic metrics for parabolic Higgs bundles*, **Journal of Geometry and Physics**, Vol. 127 (2018), pp55-67.  
DOI: [doi.org/10.1016/j.geomphys.2018.01.023](https://doi.org/10.1016/j.geomphys.2018.01.023), Arxiv: [1705.08065](https://arxiv.org/abs/1705.08065)
14. N. Ho, G. Wilkin, S. Wu, *Higgs bundles on a nonorientable manifold*, **Communications in Analysis and Geometry**, Vol. 26, No. 4 (2018), pp857-886.  
DOI: [doi.org/10.4310/CAG.2018.v26.n4.a6](https://doi.org/10.4310/CAG.2018.v26.n4.a6), Arxiv: [1211.0746](https://arxiv.org/abs/1211.0746)

15. G. Wilkin, *Equivariant Morse theory for the norm-square of a moment map on a variety*, **International Mathematics Research Notices**, Vol. 2019, No. 15, pp4730-4763.  
DOI: [doi.org/10.1093/imrn/rnx286](https://doi.org/10.1093/imrn/rnx286), Arxiv: [1702.05223](https://arxiv.org/abs/1702.05223)
16. N. Ho, G. Wilkin, S. Wu, *Conditions of smoothness of moduli spaces of flat connections and of representation varieties*, **Mathematische Zeitschrift**, Vol. 293, No. 1-2 (2019), pp1-12.  
DOI: [doi.org/10.1007/s00209-018-2158-2](https://doi.org/10.1007/s00209-018-2158-2), Arxiv: [1610.09987](https://arxiv.org/abs/1610.09987)
17. M. Pflaum, G. Wilkin, *Equivariant control data and neighbourhood deformation retractions*, **Methods and Applications of Analysis (special issue in memory of John Mather)**, Vol. 26, No. 1 (2019), pp13-36.  
DOI: [dx.doi.org/10.4310/MAA.2019.v26.n1.a2](https://dx.doi.org/10.4310/MAA.2019.v26.n1.a2), Arxiv: [1706.09539](https://arxiv.org/abs/1706.09539)
18. V. Mathai, G. Wilkin, *Fractional quantum numbers via complex orbifolds*, **Letters in Mathematical Physics**, Vol. 109, No. 11 (2019), pp2473-2484.  
DOI: [doi.org/10.1007/s11005-019-01190-y](https://doi.org/10.1007/s11005-019-01190-y), Arxiv: [1811.11748](https://arxiv.org/abs/1811.11748)
19. G. Wilkin, *The reverse Yang-Mills-Higgs flow in a neighbourhood of a critical point*, **Journal of Differential Geometry**, Vol. 115, No. 1 (2020), pp111-174.  
DOI: [doi.org/10.4310/jdg/1586224842](https://doi.org/10.4310/jdg/1586224842), Arxiv: [1605.05970](https://arxiv.org/abs/1605.05970)
20. O. Garcia-Prada, G. Wilkin, *Action of the mapping class group on character varieties and Higgs bundles*, **Documenta Mathematica**, Vol. 25 (2020), pp841-868.  
DOI: [doi.org/10.25537/dm.2020v25.841-868](https://doi.org/10.25537/dm.2020v25.841-868), Arxiv: [1612.02508](https://arxiv.org/abs/1612.02508)
21. V. Mathai, G. Wilkin, *Fractional Quantum Numbers, Complex Orbifolds and Noncommutative Geometry*, **Journal of Physics A: Mathematical and Theoretical**, Vol. 54 (2021), No. 31.  
DOI: [doi.org/10.1088/1751-8121/ac0b8c](https://doi.org/10.1088/1751-8121/ac0b8c), Arxiv: [2004.06666](https://arxiv.org/abs/2004.06666)

## Preprints

22. G. Wilkin, *Local behaviour of an analytic function near the unstable set of a critical point*, to appear in **Rocky Mountain Journal of Mathematics** (accepted 10 August 2023).  
Arxiv: [1904.08045](https://arxiv.org/abs/1904.08045)
23. G. Wilkin, *Convolution for quiver varieties via cup product on a Morse complex*, submitted.  
Arxiv: [2305.05545](https://arxiv.org/abs/2305.05545)
24. G. Wilkin, *Flow lines on the moduli space of rank 2 twisted Higgs bundles*, submitted.  
Arxiv: [2408.13098](https://arxiv.org/abs/2408.13098)

## Edited volumes

1. R. Wentworth, G. Wilkin (editors), The Geometry, Topology and Physics of Moduli Spaces of Higgs Bundles, Lecture Notes Series Volume 36, Institute for Mathematical Sciences, National University of Singapore.  
DOI: [doi.org/10.1142/10683](https://doi.org/10.1142/10683)

## Invited Talks

### Lecture series

**July 2018**      *An introduction to Morse theory* (6 hour lecture series)

Institute for Geometry and its Applications, University of Adelaide

**May 2016**     *Algebraic classification of Yang-Mills-Higgs flow lines* (3 hour lecture series)  
KIAS workshop on Higgs bundles and related topics

**July 2015**     *Lectures on the moduli space of Higgs bundles* (8 hour lecture series)  
University of Science and Technology China

### Conference/Seminar talks

**Dec 6, 2023**     *Hitchin systems from curves in an ALE space*  
Conference “Yorkshire-Durham Geometry Day”  
Durham University

**Dec 7, 2022**     *Hitchin systems from curves in an ALE space*  
University of Aberdeen Topology Seminar

**Sep 17, 2022**     *The Morse complex on singular spaces*  
A celebration of Karen Uhlenbeck’s 80th birthday  
IAS, Princeton

**May 18, 2022**     *Partial compactifications of ALE hyperkähler four manifolds of type A*  
UCL Geometry Seminar

**Mar 18, 2022**     *The Morse complex on the space of representations of a quiver with relations*  
SIAM conference on Analysis of PDEs  
Berlin, Germany

**Jun 23, 2021**     *Algebraic and geometric classification of Yang-Mills-Higgs flow lines*  
Conference “8th European Congress of Mathematics”  
Portorož, Slovenia

**Nov 24, 2020**     *Equivariant Morse theory on singular spaces*  
Rutgers University Geometric Analysis Seminar

**May 13, 2020**     *The topology and geometry of spaces of Yang-Mills-Higgs flow lines*  
Conference “Yorkshire-Durham Geometry Day”  
University of Leeds

**Feb 11, 2020**     *Morse theory on singular spaces*  
University of Oxford Geometry and Analysis Seminar

**Jan 13, 2020**     *Morse theory on singular spaces*  
University of Edinburgh Geometry Seminar (EDGE)

**Jul 26, 2019**     *Representations of the Heisenberg algebra on a singular Morse complex*  
University of Adelaide Differential Geometry Seminar

- Dec 20, 2018** *Representations of the Heisenberg algebra on a singular Morse complex*  
Conference "Character Varieties and Topological Quantum Field Theory"  
University of Auckland
- Oct 25, 2018** *Representations of the Heisenberg algebra on a singular Morse complex*  
Conference "Recent Developments in Higgs Theory"  
Laboratory of Mirror Symmetry, Higher School of Economics, Moscow
- Aug 3, 2018** *The topology and geometry of spaces of Yang-Mills-Higgs flow lines*  
University of Melbourne Pure Mathematics Seminar
- Jul 31, 2018** *The topology and geometry of spaces of Yang-Mills-Higgs flow lines*  
University of Queensland Pure Mathematics Seminar
- Jul 27, 2018** *The topology and geometry of spaces of Yang-Mills-Higgs flow lines*  
University of Adelaide Differential Geometry Seminar
- Sep 27, 2017** *Equivariant Morse theory on singular spaces*  
Stanford University Geometry Seminar
- May 15, 2017** *Equivariant Morse theory on singular spaces*  
University of Maryland Geometry Seminar
- May 9, 2017** *Equivariant Morse theory on singular spaces*  
Brown University Geometry Seminar
- May 6, 2017** *The reverse Yang-Mills-Higgs flow in a neighbourhood of a critical point*  
Conference "Geometry and Physics of Augmented Bundles"  
University of Illinois, Urbana-Champaign
- Feb 21, 2017** *The reverse Yang-Mills-Higgs flow in a neighbourhood of a critical point*  
University of Colorado Geometry Seminar
- Jun 16, 2016** *The reverse Yang-Mills-Higgs flow in a neighbourhood of a critical point*  
Conference "New perspectives on Higgs bundles, branes and quantisation"  
Simons Centre for Geometry and Physics
- Jan 11, 2016** *An algebraic description of Yang-Mills-Higgs flow lines*  
Conference "Vector Bundles on Algebraic Curves"  
Centre Interfacultaire Bernoulli, Ecole polytechnique federale de Lausanne
- Oct 9, 2015** *Classification of Yang-Mills flow lines*  
Conference "50 years of the Narasimhan-Seshadri theorem"  
Chennai Mathematical Institute
- Aug 5, 2015** *Morse theory on singular spaces*  
ISAAC 2015 Conference, Special Session on Complex Geometry  
University of Macau

- Jun 12, 2015** *Morse theory for Higgs bundles*  
2015 joint meeting of the AMS and EMS  
Special Session on Higgs Bundles and Character Varieties  
University of Porto
- Sep 25, 2014** *Topology of moduli spaces of Higgs bundles*  
University of Science and Technology China Geometry Seminar
- Jun 17, 2014** *Moment map flows and the Hecke correspondence for quivers*  
Workshop on the Geometry and Physics of Moduli Spaces  
ICMAT Madrid
- Nov 4, 2013** *Moment map flows and the Hecke correspondence for quivers*  
Workshop on Geometry and Representation Theory  
University of Hong Kong
- Sep 2, 2013** *Moment map flows and the Hecke correspondence for quivers*  
University of Maryland, Geometry and Topology Seminar
- Jul 2, 2013** *Moment map flows and the Hecke correspondence for quivers*  
Asian Mathematical Conference  
Busan, South Korea
- Mar 1, 2013** *Moment map flows and the Hecke correspondence for quivers*  
Conference on Differential and Algebraic Geometry related to bundles  
Tata Institute for Fundamental Research
- Sep 26, 2012** *Moment map flows and the Hecke correspondence for quivers*  
National Tsinghua University Geometry and Topology Seminar
- Feb 21, 2012** *Morse theory and Nakajima quiver varieties*  
University of Colorado Geometry Seminar
- Feb 20, 2012** *Some applications of Morse theory*  
University of Colorado Colloquium
- Feb 7, 2012** *Topology of moduli spaces of  $U(2, 1)$  Higgs bundles*  
Workshop on moduli spaces of representations  
Institut Henri Poincare
- Sep 19, 2011** *Cohomology of Higgs bundle moduli spaces*  
National Tsinghua University Geometry and Topology Seminar
- Apr 15, 2011** *Moment map flows and the Hecke correspondence for quivers*  
University of Wisconsin Geometry and Topology Seminar
- Mar 7, 2011** *Moment map flows and the Hecke correspondence for quivers*  
National University of Singapore

<b>Feb 10, 2011</b>	<i>Moment map flows and the Hecke correspondence for quivers</i> University of Sydney
<b>Jan 31, 2011</b>	<i>Moment map flows and the Hecke correspondence for quivers</i> University of Missouri
<b>Dec 1, 2010</b>	<i>Moment map flows and the Hecke correspondence for quivers</i> Brown University Geometry and Topology Seminar
<b>Jun 17, 2010</b>	<i>Morse theory and stable pairs</i> Conference “Vector Bundles on Algebraic Curves” Instituto Superior Tecnico, Universidade de Lisboa
<b>May 13, 2010</b>	<i>Morse theory and stable pairs</i> Workshop on Bundles on Projective Varieties Tata Institute for Fundamental Research
<b>Mar 23, 2010</b>	<i>Morse theory and stable pairs</i> Duke University Geometry and Topology Seminar

## Grants

<b>Sep 2024</b>	<b>Algebraic and Analytic Methods in Gauge Theory</b> London Mathematical Society Workshop Grant
<b>Oct 2024 - Jun 2025</b>	<b>Geometry of very stable and wobbly bundles</b> London Mathematical Society Collaborative Grant
<b>Aug 2018 - Jun 2019</b>	<b>Geometry and topology of singular spaces</b> NUS Academic Research Fund Tier 1 Grant
<b>Sep 2014 - Jan 2018</b>	<b>Morse-Kirwan theory on singular spaces</b> NUS Academic Research Fund Tier 1 Grant
<b>Aug 2011 - Dec 2014</b>	<b>Geometry and Topology of moduli spaces of Higgs bundles and quiver varieties</b> NUS Startup Grant

## Conference Organisation

<b>Sep 4-6, 2024</b>	<a href="#">Algebraic and Analytic Methods in Gauge Theory</a> <a href="#">University of York</a> Three day workshop supported by a London Mathematical Society grant
<b>Aug 1-19, 2016</b>	Geometry, Topology and Dynamics of Moduli Spaces <a href="#">Institute for Mathematical Sciences, Singapore</a> A three week program consisting of two conferences and a week for collaborative work. 96 participants, including 17 graduate students.
<b>Jul 7-Aug 29, 2014</b>	The Geometry, Topology and Physics of Moduli Spaces of Higgs Bundles <a href="#">Institute for Mathematical Sciences, Singapore</a> An eight week program consisting of a summer school, two conferences and time for collaborative work. 136 participants, including 29 graduate students.
<b>Apr 14-Jul 11, 2014</b>	Research Term on the Geometry and Physics of Moduli Spaces <a href="#">ICMAT, Madrid</a> Three month program including a summer school and two workshops.

## Student Supervision

### Supervision of PhD students

- Samuel Engleman** University of York  
August 2022-present  
Supported by an EPSRC fellowship
- Teo Yi Han** National University of Singapore  
Graduated June 2020  
Supported by a [National University of Singapore Research Scholarship](#)  
Thesis title: *Branes in the moduli space of Higgs bundles*  
Currently employed as an Instructor at the National University of Singapore
- Semin Kim** Brown University (co-supervisor)  
Graduated May 2017  
Thesis title: *Harmonic Maps and the Moduli of Higgs Bundles*  
Currently employed as a software engineer at Bloomberg, New York

### Supervision of final year project students at the National University of Singapore

*These students spent one year working on an undergraduate thesis under my supervision*

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|------------------|--|---|
| <b>2017-2018</b> | Chu Khoon Hwa<br>Toh Teck Wei<br>Doron Loh | <i>Constructing the Central Fibre of the Hitchin Fibration</i><br><i>Poincare's Last Gift in Symplectic Geometry</i><br><i>Exactly Solved Models in Statistical Mechanics</i> |
| <b>2016-2017</b> | Nicholas Chin Cheng Hoong                  | <i>Morse Theory on Hilbert Manifolds</i>  |
| <b>2015-2016</b> | Goh Jin Wen<br>Ho Ren An                   | <i>Fractals and Geometric Measure Theory</i><br><i>The Mountain Pass Theorem and its Applications</i>   |
| <b>2014-2015</b> | Tam Keng Seng                              | <i>Tropical Geometry and Auction Prices</i>   |

### Refereeing

I have refereed for a number of journals, including

- *Journal of the American Mathematical Society*
- *Duke Mathematical Journal*
- *Advances in Mathematics*
- *Memoirs of the American Mathematical Society*
- *International Mathematics Research Notices*
- *Selecta Mathematica*
- *Communications in Analysis and Geometry*
- *Asian Journal of Mathematics*
- *Transformation Groups*



- *Advances in Calculus of Variations*
- *Quarterly Journal of Mathematics*
- *Journal of Geometry and Physics*
- *Pure and Applied Mathematics Quarterly*
- *Geometricae Dedicata*
- *International Journal of Mathematics*
- *Journal of the Australian Mathematical Society, and*
- *Bulletin of the Australian Mathematical Society.*