



Disentangling Neurodegeneration with Brain Age Gap Prediction Models: A Graph Signal Processing Perspective

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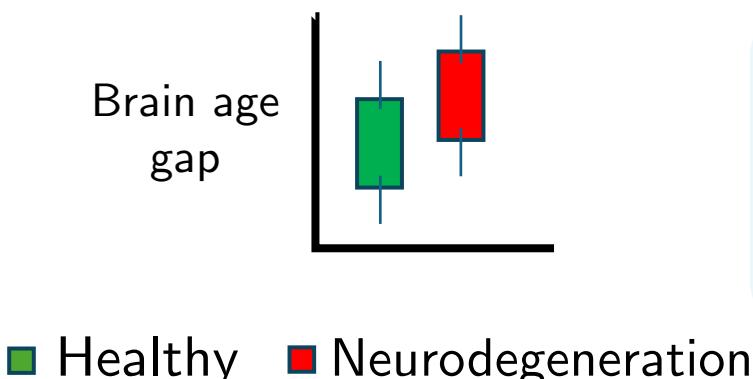
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Brain age gap

- Individual rate of “aging” is different from chronological rate of aging
 - Driven by environment, genetics, **neurodegeneration**
- **Brain age** provides a biological estimate brain age, derived from **neuroimaging**

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 - Driven by environment, genetics, **neurodegeneration**
- Brain age provides a biological estimate brain age, derived from **neuroimaging**
- The **brain age gap** is the **deviation** between brain age and chronological age



individual risks for neurological,
Brain age gap \propto neuropsychiatric
and neurodegenerative diseases

■ Healthy ■ Neurodegeneration

Neurodegeneration (in terms of cortical atrophy)

- Neurodegeneration is **accelerated decline** of structure or function of the brain
- **Cortical atrophy:** reduction in cortical **thickness/volume/area**

(characteristic of healthy aging and disorders like Alzheimer's disease (AD), frontotemporal dementia (FTD), etc.)

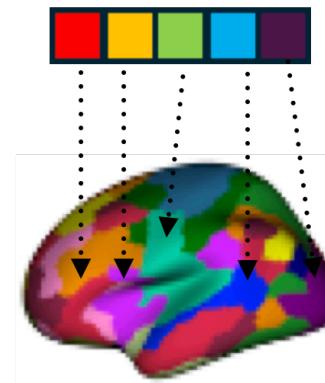


MRI scan

Preprocessing
(e.g., Freesurfer)



$$\mathbf{x} = [x_1, \dots, x_m]$$

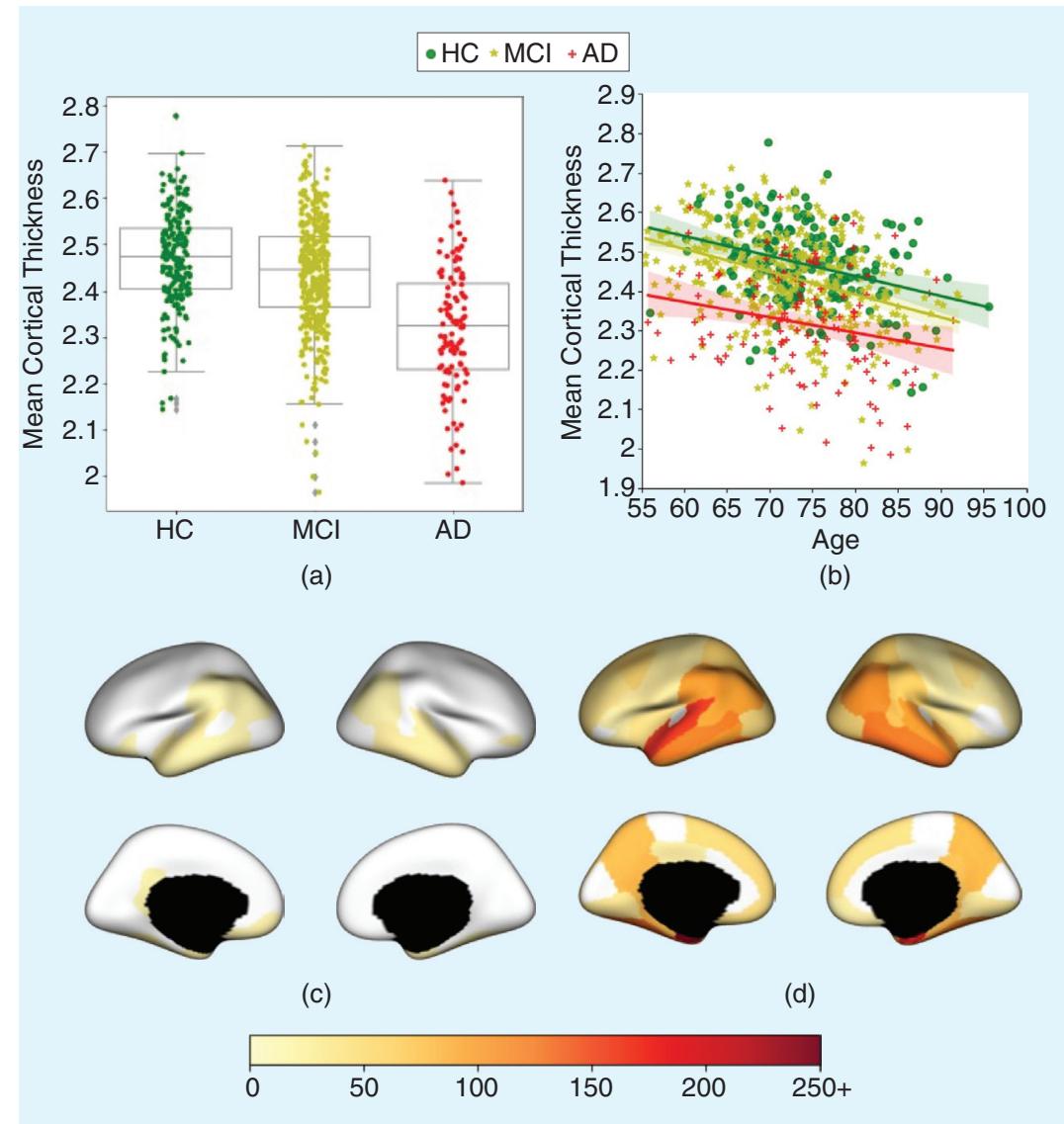


Cortical thickness features

x_i is cortical thickness for brain region i

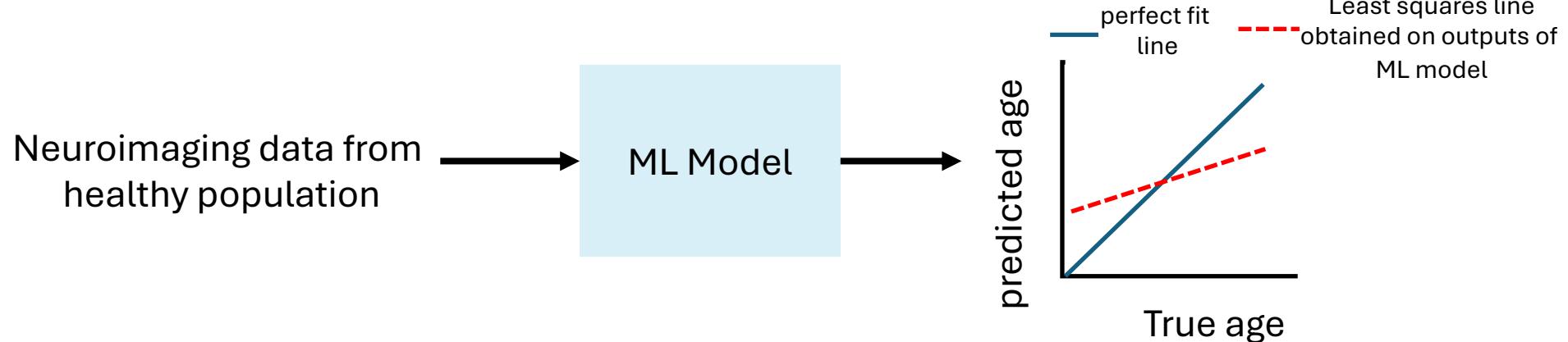
Case study (Neurodegeneration)

- **Data:** cortical thickness from 3 cohorts
 - HC (healthy)
 - MCI (Mild cognitive impairment)
 - AD (Alzheimer's disease)
- Larger **cortical atrophy** is feature of AD
- MCI is precursor to AD
 - ➡ shows intermediate cortical atrophy between HC and AD
- **Aging** also leads to cortical atrophy



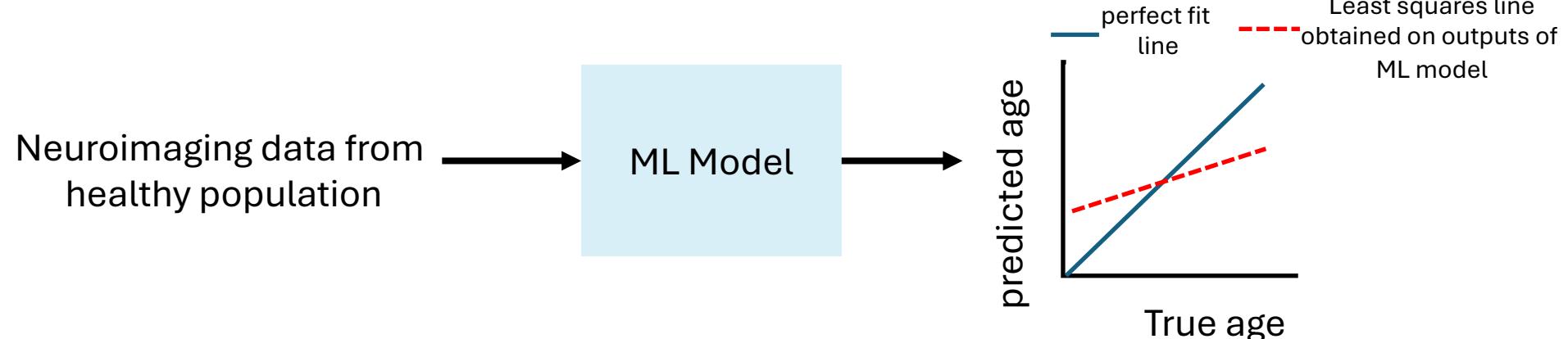
Brain age gap evaluation using ML

Step 1. Train ML model to predict chronological age for healthy controls from cortical thickness features



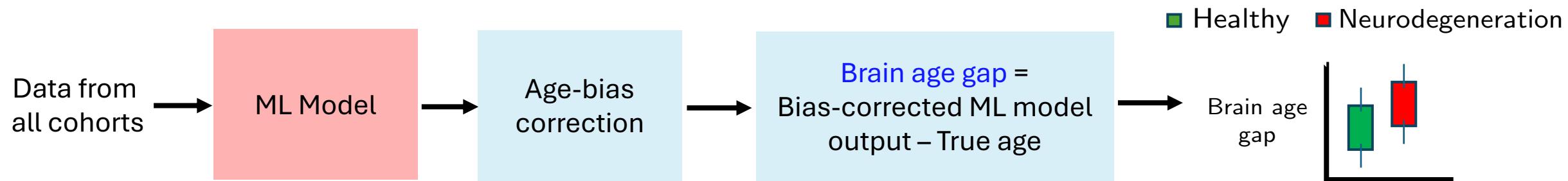
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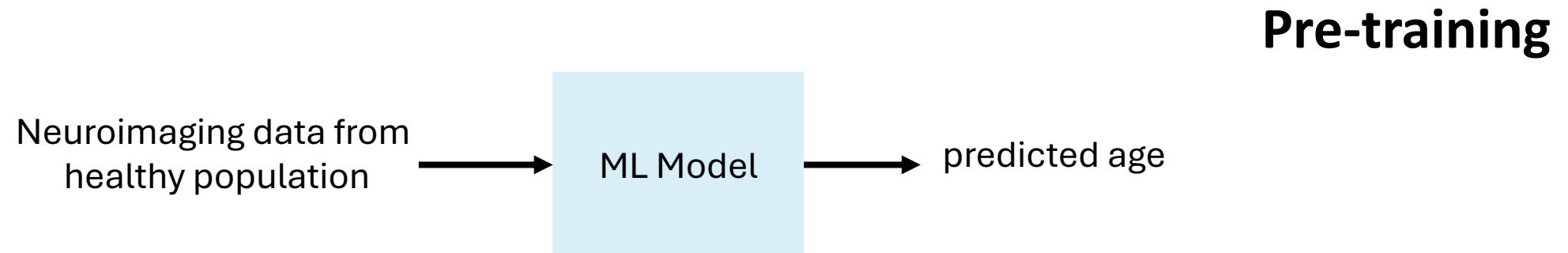
Step 2. Linear regression-based age-bias correct for outputs of ML model

Step 3. Obtain **brain age gap** for healthy controls and individuals with neurodegenerative condition.

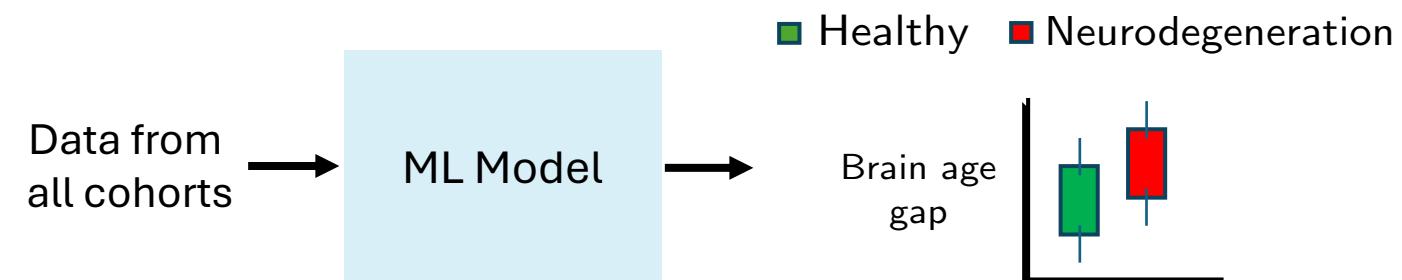


Brain age gap prediction is a transfer learning problem

- Train ML model to predict age on a **large dataset** (healthy population)



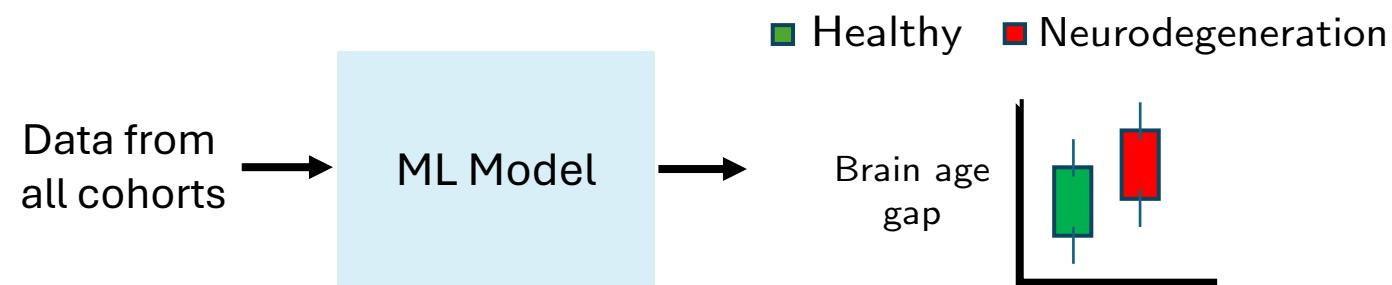
- Apply the **pre-trained** ML model on a **target dataset** (neurodegeneration)



- Brain age gap is the **residual** of the model

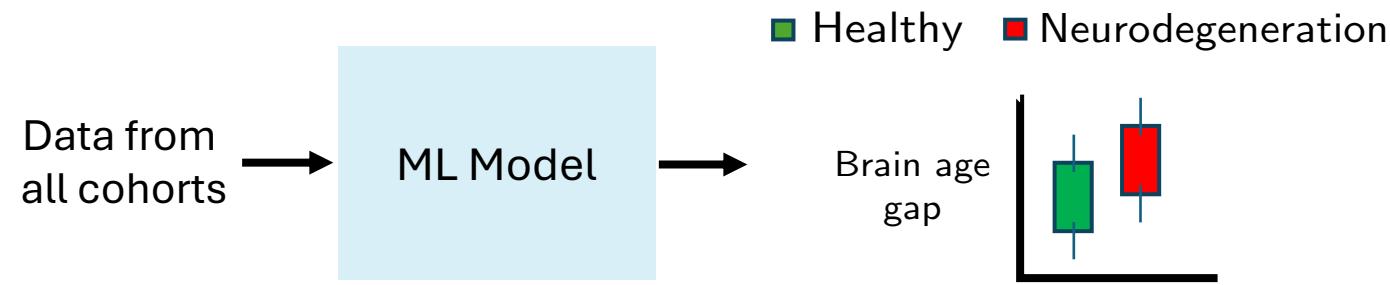
Brain age gap prediction is a transfer learning problem

- **Some observations about a meaningful brain age gap**
 - We expect model performance to **degrade** in **target population**
 - ✓ Degradation in performance (residuals) in a **specific direction**
 - ✓ Degradation in performance (residuals) \propto **disease severity/status**



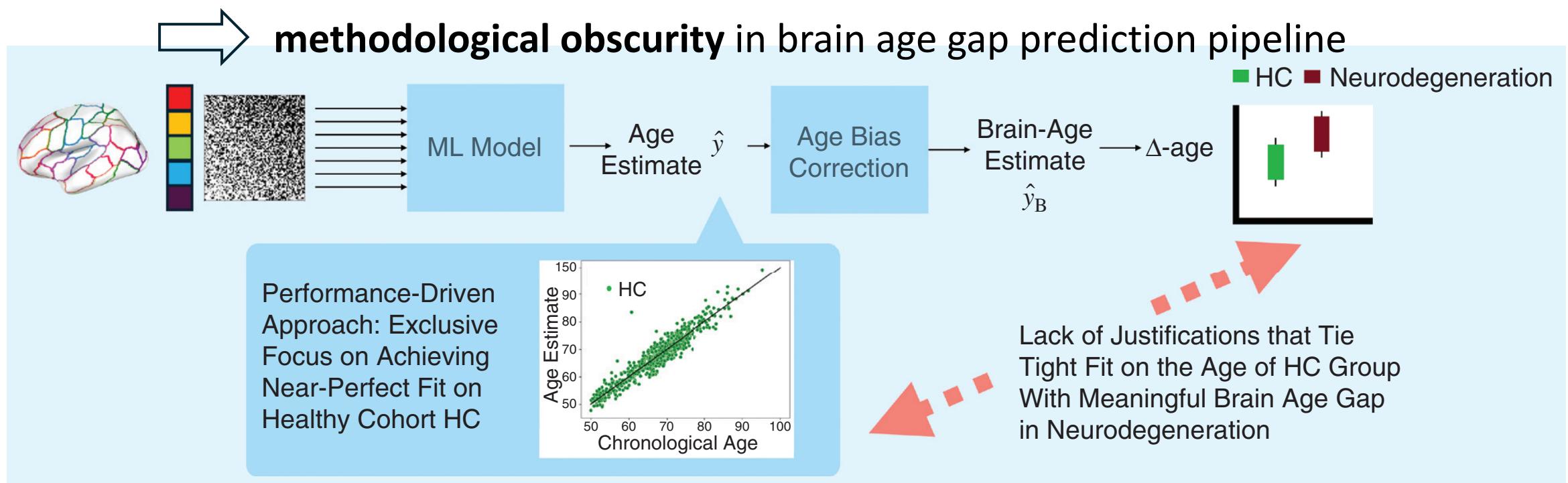
Choice of learning parametrization

- Choice of ML model dictates how data is leveraged to gauge brain age gap
- Prevalent approaches focus on achieving *perfect* pre-training performance
 - **Performance-driven approaches**
- **Performance-driven approaches** do not guarantee ‘**meaningful**’ brain age gap



Choice of learning parametrization

- Neural networks are prevalent in performance-driven approaches
- A Neural Network may **not be interpretable** and prone to **overfitting**



Choice of learning parametrization

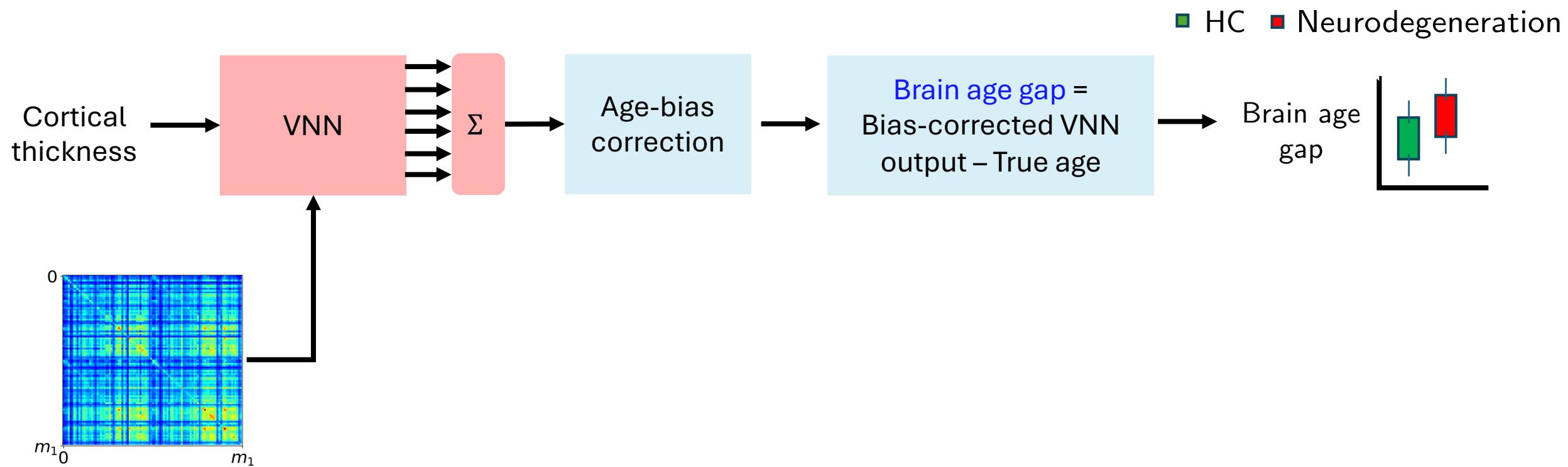
- Neural networks are prevalent in performance-driven approaches
- A Neural Network may **not be interpretable** and prone to **overfitting**
 - ➡ **methodological obscurity** in brain age gap prediction pipeline

Performance in **pre-training** does not dictate **meaningful residuals**
in **target population**

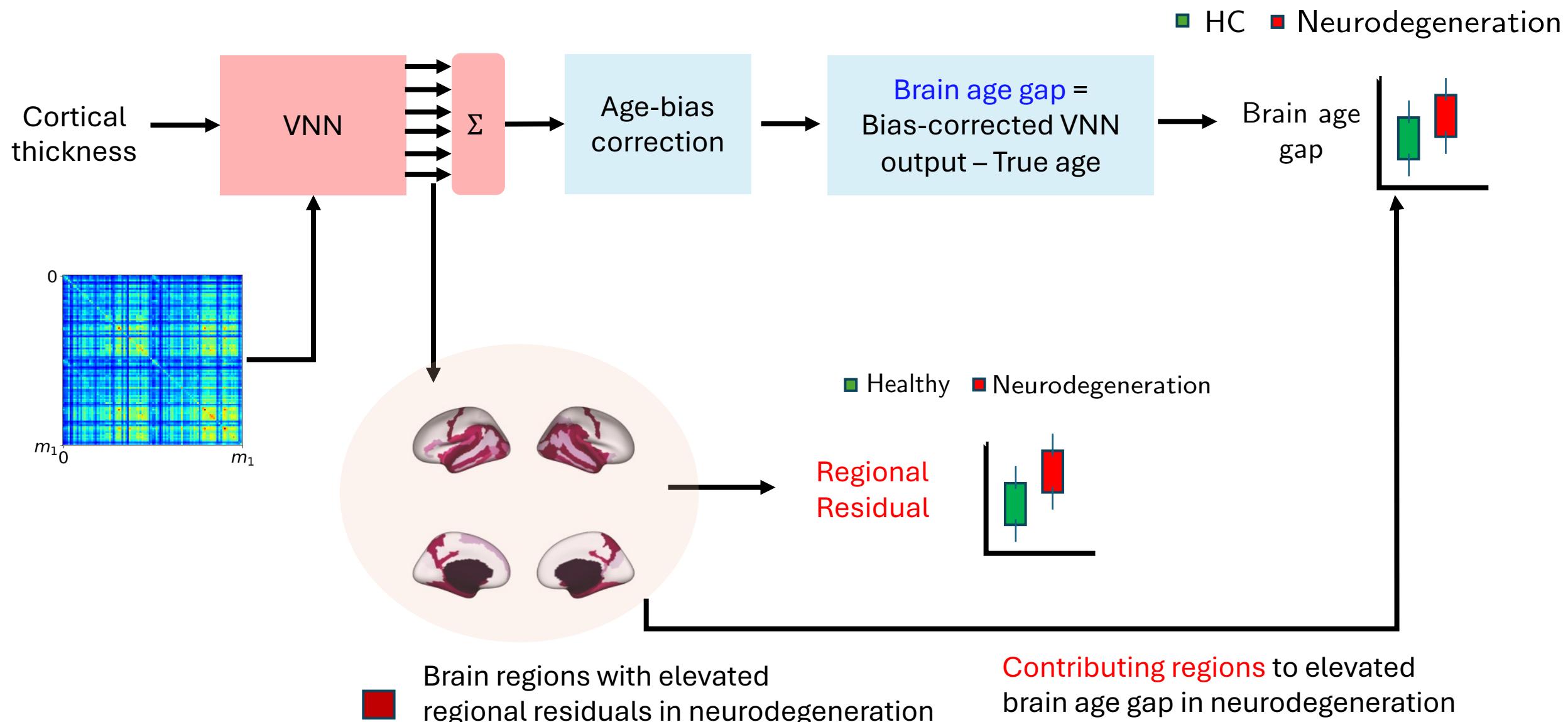
A principled approach to brain age gap prediction

- **Focus on residuals** of the ML model, not prediction performance
- **Qualitative evaluation** during pre-training
 - what does the model learn during **pre-training** on **healthy population**?
- **Interpretability/explainability:**
 - what's driving elevated brain age gap (residuals) in **neurodegeneration**?
- **Generalizability** to diverse target populations

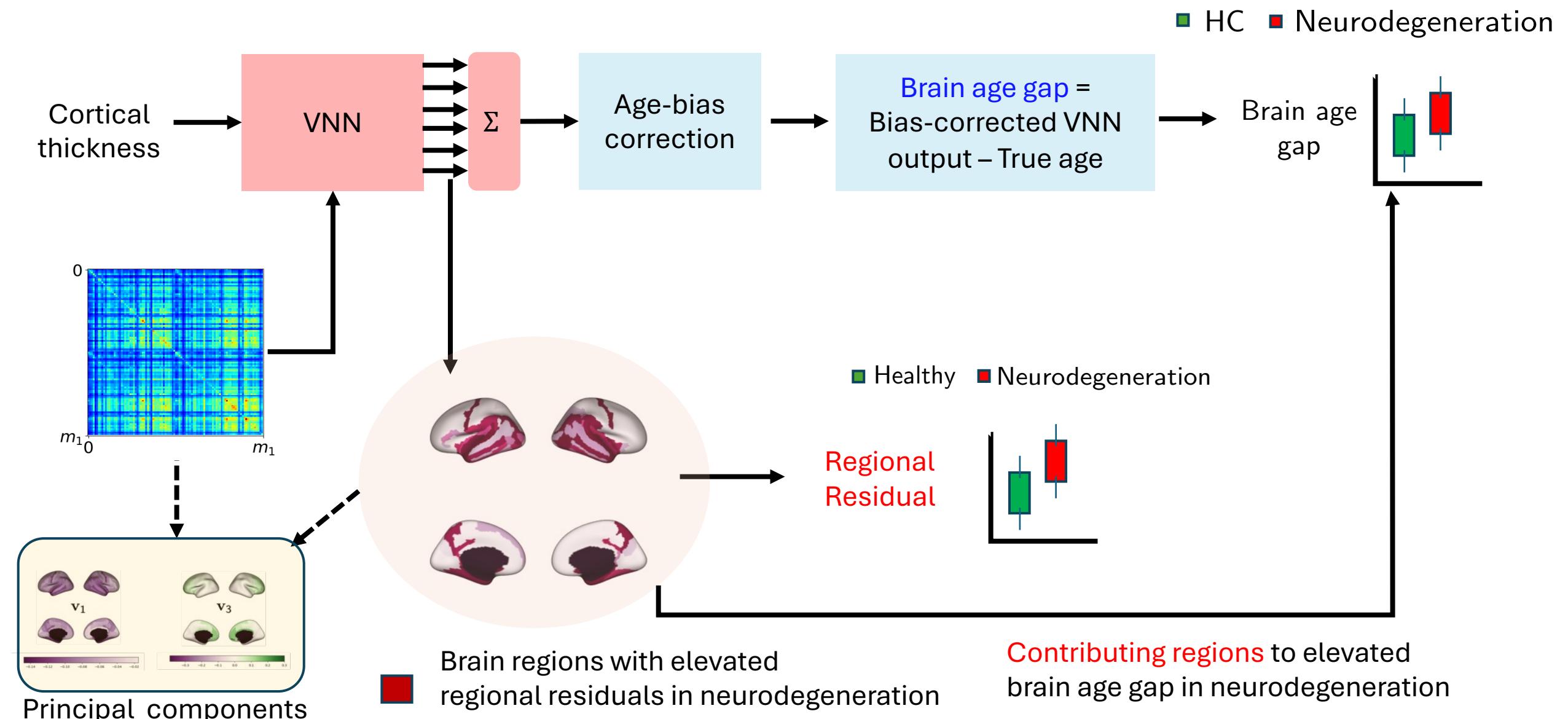
VNNs provide an anatomically interpretable and explainable brain age gap



VNNs provide an anatomically interpretable and explainable brain age gap

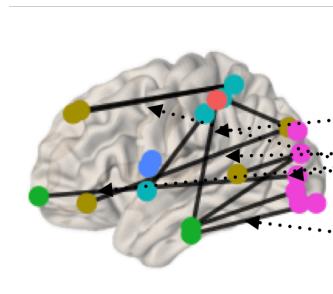


VNNs provide an anatomically interpretable and explainable brain age gap



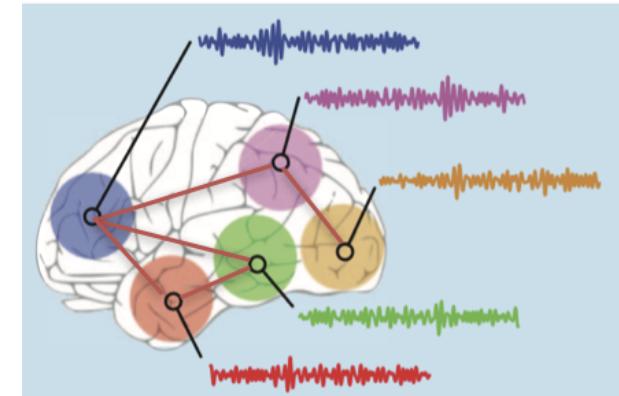
Network neuroscience

➤ Modeling brain as a network (**connectomes**)



$$C = \begin{bmatrix} c_{11} & c_{12} & \cdots & \cdots & c_{1m} \\ c_{21} & c_{22} & \cdots & \cdots & c_{2m} \\ \vdots & \vdots & & & \vdots \\ c_{m1} & c_{m2} & \cdots & c_{mm} & \vdots \end{bmatrix}$$

Anatomical covariance matrix
(structural connectome)



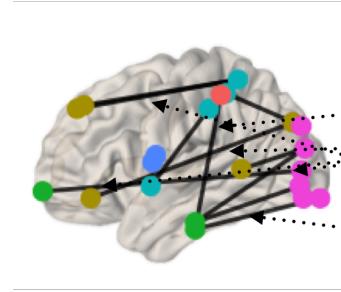
Functional connectome

➤ Motivation

- Significant redundancies in brain structural/functional features
- Brain structure/function is compromised in neurodegeneration

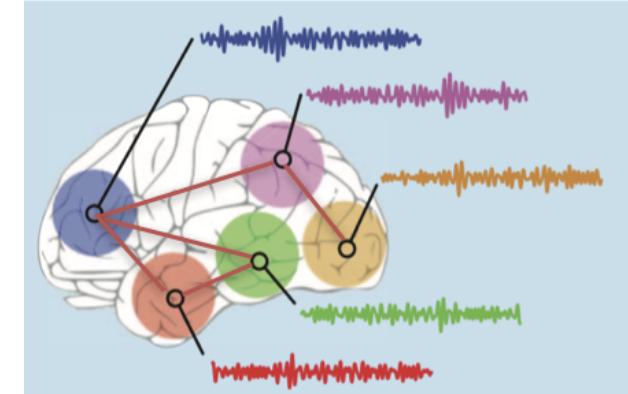
Covariance matrices in network neuroscience

- Covariance matrices appear commonly in network neuroscience



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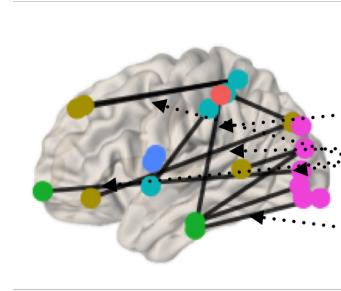
Anatomical covariance matrix



Functional connectome

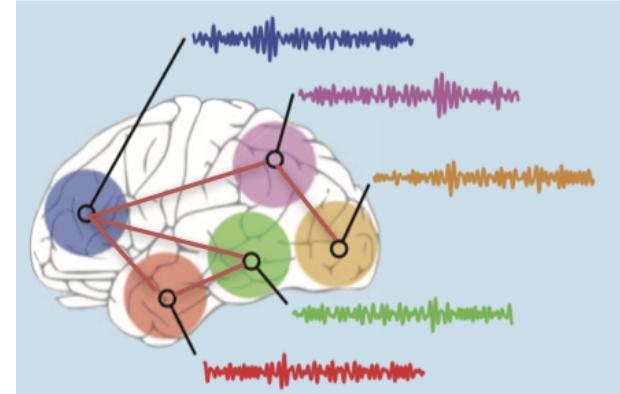
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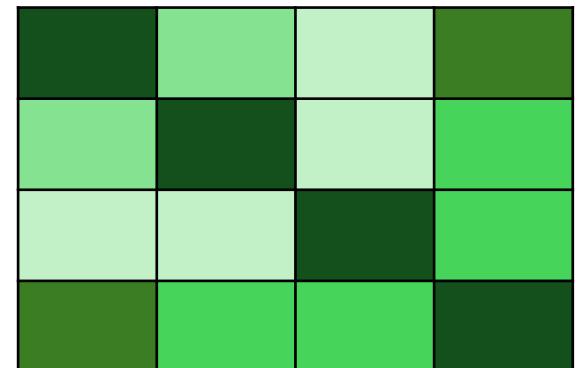
Anatomical covariance matrix



Functional connectome

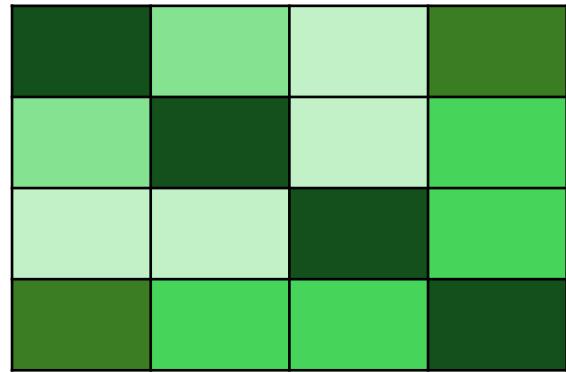
- Inference over covariance matrices in ML

- **Traditional** statistical approaches (for e.g., PCA)
 - Interpretable, suitable for low data regimes
- **Deep learning** approaches (for e.g., GNNs)
 - Enhanced expressivity, improved performance

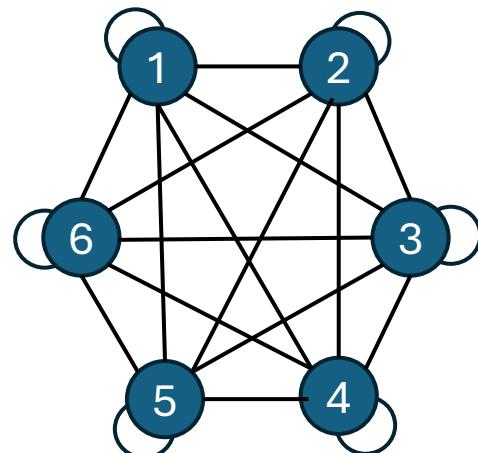


Covariance matrix as a graph

- Covariance matrix is a **data-driven** graph



$$\mathbf{x} = [x_1, \dots, x_6]^T$$



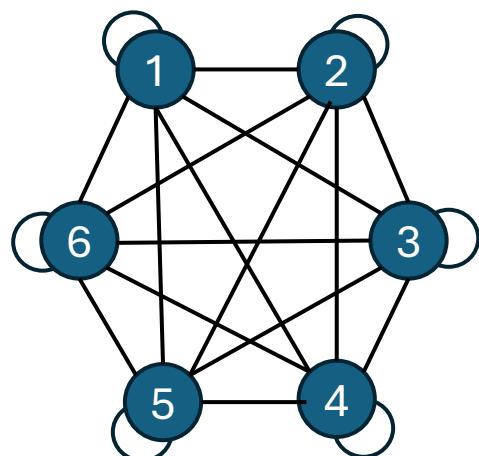
Covariance matrix as a fully-connected graph

$$\hat{\mathbf{C}} = \frac{1}{n-1} \sum_{i=1}^n (\mathbf{x}_i - \hat{\boldsymbol{\mu}})(\mathbf{x}_i - \hat{\boldsymbol{\mu}})^T, \text{ where } \hat{\boldsymbol{\mu}} = \frac{1}{n} \sum_{i=1}^n \mathbf{x}_i$$

Covariance matrix as a graph

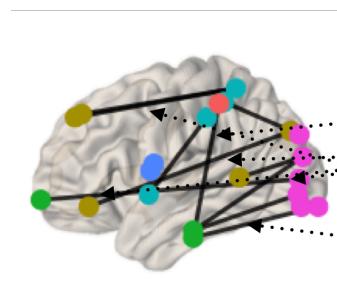
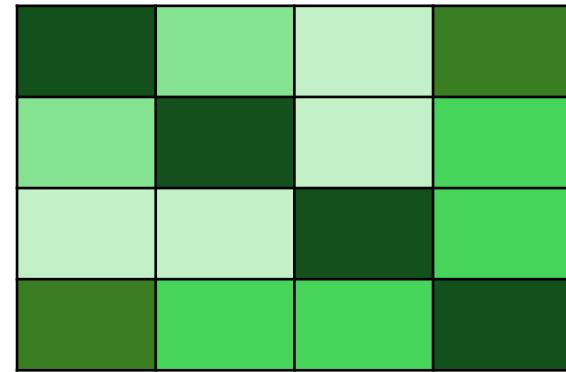
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Anatomical covariance matrix
(estimated from cortical features)

Graph signal processing

- Signal and information processing is about exploiting signal structure
- Graph signal processing (GSP): broaden classical signal processing to graphs



Graph Signal Processing: Overview, Challenges, and Applications

This article presents methods to process data associated to graphs (graph signals) extending techniques (transforms, sampling, and others) that are used for conventional signals.

By ANTONIO ORTEGA¹, Fellow IEEE, PASCAL FROSSARD, Fellow IEEE, JELENA KOVACIĆ, Fellow IEEE, JOSÉ M. F. MOURA², Fellow IEEE, and PIERRE VANDERHEYDEN³

ABSTRACT | Research in graph signal processing (GSP) aims to develop tools for processing data defined on irregular graph domains. In this paper, we first provide an overview of core ideas in GSP and their connection to conventional digital signal processing, along with a brief historical perspective to highlight how concepts recently developed in GSP build on top of prior research in other areas. We then summarize recent advances in developing basic GSP tools, including methods for sampling, filtering, or graph learning. Next, we review progress in several application areas using GSP, including processing and analysis of sensor network data, biological data, and applications to image processing and machine learning.

KEYWORDS | Graph signal processing (GSP); network science and graphs; sampling; signal processing

I. INTRODUCTION AND MOTIVATION

Data is all around us, and massive amounts of it. Almost every aspect of human life is now being recorded at all levels: from the marking and recording of processes inside the cells starting with the advent of fluorescent markers, to our personal data through health monitoring devices and apps, financial and banking data, our social networks, mobility and traffic patterns, marketing preferences, fads, and many more. The complexity of such networks [1] and interactions means that the data now reside on irregular and complex structures that do not lend themselves to standard tools.

Typical graphs that are used to represent common real-world data include Erdős-Rényi graphs, ring graphs, random geometric graphs, small-world graphs, power-law graphs, nearest-neighbor graphs, scale-free graphs, and many others. These model networks with random connections (Erdős-Rényi graphs), networks of brain neurons (small-world graphs), social networks (scale-free graphs), and others.

As in classical signal processing, graph signals can have properties that are specific to the graph structure they are defined on. They can also be represented via basis atoms and can have a spectral representation. In particular, the graph Fourier transform allows us to develop the intuition gathered in the classical setting and extend it to graphs: we can talk about the notions of frequency and bandlimitness,

Geert Leus¹, Antonio G. Marques², José M.F. Moura²,
Antonio Ortega³, and David I. Shuman¹



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SOCIETY SPECIAL ISSUE

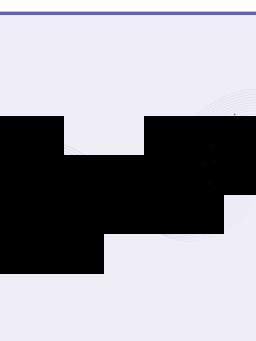
Graph Signal Processing

History, development, impact, and outlook

Xiaowen Dong, Dorina Thanou, Laura Toni,
Michael Bronstein, and Pascal Frossard

Graph Signal Processing for Machine Learning

A review and new perspectives



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GRAPH SIGNAL PROCESSING:
FOUNDATIONS AND EMERGING DIRECTIONS

Graph Signal Processing for Machine Learning

A review and new perspectives

The effective representation, processing, analysis, and visualization of large-scale structured data, especially those related to complex domains, such as networks and graphs, are one of the key questions in modern machine learning. Graph signal processing (GSP) is a branch of signal processing models and algorithms that aims at handling data supported on graphs, opens new paths of research to address this challenge. In this article, we review a few important contributions made by GSP concepts and tools, such as graph filters and transforms, to the development of novel machine learning algorithms. In particular, our discussion focuses on the following three aspects: exploiting data structure and relational priors, improving data and computational efficiency, and enhancing model interpretability. Furthermore, we provide new perspectives on the future development of GSP techniques that may serve as a bridge between applied mathematics and signal processing on one side and machine learning and network science on the other. Cross-fertilization across these different disciplines may help unlock the numerous challenges of complex data analysis in the modern age.

Introduction

We live in a connected society. Data collected from large-scale interactive systems, such as biological, social, and financial networks, become largely available. In parallel, the past few decades have seen a significant amount of interest in the machine learning community for network data processing and analysis. Networks have an intrinsic structure that conveys very specific properties to data, e.g., interdependences between data entities in the form of pairwise relationships. These properties are traditionally captured by mathematical representations such as graphs.

In this context, new trends and challenges have been developing fast. Let us consider, for example, a network of interconnected interacting nodes and the evolution of individual genes at every point in time. Some typical tasks in network biology related to this type of data are 1) discovery of key genes (via protein grouping) affected by the infection and 2) prediction of how the host organism reacts (in terms of gene expression)

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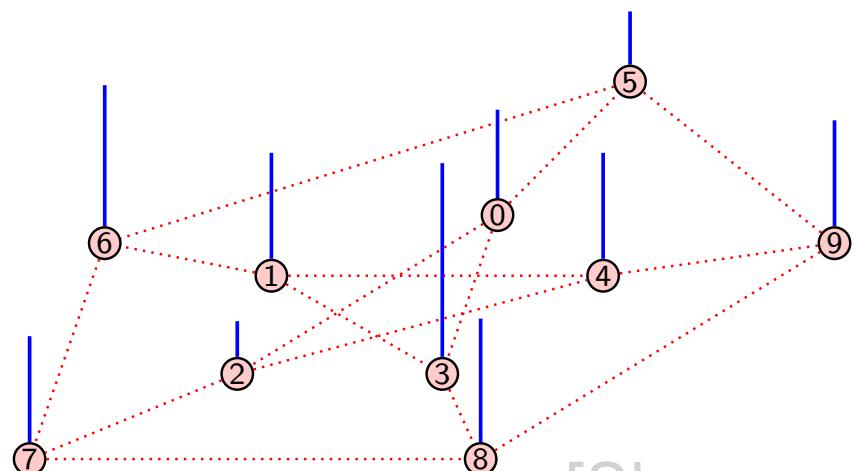
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11

Graph signal

- **Graph signals** are mappings $x: V \mapsto \mathbb{R}$
 - ➡ graph signal is defined on the vertices of the graph
- **Graph signal** can be represented as a vector $\mathbf{x} \in \mathbb{R}^m$
 - ➡ x_i denotes the graph signal at i -th vertex in V



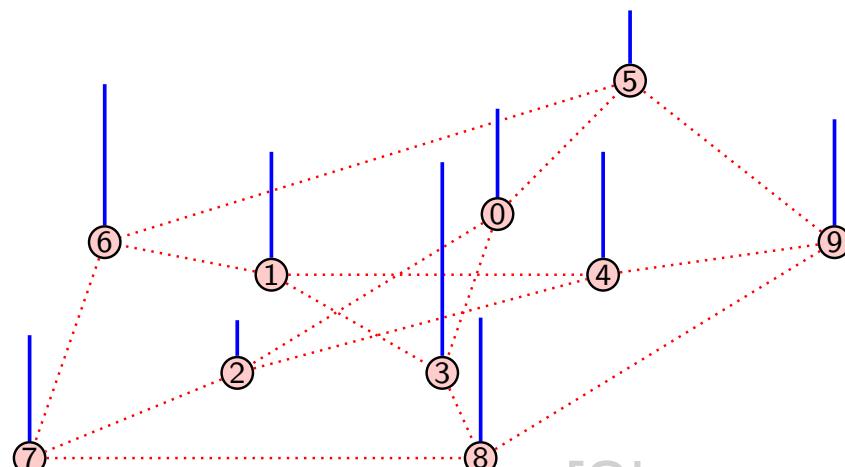
[Shuman, 2013]

$$\mathbf{x} = \begin{bmatrix} x_0 \\ x_1 \\ x_2 \\ \vdots \\ x_9 \end{bmatrix} = \begin{bmatrix} 0.6 \\ 0.7 \\ 0.3 \\ \vdots \\ 0.7 \end{bmatrix}$$

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Cortical thickness features
are graph signals



[Shuman, 2013]

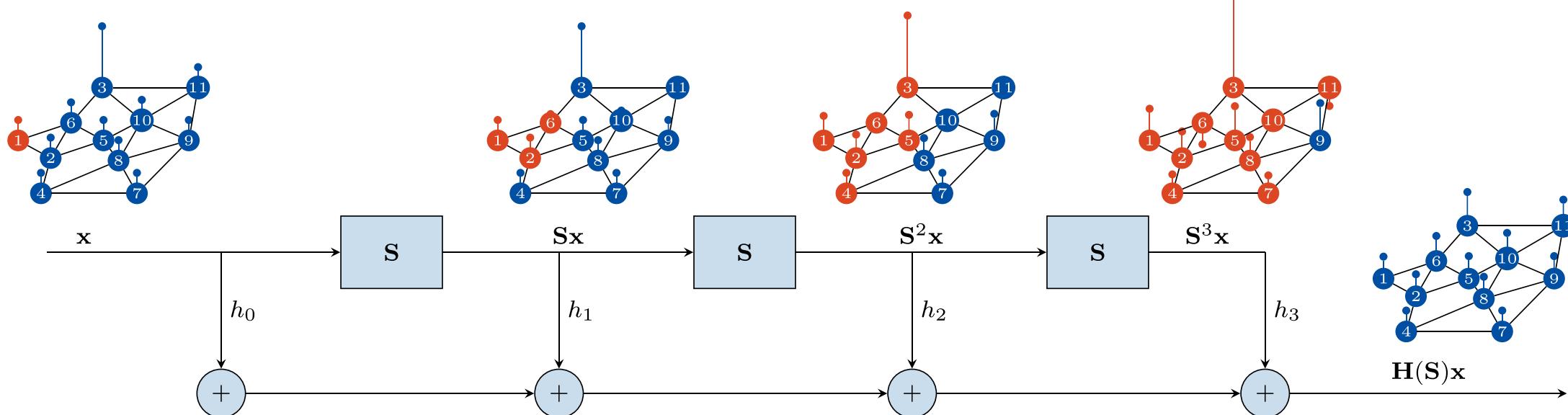
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Preliminaries: Graph filter

- **Graph filter \mathbf{H}** maps graph signal \mathbf{x} to another graph signal \mathbf{z} via linear-shift-and-sum operation

$$\mathbf{z} = \mathbf{H}(\mathbf{S})\mathbf{x},$$

$$\text{where } \mathbf{H} := h_0 \mathbf{S}^0 + h_1 \mathbf{S}^1 + h_2 \mathbf{S}^2 + \cdots + h_K \mathbf{S}^K = \sum_{k=0}^K h_k \mathbf{S}^k$$

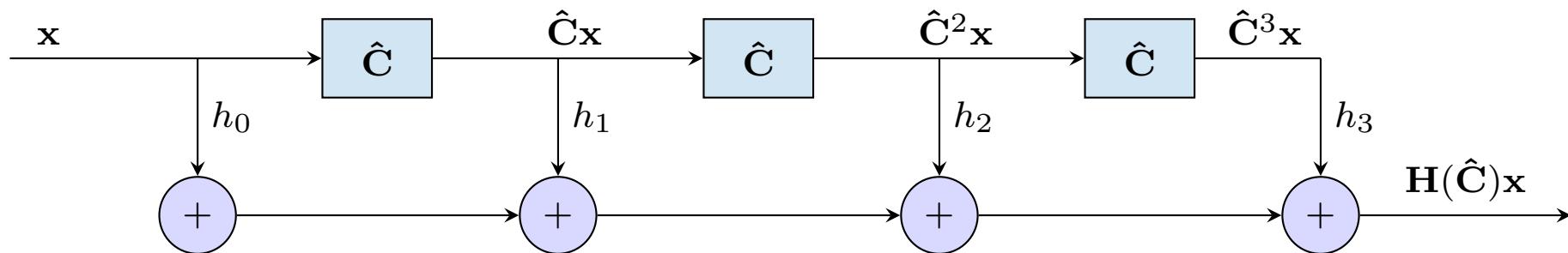
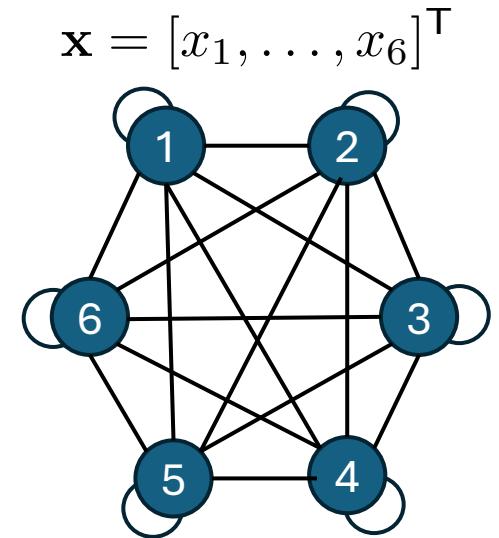


[Isufi et. al, IEEE TSP, 2024]

Graph filter on covariance matrix

- Covariance matrix forms a fully-connected graph where
 - nodes are features (brain regions)
 - edges are covariance values
- Graph filter on covariance matrix $\hat{\mathbf{C}}$ is defined as

$$\mathbf{H}(\hat{\mathbf{C}}) = \sum_{k=0}^K h_k \hat{\mathbf{C}}^k \mathbf{x}$$



CoVariance filter

- Analogy between $\mathbf{H}(\hat{\mathbf{C}})$ and PCA
 - Using eigendecomposition $\hat{\mathbf{C}} = \hat{\mathbf{V}}\hat{\Lambda}\hat{\mathbf{V}}^T$, it follows that

$$\mathbf{z} = \mathbf{H}(\hat{\mathbf{C}})\mathbf{x} = \sum_{k=0}^K h_k \hat{\mathbf{C}}^k \mathbf{x} = \sum_{k=0}^K h_k \hat{\mathbf{V}} \hat{\Lambda}^k \hat{\mathbf{V}}^T \mathbf{x} = \hat{\mathbf{V}} \left(\underbrace{\sum_{k=0}^K h_k \hat{\Lambda}^k}_{\text{Frequency response}} \right) \hat{\mathbf{V}}^T \mathbf{x}$$



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- coVariance filter and PCA are conceptually **equivalent**

$$\hat{\mathbf{V}}^T \mathbf{z} = \left(\sum_{k=0}^K h_k \hat{\Lambda}^k \right) \hat{\mathbf{V}}^T \mathbf{x}$$

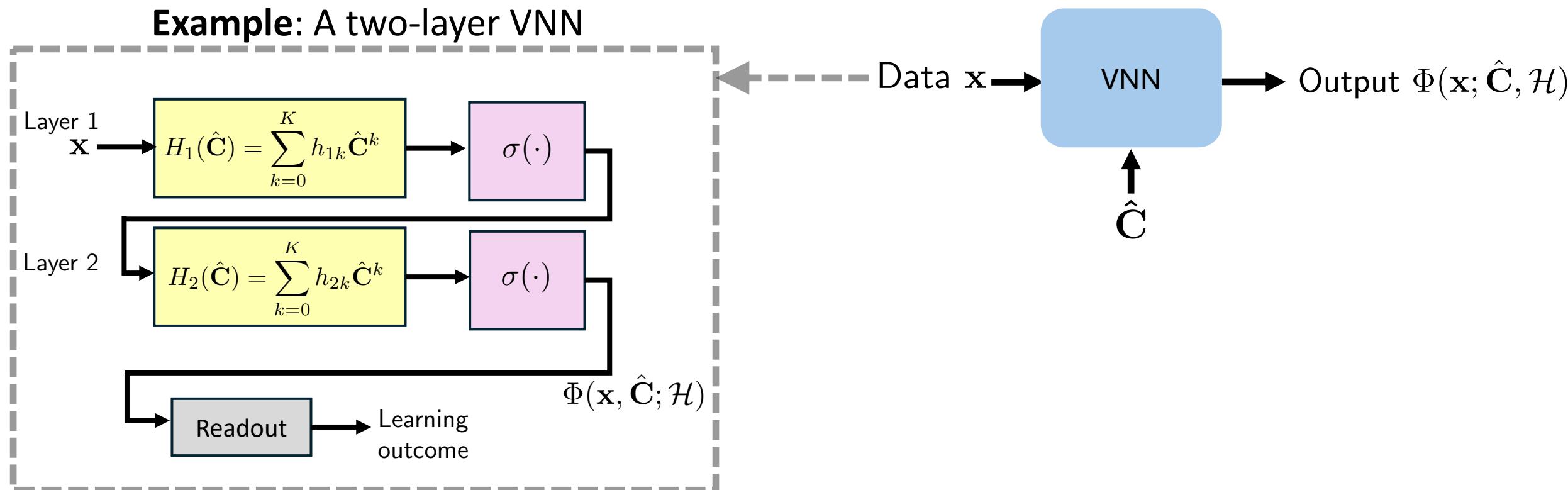
i -th component is modulated by $h(\lambda_i) = \sum_{k=0}^K h_k \lambda_i^k$

CoVariance Neural Networks (VNNs)

- coVariance filters can learn only **linear** representations
- To accommodate learn **non-linear** representations, concatenate coVariance filter with pointwise non-linearity σ (for e.g., ReLU, sigmoid, etc.)

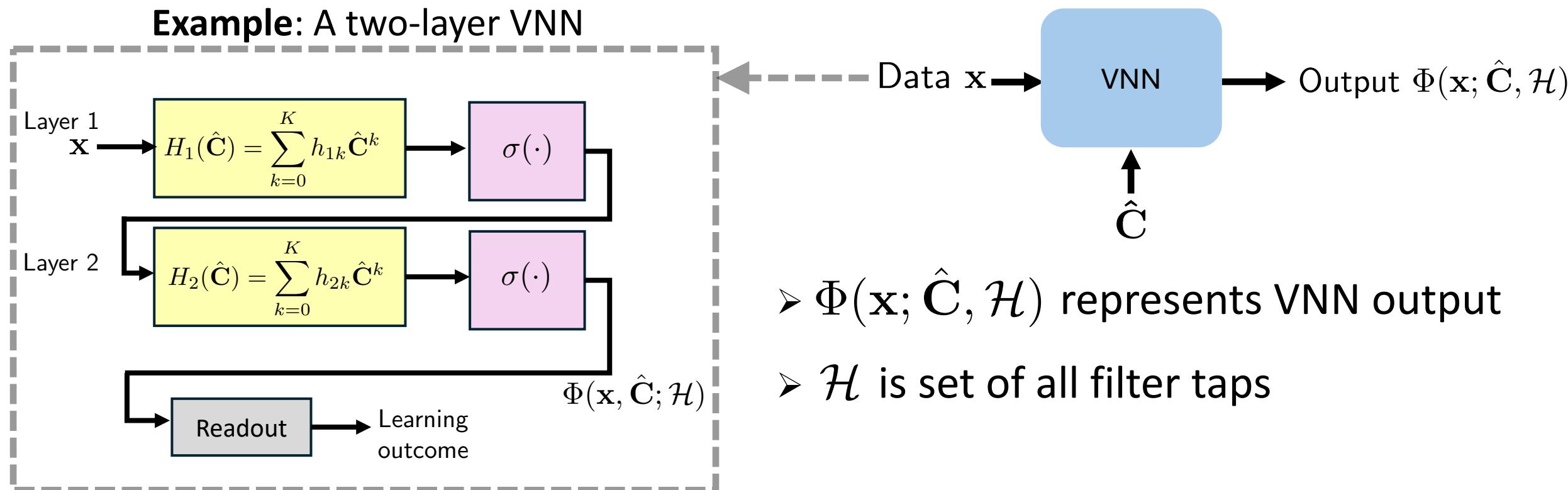
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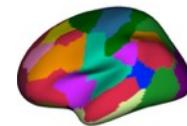


VNNs are well suited for neuroimaging data analysis

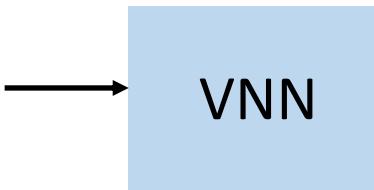
- Theoretical properties of VNNs make them appealing for neuroimaging data analysis
 - **Connections with PCA** → transparent outcomes by leveraging spectrum of covariance matrix
 - **Stability** → reproducible outcomes in limited data settings
[Sihag et al., 2022]
 - **Transferability** → enhanced generalizability and robustness to choice of brain atlases [Sihag et al., 2024]

VNN vs PCA on age prediction task

- Regression task



Cortical thickness
data

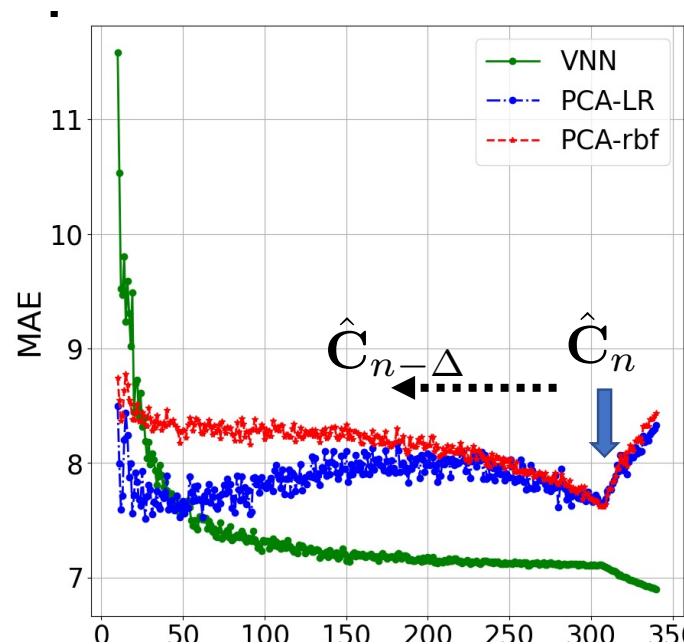


Estimate of age

- Comparison against PCA-regression

Data: cortical thickness dataset ($m = 104$) from ($n = 341$) human subjects

- **Metric:** MAE (mean absolute error)



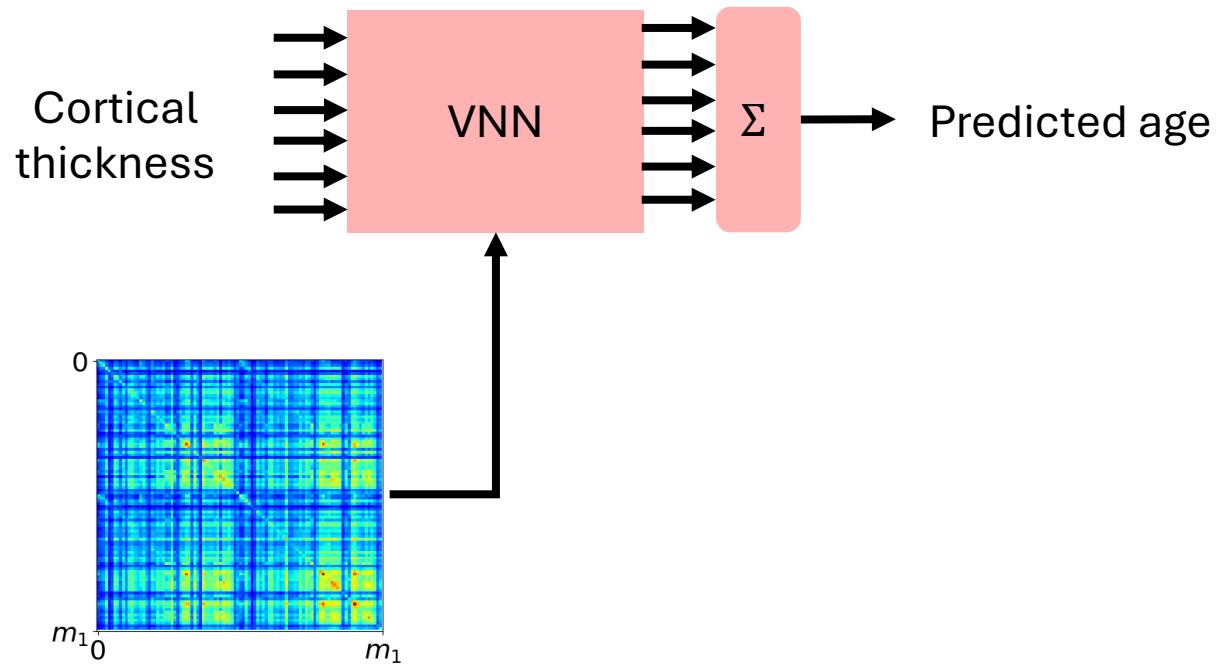
VNN: coVariance Neural Network

PCA-LR: PCA-regression with linear kernel

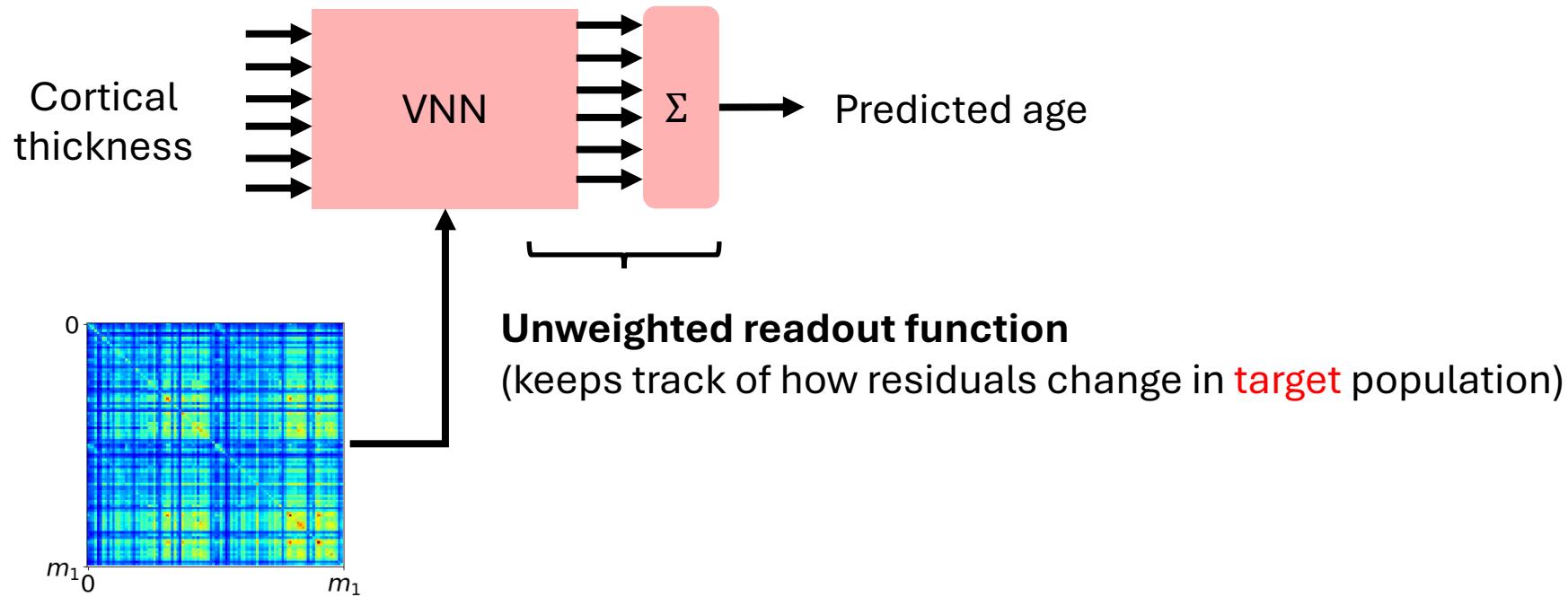
PCA-rbf: PCA regression with rbf kernel

VNN outperforms PCA and is **more stable**
[Sihag et al., 2022]

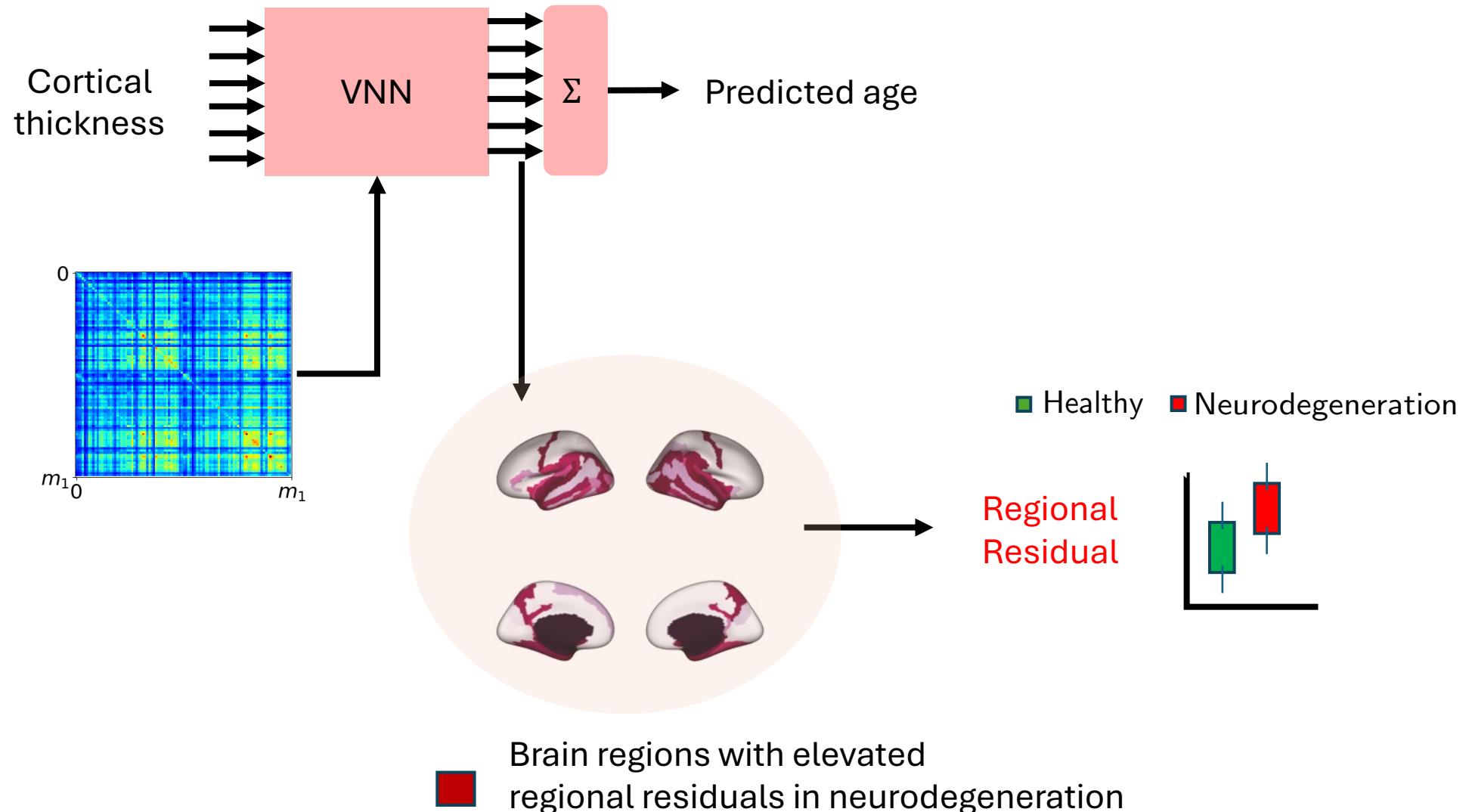
VNNs provide an anatomically interpretable and explainable brain age gap



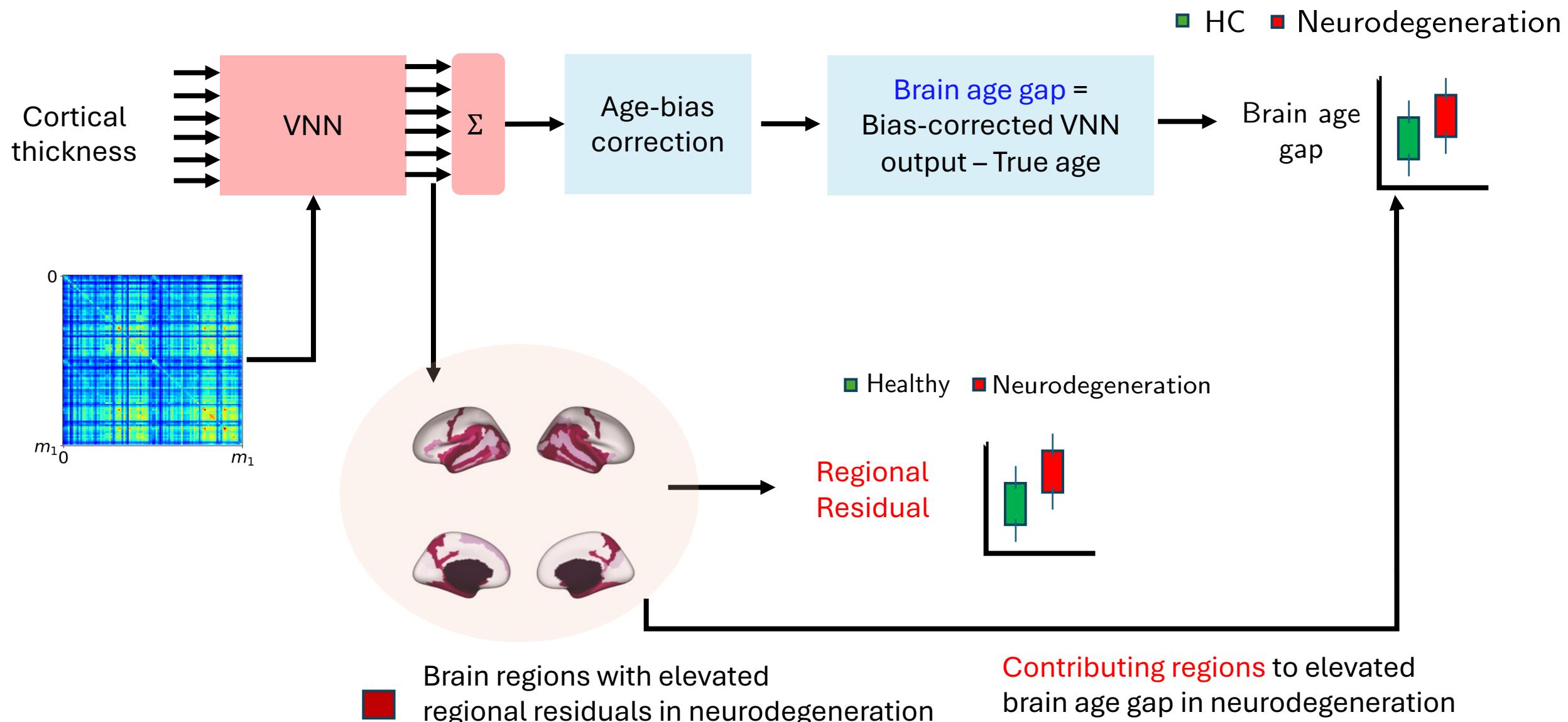
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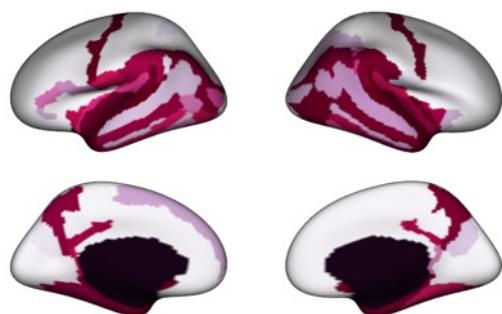
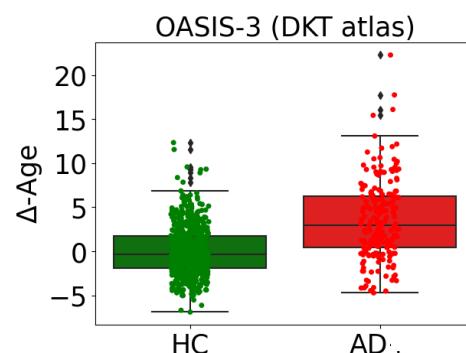
Experiments

- Participants from OASIS-3 dataset [*], 148 cortical thickness features per individual
(Distrieux brain atlas)

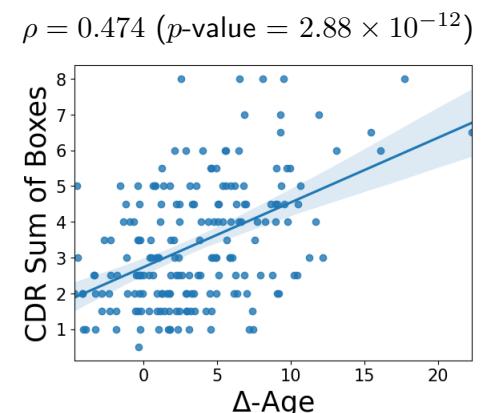
	HC	AD
Number	611	194
Age	68.38 (7.62)	74.72 (7.02)
Sex (m/f)	260/351	100/94
CDR sum of boxes	0	3.45 (1.74)

HC group: cognitively normal
AD group: AD diagnosis
CDR: Clinical dementia rating

- Brain age gap is elevated in **AD** group and correlated with CDR sum of boxes



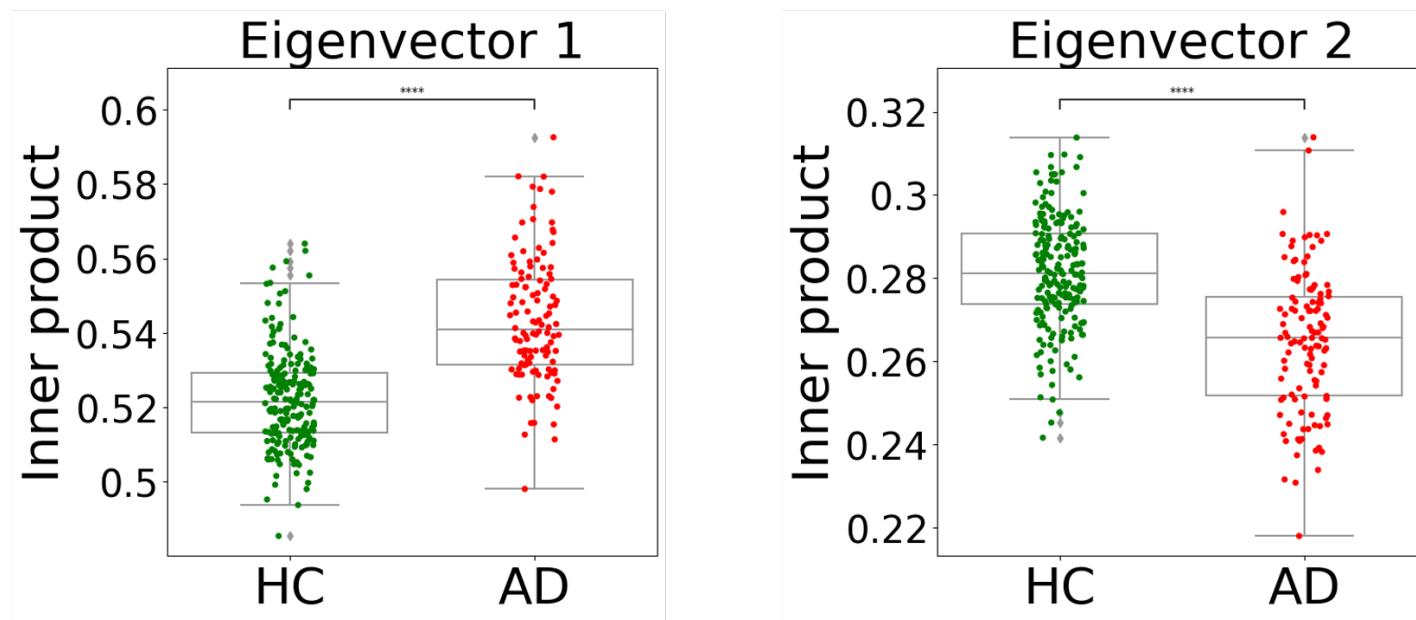
Anatomical interpretability



[*] Pamela J LaMontagne, et al. OASIS-3: longitudinal neuroimaging, clinical, and cognitive dataset for normal aging and Alzheimer disease. MedRxiv, 2019

Experiments

- VNN **distinctly** exploits eigenvectors in **AD** and **HC** groups

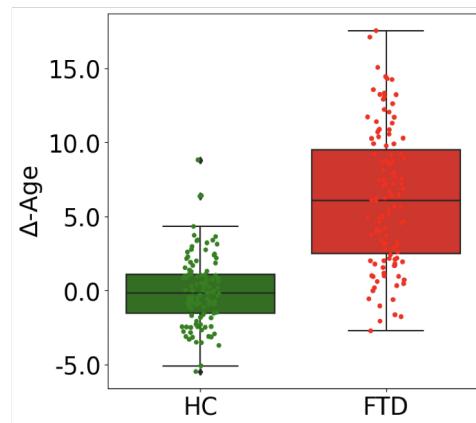


➡ explains anatomical interpretability of brain age gap in **AD**

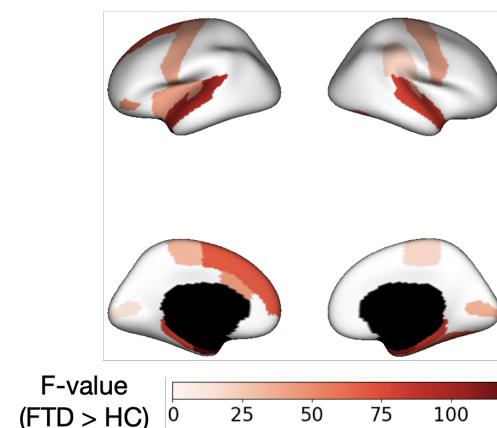
Experiments

- Whole brain cortical thickness dataset for Frontotemporal Dementia (FTD)
 - Healthy controls (HC, n = 114, age = 64.51 ± 6.51 years, 65 females)
 - FTD diagnosis (FTD, n = 119, age = 64.72 ± 6.78 years, 47 females)
- 68 cortical thickness features (Desikan-Killiany atlas)

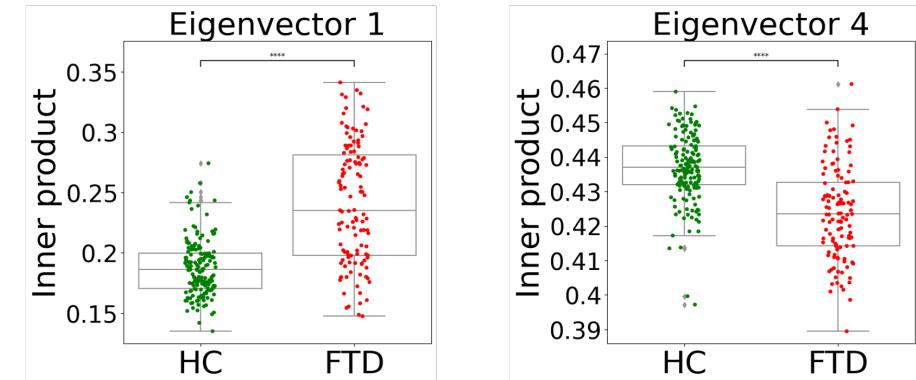
Brain age gap distributions



Anatomic interpretability



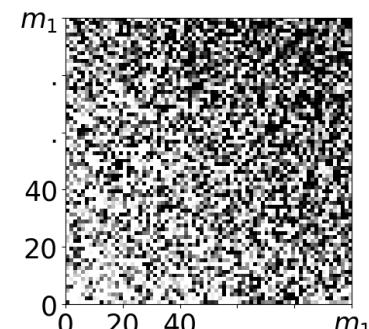
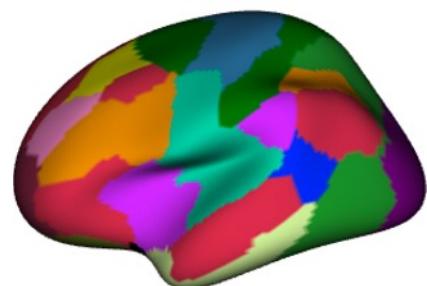
Explaining anatomic interpretability



Brain age gap prediction on multi-scale datasets

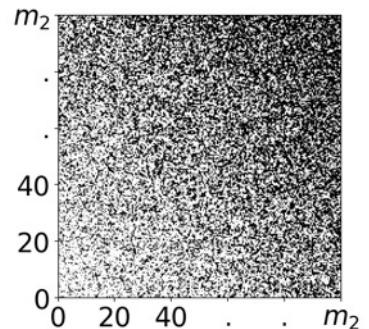
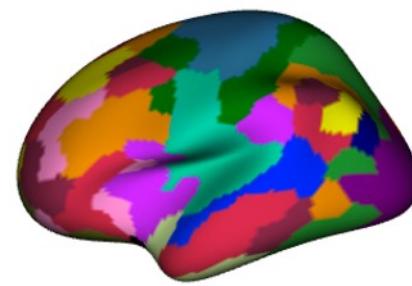
- Datasets capture information about same phenomenon at **different scales**

Dataset with m_1 features



Covariance matrix \mathbf{C}_{m_1}
(size $m_1 \times m_1$)

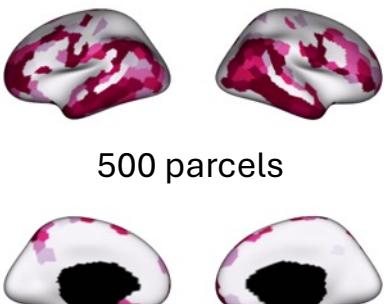
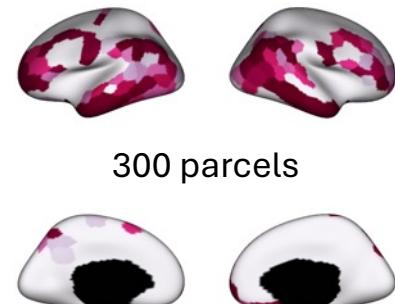
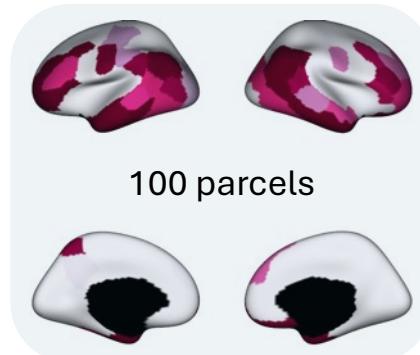
Dataset with m_2 features



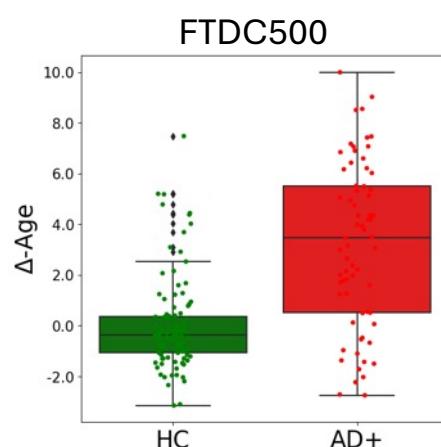
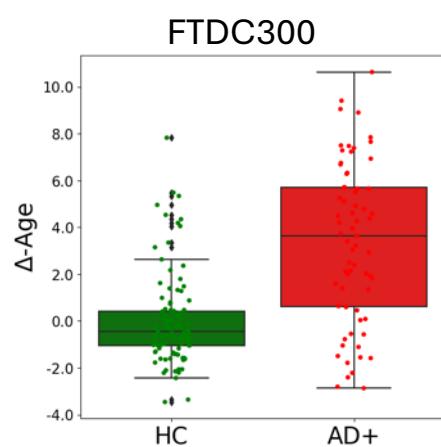
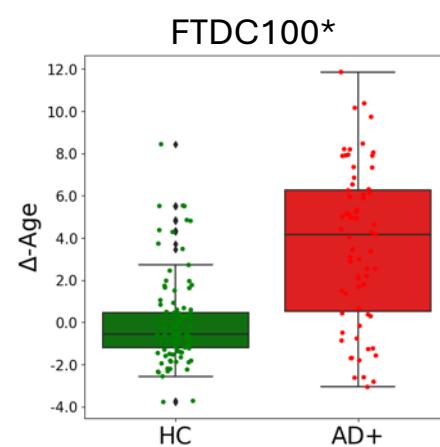
Covariance matrix \mathbf{C}_{m_2}
(size $m_2 \times m_2$)

Recap: Transferability of VNNs cross-validates brain age gap in multi-resolution setting

Objective: Brain age gap prediction in **HC (healthy)** and **AD+ (Alzheimer's)** cohorts from VNNs trained on 100-feature dataset



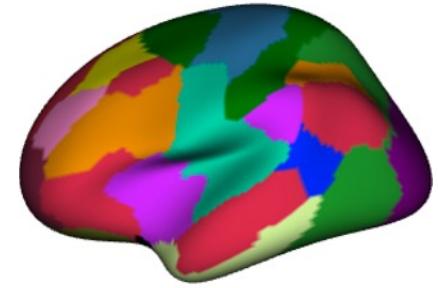
- ROIs contributing to elevated brain age gap in **AD+** across different resolutions



- Brain age gap is elevated in AD+ w.r.t **HC** cohort in 100-feature dataset
- Results on brain age gap retained after transferring VNN to 300 and 500-feature datasets

Conclusions

- Brain age gap prediction models show wide generalizability
- VNNs provide a **principled** perspective to brain age gap
 - anatomically interpretable and explainable
- VNN-derived brain age is a **biomarker** for tracking neurodegeneration and disease monitoring
- **Transferability** of VNNs help cross-validate interpretability



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