Problem Sheet: Trees

- 1. Construct all (non-isomorphic) rooted trees of heights from one to four, that have five vertices [1]. Note that there is one of height one, four of height two, three of height three, and one of height four.
- 2. Construct two non-isomorphic rooted trees both having twelve vertices, six leaves, and height four [1].
- 3. Calculate the minimum height of a ternary rooted tree with eleven leaves.
- 4. Consider a graph with eight vertices and twelve edges connected such that it can be drawn as a cube. Draw this graph, find a spanning tree of it and then high-light the edges on the drawing that are part of the tree [1].
- 5. Sketch all sixteen distinct spanning trees of the complete graph K_4 .
- 6. Draw evaluation trees representing each of the following reverse Polish notation expressions.
 - (a) 34 +
 - (b) $34 + 5 \times$
 - (c) $46 46 + \div$
 - (d) $11\ 3 \times 100\ 16\ 2 \times + \div 75 \times$

References

[1] N. Biggs. Discrete Mathematics. Oxford science publications. OUP Oxford, 2002.