

```

1  include("hw4_helpers.jl");
2
3  using ArgParse;
4
5  s = ArgParseSettings();
6  @add_arg_table s begin
7      "-A"
8          help = "Coefficient of 1/2 d(u^2)/dx, like a wave speed"
9          arg_type = Float64
10         default = 1.0
11      "-B"
12         help = "Diffusion coefficient"
13         arg_type = Float64
14         default = 1.0
15      "-C"
16         help = "Coefficient of du/dt"
17         arg_type = Float64
18         default = 1.0
19      "-H"
20         help = "Grid spacing"
21         arg_type = Float64
22         default = 0.2
23      "-K"
24         help = "Time step size"
25         arg_type = Float64
26         default = 0.01
27      "--show-plot", "-P"
28         help = "show plot of solution"
29         action = :store_true
30      "--fname", "-f"
31         help = "file name of plot"
32         default = ""
33      "--show-error", "-E"
34         help = "show L2 error"
35         action = :store_true
36  end
37
38  pa = parse_args(s);
39
40  const a = pa["A"];
41  const b = pa["B"];
42  const c = pa["C"];
43  const h = pa["H"];
44  const k = pa["K"];
45
46  # analytical solution
47  asoln(x, t) = a - c * tanh(c / (2*b) * (x - a*t));
48
49  xs = linspace(-1.0, 1.0, Int(round((2.0) / h)));
50  ts = linspace(0.0, 1.0, Int(round(1.0 / k)));
51  const M, K = length(xs), length(ts);
52
53  u = SharedArray{Float64, (M, K); init = x -> 0};
54  u[:, 1] = map(x -> asoln(x, 0.0), xs);
55
56  const α1 = (k * a) / (4 * h);
57  const α2 = (k * b) / (h^2);
58
59  for n in 1:K-1
60      for m=2:M-1
61          u[m, n+1] = u[m, n] + (-α1 * (u[m+1, n]*u[m+1, n] - u[m-1, n]*u[m-1, n])
62              + α2 * (u[m+1, n] - 2 * u[m, n] + u[m-1, n])) / c;
63      end
64      u[1, n+1] = asoln(xs[1], ts[n+1]);

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65     u[end, n+1] = asoln(xs[end], ts[n+1]);
66 end
67
68 if pa["show-plot"] || pa["fname"] != ""
69     plot_solution(xs, ts, u, asoln; t="\$a = $a, b = $b, c = $c, h = $h, k = $k\$",
70                 show_plot=pa["show-plot"], fname=pa["fname"]);
71 end
72
73 if pa["show-error"]
74     println("Relative L2 error");
75     for (t, n) in zip(ts, 1:K)
76         u_analytical = map(x -> asoln(x, t), xs);
77         println(@sprintf("%5.4lf %5.4lf", t,
78                         norm(u[:, n] - u_analytical, 2) / norm(u_analytical, 2)));
79     end
80 end

```