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Name of Assignment: Computer Assignment 3

Due Date: Nov 27th, 2022

Submission Date: Nov 26th, 2022

Hand Written Exercises 1 and 2

### Computer Assignment 3

1) A box of 100 ornamental light bulbs contains:  
40 green, 60 red, and 100 total bulbs

Find probability 3 are red given sampling is done...

a) with replacement: use Binomial:  $P(X=x) = {}_n C_x p^x q^{(n-x)}$   
 $p = .60, q = .40$

$$P(X=3) = {}_4 C_3 (0.6)^3 (0.4)^1 \approx .3456$$

b) without replacement: Use Hypergeometric:  $P(X=x) = \frac{{}_a C_x \cdot {}_b C_{n-x}}{{}_N C_n}$   $N=a+b$

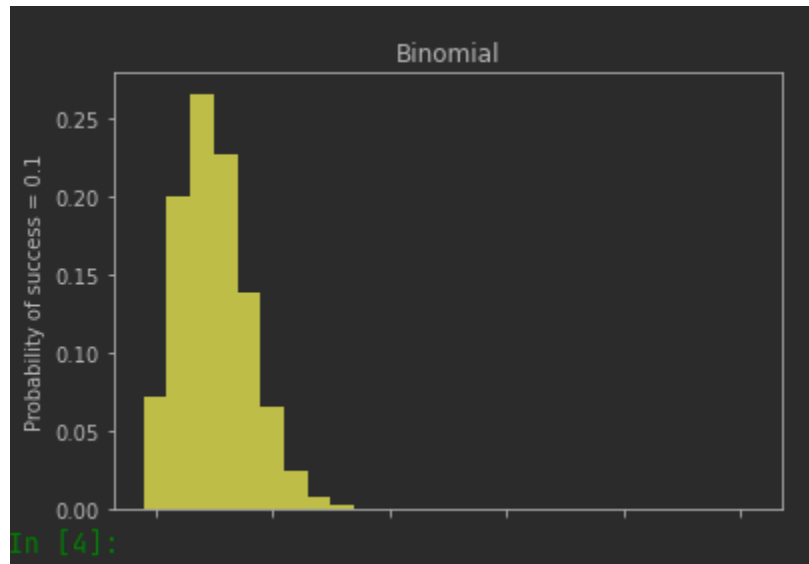
$$P(X=3) = \frac{{}_60 C_3 \cdot {}_{40} C_1}{{}_{100} C_4} \approx .3491$$

2) Prison of 40 Vulcans and 60 Humans, 100 total.  $X$  is RV of vulcans selected.  
4 are sent to be executed. From  $0 \leq X \leq 4$ ,  
Create probability table using Binomial / Hypergeometric

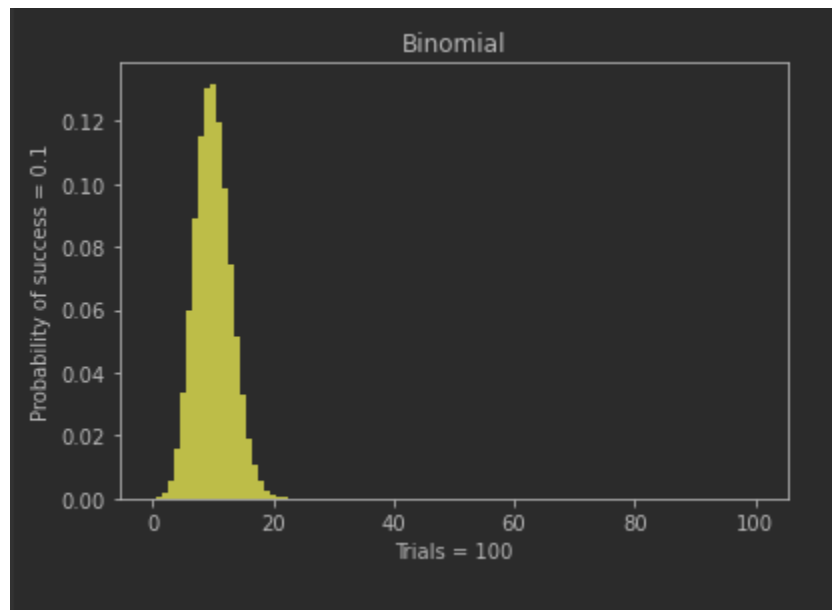
Prob of $X=x$ vulcans	Binomial	Hypergeometric
$P(X=0)$	.1296	.1244
$P(X=1)$	.3456	.3491
$P(X=2)$	.3456	.3521
$P(X=3)$	.1536	.1612
$P(X=4)$	.0256	.0233

## Binomial

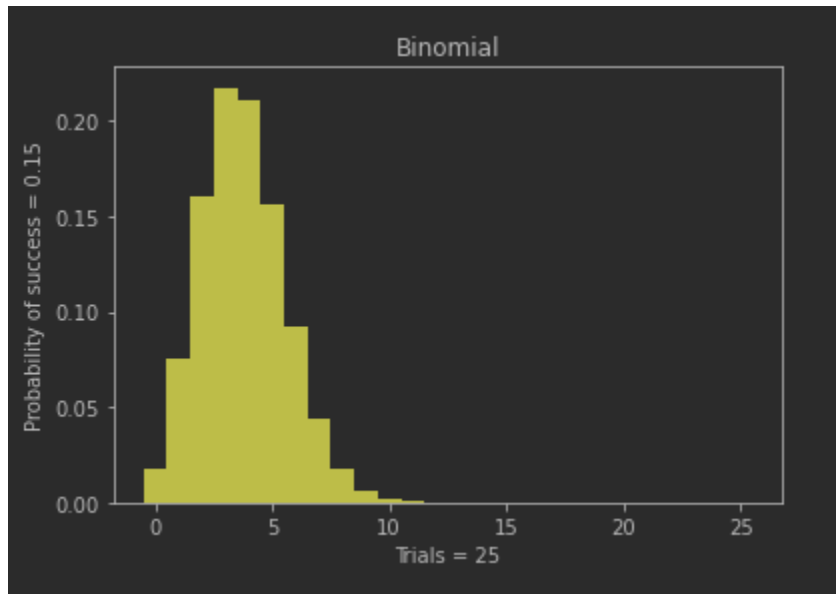
Trials: 25 Prob of Success: 0.1



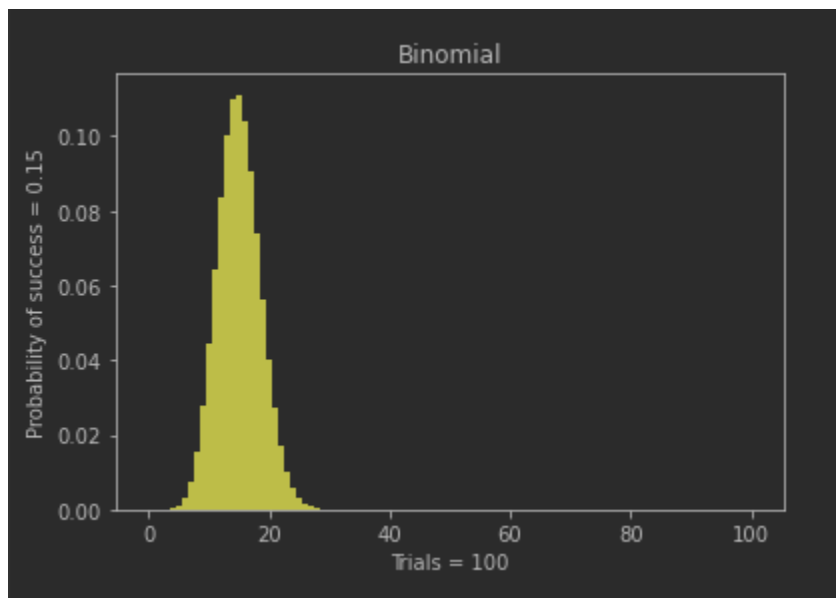
Trials: 100 Prob of Success: 0.1



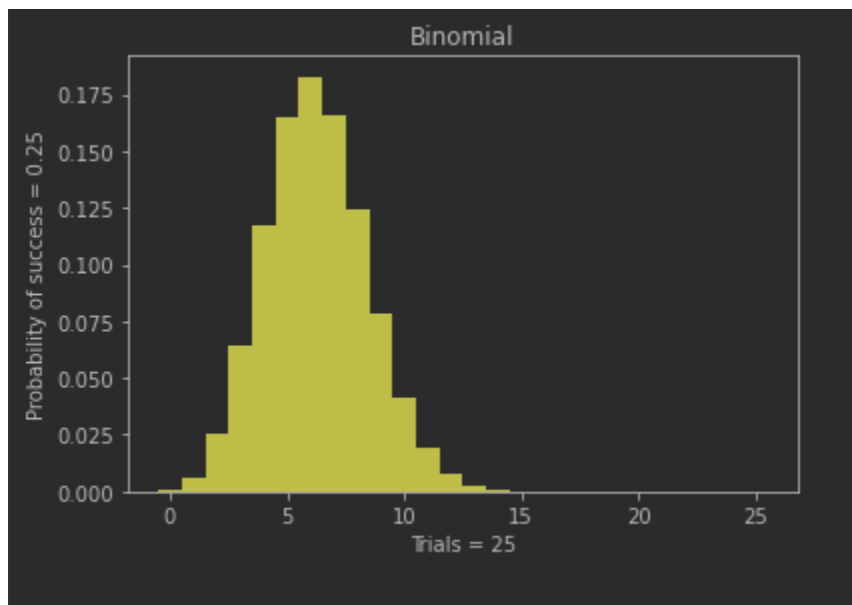
Trials: 25 Prob of Success: 0.15



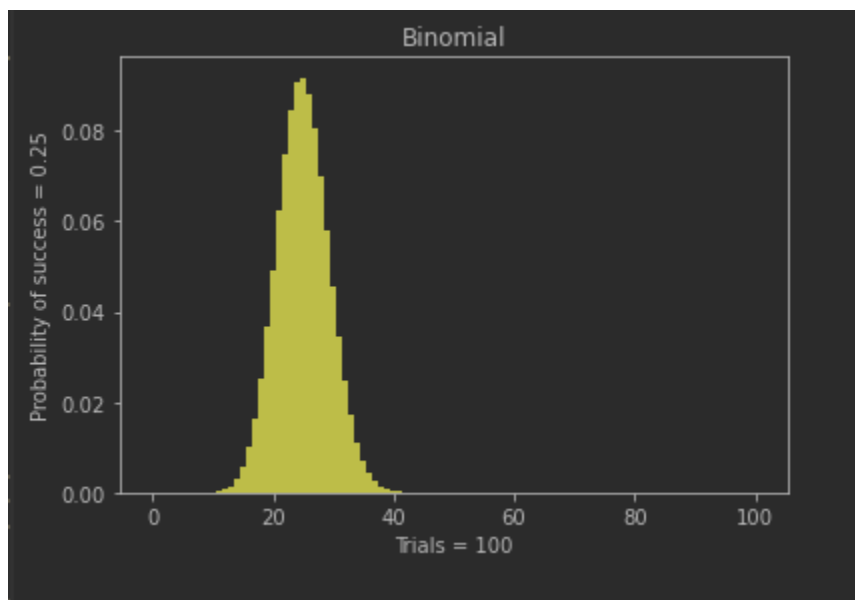
Trials: 100 Prob of Success: 0.15



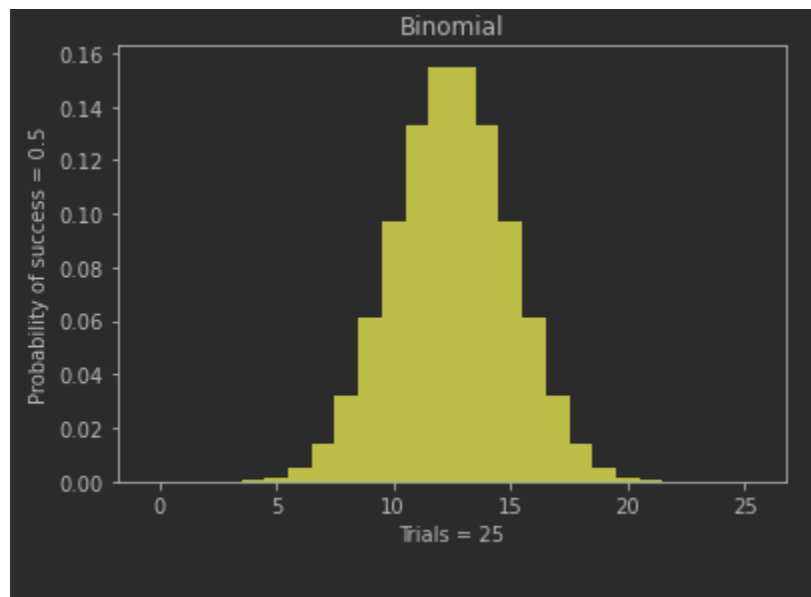
Trials: 25 Prob of Success: 0.25



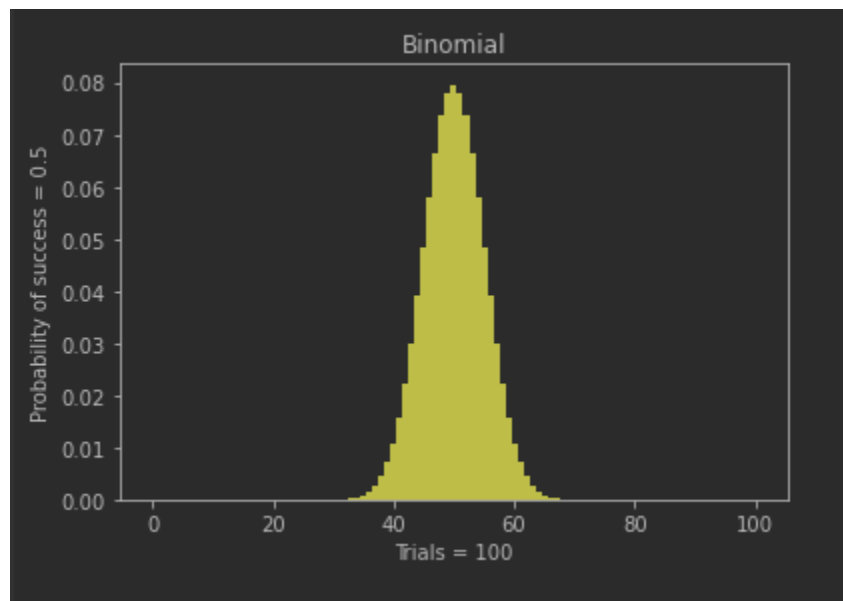
Trials: 100 Prob of Success: 0.25



Trials: 25 Prob of Success: 0.5



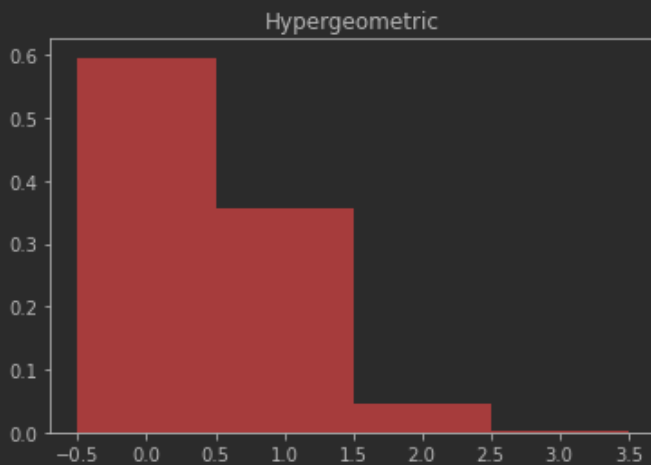
Trials: 100 Prob of Success: 0.5



## Hyper-Geometric:

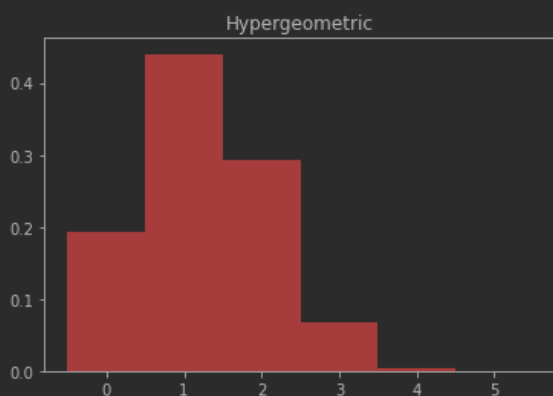
Green: 3 Red: 17

```
Input size of subpopulation of interest. >? 3
Input size of subpopulation not of interest. >? 17
Input size of sample. >? 3
[0, 1, 2, 3]
[0.5964912280701754, 0.35789473684210527, 0.04473684210526316, 0.0008771929824561404]
```

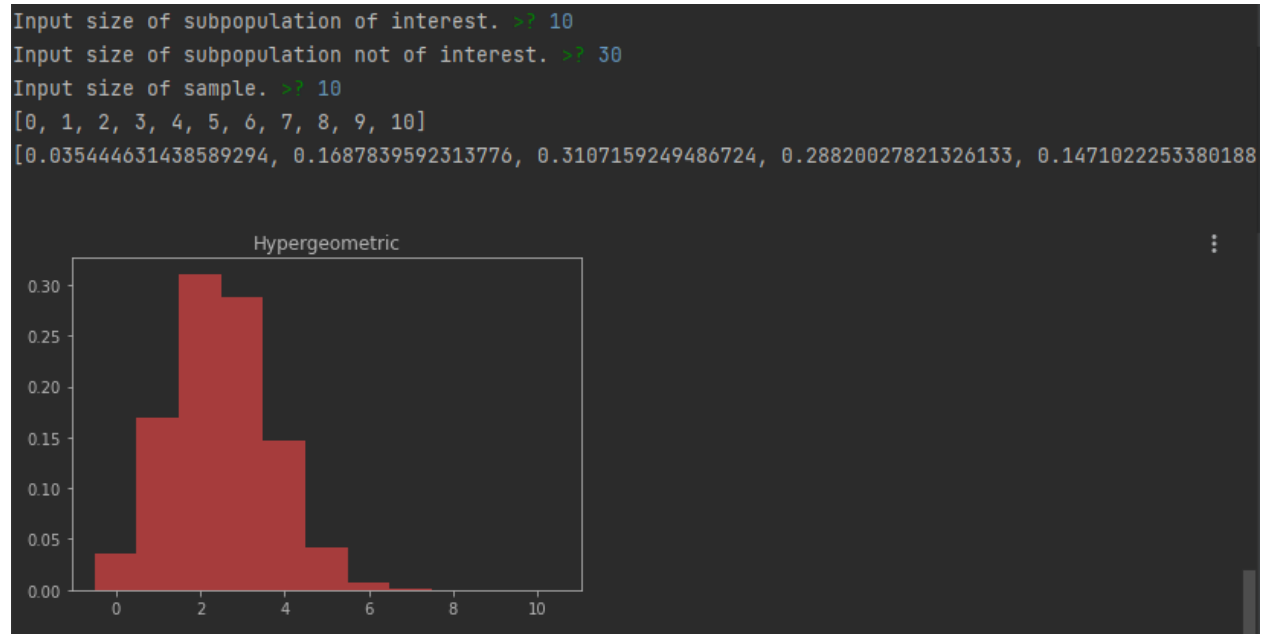


Green: 5 Red: 15

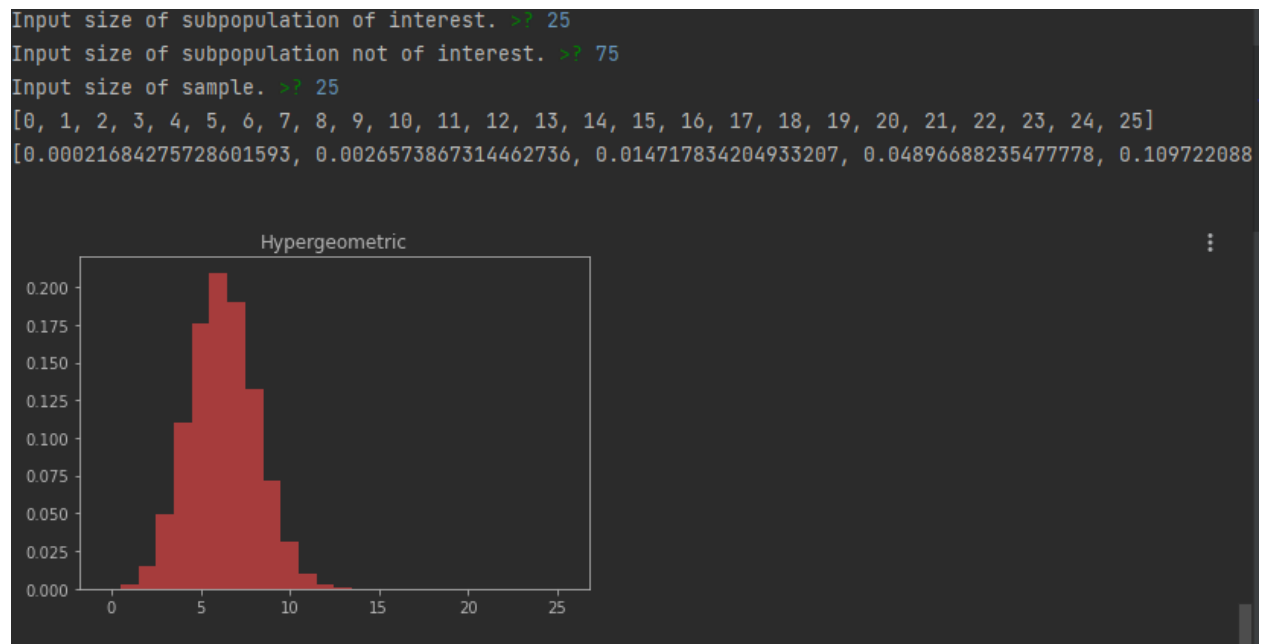
```
Input size of subpopulation of interest. >? 5
Input size of subpopulation not of interest. >? 15
Input size of sample. >? 5
[0, 1, 2, 3, 4, 5]
[0.19369195046439627, 0.44020897832817335, 0.29347265221878227, 0.06772445820433437, 0.004837461300309]
```



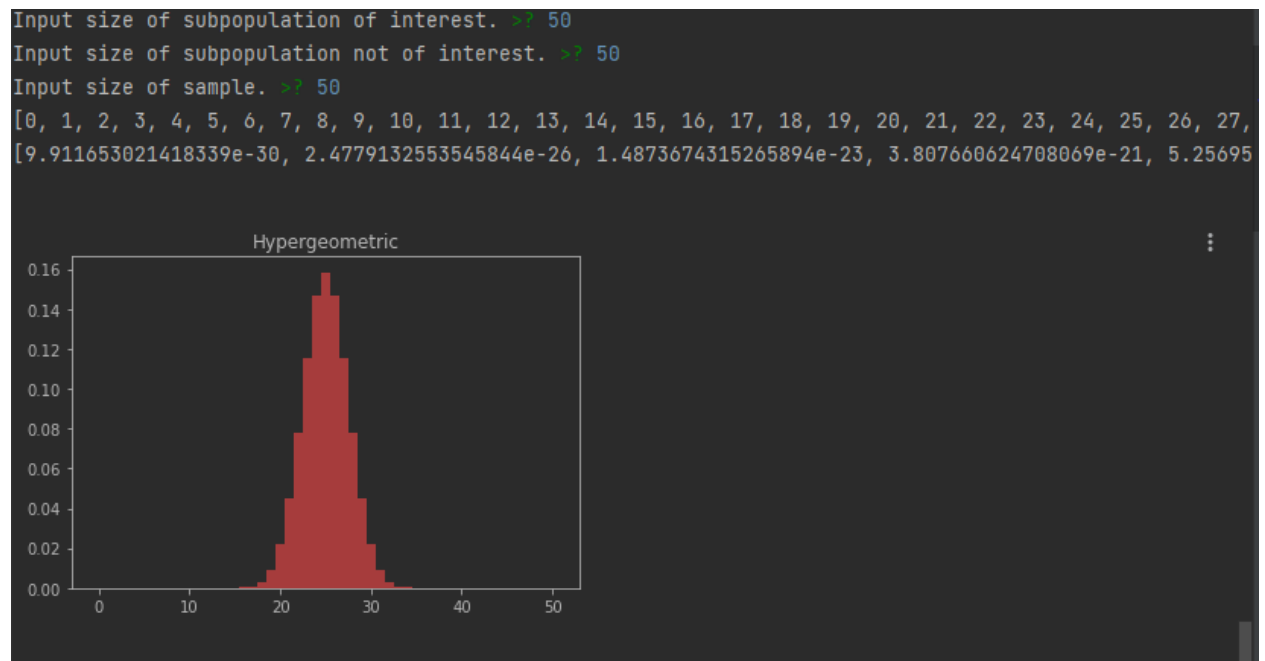
Green: 10 Red: 30



Green: 25 Red: 75



Green: 50 Red: 50



## Binomial VS Error:

Vulcan (40) VS Humans (60):

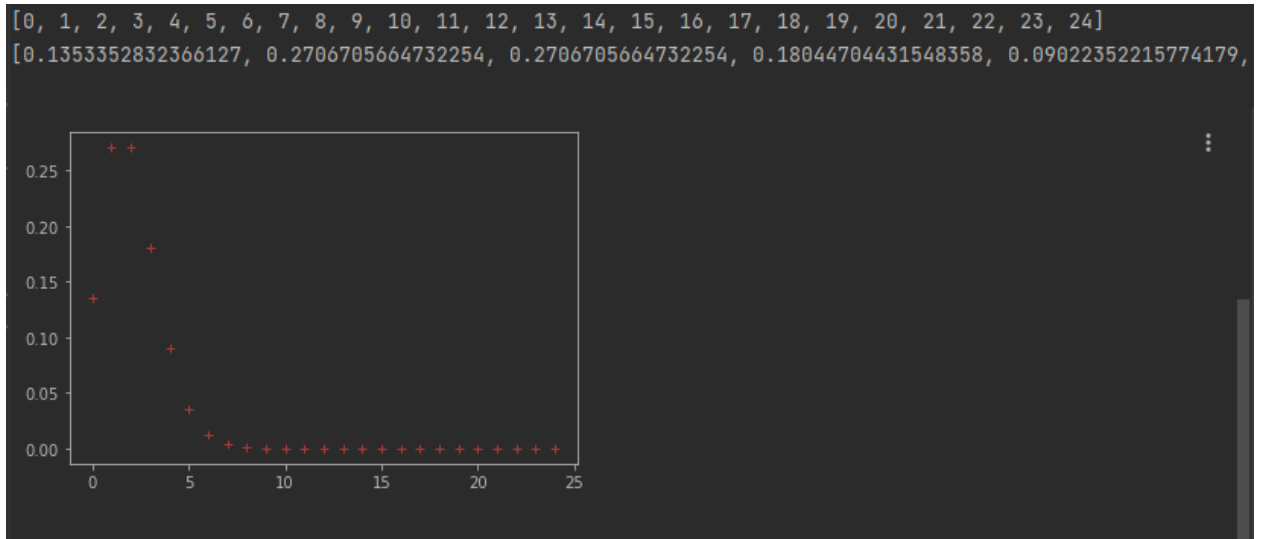
```
Binomial
[0, 1, 2, 3, 4]
[0.1296, 0.34559999999999996, 0.34560000000000001, 0.15360000000000004, 0.025600000000000005]
Hypergeometric
[0, 1, 2, 3, 4]
[0.12435782185413997, 0.3490745876607438, 0.35208385134747433, 0.15117724690626017, 0.023306492231381776]
Error
[0, 1, 2, 3, 4]
[0.005242178145860019, -0.003474587660743822, -0.0064838513474742565, 0.0024227530937398767, 0.0022935077686182283]
```



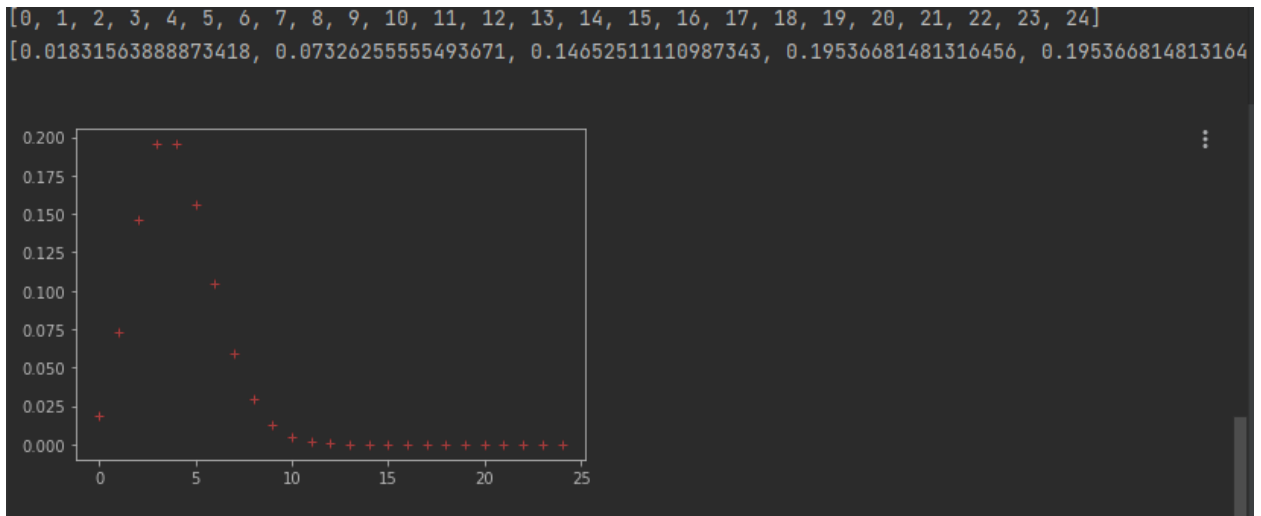


## Poisson:

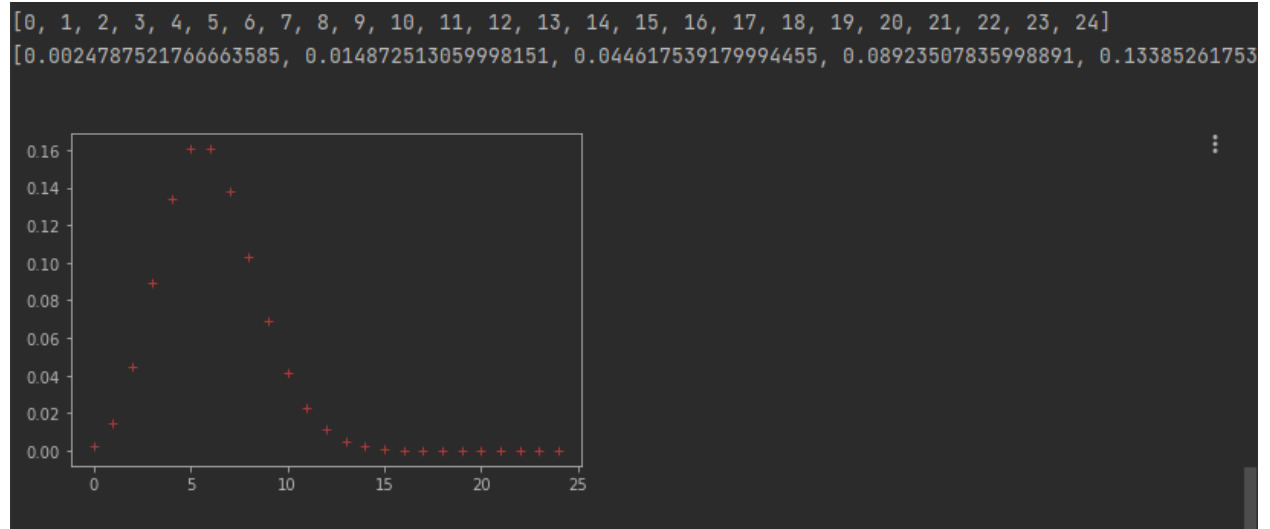
L=2



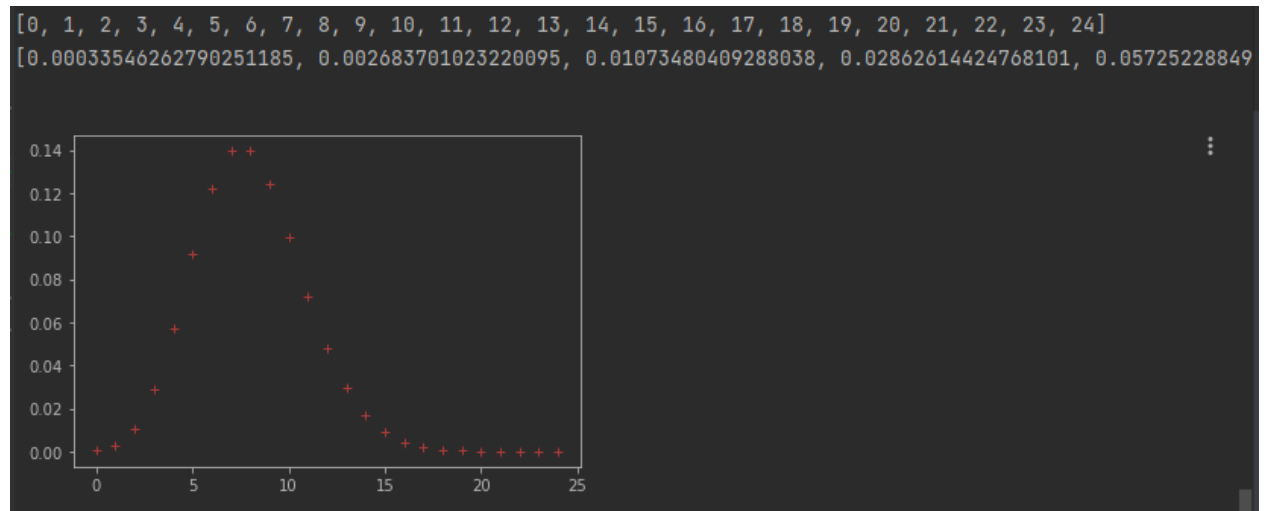
L=4



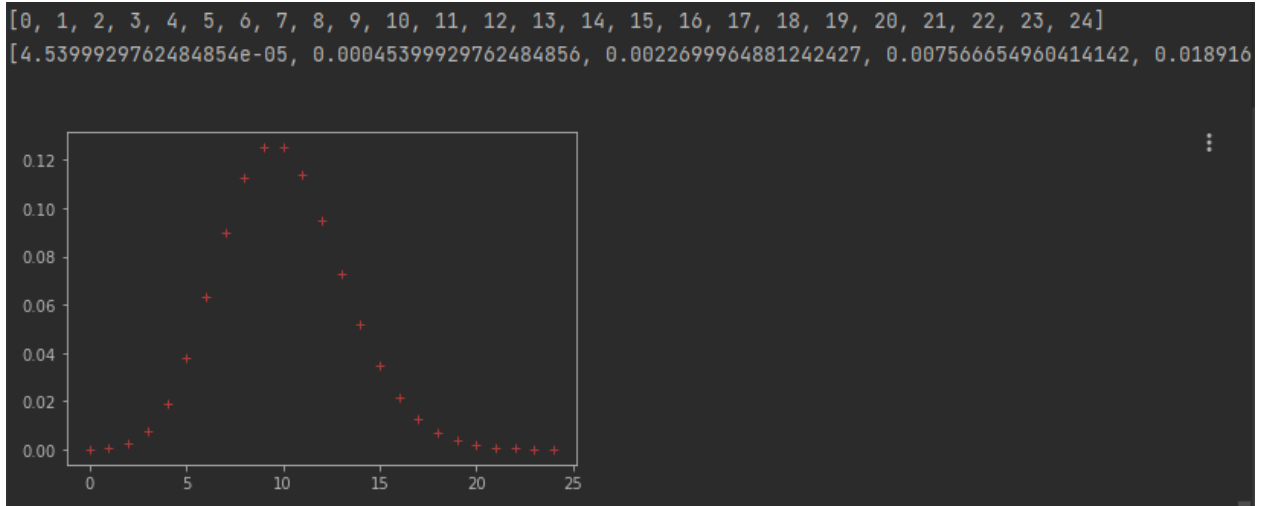
L=6



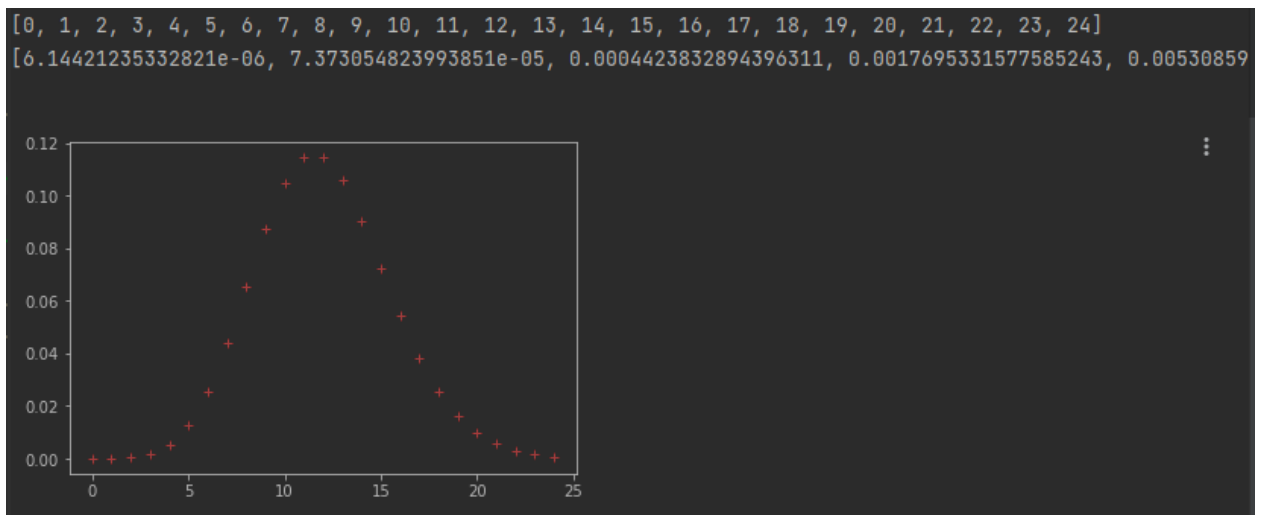
L=8



L=10



L=12



**What happens to the Poisson distribution as the value of the parameter changes?**

- If you have N number of attempts trials, the closer Lambda is to N/2, the more it resembles a standard bell curve.

**How might it play a role in the application of the central limit theorem?**

- The closer you are to the Lth (Lambda-th) trial in the Poisson distribution, the higher the odds you have of succeeding on that trial number. (probability is higher)
- Taking such probabilities of one graph, generating binomial distributions based on those probabilities, and plotting them will result in them being normally distributed at a mean of said Lambda, as dictated by the CLT.