Discussion of

Estimating Social Networks Models with Missing Links

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Outline

Summary

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Setting

• Peer effects regression:

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where G is adjacency matrix of the network

- · Many results on identification and estimation when G is perfectly observed
- · Less is known when G is unobserved or observed with error

This Paper

Peer effects regression when network data is missing at random

- 1. Shows that augmentation bias arises
- 2. Provides 2SLS-based solution when multiple networks are observed

Augmentation Bias

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- · Suppose we observe H with p proportion of links missing
- · Using H as plug-in for G leads to augmentation bias: $\frac{\lambda}{1-p}$ instead of λ
- In OLS: attenuation bias with mean zero white noise measurement error
- Missingness has negative mean
- Intuition: an individual is affected by 5 friends but we misattribute to 3

2SLS with Multiple Networks

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2SLS with Multiple Networks

- Gy is endogenous; use GX or G^2X as "friends-of-friends" instruments
- HX and H^2X are not valid instruments
- With two independent networks, $H^{(2)}X$ can instrument for $H^{(1)}y$
- Asymmetric observations of a symmetric network works too
- Estimate *p* by looking at how many links observed in one network is missing in the other

Discussion

Setting is Important

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- To limit data collection, surveyors may ask respondees to list X friends
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⇒ Results are useful!

What if adjacency matrix is row-normalized?

· Adjacency matrix is often row-normalized:

$$y_i = \lambda \left(\frac{1}{G_i} \sum_{j=1}^n y_j G_{ij} \right) + X_i \beta + \varepsilon_i \quad , \quad G_i = \sum_{j=1}^n G_{ij}$$

Denominator is also changing ⇒ no/attenuation bias?

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 - Networks data often symmetrized in practice, but maybe asymmetry might be important (Comola and Fafchamps, 2014; Auerbach, 2019; Gao, Li, and Xu, 2022)

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- Will matrix completion with low-rank assumption work instead?

Is missingness random in practice?

- · Stronger links may be more likely to be reported (Griffith, 2022)
- · Agents may have incentive to misreport links (Comola and Fafchamps, 2017)
- · What type of non-random missingness can be accommodated?

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