



Little Piplup

Contest Teamnote
UCPC 2019 ver



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Contents

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1 Settings

1.1 C++

2 Data Structures

2.1 Segment Tree - Range Minimum

필요한 연산에 따라 적당히 수정해서 쓸 수 있는 SegTree 구현. 현재 range minimum을 기준으로 작성됨.

주의 : 배열이 0-base 인덱스인 것을 가정하고 작성되어 있음.

2.2 Segment Tree Lazy Propagation

구간 업데이트 연산을 빠르게 하기 위한 Lazy Propagation이 적용된 SegTree.

주의 : 배열이 0-base 인덱스인 것을 가정하고 작성되어 있음.

2.3 Fenwick Tree

```
const int TSIZE = 100000;
int tree[TSIZE + 1];

// Returns the sum from index 1 to p, inclusive
int query(int p)
{
    int ret = 0;
    for (; p > 0; p -= p & -p)
        ret += tree[p];
    return ret;
}

// Adds val to element with index p
void add(int p, int val)
{
    for (; p <= TSIZE; p += p & -p) tree[p] += val;
}
```

2.4 Disjoint Set Union (Union - Find)

```
// Original Author : Ashishgup
struct Disjoint_Set_Union
{
    int parent[V], size[V];
    Disjoint_Set_Union(int n = V-1)
    {
        init(n);
    }
    void init(int n)
    {
        for(int i=1;i<=n;i++)
        {
            parent[i]=i;
            size[i]=1;
        }
    }
    int Find(int k)
    {
        while(k!=parent[k])
        {
            parent[k]=parent[parent[k]];
            k=parent[k];
        }
    }
}
```

```

    }
    return k;
}
int getSize(int k)
{
    return size[Find(k)];
}
void unite(int x, int y)
{
    int u=Find(x), v=Find(y);
    if(u==v)
        return;
    if(size[u]>size[v])
        swap(u, v);
    size[v]+=size[u];
    size[u] = 0;
    parent[u] = parent[v];
}
} dsu;

```

3 Mathematics

3.1 Useful Mathematical Formula

- Catalan Number : Number of valid parentheses strings with n pairs

$$C_n = \frac{1}{n+1} \binom{2n}{n}$$

- Nim Game : Remember - XOR of all piles.

- Lucas Formula : $\binom{n}{m} = \prod \binom{n_i}{m_i} \mod p$

3.2 Number of Integer Partition

```

def partitions(n):
    parts = [1]+[0]*n
    for t in range(1, n+1):
        for i, x in enumerate(range(t, n+1)):
            parts[x] += parts[i]
    return parts[n]

```

3.3 Binomial Coefficient

Fast-to-Type Binomial coefficient

3.4 Extended Euclidean Algorithm

```

int Extended_Euclid(int a, int b, int *x, int *y)
{
    if (a == 0)
    {
        *x = 0;
        *y = 1;
        return b;
    }
    int x1, y1;
    int EEd = Extended_Euclid(b%a, a, &x1, &y1);
    *x = y1 - (b/a) * x1;
    *y = x1;
    return EEd;
}

```

3.5 Fast Modulo Exponentiation

Calculating $x^y \mod p$ in $\mathcal{O}(\log y)$ time.

```

/*
Fast Modulo Exponentiation algorithm
Runs on  $O(\log y)$  time,
calculate  $x^y \bmod p$ 
*/

```

```

ll modpow(ll x, ll y, ll p)
{
    ll res = 1;
    x = x % p;
    while (y > 0)
    {
        if (y & 1)
            res = (res*x) % p;
        y = y>>1;
        x = (x*x) % p;
    }
    return res;
}

```

3.6 Miller-Rabin Primality Testing

Base values of a chosen so that results are tested to be correct up to 10^{14} .

```

bool MRwitness(ll n, ll s, ll d, ll a)
{
    ll x = modpow(a, d, n);
    ll y = -1;

    while (s)
    {
        y = (x * x) % n;
        if (y == 1 && x != 1 && x != n-1)
            return false;
        x = y;
        s--;
    }
    return (y==1);
}

bool Miller_Rabin(ll n)
{
    if (n<2)

```

```

        return false;
    if (n == 2 || n == 3 || n == 5 || n == 7 ||
        n == 11 || n == 13 || n == 17)
        return true;
    if (n%2 == 0 || n%3 == 0 || n%5 == 0)
        return false;
    ll d = (n-1) / 2;
    ll s = 1;
    while (d%2==0)
    {
        d /= 2;
        s++;
    }
    int candidate[7] = {2,3,5,7,11,13,17};
    bool result = true;
    for (auto i : candidate)
    {
        result = result & MRwitness(n,s,d,i);
        if (!result)
            break;
    }
    return result;
}

```

3.7 Pollard-Rho Factorization

```

ll PollardRho(ll n)
{
    srand (time(NULL));
    if (n==1)
        return n;
    if (n % 2 == 0)
        return 2;
    ll x = (rand()%(n-2))+2;
    ll y = x;
    ll c = (rand()%(n-1))+1;
    ll d = 1;
    while (d==1)
    {
        x = (modpow(x, 2, n) + c + n)%n;
        y = (modpow(y, 2, n) + c + n)%n;
        y = (modpow(y, 2, n) + c + n)%n;
        d = gcd(abs(x-y), n);

```

```

        if (d==n)
            return PollardRho(n);
    }
    return d;
}

```

3.8 Euler Totient

Calculating number of integers below n which is coprime with n .

```

#define ll long long
ll euler_phi(ll n)
{
    ll p=2;
    ll ephi = n;
    while(p*p<=n)
    {
        if (n%p == 0)
            ephi = ephi/p * (p-1);
        while(n%p==0)
            n/=p;
        p++;
    }
    if (n!=1)
    {
        ephi /= n;
        ephi *= (n-1);
    }
    return ephi;
}

```

3.9 Modular Multiplicative Inverse

```

ll modinv(ll x, ll p)
{
    return modpow(x,p-2,p);
}

```

4 Geometry

4.1 CCW

```

//Is 3 points Counterclockwise? 1 : -1
//0 : on same line
int CCW(Point a, Point b, Point c)
{
    int op = a.x*b.y + b.x*c.y + c.x*a.y;
    op -= (a.y*b.x + b.y*c.x + c.y*a.x);
    if (op > 0)
        return 1;
    else if (op == 0)
        return 0;
    else
        return -1;
}

```

4.2 Point in polygon

Returns boolean, if point is in the polygon (represented as vector of points).

```

// point in polygon test
inline double is_left(Point p0, Point p1, Point p2)
{
    return (p1.x - p0.x) * (p2.y - p0.y) - (p2.x - p0.x) * (p1.y - p0.y);
}
bool is_in_polygon(Point p, vector<Point>& poly)
{
    int wn = 0;
    for (int i = 0; i < poly.size(); ++i)
    {
        int ni = (i + 1 == poly.size()) ? 0 : i + 1;
        if (poly[i].y <= p.y)
        {
            if (poly[ni].y > p.y)
                if (is_left(poly[i], poly[ni], p) > 0)
                    ++wn;
        }
        else
        {
            if (poly[ni].y <= p.y)
                if (is_left(poly[i], poly[ni], p) < 0)
                    --wn;
        }
    }
}

```

```

    }
    return wn != 0;
}

```

4.3 Length of Segment Union

Length of segment union, from vector of {start, end}.

```

//Src : e-maxx
int length_union(const vector<pair<int, int>> &a)
{
    int n = a.size();
    vector<pair<int, bool>> x(n*2);
    for (int i = 0; i < n; i++)
    {
        x[i*2] = {a[i].first, false};
        x[i*2+1] = {a[i].second, true};
    }

    sort(x.begin(), x.end());

    int result = 0;
    int c = 0;
    for (int i = 0; i < n * 2; i++)
    {
        if (i > 0 && x[i].first > x[i-1].first && c > 0)
            result += x[i].first - x[i-1].first;
        if (x[i].second)
            c--;
        else
            c++;
    }
    return result;
}

```

4.4 Closest Pair Problem

Requires : Points must be sorted with x-axis.

Runs in $\mathcal{O}(n \log^2 n)$

```

int dist (Point &p, Point &q)
{
    return (p.x-q.x)*(p.x-q.x) + (p.y-q.y)*(p.y-q.y);
}

```

```

bool compare(Point &p, Point &q)
{
    return (p.x < q.x);
}

bool ycompare(Point &p, Point &q)
{
    return (p.y < q.y);
}

Point pts[101010];

int closest_pair(Point p[], int n)
{
    //printf("%p call %d\n",p,n);
    if (n==2)
    {
        return dist(p[0], p[1]);
    }
    if (n==3)
    {
        return min(dist(p[0],p[1]),
                    min(dist(p[1],p[2]),dist(p[0],p[2])));
    }
    Point mid[n];
    int line = (p[n/2 - 1].x + p[n/2].x) / 2;
    int d = min(closest_pair(p, n/2), closest_pair(p + n/2, n - n/2));
    int pp = 0;
    for (int i = 0; i < n; i++)
    {
        int t = line - p[i].x;
        if (t*t < d)
        {
            mid[pp] = p[i];
            pp++;
        }
    }
    sort(mid,mid+pp,ycompare);
    for (int i = 0; i < pp - 1; i++)
        for (int j = i + 1; j < pp && mid[j].y - mid[i].y < d; j++)
            d = min(d, dist(mid[i], mid[j]));
    return d;
}

```

4.5 Convex Hull (Graham Scan)

```
// From GeeksforGeeks.
Point nextToTop(stack<Point> &S)
{
    Point p = S.top();
    S.pop();
    Point res = S.top();
    S.push(p);
    return res;
}

int swap(Point &p1, Point &p2)
{
    Point temp = p1;
    p1 = p2;
    p2 = temp;
}

int distSq(Point p1, Point p2)
{
    return (p1.x - p2.x)*(p1.x - p2.x) +
           (p1.y - p2.y)*(p1.y - p2.y);
}

int orientation(Point p, Point q, Point r) // Basically CCW
{
    int val = (q.y - p.y) * (r.x - q.x) -
              (q.x - p.x) * (r.y - q.y);

    if (val == 0) return 0; // colinear
    return (val > 0)? 1: 2; // clock or counterclock wise
}

int compare(const void *vp1, const void *vp2)
{
    Point *p1 = (Point *)vp1;
    Point *p2 = (Point *)vp2;

    // Find orientation
    int o = orientation(p0, *p1, *p2);
    if (o == 0)
```

```
        return (distSq(p0, *p2) >= distSq(p0, *p1))? -1 : 1;

    return (o == 2)? -1: 1;
}

// Prints convex hull of a set of n points.
void convexHull(Point points[], int n)
{
    // Find the bottommost point
    int ymin = points[0].y, min = 0;
    for (int i = 1; i < n; i++)
    {
        int y = points[i].y;
        if ((y < ymin) || (ymin == y &&
            points[i].x < points[min].x))
            ymin = points[i].y, min = i;
    }

    // Place the bottom-most point at first position
    swap(points[0], points[min]);

    // Sort n-1 points with respect to the first point.
    p0 = points[0];
    qsort(&points[1], n-1, sizeof(Point), compare);

    // If two or more points make same angle with p0,
    // Remove all but the one that is farthest from p0
    int m = 1;
    for (int i=1; i<n; i++)
    {
        while (i < n-1 && orientation(p0, points[i],
            points[i+1]) == 0)

            i++;
        points[m] = points[i];
        m++;
    }

    // If modified array of points has less than 3 points,
    // convex hull is not possible
    if (m < 3) return;

    // Create an empty stack and push first three points
```



```

// to it.
stack <Point> S;
S.push(points[0]);
S.push(points[1]);
S.push(points[2]);

// Process remaining n-3 points
for (int i = 3; i < m; i++)
{
    while (orientation(nextToTop(S), S.top(), points[i]) != 2)
        S.pop();
    S.push(points[i]);
}

// Now stack has the output points, print contents of stack
while (!S.empty())
{
    Point p = S.top();
    cout << "(" << p.x << ", " << p.y << ")" << endl;
    S.pop();
}
}

```

4.6 Intersection of Line Segment

//jason9319.tistory.com/358. modified

```

int isIntersect(Point a, Point b, Point c, Point d)
{
    int ab = ccw(a, b, c)*ccw(a, b, d);
    int cd = ccw(c, d, a)*ccw(c, d, b);
    if (ab == 0 && cd == 0)
    {
        if (a > b)swap(a, b);
        if (c > d)swap(c, d);
        return (c <= b&&a <= d);
    }
    return (ab <= 0 && cd <= 0);
}

```

5 Graphs

5.1 Topological Sorting

Topological sorting with dfs

```

vector <int> graph[V];
bool visited[V];
vector <int> sorted;

void dfs(int root)
{
    visited[root] = 1;
    for (auto it:graph[root])
    {
        if (!visited[it])
            dfs(it);
    }
    sorted.push_back(root);
}

int main()
{
    int n, m;
    scanf("%d%d",&n,&m);
    for (int i = 0; i<m; i++)
    {
        int small,big;
        scanf("%d%d",&small,&big);
        graph[small].push_back(big);
    }
    for (int i = 1; i<=n; i++)
        if (!visited[i])
            dfs(i);
    reverse(sorted.begin(),sorted.end()); // must reverse!
}

```

5.2 Lowest Common Ancestor

LCA Algorithm by sparse table. minlen : (x, y) 사이를 잇는 간선 중 최소 길이 간선.
maxlen : (x, y) 사이를 잇는 간선 중 최대 길이 간선.

```

int n, k;
bool visited[101010];
int par[101010][21], maxedge[101010][21], minedge[101010][21];
int d[101010];

```

```

vector <pii> graph[101010]; // {destination, weight}
void dfs(int here,int depth) // run dfs(root,0)
{
    visited[here] = true;
    d[here] = depth;
    for (auto there : graph[here])
    {
        if (visited[there.first])
            continue;
        dfs(there.first, depth + 1);
        par[there.first][0] = here;
        maxedge[there.first][0] = there.second;
        minedge[there.first][0] = there.second;
    }
}

void precomputation()
{
    for (int i = 1; i<21; i++)
    {
        for (int j = 1; j<=n; j++)
        {
            par[j][i] = par[par[j][i-1]][i-1];
            maxedge[j][i] = max(maxedge[j][i - 1],
                               maxedge[par[j][i - 1]][i - 1]);
            minedge[j][i] = min(minedge[j][i - 1],
                               minedge[par[j][i - 1]][i - 1]);
        }
    }
}

pii lca(int x, int y)
{
    int maxlen = INT_MIN;
    int minlen = INT_MAX;
    if (d[x]>d[y])
        swap(x,y);
    for (int i = 20; i>=0; i--)
    {
        if (d[y]-d[x] >= (1<<i))
        {

```

```

            minlen = min(minlen,minedge[y][i]);
            maxlen = max(maxlen,maxedge[y][i]);
            y = par[y][i];
        }
    }
    if (x==y)
        return {minlen, maxlen};
    for (int i = 20; i>=0; i--)
    {
        if (par[x][i] != par[y][i])
        {
            minlen = min(minlen,min(minedge[x][i],minedge[y][i]));
            maxlen = max(maxlen,max(maxedge[x][i],maxedge[y][i]));
            x = par[x][i];
            y = par[y][i];
        }
    }
    minlen = min(minlen,min(minedge[x][0],minedge[y][0]));
    maxlen = max(maxlen,max(maxedge[x][0],maxedge[y][0]));

    int lca_point = par[x][0];
    return {minlen,maxlen};
}

void tobedone()
{
    dfs(1,0);
    precomputation();
}

```

5.3 MST Kruskal Algorithm

Based on Union-Find implementation

$\mathcal{O}(E \log E)$ if path-compressed Union Find.

```

int Kruskal()
{
    int mstlen = 0;
    sort(edgelist.begin(),edgelist.end());
    for (auto it:edgelist)
    {
        if (dsu.Find(it.s)==dsu.Find(it.e)) // Cycle Detection
            continue;
        else

```

```

    {
        dsu.unite(it.s,it.e);
        mstlen += it.w;
    }
}
return mstlen;
}

```

5.4 MST Prim Algorithm

```

vector <pii> Tree[101010];
// Note that we use {weight, destination} pair here.
// This is to use priority_queue!
bool visit[101010];
priority_queue <pii, vector<pii>, greater<pii>> pq;
void add(int i)
{
    visit[i] = true;
    for (auto it:Tree[i])
        pq.push(it);
}

int Prim(int start)
{
    int mstlen = 0;
    add(start);
    while(!pq.empty())
    {
        int cur = pq.top().second;
        int weight = pq.top().first;
        pq.pop();
        if (visit[cur])
            continue;
        else
        {
            mstlen+=weight;
            add(cur);
        }
    }
    return mstlen;
}

```

5.5 Dinic's Algorithm

//Original Author : <https://plzrun.tistory.com/>

```

int r[V][V]; // flow capacity
bool chk[V][V]; // edge existence
int level[V];
vector<int> v[V];
queue<int> q;

bool bfs(int src, int sink)
{
    memset(level,-1,sizeof(level));
    level[src]=0;
    q.push(src);
    while(!q.empty())
    {
        int x = q.front();
        q.pop();
        for(int y: v[x])
        {
            if(r[x][y]>0 && level[y]<0) {
                level[y]=level[x]+1;
                q.push(y);
            }
        }
    }
    return level[sink]>=0;
}

int work[V];

int dfs(int x, int sink, int f)
{
    if(x==sink) return f;
    for(int &i=work[x]; i<v[x].size(); i++)
    {
        int y=v[x][i];
        if(level[y]>level[x] && r[x][y]>0)
        {
            int t = dfs(y,sink,min(f,r[x][y]));
            if(t>0)
            {

```

```

        r[x][y] -= t;
        r[y][x] += t;
        return t;
    }
}
}
return 0;
}

int dinic(int src, int sink)
{
    int flow=0;
    while(bfs(src,sink))
    {
        int f=0;
        memset(work,0,sizeof(work));
        while((f=dfs(src,sink,INT_MAX))>0)
            flow+=f;
    }
    return flow;
}

```

6 Shortest Path

6.1 Dijkstra

$\mathcal{O}(E \log V)$ Single-Start-Shortest-Path.

Not working for graph with minus weight.

```

const int INF = 987654321;
const int MX = 105050;
struct Edge
{
    int dest, w;
    bool operator<(const Edge &p) const
    {
        return w > p.w;
    }
};

bool relax(Edge edge, int u, int dist[])
{
    bool flag = 0;
    int v = edge.dest, w = edge.w;
    if (dist[v] > dist[u] + w && (dist[u] != INF))
    {
        flag = true;
        dist[v] = dist[u] + w;
    }
    return flag;
}

int dijkstra(int dist[], int start, vector<Edge> graph[])
{
    fill(dist, dist+MX, INF);
    dist[start] = 0;
    priority_queue<Edge> pq;
    pq.push({start, 0});
    while(!pq.empty())
    {
        Edge x = pq.top();
        int v = x.dest, w = x.w;
        pq.pop();
        if (w > dist[v])
            continue;
        for (auto ed : graph[v])

```

```

        if (relax(ed, v, dist))
            pq.push({ed.dest, dist[ed.dest]});
    }
}

```

6.2 Bellman Ford

$\mathcal{O}(EV)$ Single-Start-Shortest-Path.

Not working for graph with minus cycle \rightarrow must detect.

```

struct Edge
{
    int u, v, w;
};

vector<Edge> edgelist;
int V, E;
int dist[V+1];

bool relax_all_edge()
{
    bool flag = false;
    for (auto it:edgelist)
    {
        int u = it.u, v = it.v, w = it.w;
        if (dist[v] > dist[u] + w && (dist[u] != INF))
        {
            flag = true;
            dist[v] = dist[u] + w;
        }
    }
    return flag;
}

int bellman_ford()
{
    fill(dist, dist+V+2, INF);
    dist[1] = 0;
    for (int i = 0; i < V-1; i++)
    {
        relax_all_edge();
    }
    if (relax_all_edge())

```

```

        return -1;
    else
        return 0;
}

```

6.3 SPFA Algorithm

Average $\mathcal{O}(E)$, worst $\mathcal{O}(VE)$ time. Average-case improvement of Bellman Ford by using an additional queue.

\rightarrow 데이터를 누가 짤지를 생각해 보면 그냥 이런거 집어치우는게 맞을듯. ICPC Preliminary에서나 쓰자.

6.4 Floyd-Warshall

Works on adjacency matrix, in $\mathcal{O}(V^3)$.

```

int d[120][120];
int n;
void Floyd_Warshall()
{
    for (int i = 1; i <= n; i++)
        for (int j = 1; j <= n; j++)
            for (int k = 1; k <= n; k++)
                d[j][k] = MIN(d[j][k], d[j][i] + d[i][k]);
}

```

7 Dynamic

7.1 Longest Increasing Subsequence

Find LIS in $\mathcal{O}(n \log n)$ time.

```
vector<int> sequence;
vector<int> L;
int lis_len;
int position[BIG];
int lis[BIG];
int lis_pushed[BIG];
int n;
void FindLIS(vector<int> &seq)
{
    L.push_back(seq[0]);
    position[0] = 0;
    for (int i = 1; i<n; i++)
    {
        int u = L.size();
        if (seq[i] > L[u-1])
        {
            position[i] = u;
            L.push_back(seq[i]);
        }
        else
        {
            int pos = lower_bound(L.begin(), L.end(), seq[i]) - L.begin();
            L[pos] = seq[i];
            position[i] = pos;
        }
    }
    lis_len = L.size();
    int lookingfor = lis_len - 1;
    for (int i = n - 1; i >= 0; i--)
    {
        if (lis_pushed[position[i]] == 0 && lookingfor == position[i])
        {
            lis[position[i]] = seq[i];
            lis_pushed[position[i]] = 1;
            lookingfor--;
        }
    }
}
```

```
}
```

7.2 Largest Sum Subarray

Computes sum of largest sum subarray in $\mathcal{O}(N)$

```
void consecsum(int n)
{
    dp[0] = number[0];
    for (int i = 1; i<n; i++)
        dp[i] = MAX(dp[i-1]+number[i], number[i]);
}

int maxsum(int n)
{
    consecsum(n);
    int max_sum = -INF;
    for (int i = 0; i<n; i++)
        dp[i] > max_sum ? max_sum = dp[i] : 0;
    return max_sum;
}
```

7.3 0-1 Knapsack

```
int dp[N][W];
int weight[N];
int value[N];
void knapsack()
{
    for (int i = 1; i<=n; i++)
    {
        for (int j = 0; j<=W; j++)
            dp[i][j] = dp[i-1][j];
        for (int j = weight[i]; j<=W; j++)
            dp[i][j] = max(dp[i][j], dp[i-1][j-weight[i]]+value[i]);
    }
}
```

7.4 Longest Common Subsequence

```
//input : two const char*
//output : their LCS, in c++ std::string type
string lcsf(const char *X, const char *Y)
{
    int m = (int)strlen(X);
    int n = (int)strlen(Y);
```

```

int L[m+1][n+1];
for (int i=0; i<=m; i++)
{
    for (int j=0; j<=n; j++)
    {
        if (i == 0 || j == 0)
            L[i][j] = 0;
        else if (X[i-1] == Y[j-1])
            L[i][j] = L[i-1][j-1] + 1;
        else
            L[i][j] = max(L[i-1][j], L[i][j-1]);
    }
}
int index = L[m][n];

char lcsstring[index+1];
lcsstring[index] = 0;

int i = m, j = n;
while (i > 0 && j > 0)
{
    if (X[i-1] == Y[j-1])
    {
        lcsstring[index-1] = X[i-1];
        i--; j--; index--;
    }
    else if (L[i-1][j] > L[i][j-1])
        i--;
    else
        j--;
}
string lcsstr = lcsstring;
return lcsstr;
}

```

8 String

8.1 KMP Algorithm

```

// Original Author : bowbowbow (bowbowbow.tistory.com)
vector<int> getPi(string p)
{
    int j = 0;

```

```

    int plen = p.length();
    vector<int> pi;
    pi.resize(plen);
    for(int i = 1; i< plen; i++)
    {
        while((j > 0) && (p[i] != p[j]))
            j = pi[j-1];
        if(p[i] == p[j])
        {
            j++;
            pi[i] = j;
        }
    }
    return pi;
}

vector <int> kmp(string s, string p)
{
    vector<int> ans;
    auto pi = getPi(p);
    int slen = s.length(), plen = p.length(), j = 0;
    for(int i = 0 ; i < slen ; i++)
    {
        while(j>0 && s[i] != p[j])
            j = pi[j-1];
        if(s[i] == p[j])
        {
            if(j==plen-1)
            {
                ans.push_back(i-plen+1);
                j = pi[j];
            }
            else
                j++;
        }
    }
    return ans;
}

```

8.2 Manacher's Algorithm

$A[i]$ = i 번을 중심으로 하는 가장 긴 팰린드롬이 되는 반지름.

```

//original Author : Myungwoo (blog.myungwoo.kr)
int N,A[MAXN];

```

```

char S[MAXN];

void Manachers()
{
    int r = 0, p = 0;
    for (int i=1; i<=N; i++)
    {
        if (i <= r)
            A[i] = min(A[2*p-i], r-i);
        else
            A[i] = 0;
        while (i-A[i]-1 > 0 && i+A[i]+1 <= N
            && S[i-A[i]-1] == S[i+A[i]+1])
            A[i]++;
        if (r < i+A[i])
            r = i+A[i], p = i;
    }
}

```

8.3 Trie

```

struct Trie
{
    int trie[NODE_MAX][CHAR_N];
    int nxt = 1;
    void insert(const char* s)
    {
        int k = 0;
        for (int i = 0; s[i]; i++)
        {
            int t = s[i] - 'a';
            if (!trie[k][t])
            {
                trie[k][t] = nxt;
                nxt++;
            }
            k = trie[k][t];
        }
        trie[k][26] = 1;
    }
    bool find(const char* s, bool exact = false)
    {
        int k = 0;

```

```

        for (int i = 0; s[i]; i++)
        {
            int t = s[i] - 'a';
            if (!trie[k][t])
                return false;
            k = trie[k][t];
        }
        if (exact)
        {
            return trie[k][26];
        }
        return true;
    }
};

```

8.4 Rabin-Karp Hashing

Hashmap[k]에, 길이가 len인 부분 문자열의 해시값이 k가 되는 시작점 인덱스 i를 push.

```

const ll MOD = BIG_PRIME;
int L;
char S[STR_LEN];
int safemod(int n)
{
    if(n >= 0)
        return n % MOD;
    return ((-n/MOD+1)*MOD + n) % MOD;
}
vector<int> hashmap[MOD];
void Rabin_Karp(int len)
{
    int Hash = 0;
    int pp = 1;
    for(int i=0; i<=L-len; i++)
    {
        if(i == 0)
        {
            for(int j = 0; j<len; j++)
            {
                Hash = safemod(Hash + S[len-j-1]*pp);
                if(j < len-1)
                    pp = safemod(pp*2);
            }
        }
    }
}

```



```

    else
        Hash = safemod(2*(Hash - S[i-1]*pp) + S[len+i-1]);
        hashmap[Hash].push_back(i);
    }
    return;
}

```

9 Miscellaneous

9.1 Binary and Ternary Search

Preventing stupid mistakes by writing garbage instead of proper binary search.

```

//Finding minimum value with chk() == true
while(lo+1 < hi)
{
    int mid = (lo+hi)/2;

    if(chk(mid))
        lo = mid;
    else
        hi = mid;
}

```

Ternary search

9.2 Useful Bitwise Functions in C++

```

int __builtin_clz(int x); // number of leading zero
int __builtin_ctz(int x); // number of trailing zero
int __builtin_clzll(ll x); // number of leading zero
int __builtin_ctzll(ll x); // number of trailing zero
int __builtin_popcount(int x); // number of 1-bits in x
int __builtin_popcountll(ll x); // number of 1-bits in x

```

```

lsb(n): (n & -n); // last bit (smallest)
floor(log2(n)): 31 - __builtin_clz(n | 1);
floor(log2(n)): 63 - __builtin_clzll(n | 1);

```

```

// compute next perm. ex) 00111, 01011, 01101, 01110, 10011, 10101..
ll next_perm(ll v)
{
    ll t = v | (v-1);
    return (t + 1) | (((~t & ~t) - 1) >> (__builtin_ctz(v) + 1));
}

```

9.3 List of Useful Numbers

< 10 ^k	prime	# of prime	< 10 ^k	prime
1	7	4	10	9999999967
2	97	25	11	99999999977
3	997	168	12	999999999989

4	9973	1229	13	9999999999971
5	99991	9592	14	9999999999973
6	999983	78498	15	9999999999989
7	9999991	664579	16	99999999999937
8	99999989	5761455	17	99999999999997
9	999999937	50847534	18	999999999999989

10 Checkpoints

10.1 Debugging

- $10^5 * 10^5 \Rightarrow$ INTEGER OVERFLOW.
- If unsure with overflow, use
`#define int long long` and stop caring.
- 행렬과 기하의 i, j 인덱스 조심. 헛갈리면 쓰면서 가기.
- output이 특정 수열/OX 형태 : 작은 예제를 Exhasutive Search. 모르는 무언가를 알기 위해서는 데이터가 필요하다.

10.2 Thinking

- 모든 경우를 다 할 수 없나? 왜 안 되지? 시간 복잡도 잘 생각해 보기. 정해의 Target Complexity를 먼저 생각하고 주요 알고리즘들의 Complexity로 짜맞추기.
 예를들어, 퀴리가 30만개 들어온다면 한 퀴리를 적어도 $\log n$ 에 처리할 방법이 아무튼 있다는 뜻.
- 단조함수이며, 충분히 빠르게 검증가능한가 : Binary Search.
- 차원이 높은 문제 : 차원 내려서 생각하기. $3 \rightarrow 2$.
- 이 문제가 사실 그래프 관련 문제는 아닐까?
 - 만약 그렇다면, ‘간선’ 과 ‘정점’ 은 각각..?
 - 간선과 정점이 몇 개 정도 있는가?
- 이 문제에 Overlapping Subproblem이 보이냐?
 \rightarrow Dynamic Programming 을 적용.
- 답의 상한이 Reasonable 하게 작은가?
- 마지막 생각 : 조금 추하지만 해싱이나 Random bitset 을 이용한 $n^2/64$ 같은걸로 뚫을 수 있나?

업데이트 노트 / To-Do

이 페이지는 실제 인쇄 팀노트에 포함되지 않습니다

- 190731 : Rabin-Karp Hashing 추가.
- To-do : LCA 코드에 최단 / 최장 거리 간선, 거리 구하기 추가.

- 190731 : Segment Tree Lazy Propagation 추가.
- 190731 : Segment Tree Struct 구현체로 변경.
- To-do : HLD 코드 넣기.
- To-do : Trie 구현체 두가지 방식 넣기.