# PROBLEM SET 4 Due back by noon of Tuesday April 11.

Name: LAGANA' DAISY MARTINA

Id: 199481

## Instructions:

- Make sure you are working on your problem set as each problem set is different.
- The answers to the questions of this problem set are to be given exclusively in the answer sheet
- The answers sheet MUST be printed and not photocopied. Photocopies will not be accepted.
- Questions marked with the symbol admit more than one correct answer
- Please fill the boxes in the answer sheet completely using a black pen as follows

Question 1: B C D E

- The answer sheet must not be creased or folded otherwise your problem set won't be graded.
- You can hand back your problem set after the class on Tuesday.



**Question 1** What does it mean for an estimator to be consistent?

- A The estimator converges in probability to the parameter that it is estimating.
- B The estimator is normally distributed.
- The expected value of the estimator is equal to the parameter that it is estimating.
- D The estimator is statistically significant.

**Question 2** What does it mean for an estimator to be unbiased?

- A The expected value of the estimator is equal to the parameter to be estimated.
- B The estimator converges in probability to the parameter to be estimated.
- C As the sample size tends to infinity, the estimator gets closer and closer to the true value of the parameter.
- D The estimator is equal to the parameter to be estimated.

Question 3 . Consider the following linear mode

$$hourlywage_i = \beta_0 + \beta_1 education_i + \beta_2 male_i \times education_i + \beta_3 male_i + u_i$$

We estimate the model and we find that the t-statistic for the significance of  $\beta_2$  is t = -2.18. What can we conclude?

- A The relationship between education and hourly wage depends on the gender of the individual.
- B The difference in hourly wages for men and women is negative, ceteris paribus.
- The effect of education on the hourly wage is the same for men and women.
- D The effect of education on the hourly wage is significant for both men and women.
- |E| None of these answers are correct.

**Question 4** We regress the final grade on the Applied Econometrics and Statistics final exam (from 0 to 30) on the number of hours the students spent studying. Our model is

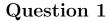
$$final qrade_i = \beta_0 + \beta_1 hours\_study_i + u_i$$

We find that  $\hat{\beta}_1 = 0.2$  and  $SE(\hat{\beta}_1) = 0.01$ . Suppose we measure the *hours\_study<sub>i</sub>* in minutes instead of hours and re-run the regression. What is the standard error of the new estimator of  $\beta_1$ ?

- A 0.00017.
- B 0.01.
- C 0.6.
- D We cannot provide an answer with the info provided.

**Question 5** In a linear model  $y_i = \beta_0 + \beta_1 x_i + u_i$ , the error are conditional homoskedastic if

- A  $Var(u_i)$  is constant.
- B  $Var(y_i|x_i)$  is constant.
- C  $E(y_i|x_i)$  is constant.
- D  $E(u_i|x_i)$  is constant.



You are asked to investigate what are the determinants of car fatalities in the US. You have traffic fatalities data on the "lower 48" US states (i.e. all states with the exception Alaska and Hawaii), for 1988. In particular, you have the following variables:

- fatal vehicle fatalities per ten thousand people
- unemp unemployment rate (measured from 0 to 100)
- income per capita personal income in 1987 (in thousands of dollars)
- beertax tax on case of beer in 1987 dollar
- miles average miles per driver
- jail =1 if state has mandatory jail for drunk driving
- service = 1 if state has mandatory community service
- youngdrivers percent of drivers aged 15-24 (measured from 0 to 1).

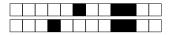
The descriptive statics of the sample are provided in Table 25.

| Statistic    | N  | Mean      | St. Dev.  | Min       | Max        |
|--------------|----|-----------|-----------|-----------|------------|
| fatalities   | 48 | 2.070     | 0.521     | 1.231     | 3.236      |
| unemp        | 48 | 5.456     | 1.838     | 2.400     | 10.900     |
| income       | 48 | 14.894    | 2.628     | 10.699    | 22.193     |
| beertax      | 48 | 0.480     | 0.435     | 0.043     | 2.194      |
| miles        | 48 | 8,615.830 | 1,115.104 | 5,789.922 | 11,812.110 |
| youngdrivers | 48 | 0.162     | 0.022     | 0.073     | 0.221      |

Table 151: Vehicle fatalities: descriptive statistics.

With this goal in mind, you estimate a linear model that relates fatalities and the other variable in the dataset. You obtain:

$$\begin{array}{ll} fatalities &=& 0.5708 + 0.049 \ unemp - 0.0573 \ income + 0.1442 \ beertax \\ &\stackrel{(0.9333)}{=} (0.0363) & (0.0248) & (0.1317) \\ &+ 0.0002 \ miles + 0.1279 \ jail + 0.0973 \ service + 0.3288 \ young drivers \\ &\stackrel{(0.0001)}{=} (0.1622) & (0.1856) & (2.6413) \end{array}$$



### Question 6 What is the interpretation of the coefficient on income?

- A Holding everything else equal, States with higher per-capita personal income have less fatalities. In particular, an extra \$1,000 is associated with a reduction of about 6 fatalities per million of people.
- B Holding everything else equal, States with higher per-capita personal income have less fatalities. In particular, an extra \$1,000 is associated with a reduction of about 0.06 fatalities per hundred of people.
- C Holding everything else equal, States with higher per-capita personal income have less fatalities. In particular, an extra \$2,000 is associated with a reduction of about 1.2 fatalities per hundred of people
- D Holding everything else equal, States with higher per-capita personal income have more fatalities. In particular, an extra \$1,000 is associated with an increase reduction of about 0.6 fatalities per thousand of people.
- E Holding everything else equal, States with higher per-capita personal income have more fatalities. In particular, an extra \$1,000 is associated with an increase reduction of about 6 fatalities per hundred of people.

## Question 7 What is the interpretation of the coefficient on youngdrivers?

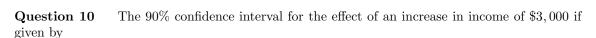
- A one percentage point increase in the fraction of youngdrivers is associated with about 33 more vehicle fatalities per hundred of people, holding everything else equal.
- B A one percentage point increase in the fraction of youngdrivers is associated with about 33 more vehicle fatalities per million of people, holding everything else equal.
- C A one percentage point increase in the fraction of youngdrivers is associated with about 0.33 more vehicle fatalities per ten thousand of people, holding everything else equal.
- D A one percentage point increase in the fraction of youngdrivers is associated with about 0.33 more vehicle fatalities per million of people, holding everything else equal.

#### Question 8 \the What is the interpretation of the coefficient on beertax?

- A Holding other variables constant, taxing a case of beer 50 cent more is associated with an increase in fatalities that can be estimated to about 7 more death per million of people.
- B Holding other variables constant, taxing a case of beer 50 cent more is associated with a decrease in fatalities that can be estimated to about 7 more death per hundred of people.
- C Holding other variables constant, taxing a case of beer one extra dollar cent more is associated with an increase in fatalities that can be estimated to about 0.14 more death per thousand of people.
- D Holding other variables constant, taxing a case of beer one extra dollar cent more is associated with an increase in fatalities that can be estimated to about 0.14 more death per million of people.
- E Holding other variables constant, taxing a case of beer 50 cent more is associated with an increase in fatalities that can be estimated to about 7 more death per hundred of people.
- F None of these answers are correct.

**Question 9** Is the coefficient on beertax statistically different from zero at the  $\alpha = 0.1$  significance level?

- A No, because the t-statistic is not larger than the associated critical value of 1.96.
- B Yes, because the t-statistic is not larger than the associated critical value of 1.96.
- C No, because the t-statistic is larger than the associated critical value of 1.96.
- D Yes, because the t-statistic is larger than the associated critical value of 1.



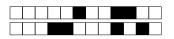
- $\boxed{A}$  (-0.294, -0.049)
- $\boxed{\text{B}}$  (-0.1926, 0.078)
- C (-3.102, -3.012)
- $\boxed{D}$  (-0.217, -0.127)

Question 11 The p-value for a two-sided test on the coefficient on income is 0.0209. What can we conclude?

- A In order to conclude anything, I need to now the whether the errors of the regression are homoskedastic or not.
- B The coefficient is statistically significant at both the  $\alpha = 0.05$  and  $\alpha = 0.10$  level, but not at the  $\alpha = 0.01$  level.
- There is a 96.3% probability that the coefficient is statistically significant.
- D The coefficient is statistically significant at the  $\alpha = 0.01$  level, but not at  $\alpha \ge 0.05$  levels.

Question 12  $\clubsuit$  The  $R^2$  of this regression is 0.64. We run a second regression including one more variable, state investment in road maintenance per mile. The  $R^2$  is now 0.69. What can we conclude?

- $\boxed{\mathbf{A}}$  We cannot conclude much, since the  $R^2$  always increases when a new variable is added to a regression.
- B We should prefer the new regression as it is more meaningful.
- $\boxed{\mathbf{C}}$  Since it increases the  $\mathbb{R}^2$ , the investment variables is statistically significant.
- D The variables in the second model capture about 69% of the variance in fatalities.
- | E | The variables in the first model capture about 64% of the variance in fatalities
- F None of these answers are correct.



## Question 2

Earnings functions are one of the most investigated relationships in economics. These typically relate the earnings to a series of explanatory variables such as education, work experience, gender, race, etc.

Consider using data on a sample of Italian employees aged between 15 and 64. The sample is from the Labor Force Survey from ISTAT which is the most comprehensive survey on labor related issues. The sample we use here is a small subsample (3,000 observations) of the one provided by ISTAT and used in class.

We estimate first a regression model linking hourlywage (monthly net wage divided the hour worked in that month) with years of education (educ) and a dummy for gender (male, which is = 1 if the individual is a male and zero otherwise). The model we consider is the following

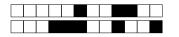
$$\log hourlywage = \beta_0 + \beta_1 educ + \beta_2 male + u.$$

The regression results are shown below:

Table 152: Labor force survey: OLS regression

|          | Dependent variable: |  |  |
|----------|---------------------|--|--|
| educ     | 0.035               |  |  |
|          | (0.006)             |  |  |
| male     | 0.052               |  |  |
|          | (0.027)             |  |  |
| Constant | 3.072               |  |  |
|          | (0.080)             |  |  |

Note: Note: Heteroskedastic robust standard errors in parenthesis.



**Question 13** Given the estimation results, what is the interpretation you can give of  $\beta_1$ , the coefficient on educ?

- $\boxed{\mathbf{A}}$  Controlling for gender, an extra 3 years of education are associated with a decrease in hourly net wage of about 10.5%
- $\fbox{B}$  Controlling for gender, an extra 3 years of education are associated with an increase in hourly net wage of about 10.5%
- $\overline{\mathbb{C}}$  Controlling for gender,  $\beta_2$  is very close to zero and so not important
- D Controlling for gender, an extra year of education is associated with 3.5 extra euro net per month

**Question 14** What would happen to  $\beta_0$  and  $\beta_1$  if we were to substitute the male dummy with a female (which would equal to 1 if the individual is a female and 0 otherwise)?

- A The new intercept will remain unchanged, while the new  $\beta_1$  will be equal to -0.052.
- B The coefficients will not change.
- $\boxed{\text{C}}$  The new coefficients would become  $\beta_0 = 3.124$  and  $\beta_1 = -0.052$ .
- D I don't know: I would need to re-run the regression to give a sensible answer.

**Question 15** Given the estimation results, what is the interpretation you can give of  $\beta_2$ , the coefficient on male?

- A Controlling for education, females work more hours and earn more money.
- B Controlling for education, females work more hours and ern more money.
- C Controlling for education, males tend to earn on average 5.2% higher hourly wage than female.
- D Controlling for education, females tend to earn on average 5.2% higher hourly wage than males.

**Question 16** Which of the following statement is false?

- |A|  $\beta_1$  is not significant at 5% significance level.
- $\boxed{\mathrm{B}}$   $\beta_1$  is statistically significant at 10% significance level.
- $\boxed{\mathbf{C}}$   $\beta_1$  is statistically significant at 0.1% significance level.
- $\square$   $\beta_1$  is statistically significant at 5% significance level.

# Question 3

Consider the following table taken from Stock and Watson's text-book.

|                                 | Dependent variable: |                  |          |         |                   |                   |                  |
|---------------------------------|---------------------|------------------|----------|---------|-------------------|-------------------|------------------|
|                                 | testscore           |                  |          |         |                   |                   |                  |
|                                 | (1)                 | (2)              | (3)      | (4)     | (5)               | (6)               | (7)              |
| str                             | -0.998              | -0.734           | -0.968   | -0.531  | 64.300            | 83.700            | 65.300           |
| 1: 1                            | (0.239)             | (0.231)          | (0.540)  | (0.300) | (25.500)          | (29.700)          | (25.500)         |
| english                         | -0.122 $(0.032)$    | -0.176 $(0.032)$ |          |         |                   |                   | -0.166 $(0.032)$ |
| $str^2$                         | (0.032)             | (0.032)          |          |         | -3.420            | -4.380            | -3.470           |
| str                             |                     |                  |          |         | -3.420<br>(1.290) | -4.380<br>(1.510) | -3.470 (1.290)   |
| $_{str}^3$                      |                     |                  |          |         | 0.059             | 0.075             | 0.060            |
| str-                            |                     |                  |          |         | (0.022)           | (0.025)           | (0.022)          |
| unch                            | -0.547              | -0.398           |          | -0.411  | -0.420            | -0.418            | -0.402           |
|                                 | (0.022)             | (0.030)          |          | (0.029) | (0.028)           | (0.029)           | (0.030)          |
| og(income)                      | (0.0==)             | 11.600           |          | 12.100  | 11.700            | 11.800            | 11.500           |
| ,                               |                     | (1.740)          |          | (1.760) | (1.730)           | (1.750)           | (1.730)          |
| $english \ge 20$                |                     | ` ′              | 5.640    | 5.500   | -5.470            | 816.000           | , ,              |
|                                 |                     |                  | (16.700) | (9.140) | (1.030)           | (435.000)         |                  |
| $str \times (english \ge 20)$   |                     |                  | -1.280   | -0.578  |                   | -123.000          |                  |
| 0                               |                     |                  | (0.844)  | (0.465) |                   | (66.400)          |                  |
| $str^2 \times (english \ge 20)$ |                     |                  |          |         |                   | 6.120             |                  |
| 9                               |                     |                  |          |         |                   | (3.350)           |                  |
| $str^3 \times (english \ge 20)$ |                     |                  |          |         |                   | -0.101            |                  |
|                                 |                     |                  |          |         |                   | (0.056)           |                  |
| Constant                        | 700.000             | 659.000          | 682.000  | 654.000 | 252.000           | 122.000           | 245.000          |
|                                 | (4.690)             | (7.680)          | (10.500) | (8.890) | (166.000)         | (192.000)         | (166.000)        |
| Observations                    | 420                 | 420              | 420      | 420     | 420               | 420               | 420              |
| $\mathbb{R}^2$                  | 0.775               | 0.796            | 0.310    | 0.797   | 0.801             | 0.803             | 0.801            |
| Adjusted R <sup>2</sup>         | 0.773               | 0.794            | 0.305    | 0.795   | 0.798             | 0.799             | 0.798            |

**Question 17** Consider the specification of column (4). What is the interpretation of the coefficient on log(income)?

- A n increase in income of 1% is associated with an increase in testscore of 1.2%
- B An increase in income of 1% is associated with an increase in testscore of 0.12%
- C An increase in income of 1% is associated with an increase in testscore of 12 testcore points
- $\boxed{\mathrm{D}}$  An increase in income of 1% is associated with an increase in testscore of 12%

Question 18 What is the fraction of variance explained by the model in column (4)?

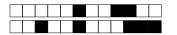
- A 3.1%
- B 80%
- C 31%
- D 78%

**Question 19** What is the fraction of variance explained by the model in column (5)?

- A 80%
- B 3.1%
- C 78%
- D 31%

**Question 20** Consider the regression in column (3). An increase in str from 18 to 19 is associated with

- A a decrease in testscore of about 1
- B a decrease in testscore of about 1.3
- C a decrease in *testscore* of about 2.2
- $\boxed{\mathrm{D}}$  an increase in testscore of about 1.3



**Question 21** Consider the regression in column (3). An increase in str from 17 to 19 is associated with

- $\overline{\mathbf{A}}$  a decrease in testscore of about 2.6
- B an increase in testscore of about 2.6
- C a decrease in *testscore* of about 2
- D a decrease in testscore of about 4.4

+76/10/6+



- Answers must be given exclusively on this sheet: answers given on the other sheets will be ignored.
- This sheet MUST be printed out and not photocopied. Photocopies will not be accepted.
- Please fill the boxes below completely using a black pen.
- Do not crease or fold.
- You can hand back your problem set by putting it into my mailbox on the fifth floor of the viale Romania campus by noon of Friday, March 25 at noon.

| Question | 1:  | A | В    | $\mathbf{C}$ | D |              |   |
|----------|-----|---|------|--------------|---|--------------|---|
| Question | 2:  | A | В    | $\mathbf{C}$ | D |              |   |
| Question | 3:  | A | В    | $\mathbf{C}$ | D | $\mathbf{E}$ |   |
| Question | 4:  | A | В    | $\mathbf{C}$ | D |              |   |
| Question | 5:  | A | В    | $\mathbf{C}$ | D |              |   |
| Question | 6:  | A | В    | $\mathbf{C}$ | D | $\mathbf{E}$ |   |
| Question | 7:  | A | В    | $\mathbf{C}$ | D |              |   |
| Question | 8:  | A | В    | $\mathbf{C}$ | D | $\mathbf{E}$ | F |
| Question | 9:  | A | В    | $\mathbf{C}$ | D |              |   |
| Question | 10: | A | ] [B | [C           | D | ]            |   |
| Question | 11: | A | В    | [C           | D | ]            |   |
| Question | 12: | A | В    | [C           | D | E            | F |
| Question | 13: | A | В    | [C           | D | ]            |   |
| Question | 14: | A | ] [B | [C           | D |              |   |
| Question | 15: | A | В    | [C           | D | ]            |   |
| Question | 16: | A | В    | [C           | D |              |   |
| Question | 17: | A | В    | [C           | D | ]            |   |
| Question | 18: | A | ] [B | [C           | D | ]            |   |
| Question | 19: | A | В    | [C           | D | ]            |   |
| Question | 20: | A | ] [B | [C           | D | ]            |   |

Question 21: A B C D