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**PROBLEM SET 5**  
**Due back by Tuesday May 2.**

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**Instructions:**

- Make sure you are working on your problem set as each problem set is different.
- **The answers to the questions of this problem set are to be given exclusively in the answer sheet**
- **The answers sheet MUST be printed and not photocopied. Photocopies will not be accepted.**
- Questions marked with the symbol ♣ admit more than one correct answer
- Please fill the boxes in the answer sheet completely using a **black pen** as follows

**Question 1:**  ☐ B ☐ C ☐ D ☐ E

- The answer sheet must not be creased or folded otherwise your problem set won't be graded.
- You can hand back your problem set at the **END** of class on May 2.



1

With a sample of 706 observations, we estimate the following model:

$$\ln(hwage_i) = \beta_0 + \beta_1 age_i + \beta_2 age_i^2 + \beta_3 educ_i + \beta_4 yngkid_i + u_i$$

and obtain these results:

$$\ln(hwage_i) = \underset{0.41175}{-1.00179} + \underset{0.01941}{0.07121}age_i - \underset{0.00024}{0.00076}age_i^2 + \underset{0.01116}{0.07131}educ_i + \underset{0.07006}{0.09439}yngkid_i$$

where  $\ln(hwage)$  is the logarithm of the hourly wage in euro,  $age$  is measured in years,  $educ$  is years of education and  $yngkid$  is a variable equal to 1 in case the person has a child younger than three years.

**Question 1** What is the interpretation of  $\beta_3$ ?

- ☐ A An increase of 1% in education is associated with a change of about 7% euros in hourly wage, on average, ceteris paribus.
- ☐ B One year more of education is associated with a change of about 0.07% in hourly wage, on average, ceteris paribus.
- ☐ C One year more of education is associated with a change of about 0.0007 in hourly wage, on average, ceteris paribus.
- ☐ D An increase of 1% in education is associated with a change of about 0.07 euros in hourly wage, on average, ceteris paribus.
- ☐ E One year more of education is associated with a change of about 7% in hourly wage, on average, ceteris paribus.
- ☐ F One year more of education is associated with a change of about 0.07 euros in hourly wage, on average, ceteris paribus.

**Question 2** What is the interpretation of  $\beta_2$ ?

- ☐ A Increasing the square of age by one year, the hourly wage decreases by 0.00077 euros on average, ceteris paribus.
- ☐ B By itself does not have a proper interpretation.
- ☐ C Increasing age by one year, the hourly wage decreases by 0.077% on average, ceteris paribus.
- ☐ D Increasing the square of age by one year, the hourly wage decreases by 0.077% on average, ceteris paribus.

**Question 3 ♣** Is  $\beta_2$  statistically significant?

- ☐ A It is at 5% level.
- ☐ B It is not at 10% level.
- ☐ C It is not at 1% level.
- ☐ D We cannot check for this, it makes no sense.
- ☐ E None of these answers are correct.

**Question 4** What is our null hypothesis when we test whether  $\beta_1$  and  $\beta_2$  are jointly significant?

- ☐ A We check whether the logarithm of hourly wage depends linearly on age.
- ☐ B We check whether the logarithm of hourly wage is 0 when age is equal to 0.
- ☐ C We check whether the logarithm of hourly wage depends on age.
- ☐ D We check whether the relationship between the logarithm of hourly wage and age is convex or concave.



**Question 5** Using a subset of the variables in the previous model, we would like to write a new one such that we obtain the elasticity of the hourly wage to education, and that, given an increase of one year in age, it returns a change in hourly wage in percent points. Choose the correct model among these:

- ☐ A  $hwage_i = \beta_0 + \beta_1 \ln(age_i) + \beta_2 educ_i + u_i$
- ☐ B  $\ln(hwage_i) = \beta_0 + \beta_1 \ln(age_i) + \beta_2 educ_i + u_i$
- ☐ C  $hwage_i = \beta_0 + \beta_1 age_i + \beta_2 \ln(educ_i) + u_i$
- ☐ D  $\ln(hwage_i) = \beta_0 + \beta_1 age_i + \beta_2 \ln(educ_i) + u_i$
- ☐ E  $\ln(hwage_i) = \beta_0 + \beta_1 age + \ln(\beta_2 educ_i) + u_i$

**Question 6** Keeping other variables fixed, at what age the logarithm of hourly wage is maximized?

- ☐ A At about 56.3 years.
- ☐ B At about 46.7 years.
- ☐ C At about 93.3 years.
- ☐ D At about 0, but this makes no sense.



2

Let us define with  $Y$  the amount of cholesterol in mlg in the blood and with  $Med$  a dummy variable which takes the value of 1 for medication B and 0 for medication A, where A and B are two different medications that lower cholesterol. Female is a dummy variable which takes the value of 1 for females and 0 otherwise.

Consider the following regression:

$$Y = \beta_0 + \beta_1 \times med + \beta_2 \times female + \beta_3 \times med \times female + u.$$

**Question 7** What is the effect of using medication B with respect to medication A for men?

- ☐ A None of the others.
- ☐ B  $\beta_0$
- ☐ C  $\beta_1$
- ☐ D  $\beta_1 - \beta_0$
- ☐ E  $\beta_0 + \beta_1$

**Question 8** What is the average cholesterol value for women using medication A?

- ☐ A  $\beta_0 + \beta_2$
- ☐ B None of the others.
- ☐ C  $\beta_0$
- ☐ D  $\beta_2$
- ☐ E  $\beta_0 + \beta_2 + \beta_3$

**Question 3**

These data are taken from the Medical Expenditure Panel Survey survey conducted in 1996. These data were provided by Professor Harvey Rosen of Princeton University and were used in his paper with Craig Perry “The Self-Employed Are Less Likely Than Wage-Earners to Have Health Insurance. So What?” in Douglas Holtz-Eakin and Harvey S. Rosen, eds., *Entrepreneurship and Public Policy*, MIT Press 2004.

Among the variables in the dataset, **ins** is a dummy equal to one if the interviewee has the insurance; **selfemp** is equal to one if the interviewee is a self-employed workers; **gender** is equal to one if the individual is a male; **married** is one if the individual is married; **health** is one if the individual reports to be in good health; **educ** is 0 if the person has no education, 1 if he/she achieved middle school diploma, 2 for the high school diploma, 3 for the bachelor degree, 4 for the master degree and 5 for the PhD; **age** is in years and **age2** is the square of age.

We estimate two models:

$$\begin{aligned} Pr(ins = 1|X) = & \beta_0 + \beta_1 \times selfemp + \beta_2 \times married + \beta_3 \times gender + \beta_4 \times health \\ & + \beta_5 \times gender * health + \beta_6 \times educ + \beta_7 \times age + \beta_8 \times age^2 \end{aligned}$$

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	0.2974634	0.0580248	5.13	0.0000003
selfemp	-0.1742361	0.0141740	-12.29	< 2e-16
married	0.1181062	0.0094187	12.54	< 2e-16
gender	-0.0232270	0.0343575	-0.68	0.49903
health	0.0744310	0.0247243	3.01	0.00262
genderxhealth	-0.0206248	0.0353131	-0.58	0.55920
educ	0.0529807	0.0029210	18.14	< 2e-16
age	0.0105315	0.0027482	3.83	0.00013
age2	-0.0000788	0.0000333	-2.37	0.01796

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Heteroskedasticity robust standard errors used

$$\begin{aligned} Pr(ins = 1|X) = & \Phi(\beta_0 + \beta_1 \times selfemp + \beta_2 \times married + \beta_3 \times gender + \beta_4 \times health \\ & + \beta_5 \times gender * health + \beta_6 \times educ + \beta_7 \times age + \beta_8 \times age^2) \quad (II) \end{aligned}$$

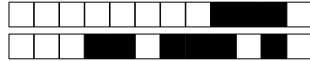
Coefficients:

	Estimate	Std. Error	z value	Pr(> z )
(Intercept)	-0.844932	0.195991	-4.31	0.000016
selfemp	-0.651923	0.046842	-13.92	< 2e-16
married	0.455241	0.034845	13.06	< 2e-16
gender	-0.040238	0.111653	-0.36	0.71856
health	0.300503	0.082988	3.62	0.00029
genderxhealth	-0.124880	0.116613	-1.07	0.28422
education	0.226139	0.012852	17.60	< 2e-16
age	0.029150	0.009899	2.94	0.00323
age2	-0.000162	0.000126	-1.29	0.19821

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**Question 9** Is being self employed significantly linked to having an insurance under model (I)?

- ☐ A No, since the coefficient  $\beta_1$  is not significant.
- ☐ B It depends on the values of all other covariates.
- ☐ C Yes, since the coefficient  $\beta_1$  is significant.
- ☐ D Yes, since the model includes the variable "selfemp".



**Question 10** What is the interpretation of  $\beta_2$  in model (II)?

- ☐ A On average, married individuals are 45.5% less likely than others to have an insurance, controlling for all other factors.
- ☐ B It does not have a proper interpretation in terms of magnitude.
- ☐ C On average, married individuals are 45.5% more likely than others to have an insurance, controlling for all other factors.
- ☐ D On average, a married worker has a probability of 45.5% to have an insurance, *ceteris paribus*.

**Question 11** Does increasing level of education have a significant impact on the probability to buy an insurance at 5% level under model (I)?

- ☐ A No, since the coefficient  $\beta_6$  is not significant.
- ☐ B It depends on the values of all other covariates.
- ☐ C Yes, since the model includes the variable "educ".
- ☐ D Yes, since the coefficient  $\beta_6$  is significant.

**Question 12** Does increasing level of education have a positive impact on the probability to buy an insurance at 5% level under model (II)?

- ☐ A Yes, since the model includes the variable "educ".
- ☐ B No, since the coefficient  $\beta_6$  is not significant.
- ☐ C It depends on the values of all other covariates.
- ☐ D Yes, since the t-test on the coefficient  $\beta_6$  is higher than 1.64.

**Question 13 ♣** Under model (I), which of the following statements are true?

- ☐ A Statistically speaking, having a good health has the same impact on the probability of having an insurance for men and women.
- ☐ B The probability of having an insurance is linked to age in a linear fashion.
- ☐ C The older an individual grows, the higher the probability of having an insurance.
- ☐ D On average, self employed people are less likely to have an insurance, controlling for all other factors.
- ☐ E *None of these answers are correct.*

**Question 14 ♣** Under model (I), which of the following statements are true?

- ☐ A Statistically speaking, having a good health has the same impact on the probability of having an insurance for male and female, holding other factors constant.
- ☐ B A higher education is associated, on average, with an higher probability of having an insurance, *ceteris paribus*.
- ☐ C We cannot interpret the estimated coefficients in terms of magnitude.
- ☐ D If the person is a female, the effect of good health on the probability to have an insurance is  $\beta_4 + \beta_5$ .
- ☐ E *None of these answers are correct.*



**Question 15** Under model (I), at which age is the probability of having an insurance maximized?

- ☐ A It is maximized at the highest possible value of age in our sample.
- ☐ B When the person is 66.82 years old.
- ☐ C We cannot say: we need more data.
- ☐ D When the person is 133.6 years old, but this is unreasonable.

**Question 16** What is the estimated probability that a 24 years old non-educated non-self-employed single female who is not in good health and with middle school diploma will buy insurance coverage?

- ☐ A Approximately 0.5.
- ☐ B More than 95%.
- ☐ C Less than 5%.
- ☐ D I cannot say because the model is nonlinear.







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  - Due back: Tuesday, May 2 (right after class)
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Question 1: ☐ A ☐ B ☐ C ☐ D ☐ E ☐ F

Question 2: ☐ A ☐ B ☐ C ☐ D

Question 3: ☐ A ☐ B ☐ C ☐ D ☐ E

Question 4: ☐ A ☐ B ☐ C ☐ D

Question 5: ☐ A ☐ B ☐ C ☐ D ☐ E

Question 6: ☐ A ☐ B ☐ C ☐ D

Question 7: ☐ A ☐ B ☐ C ☐ D ☐ E

Question 8: ☐ A ☐ B ☐ C ☐ D ☐ E

Question 9: ☐ A ☐ B ☐ C ☐ D

Question 10: ☐ A ☐ B ☐ C ☐ D

Question 11: ☐ A ☐ B ☐ C ☐ D

Question 12: ☐ A ☐ B ☐ C ☐ D

Question 13: ☐ A ☐ B ☐ C ☐ D ☐ E

Question 14: ☐ A ☐ B ☐ C ☐ D ☐ E

Question 15: ☐ A ☐ B ☐ C ☐ D

Question 16: ☐ A ☐ B ☐ C ☐ D