Little Piplup

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1 Settings

1.1 C++

```
#include <bits/stdc++.h>
#pragma GCC optimize("03")
#pragma GCC optimize("0fast")
#pragma GCC target("avx,avx2,fma")
#define ll long long
#define eps 1e-7
#define all(x) ((x).begin()),((x).end())
#define usecppio ios::sync_with_stdio(0);cin.tie(0);cout.tie(0);
using namespace std;
using pii = pair<int, int>;
```

2 Data Structures

2.1 Segment Tree - Range Minimum

필요한 연산에 따라 적당히 수정해서 쓸 수 있는 SegTree 구현. 현재 range minimum을 기준으로 작성됨.

주의: 배열이 0-base 인덱스인 것을 가정하고 작성되어 있음.

2.2 Segment Tree Lazy Propagation

구간 업데이트 연산을 빠르게 하기 위한 Lazy Propagation이 적용된 SegTree. 주의 : 배열이 0-base 인덱스인 것을 가정하고 작성되어 있음.

2.3 Fenwick Tree const int TSIZE = 100000; int tree[TSIZE + 1]; // Returns the sum from index 1 to p, inclusive int query(int p) int ret = 0; for (; p > 0; p -= p & -p) ret += tree[p]; return ret; } // Adds val to element with index p void add(int p, int val) for (; p <= TSIZE; p += p & -p) tree[p] += val;</pre> 2.4 Disjoint Set Union (Union - Find) // Original Author : Ashishgup struct Disjoint_Set_Union int connected; int parent[V], size[V]; void init(int n) for(int i=1;i<=n;i++) parent[i]=i; size[i]=1; connected=n; } int Find(int k) while(k!=parent[k]) parent[k]=parent[parent[k]]; k=parent[k];

```
return k;
}
int getSize(int k)
{
    return size[Find(k)];
}
void unite(int x, int y)
{
    int u=Find(x), v=Find(y);
    if(u==v)
        return;
    if(size[u]>size[v])
        swap(par1, par2);
    size[v]+=size[u];
    size[u] = 0;
    parent[u] = parent[v];
}
} dsu;
```

3 Mathematics

3.1 Useful Mathematical Formula

 \bullet Catalan Number: Number of valid parantheses strings with n pairs

$$C_n = \frac{1}{n+1} \binom{2n}{n}$$

- Nim Game : Remember XOR of all piles.
- Lucas Formula : $\binom{n}{m} = \prod \binom{n_i}{m_i} \mod p$

3.2 Number of Integer Partition

```
def partitions(n):
    parts = [1]+[0]*n
    for t in range(1, n+1):
        for i, x in enumerate(range(t, n+1)):
            parts[x] += parts[i]
    return parts[n]
```

3.3 Binomial Coefficient

Fast-to-Type Binomial coefficient, in O(k) time.

```
int Binom(int n, int k)
{
    if (n < k)
        return 0;
    if (k == n || k == 0)
        return 1;
int res = 1;
if ( k > n - k )
    k = n - k;
for (int i = 0; i < k; ++i)
{
    res *= (n - i);
    res /= (i + 1);
}
return res;
}</pre>
```

3.4 Extended Euclidean Algorithm

```
int Extended_Euclid(int a, int b, int *x, int *y)
{
```

```
if (a == 0)
        *x = 0;
        *y = 1;
        return b;
    int x1, y1;
    int EEd = Extended_Euclid(b%a, a, &x1, &y1);
    *x = y1 - (b/a) * x1;
    *v = x1;
    return EEd;
3.5 Fast Modulo Exponentiation
Calculating x^y \mod p in \mathcal{O}(\log y) time.
```

```
Fast Modulo Exponentiation algorithm
Runs on O(log y) time,
calculate x^y mod p
*/
ll modpow(ll x, ll y, ll p)
    ll res = 1;
   x = x \% p;
    while (y > 0)
        if (y & 1)
            res = (res*x) % p;
        y = y >> 1;
        x = (x*x) \% p;
```

3.6 Miller-Rabin Primality Testing

return res;

```
Base values of a chosen so that results are tested to be correct up to 10^{14}.
bool MRwitness(ll n, ll s, ll d, ll a)
{
    11 x = modpow(a, d, n);
```

```
11 y = -1;
    while (s)
        y = (x * x) % n;
        if (y == 1 \&\& x != 1 \&\& x != n-1)
            return false;
        x = y;
        s--;
    return (y==1);
bool Miller_Rabin(ll n)
    if (n<2)
        return false:
    if (n == 2 || n == 3 || n == 5 || n == 7 ||
     n == 11 || n == 13 || n == 17)
        return true;
    if (n\%2 == 0 || n\%3 == 0 || n\%5 == 0)
        return false;
    11 d = (n-1) / 2;
    11 s = 1;
    while (d\%2 == 0)
        d /= 2;
        s++;
    int candidate[7] = \{2,3,5,7,11,13,17\};
    bool result = true;
    for (auto i : candidate)
        result = result & MRwitness(n,s,d,i);
        if (!result)
            break:
    return result;
3.7 Pollard-Rho Factorization
```

11 PollardRho(11 n)

```
srand (time(NULL));
    if (n==1)
        return n;
   if (n \% 2 == 0)
        return 2;
   11 x = (rand()\%(n-2))+2;
   11 y = x;
   11 c = (rand()\%(n-1))+1;
   11 d = 1;
   while (d==1)
        x = (modpow(x, 2, n) + c + n)%n;
       y = (modpow(y, 2, n) + c + n)%n;
        y = (modpow(y, 2, n) + c + n)%n;
        d = gcd(abs(x-y), n);
        if (d==n)
            return PollardRho(n);
   }
    return d;
}
3.8 Euler Totient
Calculating number of integers below n which is coprime with n.
#define ll long long
ll euler_phi(ll n)
   11 p=2;
   ll ephi = n;
   while(p*p<=n)
        if (n\%p == 0)
            ephi = ephi/p * (p-1);
        while(n\%p==0)
            n/=p;
        p++;
   }
   if (n!=1)
        ephi /= n;
        ephi *= (n-1);
```

```
return ephi;
}
3.9 Modular Multiplicative Inverse
11 modinv(ll x, ll p)
   return modpow(x,p-2,p);
}
```

4 Geometry

```
4.1 CCW
```

```
//Is 3 points Counterclockwise? 1 : -1
//0 : on same line
int CCW(Point a, Point b, Point c)
{
    int op = a.x*b.y + b.x*c.y + c.x*a.y;
    op -= (a.y*b.x + b.y*c.x + c.y*a.x);
    if (op > 0)
        return 1;
    else if (op == 0)
        return 0;
    else
        return -1;
}
```

4.2 Point in polygon

if (is_left(poly[i], poly[ni], p) < 0)</pre>

if $(poly[ni].y \le p.y)$

--wn;

```
return wn != 0;
4.3 Length of Segment Union
Length of segment union, from vector of {start, end}.
//Src : e-maxx
int length_union(const vector<pair<int, int>> &a)
    int n = a.size();
    vector<pair<int, bool>> x(n*2);
    for (int i = 0; i < n; i++)
        x[i*2] = {a[i].first, false};
        x[i*2+1] = \{a[i].second, true\};
    }
    sort(x.begin(), x.end());
    int result = 0;
    int c = 0;
    for (int i = 0; i < n * 2; i++)
        if (i > 0 \&\& x[i].first > x[i-1].first \&\& c > 0)
            result += x[i].first - x[i-1].first;
        if (x[i].second)
            c--;
        else
            c++;
    return result;
}
4.4 Closest Pair Problem
Requires: Points must be sorted with x-axis.
Runs in \mathcal{O}(n\log^2 n)
int dist (Point &p, Point &q)
    return (p.x-q.x)*(p.x-q.x) + (p.y-q.y)*(p.y-q.y);
}
```

```
bool compare(Point &p, Point &q)
{
   return (p.x < q.x);
bool ycompare(Point &p, Point &q)
{
    return (p.y<q.y);
Point pts[101010];
int closest_pair(Point p[], int n)
    //printf("%p call %d\n",p,n);
    if (n==2)
        return dist(p[0], p[1]);
    if (n==3)
        return min(dist(p[0],p[1]),
        min(dist(p[1],p[2]),dist(p[0],p[2])));
    Point mid[n];
   int line = (p[n/2 - 1].x + p[n/2].x) / 2;
    int d = min(closest_pair(p, n/2), closest_pair(p + n/2, n - n/2));
    int pp = 0;
   for (int i = 0; i < n; i++)
        int t = line - p[i].x;
        if (t*t < d)
        {
           mid[pp] = p[i];
            pp++;
        }
    sort(mid,mid+pp,ycompare);
   for (int i = 0; i < pp - 1; i++)
        for (int j = i + 1; j < pp && mid[j].y - mid[i].y < d; j++)
            d = min(d, dist(mid[i], mid[j]));
    return d;
```

```
}
4.5 Convex Hull (Graham Scan)
// From GeeksforGeeks.
Point nextToTop(stack<Point> &S)
    Point p = S.top();
    S.pop();
    Point res = S.top();
    S.push(p);
    return res;
int swap(Point &p1, Point &p2)
    Point temp = p1;
    p1 = p2;
    p2 = temp;
int distSq(Point p1, Point p2)
    return (p1.x - p2.x)*(p1.x - p2.x) +
          (p1.y - p2.y)*(p1.y - p2.y);
}
int orientation(Point p, Point q, Point r) // Basically CCW
    int val = (q.y - p.y) * (r.x - q.x) -
             (q.x - p.x) * (r.y - q.y);
    if (val == 0) return 0; // colinear
    return (val > 0)? 1: 2; // clock or counterclock wise
}
int compare(const void *vp1, const void *vp2)
{
   Point *p1 = (Point *)vp1;
   Point *p2 = (Point *)vp2;
   // Find orientation
   int o = orientation(p0, *p1, *p2);
```

```
if (o == 0)
    return (distSq(p0, *p2) >= distSq(p0, *p1))? -1 : 1;
  return (o == 2)? -1: 1:
// Prints convex hull of a set of n points.
void convexHull(Point points[], int n)
  // Find the bottommost point
   int ymin = points[0].y, min = 0;
  for (int i = 1; i < n; i++)
     int y = points[i].y;
    if ((y < ymin) || (ymin == y &&
         points[i].x < points[min].x))</pre>
        ymin = points[i].y, min = i;
  }
  // Place the bottom-most point at first position
  swap(points[0], points[min]);
   // Sort n-1 points with respect to the first point.
   p0 = points[0];
   gsort(&points[1], n-1, sizeof(Point), compare);
  // If two or more points make same angle with p0,
  // Remove all but the one that is farthest from p0
   int m = 1;
  for (int i=1; i<n; i++)
       while (i < n-1 && orientation(p0, points[i],
                                    points[i+1]) == 0)
          i++;
       points[m] = points[i];
       m++;
   }
  // If modified array of points has less than 3 points,
  // convex hull is not possible
   if (m < 3) return;
```

```
// Create an empty stack and push first three points
   // to it.
   stack <Point> S:
   S.push(points[0]);
   S.push(points[1]);
   S.push(points[2]);
   // Process remaining n-3 points
   for (int i = 3; i < m; i++)
      while (orientation(nextToTop(S), S.top(), points[i]) != 2)
         S.pop();
      S.push(points[i]);
   }
   // Now stack has the output points, print contents of stack
   while (!S.empty())
   {
       Point p = S.top();
       cout << "(" << p.x << ", " << p.y <<")" << endl;
       S.pop();
}
     Intersection of Line Segment
//jason9319.tistory.com/358. modified
int isIntersect(Point a, Point b, Point c, Point d)
    int ab = ccw(a, b, c)*ccw(a, b, d);
    int cd = ccw(c, d, a)*ccw(c, d, b);
    if (ab == 0 && cd == 0)
        if (a > b)swap(a, b);
        if (c > d)swap(c, d);
        return (c <= b&&a <= d);
   }
    return (ab <= 0 && cd <= 0);
```

5 Graphs

5.1 Topological Sorting

```
Topological sorting with dfs
vector <int> graph[V];
bool visited[V];
vector <int> sorted;
void dfs(int root)
    visited[root] = 1;
    for (auto it:graph[root])
        if (!visited[it])
            dfs(it):
    }
    sorted.push_back(root);
}
int main()
    int n, m;
    scanf("%d%d",&n,&m);
    for (int i = 0; i < m; i++)
        int small, big;
        scanf("%d%d",&small,&big);
        graph[small].push_back(big);
    for (int i = 1; i<=n; i++)
        if (!visited[i])
            dfs(i);
    reverse(sorted.begin(),sorted.end()); // must reverse!
}
```

5.2 Lowest Common Ancestor

LCA Algorithm by sparse table. minlen : (x,y) 사이를 잇는 간선 중 최소 길이 간선. maxlen : (x,y) 사이를 잇는 간선 중 최대 길이 간선.

```
int n, k;
bool visited[101010];
int par[101010][21], maxedge[101010][21], minedge[101010][21];
```

```
int d[101010];
vector <pii> graph[101010]; // {destination, weight}
void dfs(int here,int depth) // run dfs(root,0)
{
    visited[here] = true;
    d[here] = depth;
    for (auto there : graph[here])
        if (visited[there.first])
            continue;
        dfs(there.first, depth + 1);
        par[there.first][0] = here;
        maxedge[there.first][0] = there.second;
        minedge[there.first][0] = there.second;
}
void precomputation()
    for (int i = 1; i < 21; i++)
        for (int j = 1; j \le n; j + +)
            par[j][i] = par[par[j][i-1]][i-1];
            maxedge[j][i] = max(maxedge[j][i - 1],
                maxedge[par[j][i - 1]][i - 1]);
            minedge[j][i] = min(minedge[j][i - 1],
                minedge[par[j][i - 1]][i - 1]);
        }
    }
}
pii lca(int x, int y)
    int maxlen = INT_MIN;
    int minlen = INT_MAX;
    if (d[x]>d[y])
        swap(x,y);
    for (int i = 20; i >= 0; i --)
        if (d[y]-d[x] >= (1 << i))
        {
```

```
minlen = min(minlen,minedge[y][i]);
            maxlen = max(maxlen, maxedge[y][i]);
            y = par[y][i];
        }
    }
    if (x==y)
        return {minlen, maxlen};
    for (int i = 20; i > = 0; i - -)
        if (par[x][i] != par[y][i])
        {
            minlen = min(minlen,min(minedge[x][i],minedge[y][i]));
            maxlen = max(maxlen,max(maxedge[x][i],maxedge[y][i]));
            x = par[x][i];
            y = par[y][i];
        }
    minlen = min(minlen,min(minedge[x][0],minedge[y][0]));
    maxlen = max(maxlen, max(maxedge[x][0], maxedge[y][0]));
    int lca_point = par[x][0];
    return {minlen,maxlen};
}
void tobedone()
{
    dfs(1,0);
    precomputation();
    MST Kruskal Algorithm
Based on Union-Find implementation
\mathcal{O}(E \log E) if path-compressed Union Find.
int Kruskal()
    int mstlen = 0;
    sort(edgelist.begin(),edgelist.end());
    for (auto it:edgelist)
        if (Find(it.s)==Find(it.e)) // Cycle Detection
            continue;
```

```
else
            Union(it.s,it.e);
            mstlen += it.w;
    }
    return mstlen;
}
5.4 MST Prim Algorithm
vector <pii> Tree[101010];
// Note that we use {weight, destination} pair here.
// This is to use priority_queue!
bool visit[101010];
priority_queue <pii, vector<pii>, greater<pii>> pq;
void add(int i)
    visit[i] = true;
    for (auto it:Tree[i])
        pq.push(it);
}
int Prim(int start)
{
    int mstlen = 0;
    add(start);
    while(!pq.empty())
        int cur = pq.top().second;
        int weight = pq.top().first;
        pq.pop();
        if (visit[cur])
            continue;
        else
        {
            mstlen+=weight;
            add(cur);
    }
    return mstlen;
}
```

5.5 Dinic's Algorithm

```
//Original Author : https://plzrun.tistory.com/
int r[V][V]; // flow capacity
bool chk[V][V]; // edge existence
int level[V];
vector<int> v[V];
queue<int> q;
bool bfs(int src, int sink)
    memset(level,-1,sizeof(level));
   level[src]=0;
    q.push(src);
    while(!q.empty())
        int x = q.front();
        q.pop();
        for(int y: v[x])
        {
            if(r[x][y]>0 && level[y]<0) {
                level[y]=level[x]+1;
                q.push(y);
            }
        }
    return level[sink]>=0;
int work[V];
int dfs(int x, int sink, int f)
    if(x==sink) return f;
   for(int &i=work[x]; i<v[x].size(); i++)</pre>
        int y=v[x][i];
        if(level[y]>level[x] && r[x][y]>0)
            int t = dfs(y,sink,min(f,r[x][y]));
            if(t>0)
```

```
r[x][y]=t;
                r[y][x] += t;
                return t;
        }
    return 0;
int dinic(int src, int sink)
    int flow=0;
    while(bfs(src,sink))
        int f=0:
        memset(work,0,sizeof(work));
        while((f=dfs(src,sink,INT_MAX))>0)
            flow+=f;
   }
    return flow;
}
```

6 Shortest Path

6.1 Dijkstra

```
\mathcal{O}(E \log V) Single-Start-Shortest-Path.
Not working for graph with minus weight.
const int INF = 987654321;
const int MX = 105050;
struct Edge
    int dest, w;
    bool operator<(const Edge &p) const</pre>
        return w > p.w;
};
bool relax(Edge edge, int u, int dist[])
    bool flag = 0;
    int v = edge.dest, w = edge.w;
    if (dist[v] > dist[u] + w && (dist[u]!=INF))
        flag = true;
        dist[v] = dist[u]+w;
    }
    return flag;
}
int dijkstra(int dist[], int start, vector<Edge> graph[])
    fill(dist,dist+MX,INF);
    dist[start] = 0;
    priority_queue<Edge> pq;
    pq.push({start,0});
    while(!pq.empty())
        Edge x = pq.top();
        int v = x.dest, w = x.w;
        pq.pop();
        if (w>dist[v])
             continue;
```

```
for (auto ed : graph[v])
            if (relax(ed, v, dist))
                 pq.push({ed.dest,dist[ed.dest]});
    }
}
6.2 Bellman Ford
\mathcal{O}(EV) Single-Start-Shortest-Path.
Not working for graph with minus cycle \rightarrow must detect.
struct Edge
    int u, v, w;
};
vector <Edge> edgelist;
int V, E;
int dist[V+1];
bool relax_all_edge()
    bool flag = false;
    for (auto it:edgelist)
        int u = it.u, v = it.v, w = it.w;
        if (dist[v] > dist[u] + w && (dist[u]!=INF))
        {
            flag = true;
            dist[v] = dist[u]+w;
        }
    }
    return flag;
}
int bellman_ford()
    fill(dist,dist+V+2,INF);
    dist[1] = 0;
    for (int i = 0; i < V-1; i++)
        relax_all_edge();
    }
    if (relax_all_edge())
```

```
return -1;
    else
        return 0;
     SPFA Algorithm
Average \mathcal{O}(E), worst \mathcal{O}(VE) time. Average-case improvement of Bellman Ford by
using an additional queue.
//https://www.crocus.co.kr/1089
struct Edge
    int dest, w;
    bool operator<(const Edge &p) const</pre>
        return w > p.w;
};
bool inQ[100500];
int cycle[100500];
int spfa(int dist[], int start, vector<Edge> graph[])
    fill(dist, dist + MX, INF);
    queue<int> q;
    dist[start] = 0;
    inQ[start] = true;
    q.push(start);
    cycle[start]++;
    while (!q.empty())
        int here = q.front();
        q.pop();
        inQ[here] = false;
        for (int i = 0; i < graph[here].size(); i++)</pre>
            int next = graph[here][i].dest;
```

```
int cost = graph[here][i].w;
             if(dist[next] > dist[here] + cost)
                 dist[next] = dist[here] + cost;
                 if (!inQ[next])
                 {
                     cycle[next]++;
                     if (cycle[next] >= graph->size())
                         printf("-1\n");
                         return 0;
                     q.push(next);
                     inQ[next] = true;
            }
        }
    }
}
6.4 Floyd-Warshall
Works on adjacency matrix, in \mathcal{O}(V^3).
int d[120][120];
int n;
void Floyd_Warshall()
    for (int i = 1; i <= n; i++)
        for (int j = 1; j \le n; j ++)
            for (int k = 1; k \le n; k++)
                 d[j][k] = MIN(d[j][k],d[j][i]+d[i][k]);
```

7 Dynamic

7.1 Longest Increasing Subsequence

```
Find LIS in \mathcal{O}(n \log n) time.
vector <int> sequence;
vector <int> L;
int lis_len;
int position[BIG];
int lis[BIG];
int lis_pushed[BIG];
int n;
void FindLIS(vector <int> &seq)
    L.push_back(seq[0]);
    position[0] = 0;
    for (int i = 1; i<n; i++)
        int u = L.size();
        if (seq[i] > L[u-1])
        {
            position[i] = u;
            L.push_back(seq[i]);
        }
        else
            int pos = lower_bound(L.begin(),L.end(),seq[i])-L.begin();
            L[pos] = seq[i];
            position[i] = pos;
        }
    lis_len=L.size();
    int lookingfor = lis_len-1;
    for (int i = n-1; i >= 0; i--)
        if (lis_pushed[position[i]]==0 && lookingfor == position[i])
        {
            lis[position[i]] = seq[i];
            lis_pushed[position[i]]=1;
            lookingfor--;
        }
    }
```

```
}
7.2 Largest Sum Subarray
Computes sum of largest sum subarray in \mathcal{O}(N)
void consecsum(int n)
    dp[0] = number[0];
    for (int i = 1; i<n; i++)
        dp[i] = MAX(dp[i-1]+number[i],number[i]);
}
int maxsum(int n)
    consecsum(n);
    int max_sum=-INF;
    for (int i = 0; i < n; i++)
        dp[i] > max_sum ? max_sum = dp[i] : 0;
    return max_sum;
}
7.3 0-1 Knapsack
int dp[N][W];
int weight[N];
int value[N];
void knapsack()
    for (int i = 1; i<=n; i++)
        for (int j = 0; j \le W; j + +)
            dp[i][j] = dp[i-1][j];
        for (int j = weight[i]; j<=W; j++)</pre>
            dp[i][j] = max(dp[i][j], dp[i-1][j-weight[i]]+value[i]);
}
7.4 Longest Common Subsequence
//input : two const char*
//output : their LCS, in c++ std::string type
string lcsf(const char *X,const char *Y)
    int m = (int)strlen(X);
    int n = (int)strlen(Y);
```

```
int L[m+1][n+1];
    for (int i=0; i<=m; i++)
        for (int j=0; j<=n; j++)
            if (i == 0 || j == 0)
                L[i][j] = 0;
            else if (X[i-1] == Y[j-1])
                L[i][j] = L[i-1][j-1] + 1;
            else
                L[i][j] = max(L[i-1][j], L[i][j-1]);
        }
    int index = L[m][n];
    char lcsstring[index+1];
    lcsstring[index] = 0;
    int i = m, j = n;
    while (i > 0 \&\& j > 0)
        if (X[i-1] == Y[j-1])
        {
           lcsstring[index-1] = X[i-1];
            i--; j--; index--;
        else if (L[i-1][j] > L[i][j-1])
            i--;
        else
            j--;
    string lcsstr = lcsstring;
    return lcsstr;
    Edit Distance
int edit_dist[1010][1010];
int Editdist(string &s, string &t)
    int slen = s.length();
    int tlen = t.length();
```

}

```
for (int i = 1; i <= slen; i++)
        edit_dist[i][0] = i;
    for (int i = 1; i<=tlen; i++)
        edit_dist[0][i] = i;
    for (int i = 1; i<=tlen; i++)
        for (int j = 1; j \le slen; j++)
            if (s[j-1]==t[i-1])
                edit_dist[j][i] = edit_dist[j-1][i-1];
            else
                edit_dist[j][i] = min(edit_dist[j-1][i]+1,
                    min(edit_dist[j-1][i-1]+1,edit_dist[j][i-1]+1));
        }
    }
    return edit_dist[slen][tlen];
}
    String
8.1 KMP Algorithm
// Original Author : bowbowbow (bowbowbow.tistory.com)
vector<int> getPi(string p)
    int j = 0;
    int plen = p.length();
    vector<int> pi;
    pi.resize(plen);
    for(int i = 1; i< plen; i++)</pre>
        while((j > 0) && (p[i] != p[j]))
            j = pi[j-1];
        if(p[i] == p[i])
        {
            j++;
            pi[i] = j;
        }
    }
    return pi;
vector <int> kmp(string s, string p)
{
```

```
vector<int> ans;
    auto pi = getPi(p);
   int slen = s.length(), plen = p.length(), j = 0;
   for(int i = 0; i < slen; i++)
       while(j>0 && s[i] != p[j])
           j = pi[j-1];
       if(s[i] == p[j])
       {
           if(j==plen-1)
               ans.push_back(i-plen+1);
                j = pi[j];
            else
               j++;
       }
   return ans;
8.2 Manacher's Algorithm
A[i] = i 번을 중심으로 하는 가장 긴 팰린드롬이 되는 반지름.
//original Author : Myungwoo (blog.myungwoo.kr)
int N,A[MAXN];
char S[MAXN];
void Manachers()
   int r = 0, p = 0;
   for (int i=1;i<=N;i++)
       if (i <= r)
           A[i] = \min(A[2*p-i], r-i);
        else
           A[i] = 0;
        while (i-A[i]-1 > 0 \&\& i+A[i]+1 <= N
       && S[i-A[i]-1] == S[i+A[i]+1])
           A[i]++;
        if (r < i+A[i])
           r = i+A[i], p = i;
```

```
}
}
8.3 Trie
struct Trie
    int trie[NODE_MAX][CHAR_N];
    int nxt = 1:
    void insert(const char* s)
        int k = 0;
        for (int i = 0; s[i]; i++)
            int t = s[i] - 'a';
            if (!trie[k][t])
                trie[k][t] = nxt;
                nxt++;
            k = trie[k][t];
        trie[k][26] = 1;
    bool find(const char* s, bool exact = false)
    {
        int k = 0;
        for (int i = 0; s[i]; i++)
            int t = s[i] - 'a';
            if (!trie[k][t])
                return false;
            k = trie[k][t];
        if (exact)
            return trie[k][26];
        return true;
    }
};
```

8.4 Rabin-Karp Hashing

```
\operatorname{Hashmap}[k]에, 길이가 len인 부분 문자열의 해시값이 k 가 되는 시작점 인덱스 i 를 push.
const 11 MOD = BIG_PRIME;
int L;
char S[STR_LEN];
int safemod(int n)
    if(n >= 0)
        return n % MOD;
    return ((-n/MOD+1)*MOD + n) \% MOD;
vector <int> hashmap[MOD];
void Rabin_Karp(int len)
    int Hash = 0;
    int pp = 1;
    for(int i=0; i<=L-len; i++)</pre>
        if(i == 0)
        {
            for(int j = 0; j < len; <math>j + +)
                Hash = safemod(Hash + S[len-j-1]*pp);
                 if(i < len-1)
                     pp = safemod(pp*2);
            }
        }
        else
            Hash = safemod(2*(Hash - S[i-1]*pp) + S[len+i-1]);
        hashmap[Hash].push_back(i);
    return;
```

9 Miscellaneous

9.1 Binary and Ternary Search

Preventing stupid mistakes by writing garbage instead of proper binary search. Depends on problem and situation, what we want is either lo or hi.

```
//Finding minimum value with chk() == true
while(lo+1 < hi)
    int mid = (lo+hi)/2;
    if(chk(mid))
        lo = mid;
    else
        hi = mid;
}
Ternary search
double ternary_search(double 1, double r)
    double eps = 1e-9;
                                    //set the error limit here
    while (r - 1 > eps)
        double m1 = 1 + (r - 1) / 3;
        double m2 = r - (r - 1) / 3;
        double f1 = f(m1);
                                //evaluates the function at m1
        double f2 = f(m2);
                                //evaluates the function at m2
        if (f1 < f2)
            1 = m1;
        else
            r = m2:
   }
    return f(1);
                                    //return the maximum of f(x) in [1, r]
}
```

9.2 Useful Bitwise Functions in C++

```
int __builtin_clz(int x);// number of leading zero
int __builtin_ctz(int x);// number of trailing zero
int __builtin_clzll(ll x);// number of leading zero
int __builtin_ctzll(ll x);// number of trailing zero
int __builtin_popcount(int x);// number of 1-bits in x
int __builtin_popcountll(ll x);// number of 1-bits in x
```

```
lsb(n): (n & -n); // last bit (smallest)
floor(log2(n)): 31 - __builtin_clz(n | 1);
floor(log2(n)): 63 - __builtin_clzll(n | 1);

// compute next perm. ex) 00111, 01011, 01101, 01110, 10011, 10101.
ll next_perm(ll v)
{
    ll t = v | (v-1);
    return (t + 1) | (((~t & -~t) - 1) >> (__builtin_ctz(v) + 1));
}
```

9.3 List of Useful Numbers

< 10^k	x prime	# of prime	< 10^1	x prime
1	7	4	10	999999967
2	97	25	11	9999999977
3	997	168	12	99999999989
4	9973	1229	13	999999999971
5	99991	9592	14	9999999999973
6	999983	78498	15	99999999999989
7	9999991	664579	16	99999999999937
8	99999989	5761455	17	999999999999997
9	99999937	50847534	18 9	999999999999999

10 Checkpoints

10.1 Debugging

- $10^5 * 10^5 \Rightarrow \text{INTEGER OVERFLOW}$. 특히 for문 안에서 i * i 할 때 조심하기.
- If unsure with overflow, use #define int long long and stop caring.
- 행렬과 기하의 i, j 인덱스 조심. 헷갈리면 쓰면서 가기.
- output이 특정 수열/OX 형태 : 작은 예제를 Exhasutive Search. 모르는 무언가를 알기 위해서는 데이터가 필요하다.

10.2 Thinking

- 모든 경우를 다 할 수 없나? 왜 안 되지? 시간 복잡도 잘 생각해 보기. 정해의 Target Complexity를 먼저 생각하고 주요 알고리즘들의 Complexity로 짜맞추기. 예를들어, 쿼리가 30만개 들어온다면 한 쿼리를 적어도 log n 에 처리할 방법이 아무튼 있다는 뜻.
- 단조함수이며, 충분히 빠르게 검증가능한가 : Binary Search.
- 차원이 높은 문제 : 차원 내려서 생각하기. 3 → 2.
- 이 문제가 사실 그래프 관련 문제는 아닐까?
 - 만약 그렇다면, '간선' 과 '정점' 은 각각..?
 - 간선과 정점이 몇 개 정도 있는가?
- 이 문제에 Overlapping Subproblem이 보이나?
 → Dynamic Programming 을 적용.
- 답의 상한이 Reasonable 하게 작은가?
- 그래프 문제에서, 어떤 "조건" 이 들어갔을 때 → 이 문제를 "정점을 늘림으로써" 단순한 그래프 문제로 바꿀 수 있나? (ex : SNUPC 2018 달빛 여우) 이를테면, 홀짝성에 따라 점을 2배로 늘림으로써?
- DP도 마찬가지. 어떤 조건을 단순화하기 위해 상태의 수를 사이사이에 집어넣을 수 있나?
- 마지막 생각 : 조금 추하지만 해싱이나 Random, bitset 을 이용한 $n^2/64$ 같은걸로 뚫을 수 있나?

업데이트 노트 / To-Do

이 페이지는 실제 인쇄 팀노트에 포함되지 않습니다

- 190731 : Rabin-Karp Hashing 추가.
- 190731 : LCA 코드에 최단 / 최장 거리 간선, 거리 구하기 추가.
- 190731 : Segment Tree Lazy Propagation 추가.

- 190731 : Segment Tree Struct 구현체로 변경. (UCPC Finalized)
- 190817 : SPFA Algorithm 추가.
- To-do : HLD 코드 넣기.
- To-do : Trie 구현체 두가지 방식 넣기.