

These questions are largely taken from Sipser's book [1].

1. Draw a DFA that accepts all strings over  $\{a, b\}$  that have at least three  $a$ 's.
2. Draw a DFA that accepts all strings over  $\{a, b\}$  that have at least two  $b$ 's.
3. Draw a DFA that accepts all strings over  $\{a, b\}$  that have exactly two  $a$ 's.
4. Draw a DFA that accepts all strings over  $\{a, b\}$  that have an odd number of  $a$ 's.
5. Draw a DFA that accepts all strings over  $\{a, b\}$  that have at least three  $a$ 's and at least two  $b$ 's.
6. Define all of the above automata.
7. Draw an NFA that recognises, over the alphabet  $\{0, 1\}$ , both strings that begin with a 1 and end with a 0 and strings that contain at least three 1's.
8. Draw an NFA that recognises, over the alphabet  $\{0, 1\}$ , both strings that contain the substring 0101 and strings that don't contain the substring 110.
9. Draw an NFA that recognises, over the alphabet  $\{0, 1\}$ , the concatenations of strings of length at most five and strings where every odd position is a 1.
10. Draw an NFA that recognises, over the alphabet  $\{0, 1\}$ , the Kleene star of the language containing strings with at least two 0's and at most one 1.

## References

- [1] Michael Sipser. *Introduction to the Theory of Computation*. International Thomson Publishing, 3rd edition, 1996.