

Deep learning-based channel coding of short packets : an IoT opportunity

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Neural-based communication algorithms

Intended learning outcomes

- Implement a communication chain with a Maximum A Posteriori (MAP) detector
- Implement basic classifiers using neural network
- Implement a neural based decoder which approaches the MAP
- Implement an auto-encoder to implement a point to point communication chain

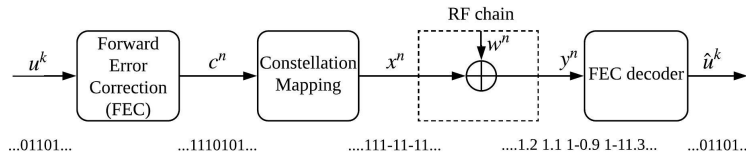
About ...

- Format : short project
- Working teams : in pairs or triplets
- Evaluation : competition at the end of the course

The channel coding problem

Deep channel decoding

The channel coding problem



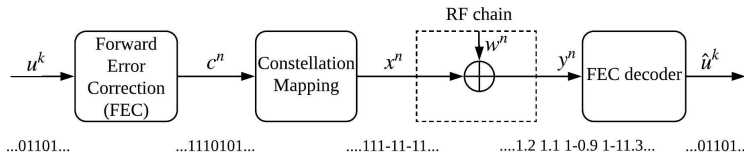
- An information source : bitstream u^k (k bits)
- An error correction code (FEC) : codewords c^n (n bits)
- A constellation mapping, BPSK for instance : channel input x^n (n symbols)
- Adjunction of a memoryless additive noise

$$y^n = x^n + w^n$$

with associated density $P(y^n|x^n)$

- A FEC decoder : an estimate \hat{u}^k (k bits) of u^k

The channel coding problem (cont.)



Construct a FEC encoder and decoder

- Reliability

$$P_e = \mathbb{P}(\hat{U}^k \neq U^k) \rightarrow 0$$

- Spectral efficiency

$$\frac{k}{n} \text{ as high as possible}$$

- Decoding complexity/latency as low as possible

What is the best channel encoder/decoder to achieve the tradeoff?

A bit of History

Shannon enunciated the **capacity** formula in 1948

$$P_e = \mathbb{P}(\hat{U}^k \neq U^k) \rightarrow 0 \quad \text{i.i.f} \quad \frac{k}{n} \leq \max_{P_X} I(X; Y) = f(P_{Y|X})$$

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- Multi-level codes (Ungerbock 1976, Imai & Hirakawa 1977) : Successive cancellation decoding
- LDPC codes (Gallager 1960s, McKay 2000) : Belief propagation
- Turbo-codes (Glavieux & Bérrou 1990) : BCJR, Viterbi
- **Polar codes** (Arikan 2008) : List successive cancellation

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Linear block codes

$$\begin{array}{lcl}
 \text{Encoding} & \underbrace{c^n}_{\text{codeword}} = \underbrace{G}_{\text{generator}} \times \underbrace{u^k}_{\text{information}} \bmod[2] \\
 \text{Decoding} & \underbrace{\hat{u}^k}_{\text{information}} = \underbrace{f_{\text{dec}}}_{\text{decoder}} (\underbrace{y^n}_{\text{received}})
 \end{array}$$

Yet, in IoT ...

Communications are quite costly

- Power consumption
- Memory available
- Computational complexity



<https://www.cio.com/article/2983713/internet>

At **short** and medium blocklength n

- Encoding complexity is reasonable (linear block codes)
- Sub-optimal decoding performances (BP and cycles, Polar and list size)
- Often, high latency/complexity

The need for low complexity, quasi optimal decoders!

The channel coding problem

Deep channel decoding

From Biology to Computer Science

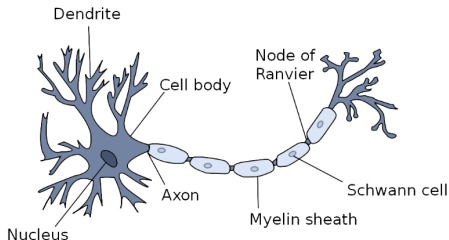
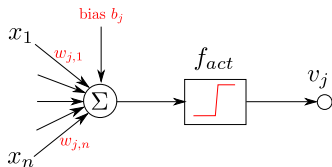
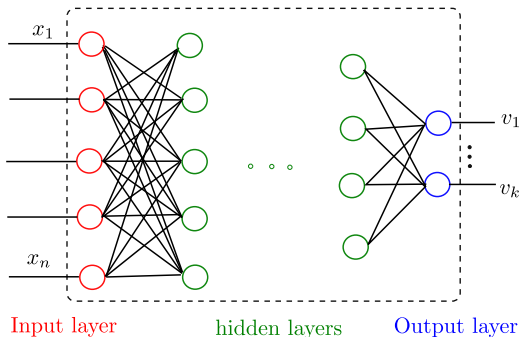


FIGURE – D. Kriesel – A Brief Introduction to Neural Networks



$$v_j = f_{act} \left(\sum_i w_{i,j} x_i + b_j \right)$$

Artificial neural networks

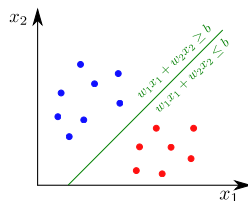


- Set of input vectors $x^n = (x_1, \dots, x_n)$
- Set of expected outputs $v^k = (v_1, \dots, v_k)$
- Training : optimization problem (backpropagation)

$$W^* = \operatorname{argmin}_W \operatorname{Loss} \left(v^k - \hat{v}^k \right)$$

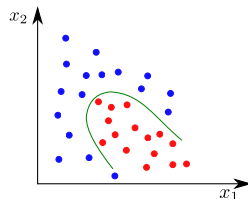
Function approximation

With one layer of perceptrons : all linearly separable functions



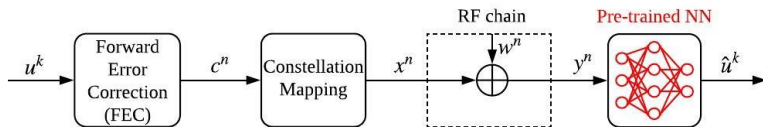
With two layers : all functions

With three layers : all functions and their derivatives

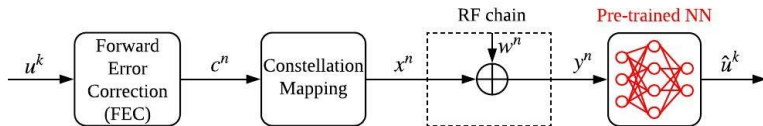


Neural networks are universal function approximators

Neural network-based decoders



Neural network-based decoders



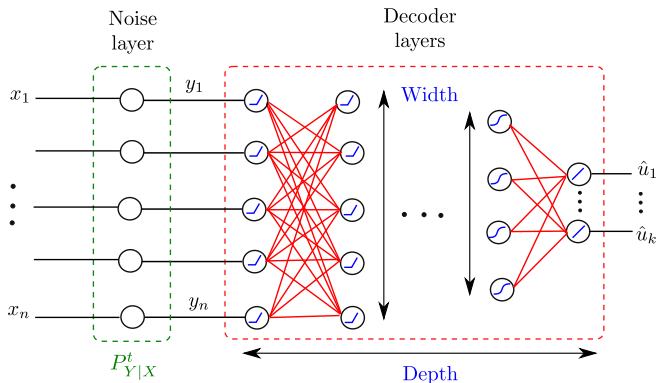
- Fix a FEC encoder $f_e(\cdot)$

$$c^n = f_e(u^k)$$

- Fix a constellation mapping
- Generate the training and validation data set
- Train a neural network offline to recover the sequence

Trade online complexity at the receiver with off-line complexity at the transmitter

Design meta-parameters : Training



How to choose the optimal design metaparameters ?

What's around in literature

Early contributions

- Linear block code decoder [BruckBlaum'89]
- Hamming codes [TalliniCull'95]
- Viterbi decoders [WangWicker'96]

More recent ones

- Improved message passing algorithm [NachmaniBe'eryBurshtein'16]
- Polar decoding [GruberCammererHoydisTenBrink'17]
- LDPC codes [LewandowskiBauch'17]
- Syndrome decoding of block codes [BennatanChoukrounKissilev'18]

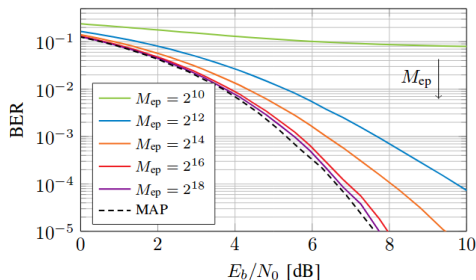
Design is often **heuristic** or **mimics** existing algorithms

What's around in literature

[Gruber-Cammerer-Hoydis-TenBrink'17] investigated

- FEC encoder : Polar code
($k = 8, n = 16$)
- BPSK modulation
- Channel $P_{Y|X}$ Gaussian with variance σ^2
- Network size $[16, 128, 64, 32, 8]$
- Various channel conditions

$$E_b/N_0 = -10 \log_{10}(\sigma^2)$$



A neural network can approach the Maximum A Posteriori