

Recursion

→ Process in which function calls itself. That function is called recursive function.

1) Mathematical representation :

→ Let function $f(x)$ be recursive function. Then;

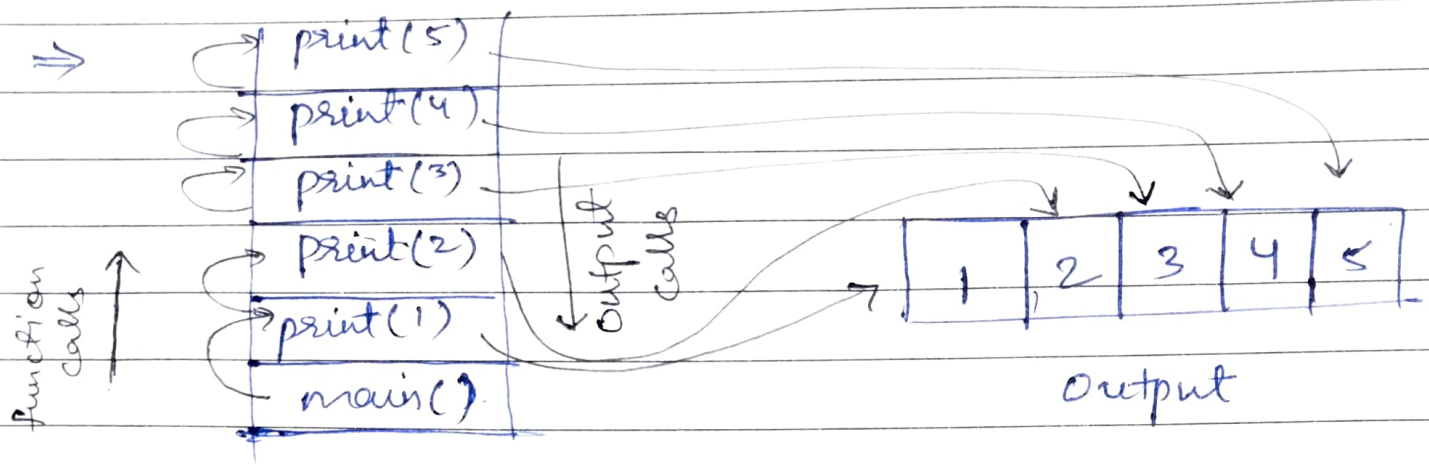
$$f(x) = \begin{cases} 1; & x = 1 \\ x + f(x-1); & x \geq 1 \end{cases}$$

→ Always include base case condition at the start of function.

2) Internal working :

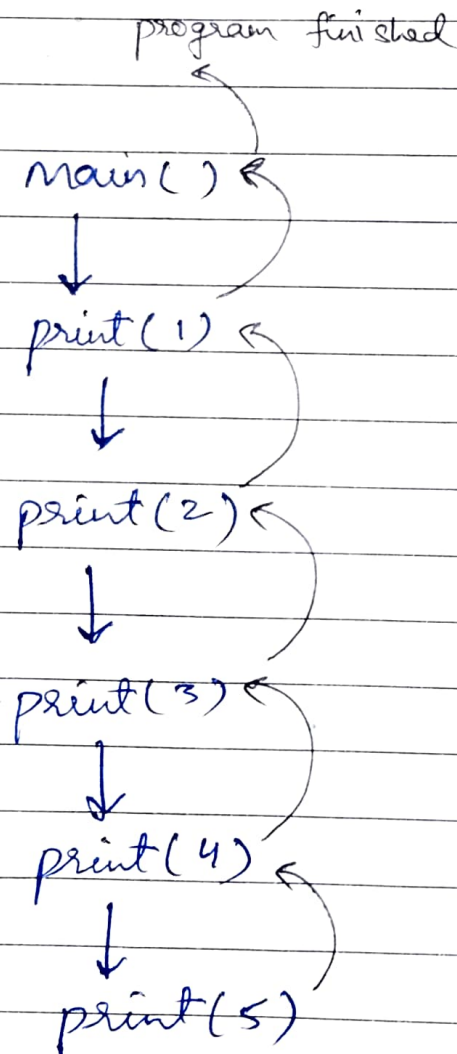
→ Let's print 1 to 5, without multiple calling of functions or o/p statements.

<pre> ⇒ void print (int n) { if (n == 5) { cout << n; return; } cout << n; print (n+1); } </pre>	<pre> void main () { cout << print (1); } </pre>
---	--



Stack
(LIFO rule)

3) Recursive Tree :



4) Stackoverflow condition :

→ If the base case is never reached, then stack overflow occurs.

Ex:

```
int fact(int n)
{
    if (n == 50)
        return 1;
    else
        return n * fact(n-1);
}
```

→ So, for $n=10$, ^{case} base[^] is never reached.

5) Tail recursion :

→ Recursive function is tail recursive when a recursive call is last thing executed by function.

→ It has an advantage in terms of stack usage.

6) Recurrence relations :

→ For factorial : $f(n) = n * f(n-1)$

→ For fibonacci : $f(n) = f(n-1) + f(n-2)$



Date _____

Page no. _____

areBiltz

7) Steps to solve problems :

- Identify if you can break problem into smaller ones.
- Try to form recurrence relation.
- Draw recursive tree
- Understand functions through tree by forming left & right branches.
- Observe what values are returned at each step.