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Problem 5b.
8 total elements.
P(A x B) =
1. {empty_set,
2. {{1, 'beta'}},
3. {{2, 'beta'}},
4. {{3, 'beta'}},
5. {{1, 'beta'}, {2, 'beta'}},
6. {{1, 'beta'}, {3, 'beta'}},
7. {{2, 'beta'}, {3, 'beta'}},
8. {{1, 'beta'}, {2, 'beta'}, {3, 'beta'}}}
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Problem 5e.
  16 total elements.
  P(P(P(A))) =
1. {empty set,
2. {empty_set},
3. {{empty set}},
4. {{ 'beta'}},
5. {{empty set, {beta'}}},
6. {empty_set, {empty_set}},
7. {empty_set, {{'beta'}}},
8. {empty set, {empty set, {'beta'}}},
9. {{empty set}, {{'beta'}}},
10. {{empty_set}, {empty_set, {'beta'}}},
11. {{{'beta'}}, {empty set, {'beta'}}},
12. {empty_set, {empty_set}, {{'beta'}}},
13. {empty_set, {empty_set}, {empty_set, {'beta'}}},
14. {empty set, {{'beta',}}, {empty set, {'beta'}}},
15. {{empty_set}, {{'beta'}}, {empty_set, {'beta'}}},
16. {empty set, {empty set}, {{'beta'}}}, {empty set, {'beta'}}}
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Problem 5d.
   256 total elements.
   P(P(P(A))) =
1. {empty_set,
2. {empty set},
3. \{\{1\}\},
4. {{2}},
5. {{3}},
6. \{\{1, 2\}\},\
7. {{1, 3}},
8. {{2, 3}},
9. {{1, 2, 3}},
10. {empty set, {1}},
11. {empty set, {2}},
12. {empty_set, {3}},
13. \{\text{empty set, } \{1, 2\}\},\
14. {empty_set, {1, 3}},
15. {empty_set, {2, 3}},
16. {empty set, {1, 2, 3}},
17. \{\{1\}, \{2\}\},
18. \{\{1\}, \{3\}\},\
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21. {{1}, {2, 3}},
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33. \{\{1, 2\}, \{2, 3\}\},\
34. \{\{1, 2\}, \{1, 2, 3\}\},\
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42. {empty set, {1}, {2, 3}},
43. {empty_set, {1}, {1, 2, 3}},
44. {empty set, {2}, {3}},
45. {empty_set, {2}, {1, 2}},
46. {empty_set, {2}, {1, 3}},
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