

Homework 03

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Numpy Introduction

- 1a) Create two numpy arrays (a and b). a should be all integers between 25-34 (inclusive), and b should be ten evenly spaced numbers between 1-6. Print all the results below:
- i) Cube (i.e. raise to the power of 3) all the elements in both arrays (element-wise)
- ii) Add both the cubed arrays (e.g., [1,2] + [3,4] = [4,6])
- iii) Sum the elements with even indices of the added array.
- iv) Take the square root of the added array (element-wise square root)___

```
In [25]: import numpy as np
         #a is a numpy array with integers 25-34 inclusive
         a = np.arange(25,35)
         print ("array a: ", a)
         #b is an array of ten evenly spaced numbers between 1 and 6
         b = np.linspace(1,6,num=10)
         print ("array b: ", b)
         #then print
         #i) element wise cube of both
         cubeA = np.power(a,3)
         print ("cube of a: ", cubeA)
         cubeB = np.power(b,3)
         print ("cube of b: ", cubeB)
         #ii) add both cubed arrays (element wise)
         sumCube = cubeA + cubeB
         print ("element added cubed arrays: ", sumCube)
         #iii) sum the elements of even indicies in the new added array
         evenSumCube = sumCube[::2]
         print ("sum of even elements in cube array: ", (evenSumCube))
         #vi) take the square root of array (iii)
         sqrtSumCube = np.power(sumCube, .5)
         print ("square root of the added cube array : ", sqrtSumCube)
         array a: [25 26 27 28 29 30 31 32 33 34]
                               1.55555556 2.11111111 2.66666667 3.22222222 3.777
         array b: [1.
         77778
          4.33333333 4.88888889 5.4444444 6.
         cube of a: [15625 17576 19683 21952 24389 27000 29791 32768 35937 3930
         4 ]
         cube of b: [ 1.
                                    3.76406036 9.40877915 18.96296296 33.45
```

1b) Append b to a, reshape the appended array so that it is a 4x5, 2d array and store the results in a variable called m. Print m.

```
In [27]: temp = np.concatenate([a, b], axis = 0) #append b to a
         print (temp)
         m = temp.reshape(4,5) #reshape the concatenation to a 4x5 matrix
         print (m)
         [25.
                       26.
                                   27.
                                               28.
                                                            29.
                                                                        30.
          31.
                       32.
                                   33.
                                               34.
                                                             1.
                                                                         1.555555
         6
           2.11111111 2.66666667 3.22222222 3.77777778 4.33333333 4.8888888
           5.4444444
                        6.
         [[25.
                        26.
                                    27.
                                                28.
                                                             29.
                                                                        ]
          [30.
                        31.
                                    32.
                                                33.
                                                             34.
                                                                        1
          [ 1.
                        1.5555556 2.11111111 2.66666667
                                                              3.22222221
          [ 3.77777778 4.33333333 4.88888889 5.44444444
                                                              6.
                                                                        ]]
```

1c) Extract the third and the fourth column of the m matrix. Store the resulting 4x2 matrix in a new variable called m2. Print m2.

1d) Take the dot product of m2 and m store the results in a matrix called m3. Print m3. Note that Dot product of two matrices $A.B = A^{T}B$

1e) Round the m3 matrix to three decimal points. Store the result in place and print the new m3.

```
In [35]: m3 = np.around(m3, decimals=3)
    print (m3)

[[1713.235 1778.741 1844.247 1909.753 1975.259]
       [1770.889 1839.012 1907.136 1975.259 2043.383]]
```

1f) Sort the m3 array so that the highest value is at the bottom right and the lowest value is at the top left. Print the sorted m3 array.

```
In [52]: m3 = m3.reshape(1,10)

m3 = np.sort(m3)

m3 = m3.reshape(2,5)

print (m3)

[[1713.235 1770.889 1778.741 1839.012 1844.247]
      [1907.136 1909.753 1975.259 1975.259 2043.383]]
```

NumPy and Masks

2a) create an array called 'f' where the values are cosine(x) for x from 0 to pi with 50 equally spaced values in f

- print f
- use a 'mask' and print an array that is True when $f \ge 1/2$ and False when f < 1/2
- create and print an array sequence that has only those values where f>= 1/2

```
In [42]: f = np.linspace(0,np.pi,50)
                                          f = np.cos(f)
                                         print (f)
                                         mask = (f>=1/2)
                                         print (mask)
                                          fWithMask = f[mask]
                                         print (fWithMask)
                                          [ 1.
                                                                                                        0.99794539 0.99179001
                                                                                                                                                                                                                   0.98155916
                                                                                                                                                                                                                                                                        0.96729486
                                                                                                                                                                                                                                                                                                                              0.9490557
                                                                                                    0.90096887 0.8713187
                                                                                                                                                                                                                   0.8380881
                                                                                                                                                                                                                                                                         0.80141362
                                                  0.92691676
                                                                                                                                                                                                                                                                                                                              0.7614459
                                         6
                                                   0.71834935 0.67230089 0.6234898
                                                                                                                                                                                                                   0.57211666
                                                                                                                                                                                                                                                                        0.51839257
                                                                                                                                                                                                                                                                                                                              0.4625382
                                                  0.40478334 0.34536505 0.28452759 0.22252093 0.1595999
                                                                                                                                                                                                                                                                                                                              0.0960230
                                         3
                                                  0.03205158 - 0.03205158 - 0.09602303 - 0.1595999 - 0.22252093 - 0.2845275
                                              -0.34536505 -0.40478334 -0.46253829 -0.51839257 -0.57211666 -0.6234898
                                              -0.67230089 \ -0.71834935 \ -0.76144596 \ -0.80141362 \ -0.8380881 \ -0.8713187
                                              -0.90096887 -0.92691676 -0.94905575 -0.96729486 -0.98155916 -0.9917900
                                              -0.99794539 -1.
                                          [ True True True
                                                                                                                                                            True
                                                                                                                                                                                                                                             True
                                                                                                                                  True
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                                             False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False False 
                                             False False
                                                                                               0.99794539 0.99179001 0.98155916 0.96729486 0.94905575
                                              0.92691676 0.90096887 0.8713187
                                                                                                                                                                                                0.8380881 0.80141362 0.76144596
                                              0.71834935 0.67230089 0.6234898 0.57211666 0.51839257
```

NumPy and 2 Variable Prediction

Let 'x' be the number of miles a person drives per day and 'y' be the dollars spent on buying car fuel (per day).

We have created 2 numpy arrays each of size 100 that represent x and y. x (number of miles) ranges from 1 to 10 with a uniform noise of (0,1/2) y (money spent in dollars) will be from 1 to 20 with a uniform noise (0,1)

```
In [44]: # seed the random number generator with a fixed value
   import numpy as np
   np.random.seed(500)

x=np.linspace(1,10,100)+ np.random.uniform(low=0,high=.5,size=100)
   y=np.linspace(1,20,100)+ np.random.uniform(low=0,high=1,size=100)
   print ('x = ',x)
   print ('y= ',y)
```

```
x = [1.34683976 1.12176759]
                              1.51512398 1.55233174 1.40619168 1.65
075498
  1.79399331
              1.80243817
                         1.89844195
                                      2.00100023
                                                  2.3344038
                                                               2,2242487
2
  2.24914511
              2.36268477
                          2.49808849
                                       2.8212704
                                                   2.68452475
                                                               2.6822942
7
  3.09511169
              2.95703884
                          3.09047742
                                       3.2544361
                                                   3.41541904
                                                               3.4088637
5
  3.50672677
              3.74960644
                          3.64861355
                                       3.7721462
                                                   3.56368566
                                                               4.0109270
1
  4.15630694
              4.06088549
                          4.02517179
                                       4.25169402
                                                   4.15897504
                                                               4.2683533
3
  4.32520644
              4.48563164
                          4.78490721
                                       4.84614839
                                                   4.96698768
                                                               5.1875425
9
  5.29582013
              5.32097781
                          5.0674106
                                       5.47601124
                                                   5.46852704
                                                               5.6453745
2
  5.49642807
              5.89755027
                          5.68548923
                                       5.76276141
                                                   5.94613234
                                                               6.1813571
3
  5.96522091
              6.0275473
                          6.54290191
                                       6.4991329
                                                   6.74003765
                                                               6.8180980
7
  6.50611821
              6.91538752
                          7.01250925
                                       6.89905417
                                                   7.31314433
                                                               7.2047229
7
  7.1043621
              7.48199528
                          7.58957227
                                       7.61744354
                                                   7.6991707
                                                               7.8543682
2
  8.03510784
              7.80787781
                          8.22410224
                                       7.99366248
                                                   8.40581097
                                                               8.2891379
2
  8.45971515
              8.54227144
                          8.6906456
                                       8.61856507
                                                   8.83489887
                                                               8.6630965
R
  8.94837987
              9.20890222
                          8.9614749
                                       8.92608294
                                                   9.13231416
                                                               9.5588989
6
  9.61488451
              9.54252979
                          9.42015491 9.90952569 10.00659591 10.0250426
5
 10.07330937 9.93489915 10.0892334 10.365099911
    [ 1.6635012
                  2.0214592
                              2.10816052 2.26016496 1.96287558 2.955
4635
  3.02881887
              3.33565296
                         2.75465779 3.4250107
                                                   3.39670148
                                                               3.3937776
7
              4.38293049
                         4.32963586
                                       4.03925039
                                                   4.73691868
  3.78503343
                                                               4.3009839
9
  4.8416329
              4.78175957
                          4.99765787
                                       5.31746817
                                                   5.76844671
                                                               5,9372374
  5.72811642
              6.70973615
                          6.68143367
                                       6.57482731
                                                   7.17737603
                                                               7.5486325
2
  7.30221419
              7.3202573
                          7.78023884
                                       7.91133365
                                                   8.2765417
                                                               8.6920328
1
  8.78219865
              8,45897546
                         8.89094715 8.81719921
                                                  8.87106971
                                                               9,6619256
2
  9.4020625
              9.85990783 9.60359778 10.07386266 10.6957995 10.6672191
6
 11.18256285 10.57431836 11.46744716 10.94398916 11.26445259 12.0975482
 12.11988037 12.121557
                         12.17613693 12.43750193 13.00912372 12.8640719
 13.24640866 12.76120085 13.11723062 14.07841099 14.19821707 14.2728900
 14.30624942 14.63060835 14.2770918 15.0744923 14.45261619 15.1189731
```

```
15.2378667 15.27203124 15.32491892 16.01095271 15.71250558 16.2948850 6
16.70618934 16.56555394 16.42379457 17.18144744 17.13813976 17.6961362 5
17.37763019 17.90942839 17.90343733 18.01951169 18.35727914 18.1684126 9
18.61813748 18.66062754 18.81217983 19.44995194 19.7213867 19.7196672 6
19.78961904 19.64385088 20.69719809 20.07974319]
```

3a) Find Expected value of x and the expected value of y

```
In [45]: avX = np.average(x)
avY = np.average(y)

print ("E[x] = ", avX)
print ("E[y] = ", avY)

E[x] = 5.782532541587923
E[y] = 11.012981683344968
```

3b) Find variance of distributions of x and y

```
In [46]: varX = np.var(x)
    print ("var(x) = ", varX)
    var(x) = 7.03332752947585

In [47]: varY = np.var(y)
    print ("var(y) = ", varY)
    var(y) = 30.113903575509635
```

3c) Find co-variance of x and y.

```
In [50]: EofXY = np.average(np.multiply(x, y))
#print ("E[XY] = ", EofXY)

covXY = EofXY - (avX*avY)

print (covXY)
```

14.511166394475424

3d) Assuming that number of dollars spent in car fuel is only dependant on the miles driven, by a linear relationship.

Write code that uses a linear predictor to calculate a predicted value of y for each x ie y_p redicted = $f(x) = y_p$.

```
In [57]:
         def linear predictor for 3d(input array):
             slope = covXY/varX
             yInt = avY - (slope*avX)
             y predicted = (slope*(input array))+yInt
             return y predicted
In [58]:
         linear_predictor_for_3d(x)
Out[58]: array([ 1.86125717,
                               1.39688809,
                                            2.20846128,
                                                         2.28522836,
                                                                       1.98371207,
                 2.48829527,
                               2.78382468,
                                            2.80124813,
                                                         2.9993232 ,
                                                                       3.21092152,
                 3.8988
                               3.67152796,
                                            3.7228942 ,
                                                         3.9571493 ,
                                                                       4.23651436,
                 4.9033035 ,
                               4.62116978,
                                                         5.46829307,
                                            4.61656787,
                                                                       5.18342105,
                 5.45873164,
                               5.79701128,
                                            6.12915141,
                                                         6.11562653,
                                                                       6.31753758,
                 6.81864709,
                               6.61027849,
                                            6.86515115,
                                                         6.43505522,
                                                                       7.35780389,
                 7.65775187,
                              7.46087825,
                                            7.38719373,
                                                         7.85455455,
                                                                       7.66325667,
                 7.88892606,
                              8.00622544,
                                            8.33721481,
                                                         8.95468038,
                                                                       9.08103323,
                               9.78539799, 10.00879629, 10.06070164,
                 9.33034895,
                                                                       9.53754157,
                10.38056671, 10.36512531, 10.72999716, 10.42269073, 11.25028634,
                10.81276185, 10.97218988, 11.35052091, 11.83583685, 11.38990445,
                11.51849632, 12.58177632, 12.49147206, 12.98850691, 13.14956122,
                12.50588416, 13.35028889, 13.5506705 , 13.31658991, 14.17094102,
                13.947246 , 13.74018137, 14.51931443, 14.74126735, 14.79877137,
                14.96739089, 15.28759454, 15.66049665, 15.1916755, 16.05043004,
                15.57498655, 16.42533161, 16.18461169, 16.53654675, 16.70687695,
                17.01300263, 16.86428603, 17.31062607, 16.95616347, 17.54476017,
                18.08227006, 17.57177784, 17.49875711, 17.92425351, 18.80438359,
                18.91989301, 18.77061069, 18.51812677, 19.5277969, 19.72807224,
                19.76613158, 19.8657155 , 19.58014745, 19.89856998, 20.4677379
         7])
```

3e) Predict y for each value in x, put the error into an array called y error

```
In [59]: predicted_y = linear_predictor_for_3d(x)
         y error = predicted y - y
         print (y_error)
         [ \ 0.19775597 \ -0.62457111 \ \ 0.10030076 \ \ 0.02506341 \ \ 0.02083649 \ -0.4671682
          -0.24499418 -0.53440482 0.24466541 -0.21408918 0.50209852
                                                                          0.2777502
         9
          -0.06213923 -0.42578118 -0.0931215
                                                0.86405311 -0.1157489
                                                                          0.3155838
           0.62666017 0.40166149 0.46107377 0.47954311 0.3607047
                                                                          0.1783890
           0.58942116 0.10891094 -0.07115518 0.29032384 -0.74232081 -0.1908286
           0.35553767 0.14062095 -0.39304511 -0.0567791 -0.61328502 -0.8031067
          -0.77597321 \ -0.12176065 \ 0.06373323 \ 0.26383402 \ 0.45927925 \ 0.1234723
           0.60673379 0.20079382 - 0.0660562
                                                 0.30670405 -0.33067419
                                                                          0.062778
          -0.75987212 \quad 0.67596798 \quad -0.65468531 \quad 0.02820071 \quad 0.08606832 \quad -0.2617114
          -0.72997592 -0.60306068 0.40563939 0.05397013 -0.02061681
                                                                          0.2854892
          -0.7405245
                        0.58908804 0.43343988 -0.76182107 -0.02727604 -0.3256440
          -0.56606805 -0.11129392 0.46417555 -0.27572093 0.5147747
                                                                          0.1686214
           0.42262995 - 0.08035574 \quad 0.72551112 - 0.43596616 \quad 0.71282602 - 0.1102733
          -0.16964259 0.14132301 0.58920807 -0.31716141 0.17248631 -0.7399727
           0.16712997 0.17284167 -0.33165948 -0.52075457 -0.43302563
                                                                          0.6359709
           0.30175553 0.10998314 -0.29405306 0.07784496 0.00668554
                                                                          0.0464643
         1
           0.07609646 - 0.06370343 - 0.79862812 0.387994771
In [61]: print (np.average(y_error))
```

1.27675647831893e-15

3f) Write code that calculates the root mean square error(RMSE), that is root of average of y-error squared