Grant Molnar

Curriculum Vitae

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Education

PhD, Mathematics, Dartmouth College, Hanover, NH Fall 2018 - Spring 2023

Advisor: John Voight

Thesis: Counting elliptic curves with a cyclic m-isogeny over $\mathbb Q$

MA, Mathematics, Dartmouth College, Hanover, NH Fall 2018 - Winter 2020

Advisor: John Voight

MS, Mathematics, Brigham Young University, Provo, UT Winter 2017 - Summer 2018

Advisors: Michael Griffin and Paul Jenkins Thesis: *The arithmetic of modular grids*

BS, Mathematics, *Brigham Young University*, Provo, UT Fall 2013 - Fall 2016

Professional Experience

Academic Researcher at BYU and Dartmouth

Fall 2013 - Spring 2023

At BYU, I proved results about modular forms and algorithms on graphs. At Dartmouth, I instigated successful research into summing divergent series, the Prisoner's Dilemma, and the Ramanujan-Robin criterion. My thesis develops the arithmetic statistics of elliptic curves with cyclic m-isogeny. See Research Publications and Preprints below.

Math Instructor at BYU and Dartmouth

Winter 2017 - Spring 2023

I taught 30-student calculus courses in three different styles: lecturing, virtually with a "flipped classroom", and with handouts and group exercises. I TAed for lower-division courses, and by special request for upper-division courses as well. See Teaching Experience below.

Computer Skills

Fluent in...

 $\mathsf{Bash} \, \bullet \, \mathsf{Git} \, \bullet \, \mathsf{Go} \, \bullet \, \mathsf{Java} \, \bullet \, \mathsf{LATEX} \, \bullet \, \mathsf{Python} \, \bullet \, \mathsf{R} \, \bullet \, \mathsf{SageMath} \, \bullet \, \mathsf{YAML}$

Experience with...

C++ • gRPC • HTML • Magma • Mathematica • MatLab • MongoDB • PARI/GP • Rust

Books

Puzzle and Proof: A Decade of Problems from the Utah Math Olympiad, with Samuel Dittmer, Hiram Golze, and Caleb Stanford

AK Peters/CRC Recreational Mathematics Series.

This book is a collection of 70 mathematical problems and puzzles from the first ten years of the Utah Math Olympiad (UMO), 2013–2022. These problems are distinguished in two respects. First, they aim to be *understandable* to an advanced high school audience, even if solving them can sometimes be quite difficult. Second, all of the problems ask for not only an answer, but a *proof*.

Research Publications

Counting elliptic curves over the rationals with a 7-isogeny, with John Voight

Research in Number Theory 9, 75 (2023). arXiv: 2212.11354

We count by height the number of elliptic curves over the rationals, both up to isomorphism over the rationals and over an algebraic closure thereof, that admit a cyclic isogeny of degree 7.

Reactive means in the Iterated Prisoner's Dilemma, with Caroline Hammond and Feng Fu Applied Mathematics and Computation 458 128201 (2023). arXiv: 2302.13909

The Iterated Prisoner's Dilemma (IPD) is a well studied framework for understanding direct reciprocity and cooperation in pairwise encounters. However, measuring the morality of various IPD strategies is still largely lacking. Here, we partially address this issue by proposing a suit of plausible morality metrics to quantify four aspects of justice. We focus our closed-form calculation on the class of reactive strategies because of their mathematical tractability and expressive power. We define reactive means as a tool for studying how actors in the IPD and Iterated Snowdrift Game (ISG) behave under typical circumstances. We compute reactive means for four functions intended to capture human intuitions about "goodness" and "fair play". Two of these functions are strongly anticorrelated with success in the IPD and ISG, and the other two are weakly anticorrelated with success. Our results will aid in evaluating and comparing powerful IPD strategies based on machine learning algorithms, using simple and intuitive morality metrics.

The arithmetic of modular grids, with Michael Griffin and Paul Jenkins

Mathematika 68, 1080-1119 (2022). arXiv: 2012.14403

A modular grid is a pair of sequences $(f_m)_m$ and $(g_n)_n$ of weakly holomorphic modular forms such that for almost all m and n, the coefficient of q^n in f_m is the negative of the coefficient of q^m in g_n . Zagier proved this coefficient duality in weights 1/2 and 3/2 in the Kohnen plus space, and such grids have appeared for Poincaré series, for modular forms of integral weight, and in many other situations. We give a general proof of coefficient duality for canonical row-reduced bases of spaces of weakly holomorphic modular forms of integral or half-integral weight for every group $\Gamma \subseteq \operatorname{SL}_2(\mathbb{R})$ commensurable with $\operatorname{SL}_2(\mathbb{Z})$. We construct bivariate generating functions that encode these modular forms, and study linear operations on the resulting modular grids.

Odd, spoof perfect factorizations, with the BYU Computational Number Theory Group Journal of Number Theory **234**, 31-47 (2022). Quanta article. arXiv: 2006.10697

We investigate the integer solutions of Diophantine equations related to perfect numbers. These solutions generalize the example, found by Descartes in 1638, of an odd, "spoof" perfect factorization $3^2 \cdot 7^2 \cdot 11^2 \cdot 22021^1$. More recently, Voight found the spoof perfect factorization $3^4 \cdot 7^2 \cdot 11^2 \cdot 19^2 \cdot (-127)^1$. No other examples appear in the literature. We compute all nontrivial, odd, primitive spoof perfect factorizations with fewer than seven bases – there are twenty-one in total. We show that the structure of odd, spoof perfect factorizations is extremely rich, and there are multiple infinite families of them. This implies that certain approaches to the odd perfect number problem that use only the multiplicative nature of the sum-of-divisors function are unworkable. On the other hand, we prove that there are only finitely many nontrivial, odd, primitive spoof perfect factorizations with a fixed number of bases.

Zagier duality for level p weakly holomorphic modular forms, with Paul Jenkins

The Ramanujan Journal 50, 93-109 (2019). arXiv: 1709.10023

We prove Zagier duality between the Fourier coefficients of canonical bases for spaces of weakly holomorphic modular forms of prime level p with $11 \le p \le 37$ with poles only at the cusp at ∞ , and special cases of duality for an infinite class of prime levels. We derive generating functions for the bases for genus 1 levels.

Graphs with the strong Havel-Hakimi property, with Michael Barrus

Graphs and Combinatorics 32, 1689–1697 (2016). arXiv: 1505.00085

The Havel–Hakimi algorithm iteratively reduces the degree sequence of a graph to a list of zeroes. As shown by Favaron, Mahéo, and Saclé, the number of zeroes produced, known as the residue, is a lower bound on the independence number of the graph. We say that a graph has the strong Havel–Hakimi property if in each of its induced subgraphs, deleting any vertex of maximum degree reduces the degree sequence in the same way that the Havel–Hakimi algorithm does. We characterize graphs having this property (which include all threshold and matrogenic graphs) in terms of minimal forbidden induced subgraphs. We further show that for these graphs the residue equals the independence number, and a natural greedy algorithm always produces a maximum independent set.

Research Preprints

A database of basic numerical invariants of Hilbert modular surfaces, with Eran Assaf, Angelica Babei, Ben Breen, Edgar Costa, Juanita Duque-Rosero, Aleksander Horawa, Jean Kieffer, Avinash Kulkarni, Sam Schiavone, and John Voight

Preprint. arXiv: 2301.10302

We describe algorithms for computing geometric invariants for Hilbert modular surfaces, and we report on their implementation.

Multiplicative summations into algebraically closed fields, with Robert Dawson

Preprint. arXiv: 2111.09938

In this paper, extending our earlier program, we derive maximal canonical extensions for multiplicative summations into algebraically closed fields. We show that there is a well-defined analogue to minimal polynomials for a series algebraic over a ring of series, the "scalar polynomial". When that ring is the domain of a summation \mathfrak{S} , we derive the related concepts of the \mathfrak{S} -minimal polynomial for a series, which is mapped by \mathfrak{S} to a scalar polynomial. When the scalar polynomial for a series has the form $(t-a)^n$, a is the unique value to which the series can be mapped by an extension of the original summation.

Telescopic, multiplicative, and rational extensions of summations, with Robert Dawson

Preprint. arXiv: 2105.04592

A summation is a shift-invariant R-module homomorphism from a submodule of R to R or another ring. Dawson formalized a method for extending a summation to a larger domain by telescoping. In this paper, we revisit telescoping, we study multiplicative closures of summations (such as the usual summation on convergent series) that are not themselves multiplicatively closed, and we study rational extensions as a generalization of telescoping.

Expository Notes

Minimalist practical numbers

Unpublished.

A natural number n is practical if every smaller number can be written as a sum of distinct divisors of n. We say that a practical number n is minimalist if this representation is unique. In this note, we prove that a practical number is minimalist if and only if it is a power of 2.

Fast-growing series are transcendental, with Robert Dawson

Unpublished. arXiv: 2102.12995

Let R be a subring of $\mathbb{C}[[z]]$, and let $X \in \mathbb{C}[[z]]$. The Newton-Puiseux Theorem implies that if the coefficients of X grow sufficiently rapidly relative to the coefficients of the series in R, then X is transcendental over R. We provide an alternative proof of this result by establishing a relationship between the coefficients of A(X) and A'(X), where A(T) is a polynomial over $\mathbb{C}[[z]]$.

Manuscripts in Preparation

A family of analogues to the

Ramanujan-Robin criterion, with Steve Fan and Mits Kobayashi
Odd, spoof quasiperfect factorizations, with Jonathon Hales
Visualizing Basel's problem, with Mits Kobayashi

Selected Git Projects

Spoof Quasiperfect Factorizations

Fall 2021

https://github.com/grantmolnar/Spoof-Quasiperfect-Factorizations

Awards and Fellowships

Dartmouth Graduate Fellowship	Fall 2018 - Summer 2023
Gridley Fund for Graduate Mathematics	Fall 2018 - Summer 2019
NSF Graduate Research Fellowship Honorable Mention	April 2018
BYU Academic Scholarship	Spring 2015 - Winter 2016
BYU Math Department Scholarship	Fall 2016
BYU Math Department Scholarship	Fall 2015
BYU Academic Scholarship	Fall 2013 - Winter 2014

Teaching Experience

Dartmouth College	Hanover, NH	(Instructor)
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Math 8 (Calculus of One and Several Variables)	Fall 2021
Math 1 (Algebra and Calculus)	Fall 2020

Dartmouth College, Hanover, NH (Teacher's Assistant)

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Math 100 / Computer Science 49/149 (Random Walk)	Spring 2022
Math 100 / Computer Science 49/149 (Decision Theory)	Spring 2021
Math 23 (Differential Equations)	Winter 2020
Math 3 (Calculus)	Fall 2019
Math 22 (Linear Algebra)	Spring 2019
Math 22 (Linear Algebra)	Fall 2018

Brigham Young University, Provo, UT (Instructor)

Math 112 (Calculus I)	Summer 2017
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Brigham Young University, Provo, UT (Teacher's Assistant)

Math 112 (Calculus I)	Fall 2017
Math 113 (Calculus II)	Winter 2017

Brigham Young University, Provo, UT (Grader)

Math 570 (Matrix Analysis)	Winter 2017
Math 112 (Calculus I)	Fall 2015

Leadership and Community Service

Referee	
Journal of Number Theory	2018 - Present
Mathematische Zeitschrift	2022 - Present
Theory and Decision	2024 - Present
Reviewer	
zbMATH Open	2021 - Present
K-12 Outreach	
Utah Math Olympiad Committee Member	2015 - Present
Lumiere Mentor	2024 - Present
Activity Leader at Dartmouth Science Day (Games & Surreal Numbers)	April 8, 2023
Activity Leader at Lebanon Ward Pi Day	
(Trachtenberg Arithmetic & Random Walk)	March 25, 2023
Session Leader at Dartmouth Sonia Kovalevsky Day	
(Trachtenberg Arithmetic)	May 21, 2022
Activity Leader at Lebanon Ward Pi Day (Random Walk)	April 8, 2022
Exploring Mathematics Camp Leader (Graph Theory)	July 27-31, 2020
Exploring Mathematics Camp Leader (Cryptography)	July 13-17, 2020
Activity Leader at Lebanon Ward Pi Day (Random Walk)	March 7, 2020
Volunteer at Dartmouth Sonia Kovalevsky Day	May 11, 2019
Activity Leader at Dartmouth Science Day (Nim)	May 4, 2019
Math Circles Guest Speaker (Tropical Algebra)	February 24, 2018
Math Circles Guest Speaker (Continued Fractions)	October 21, 2017
Proofreader for Utah State Math Contest	February 2017
Math Circles Counselor	2013 - 2015
Dartmouth Graduate Student Council	
Ad Hoc Healthcare Committee Founder and Co-Chair	2022 - 2023
 Budget Committee Member 	Summer 2022
Finance Officer	2021 - 2022
 Budget Committee Member 	Summer 2021
Representative for Math Department	2020 - 2021
 Service Committee Member 	2020 - 2021
 Budget Committee Member 	Summer 2020
Dartmouth Directed Reading Program	
Mentor (Fuzzy Logic)	Winter 2023
Mentor (Decision Theory)	Spring 2022
Mentor (Fractional Calculus)	Winter 2022
Other	
LMFDB Contributor	2019 - 2023
Dartmouth Algebra and Number Theory Seminar Organizer	2019 - 2022
BYU Putnam Team Captain	2014 - 2016

Thesis Defenses	
Counting elliptic curves with a cyclic m -isogeny over $\mathbb Q$	April 24, 2023
Dartmouth College PhD Thesis Defense	
The arithmetic of modular grids	June 22, 2018
BYU Master's Thesis Defense	
Invited Talks	
Counting elliptic curves with a cyclic <i>m</i> -isogeny	February 9, 2023
Job Talk at Metron	1 cbidary 5, 2025
Counting elliptic curves with a 7-isogeny	January 19, 2023
BYU Colloquium	•
Counting elliptic curves with a 7-isogeny	January 11, 2023
Simons Collaboration Annual Meeting	
Counting 7-isogenies	January 6, 2023
2023 Joint Mathematics Meeting	
A family of analogues to the Ramanujan-Robin Criterion	October 27, 2022
BYU Number Theory Seminar	
Other Conference Talks	
Intersecting varieties with transcendental graphs	March 8, 2023
Arizona Winter School 2023: Unlikely Intersections	0
The LCM product and Grönwall's theorem	October 3, 2021
2021 Maine-Québec Number Theory Conference (virtual)	6
Formal summation of divergent series	September 26, 2020
2020 Conférence de Théorie des Nombres Québec-Maine (virtual)	0
The arithmetic of modular grids	October 5, 2019
2019 Maine-Québec Number Theory Conference	M 1 0 0010
The arithmetic of modular grids	March 8, 2019
33 rd Automorphic Forms Workshop	I.J. 17 0010
The arithmetic of modular grids Building Bridges: 4th EU/US Summer School + Workshop on Automorphic Fo	July 17, 2018
Zagier duality in level p modular spaces	
32^{nd} Automorphic Forms Workshop	March 21, 2018
Zagier duality in level p modular spaces	March 3, 2018
2018 BYU Student Research Conference	
Zagier duality in level p modular spaces	May 24, 2017
Modular Forms are Everywhere Conference	
Weakly holomorphic modular forms of level 11	March 7, 2017
31st Automorphic Forms Workshop	
Weakly holomorphic modular forms of level 11	March 4, 2017
2017 BYU Student Research Conference	7 M L 01 001
Congruence relations in modular forms of prime levels greater than	7 March 21, 2015
2015 BYU Student Research Conference	

2014 BYU Student Research Conference	March 15, 2
2014 BTO Student Research Conference	
Other Seminar Talks	
The Fox H -function	March 28, 2
Dartmouth Graduate Student Seminar	
Geometric deep learning	February 14, 2
Dartmouth Graduate Student Seminar	
Nearing nearrings	September 14, 2
Dartmouth Graduate Student Seminar	Mayala 20 0
Universal algebra and coalgebra Dartmouth Graduate Student Seminar	March 30, 2
Cogalois theory	February 16, 2
Dartmouth Graduate Student Seminar	rebluary 10, 2
Cyclic resolution of singularities	January 25, 2
Reading Seminar on Hilbert Modular Surfaces	,
What if the Riemann hypothesis is false?	January 19, 2
Dartmouth Graduate Student Seminar	,
Inverse semigroups: groups without identity	November 9, 2
Dartmouth Graduate Student Seminar	
Counting 7-isogenies	November 8, 2
Dartmouth Algebra and Number Theory Seminar	
A sober look at pointless topology	September 21, 2
Dartmouth Graduate Student Seminar	A !! 04 0
Fast-growing series are transcendental	April 21, 2
Dartmouth Graduate Student Seminar (virtual)	• " 0
Coalgebras and Hopf algebras	April 15, 2
Reading Seminar on Affine Group Schemes (virtual)	
Absurd equalities and Runge's method: the degenerate case	March 30, 2
Dartmouth Algebra and Number Theory Seminar (virtual)	
p-adic Hodge theory	March 2, 2
Reading Seminar on Classical and Quadratic Chabauty (virtual)	
Odd, spoof quasiperfect factorizations	February 9, 2
Dartmouth Algebra and Number Theory Seminar (virtual)	
A primer in social choice theory	January 20, 2
Dartmouth Graduate Student Seminar (virtual)	
Examples of Kedlaya's algorithm	November 19, 2
Reading Seminar on Classical and Quadratic Chabauty (virtual)	
The LCM product and Grönwall's theorem	November 17, 2
Dartmouth Algebra and Number Theory Seminar (virtual)	
Reactive means and the prisoner's dilemma	October 7, 2
Dartmouth Graduate Student Seminar (virtual)	
Formal summation of divergent series: an algebraic approach	April 28, 2

On the infinitude of the natural numbers	February 12, 2020
Dartmouth Graduate Student Seminar	
Variations of Hodge structures	November 26, 2019
Reading Seminar on Shimura Varieties	
Hodge structures	November 14, 2019
Reading Seminar on Shimura Varieties	
Savage's expected utility and making good decisions	November 13, 2019
Dartmouth Graduate Student Seminar	0
Geometric and generalized calculus	October 8, 2019
Dartmouth Graduate Student Seminar	1 1 21 221
Summing divergent series	July 31, 2019
Dartmouth Graduate Student Seminar	A
Real analysis: a nonstandard approach	April 17, 2019
Dartmouth Graduate Student Seminar	I 16 2010
Why save the universe? Set theory with a universal set	January 16, 2019
Dartmouth Graduate Student Seminar	Contambor 26 2010
The arithmetic of modular grids Dartmouth Graduate Student Seminar	September 26, 2018
Dioids and idempotent geometry II	March 13, 2018
BYU Algebra Seminar	Waren 15, 2010
Dioids and idempotent geometry I	February 27, 2018
BYU Algebra Seminar	rebruary 21, 2010
Zagier duality in level p modular spaces	February 22, 2018
BYU Number Theory Seminar	1 ebiliary 22, 2010
Average values of arithmetic functions	October 12, 2017
BYU Number Theory Seminar	October 12, 2017
•	Falaman, 0, 2017
Weakly holomorphic modular forms of level 11 BYU Number Theory Seminar	February 9, 2017
Generating functions for canonical bases of certain	
level 11 weakly holomorphic modular forms	January 26, 2017
BYU Number Theory Seminar	January 20, 2017
High rank elliptic curves with prescribed torsion	December 1, 2016
BYU Number Theory Seminar	·
Heuristics for elliptic curves of high rank	October 20, 2016
BYU Number Theory Seminar	,
A lemma regarding the Feit-Thompson conjecture	November 12, 2015
BYU Number Theory Seminar	,
Algebraic number theory and the Feit-Thompson conjecture	October 1, 2015
BYU Number Theory Seminar	·
Congruence relations in modular forms of prime levels greater than 7	March 19, 2015
BYU Number Theory Seminar	·
Hensel's lemma	February 12, 2015
BYU Number Theory Seminar	•

Newton polynomials March 27, 2014 BYU Number Theory Seminar Other **Achievements and Honors** 3^{rd} Place in Virginia Tech Regional Math Competition October 2016 2nd Place in Search for High Rank Elliptic Curve at 2016 Connecticut Summer School in Number Theory August 2016 Gold Palm Eagle Scout December 2012 Black Belt (Taekwondo) August 2012 **Special Training** Dartmouth Mathematics Teaching Seminar Spring 2020 Fall 2018 BYU Mathematics Teaching Seminar Academic Interests Analytic Number Theory • Arithmetic Geometry • Game Theory • Logic **Personal Interests** Reading • Writing • Philosophy • Hiking Conferences and Workshops Attended 2024 Simons Collaboration on Arithmetic Geometry, Number Theory, and Computation Annual Meeting January 11-12, 2024 Virtual (Simons Foundation's Gerald D. Fischbach Auditorium, New York City) Big Data Conference 2023 August 31 - September 1, 2022 Virtual (Harvard University, Cambridge) May 8-12, 2023 Hilbert Modular Forms Infrastructure Week 4 Dartmouth College, Hanover Arizona Winter School 2023: Unlikely Intersections March 4-8, 2023 University of Arizona, Tucson 2023 Simons Collaboration on Arithmetic Geometry. Number Theory, and Computation Annual Meeting January 11-12, 2023 Simons Foundation's Gerald D. Fischbach Auditorium, New York City 2023 Joint Mathematics Meetings January 4-7, 2023 Hynes Convention Center, Boston Hilbert Modular Forms Infrastructure Week 3 December 12-16, 2022 Dartmouth College, Hanover Modular Curves Workshop 2 November 5-9, 2022 MIT, Boston Big Data Conference 2022 August 26, 2022

April 11-15, 2022

Virtual (Harvard University, Cambridge)

Explicit Methods for Modularity

Virtual (Simons Collaboration)

Arizona Winter School 2022 : Automorphic Forms Beyond GL_2 Virtual (University of Arizona, Tucson)	March 5-9, 2022
Hilbert Modular Forms Infrastructure Week 2 Dartmouth College, Hanover	February 21-25, 2022
2021 Maine-Québec Number Theory Conference Virtual (University of Maine, Orono)	October 2-3, 2021
Spring 2021 Algebraic Geometry Northeastern Series Virtual (Brown University, Providence)	May 4-5, 2021
$21^{\rm st}$ Algebra, Geometry and Combinatorics Day Virtual (University of Notre Dame, Notre Dame)	April 10, 2021
2021 Joint Mathematics Meetings Virtual (American Math Society, Mathematical Association of America)	January 6-9, 2021
Fall 2020 Algebraic Geometry Northeastern Series Virtual (Stony Brook University, Stony Brook)	October 23-25, 2020
2020 Conférence de Théorie des Nombres Québec-Maine Virtual (Université Laval, Québec)	September 26-27, 2020
$14^{ m th}$ Algorithmic Number Theory Symposium Virtual (University of Auckland, Auckland)	June 29 - July 4, 2020
UNCG Summer School in Computational Number Theory and Algebra: Ergodic Theory with Applications to Continued Fractions Virtual (University of North Carolina, Greensboro)	May 18-22, 2020
2019 Maine-Québec Number Theory Conference	October 5-6, 2019
University of Maine, Orono	C
Fall 2019 Algebraic Geometry Northeastern Series Boston College, Boston	September 20-22, 2019
33 rd Automorphic Forms Workshop Duquesne University, Pittsburgh	March 6-10, 2019
Building Bridges: 4^{th} EU/US Summer School $+$ Workshop on Automorphic Forms and Related Topics Alfréd Rényi Institute of Mathematics, Budapest	July 9-20, 2018
32 nd Automorphic Forms Workshop Tufts University, Medford	March 19-22, 2018
Modular Forms are Everywhere Max Planck Institute for Mathematics, Bonn	May 15-26, 2017
31st Automorphic Forms Workshop East Tennessee State University, Johnson City	March 6-9, 2017
2017 BYU Student Research Conference Brigham Young University, Provo	March 4, 2017
2016 Connecticut Summer School in Number Theory University of Connecticut, Storrs	August 8-14, 2016
2015 BYU Student Research Conference Brigham Young University, Provo	March 21, 2015

 $2014 \ \textit{BYU Student Research Conference} \\ \text{Brigham Young University, Provo}$

March 15, 2014