## **Solution 1**

- (1) Probability Distribution of X: Poisson Distribution.

  How it satisfies: Poisson distribution is generally used to model the number of successes per unit area or time (here Cars arrival is the occurrence/success)
- (2)

```
> dpois(5,6.7)
[1] 0.1384904
```

(3)

```
> ppois(5,6.7)
[1] 0.3406494
```

## **Solution 2**

(1)

```
> 1-punif(37,30,40)
[1] 0.3
```

(2)

```
> punif(32,30,40)
[1] 0.2
```

(3)

```
> punif(38,30,40) - punif(34,30,40)
[1] 0.4
```

### **Solution 3**

## **Solution 4**

(1) Probability density function,  $f(x) = \lambda e^{-\frac{\lambda}{x}}$ , where  $\lambda = \frac{1}{5} = 0.2$  and x = 0.2 and x = 0.2 are  $\lambda e^{-\frac{\lambda}{x}}$ .

(2)

```
> pexp(6,rate = 1/5)
[1] 0.6988058
```

(3)

```
> pexp(5,rate = 1/5) - pexp(3,rate = 1/5)
[1] 0.1809322
```

## **Solution 5**

(1)

```
> dbinom(25,400,.07)
[1] 0.06867971
```

(2)

```
> pbinom(24,400,.07)
[1] 0.2511457
```

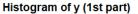
(3)

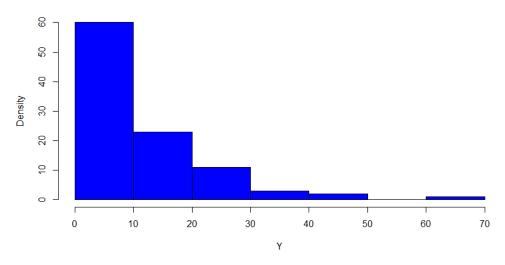
```
> pbinom(25,400,.07) - pbinom(20,400,.07)
[1] 0.2541306
```

### **Solution 6**

1)

```
> x<-rpois(100,3)
> y<-x^2
> hist(y,main = "Histogram of y (1st part)",col = "blue",xlab = "Y", ylab = "Densit
y")
```





2)

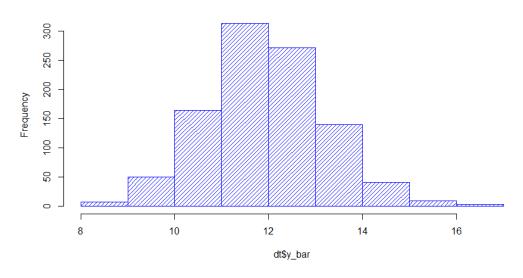
```
> dt<-data.frame(y_bar=0,sd=0) #Initializing an empty data frame
> for (i in 1:1000) { #looping 1000 times to store y_bar in dt
+ x<-rpois(100,3)
+ y<-x^2
+ y_bar<-mean(y)</pre>
```

```
+ sd<-sd(y)
+ dt<-rbind(dt,cbind(y_bar,sd))
+ }
> dt<-data.frame(dt[2:1001,])
> hist(dt$y_bar,col = "blue",density = 20, main = "Histogram of y_bar (1st part)")
```

Histogram below (normally shaped) is generated from random variable X (poisson distributed)

 $E(Y) = approximated by the mean of \overline{Y} \cong 11.94$ 

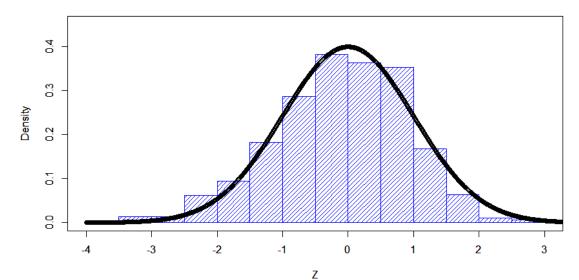
# Histogram of y\_bar (1st part)



3)

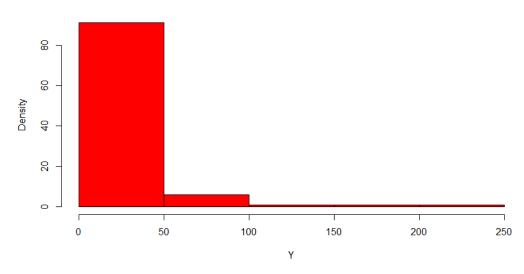
```
> u_bar<-mean(dt$y_bar)
> dt$z<-with(dt, (dt$y_bar - u_bar)/(dt$sd/10))
> hist(dt$z,density = 20,col = "blue", main = "Histogram of Z & fitted normal curve
(1st part)",xlim = c(-4,3),ylim = c(0,0.45),probability = TRUE,xlab = "Z",ylab = "D
ensity")
> par(new = TRUE)
```

### Histogram of Z & fitted normal curve (1st part)



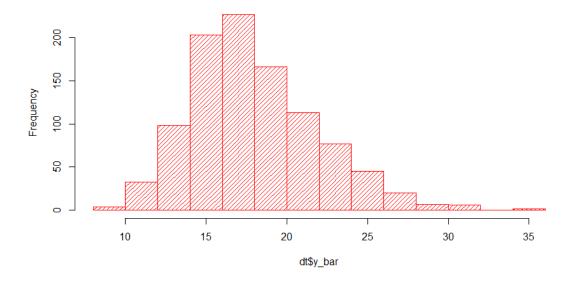
```
> x<-rexp(100,1/3)
> y<-x^2
> hist(y,main = "Histogram of Y (2nd part)", col = "red",xlab = "Y", ylab = "Densit
y")
```

## Histogram of Y (2nd part)



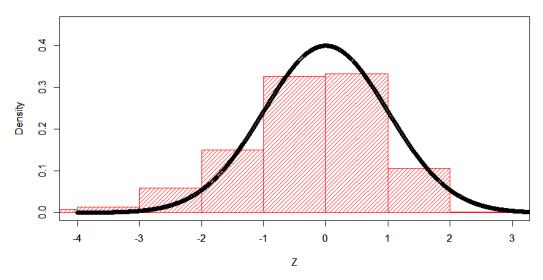
```
> dt<-data.frame(y_bar=0,sd=0) #Initializing an empty data frame
> for (i in 1:1000) { #looping 1000 times to store y_bar in dt
+ x<-rexp(100,1/3)
+ y<-x^2
+ y_bar<-mean(y)
+ sd<-sd(y)
+ dt<-rbind(dt,cbind(y_bar,sd))
+ }
> dt<-data.frame(dt[2:1001,])
> hist(dt$y_bar,col = "red",density = 20, main = "Histogram of y_bar (2nd part)")
```

### Histogram of y\_bar (2nd part)



```
> u_bar<-mean(dt$y_bar)
> dt$z<-with(dt, (dt$y_bar - u_bar)/(dt$sd/10))
> hist(dt$z,density = 20,col = "red", main = "Histogram of Z & fitted normal curve
(2nd part)",xlim = c(-4,3),ylim = c(0,0.45),probability = TRUE,xlab = "Z",ylab = "D
ensity")
> par(new = TRUE)
> plot(seq(-4,4,by = 0.005),dnorm(seq(-4,4,by = 0.005)),xlim = c(-4,3),ylim = c(0,0
.45),xlab = "Z",ylab = "Density")
```

## Histogram of Z & fitted normal curve (2nd part)



<u>Comment:</u> Normal curve fit very good on both the distribution in part 1 { poison: (1), (2), (3) } & part 2 { (4) - exponential}. It implies that whatever was our X (exponential or poison), the distribution of the mean of their samples  $\overline{Y}$  is normally distributed.