

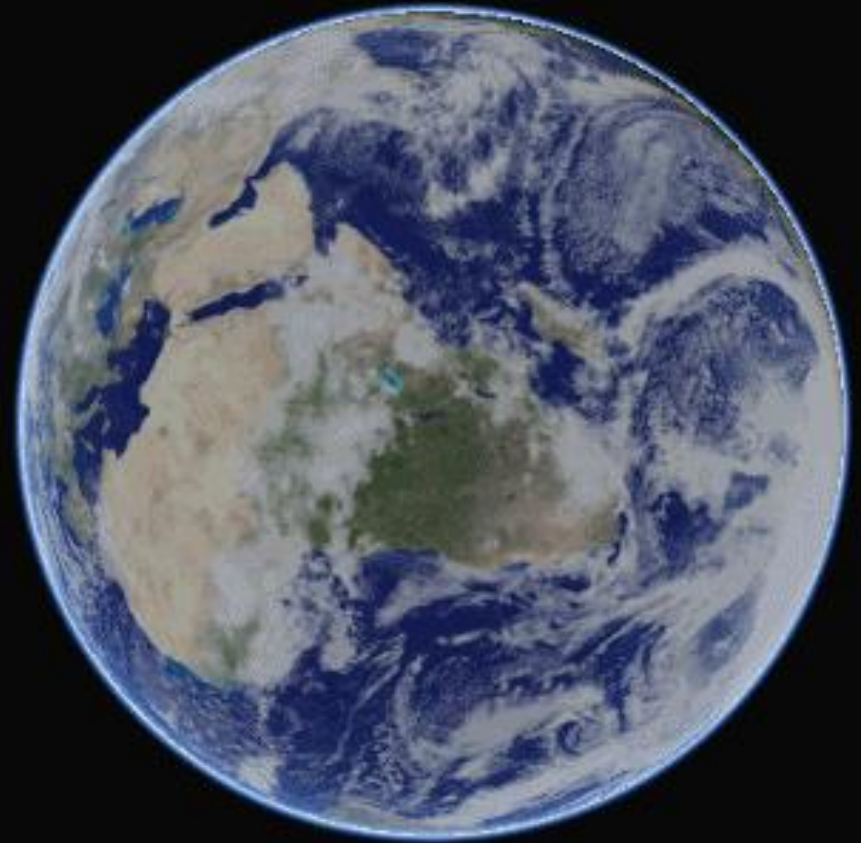
# RENDERING ATMOSPHERIC LIGHT SCATTERING

*V1.0 Single Scattering*

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LaSalle URL

2017-2018



# OUTLINE

INTRODUCTION

BASICS

SCATTERING THEORY

CAVEATS OF NAIVE IMPLEMENTATION

ACTUAL IMPLEMENTATION

DEMO

CONCLUSIONS AND FUTURE WORK

REFERENCES

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INTRODUCTION

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# Who am I?



**CL3VER**

- Multimedia Engineering student
- Internship at Cl3ver, *1 year and 5 months*
- TFG at atmospheric light scattering
- Interested in Computer Graphics (mostly real time)

# OUTLINE

INTRODUCTION

BASICS

- Introduction – Atmospheric Light Scattering
- How we will compute it?
- The midpoint rule

SCATTERING THEORY

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# Introduction – Atmospheric Light Scattering

- Difficult problem but very important for outdoor environments rendering
- Difficult complex equations, hard to achieve real time
- Real-Time algorithm running on GPU using methods described by Nishita et al. 1993. [\[REF1\]](#)
- Paper done by Sean O'Neil, described at Nvidia GPU Gems2 [\[REF2\]](#)



# Atmospheric Scattering

- Sky color
- Fog
- Clouds
- “God rays”
- Light shafts
- Volumetric shadows



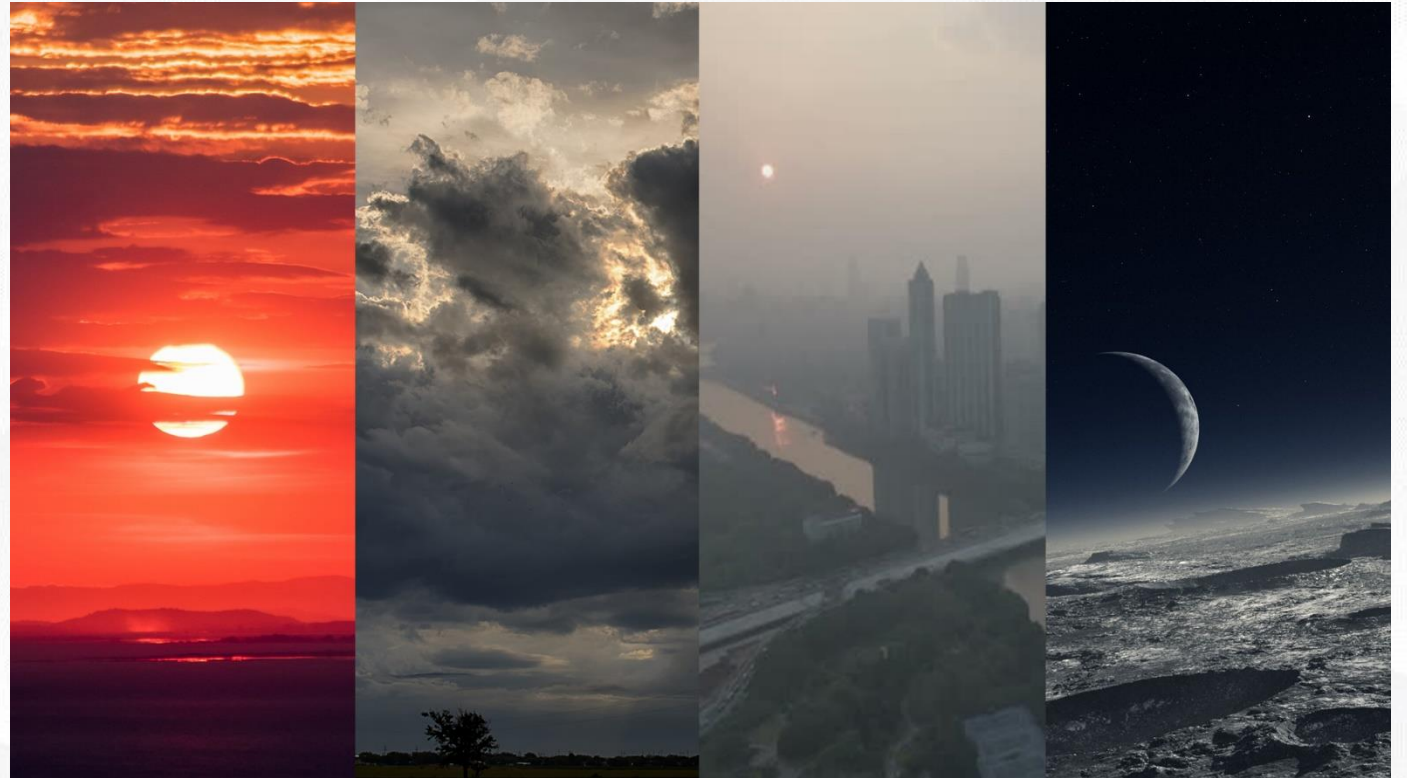
# Atmospheric Light Scattering

- Atmosphere scatters light
- Responsible for the sky color
- Caused by a variety of particles
  - Molecules, dust, water vapor, etc.
- Illuminates the sky
- Attenuates and colors the Sun
- Attenuates and colors distant objects (aerial perspective)



# Atmospheric Light Scattering

- Varies by
  - Time of day
  - Weather
  - Pollution
  - Planet atmosphere



# How we will compute it? (1)

- We have a ray from the camera through the atmosphere to a vertex
- Vertex can be part of terrain, part of sky dome, part of cloud or object in space
- If ray passes through atmosphere scattering needs to be calculated
- A ray has two points defined, where starts passing through atmosphere and where it stops. A and B respectively
- Depends on the situation we have to do a sphere-check intersection to find the point. (camera in space; or camera in atmosphere)

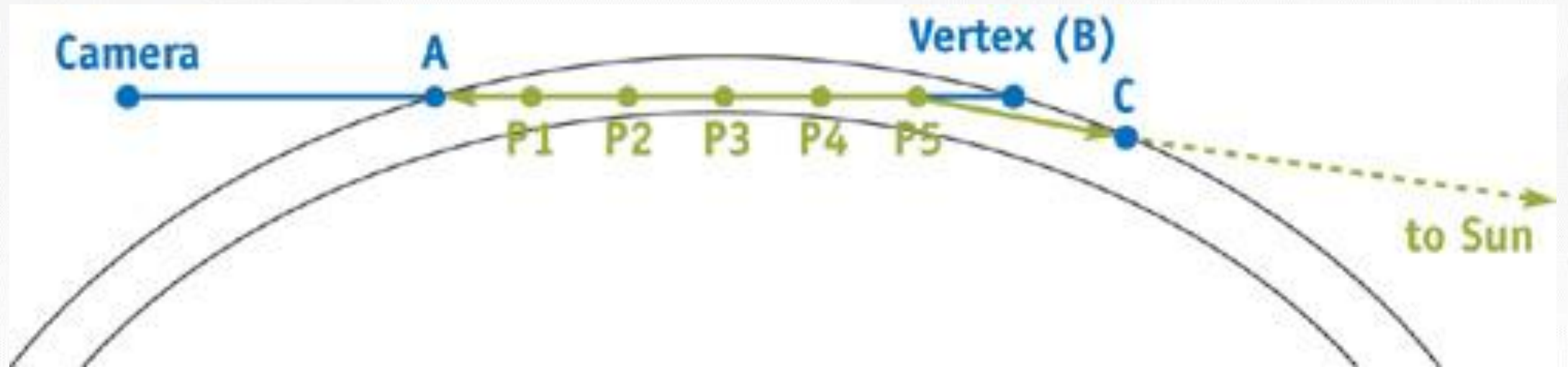


# How we will compute it? (2)

- We have a line segment defined from point A to B
- Our goal is to approximate the integral that describes atmospheric scattering across its length
- **Lets take five sample positions,  $P_1$  through  $P_5$ .** Each point represents a point in the atmosphere where light scatters
- At  $P_5$  light comes from the sun, in a straight line. At  $P_5$  some of this light is scattered directly towards the camera.
- As this light travels to the camera, some of it gets scattered away again
- The same happens for every sample point
- For calculating the integral: The **midpoint rule method**



# How we will compute it? (3)



# The midpoint rule

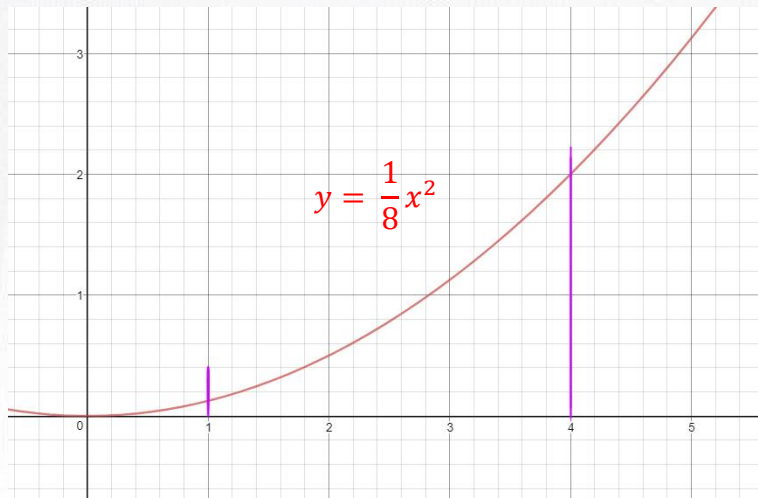
- Method for approximating a definite integral
- Weighted sum calculated in a loop

## MIDPOINT RULE:

- Definite integral
- Break definite integral into  $n$  segments
- Evaluate integral at center of each segment
- Multiply each result by length of segment
- Add them up
- PROFIT!

# The midpoint rule

## -EXAMPLE



Use the Midpoint rule with  $n = 4$  to approximate the definite integral  $\int_1^4 \frac{1}{8} x^2 dx$

*The Midpoint Rule*

$$\text{Area} \approx \sum_{i=1}^n f\left(\frac{x_{i-1} + x_i}{2}\right) \Delta x$$

$$\Delta x = \frac{b - a}{n}$$

$$x_i = a + i\Delta x$$

$$\begin{aligned} n &= 4 \\ a &= 1 \\ b &= 4 \end{aligned}$$

$$\Delta x = \frac{4 - 1}{4} = \frac{3}{4}$$

$$x_0 = 1$$

$$x_1 = 1 + \frac{3}{4} = \frac{7}{4}$$

$$x_2 = 1 + 2\frac{3}{4} = \frac{10}{4}$$

$$x_3 = 1 + 3\frac{3}{4} = \frac{13}{4}$$

$$x_4 = 1 + 4\frac{3}{4} = 4$$

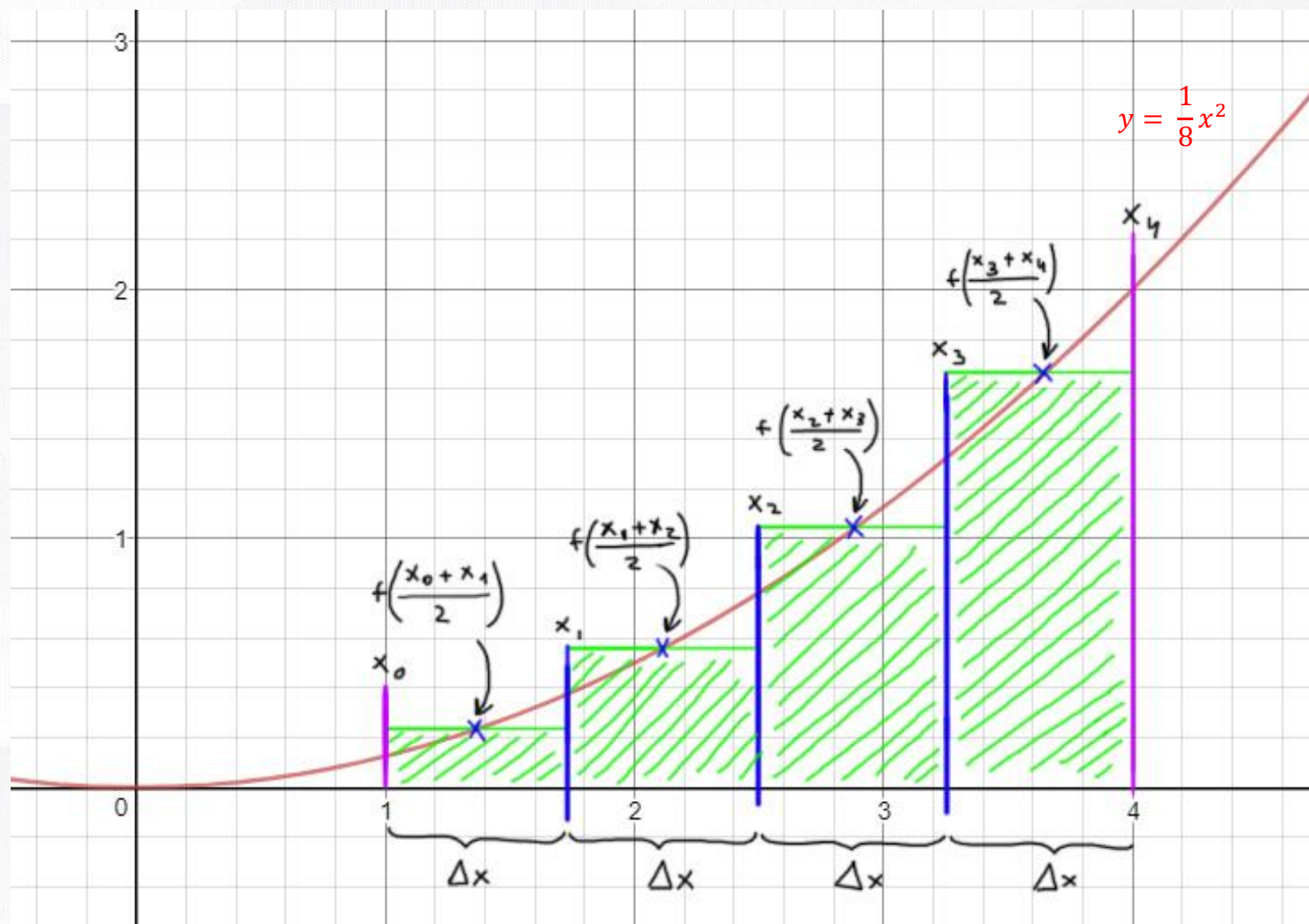
$$\begin{aligned} \int_1^4 \frac{1}{8} x^2 dx &\approx f\left(\frac{1+7/4}{2}\right) \left(\frac{3}{4}\right) + f\left(\frac{7/4+10/4}{2}\right) \left(\frac{3}{4}\right) + f\left(\frac{10/4+13/4}{2}\right) \left(\frac{3}{4}\right) + f\left(\frac{13/4+4}{2}\right) \left(\frac{3}{4}\right) = \\ &= \frac{3}{4} \left[ f\left(\frac{11}{8}\right) + f\left(\frac{17}{8}\right) + f\left(\frac{23}{8}\right) + f\left(\frac{29}{8}\right) \right] = \frac{3}{4} [0.2363 + 0.5644 + 1.03 + 1.64] = 2.605 \end{aligned}$$

$$\int_1^4 \frac{1}{8} x^2 dx \approx 2.605$$

$$\int_1^4 \frac{1}{8} x^2 dx = 2.625$$



# The midpoint rule



# OUTLINE

## BASICS

## SCATTERING THEORY

- Scattering principles
- Rayleigh and Mie Scattering
- The Phase Function
- The Out-Scattering Equation
- The In-Scattering Equation

## CAVEATS OF NAIVE IMPLEMENTATION

## ACTUAL IMPLEMENTATION

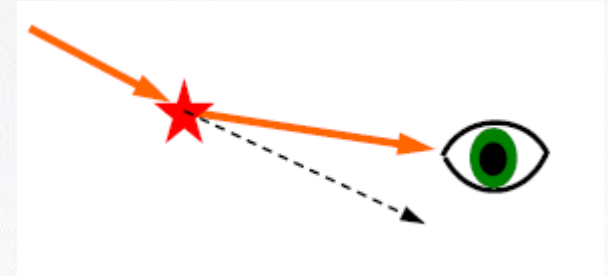
## DEMO

## CONCLUSIONS AND FUTURE WORK

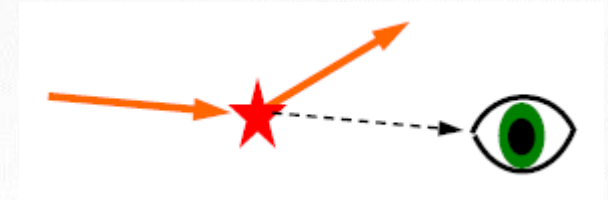
## REFERENCES

# Scattering events **at each sample**:

- Light scattered into the line of sight (in-scattering)



- Light scattered out of the line of sight (out-scattering)

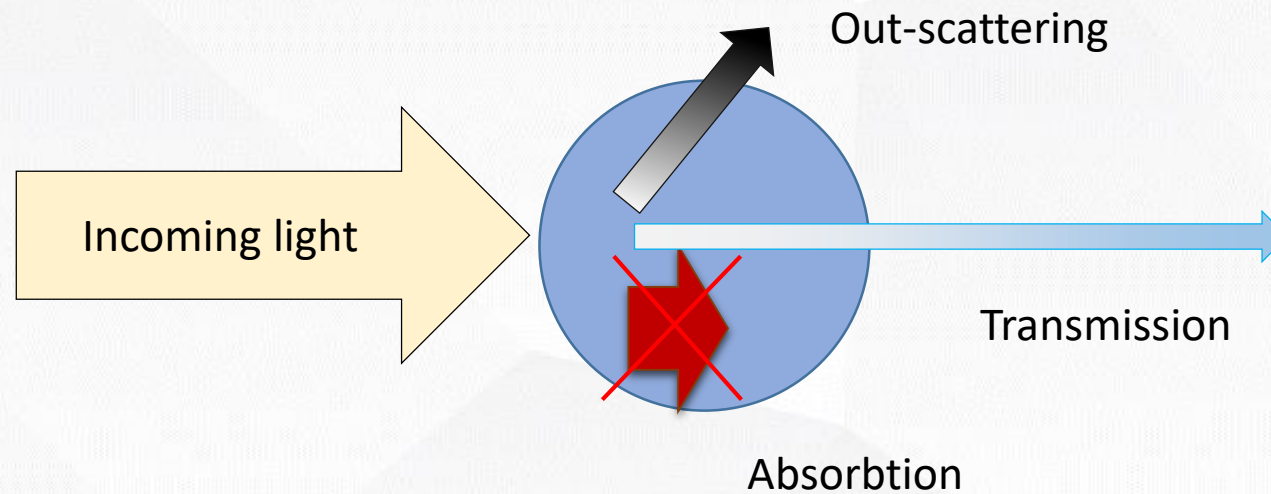


- Light absorbed altogether (absorption)



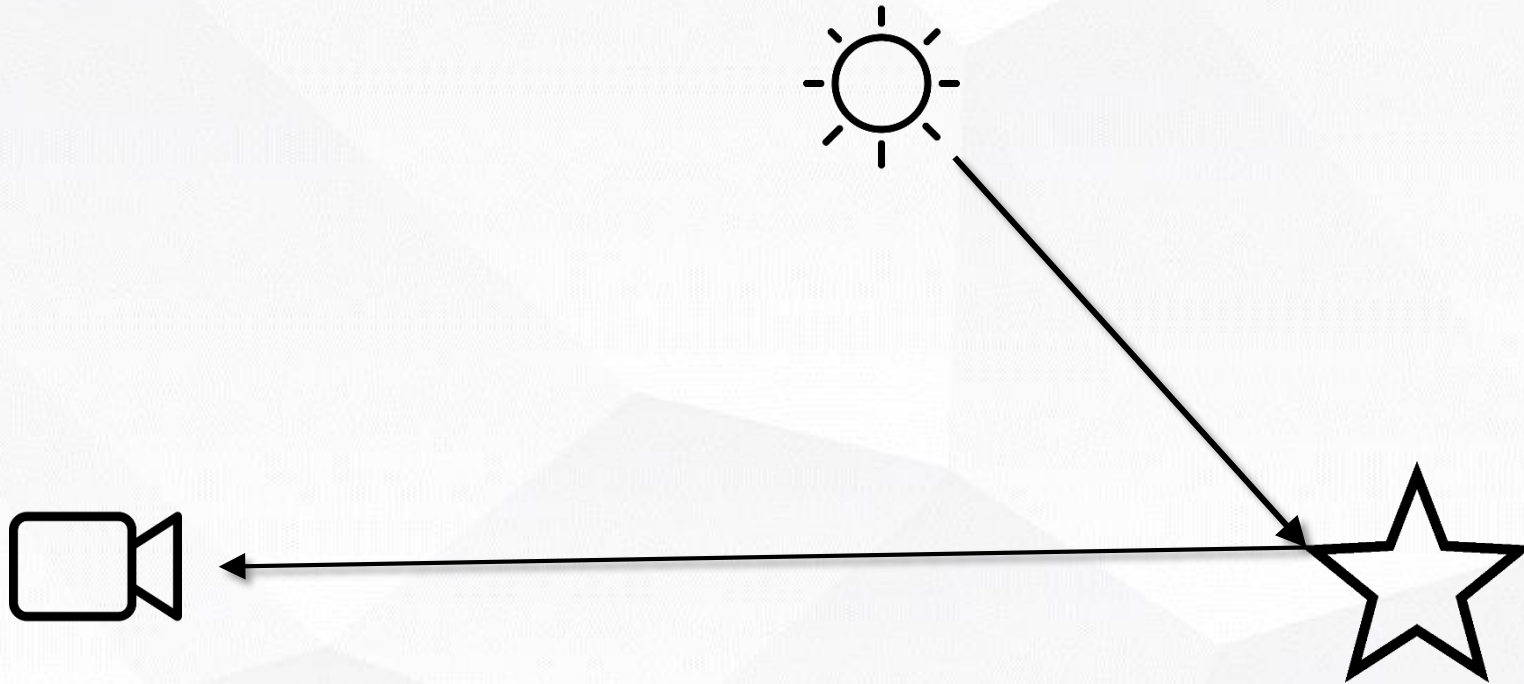


# Scattering Principles. Atmospheric scattering



$$L_{incoming} = L_{transmitted} + L_{absorbed} + L_{scattered}$$

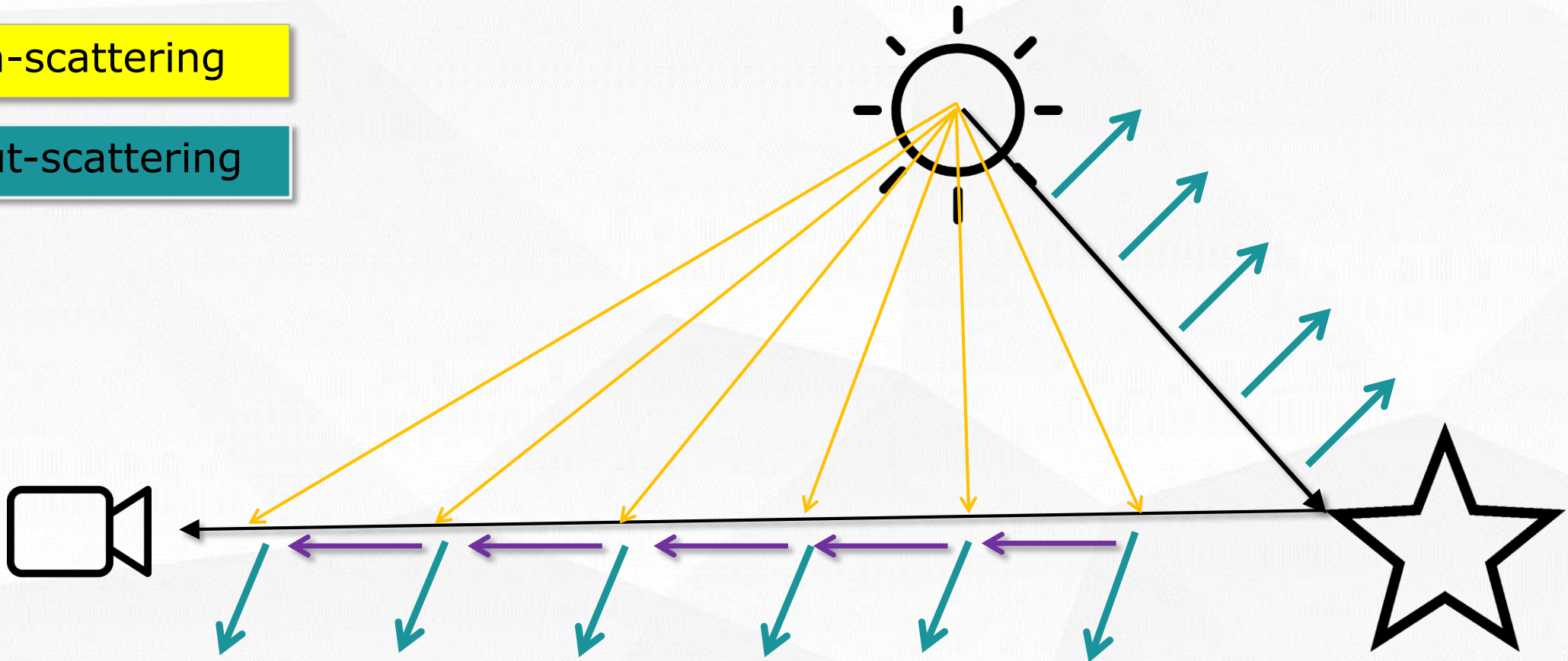
# Scattering Principles. No scattering



# Scattering Principles. Light Scattering

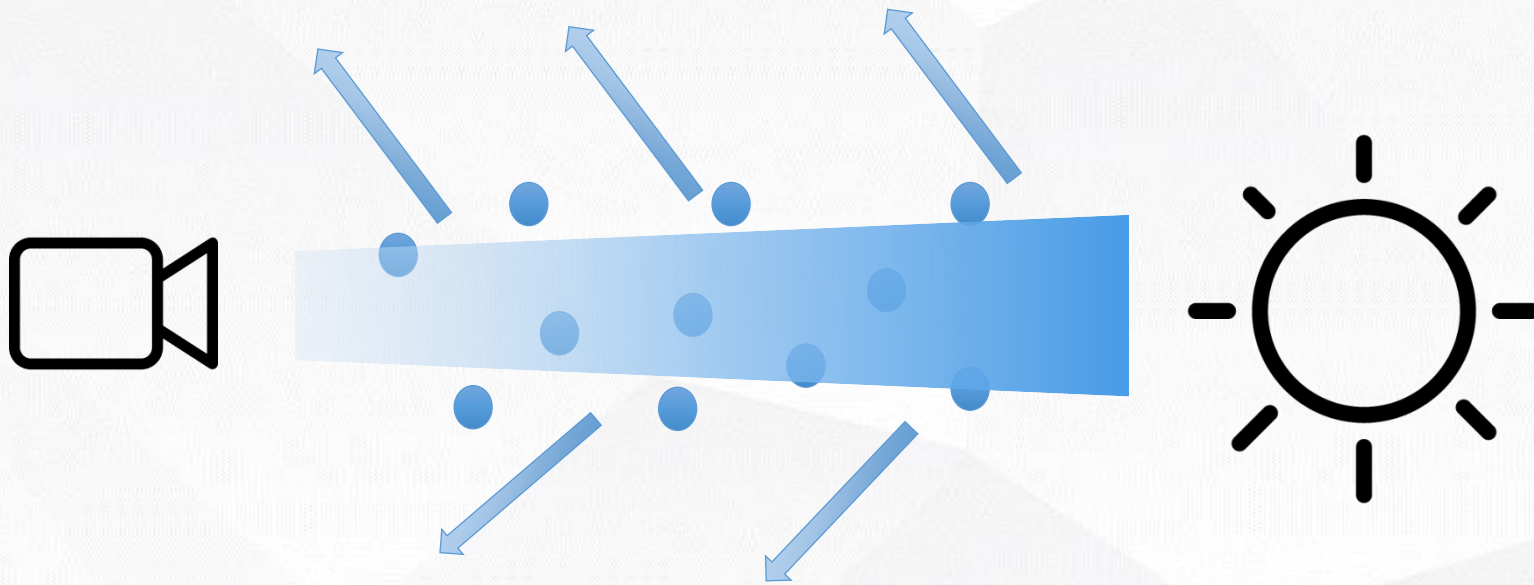
In-scattering

Out-scattering





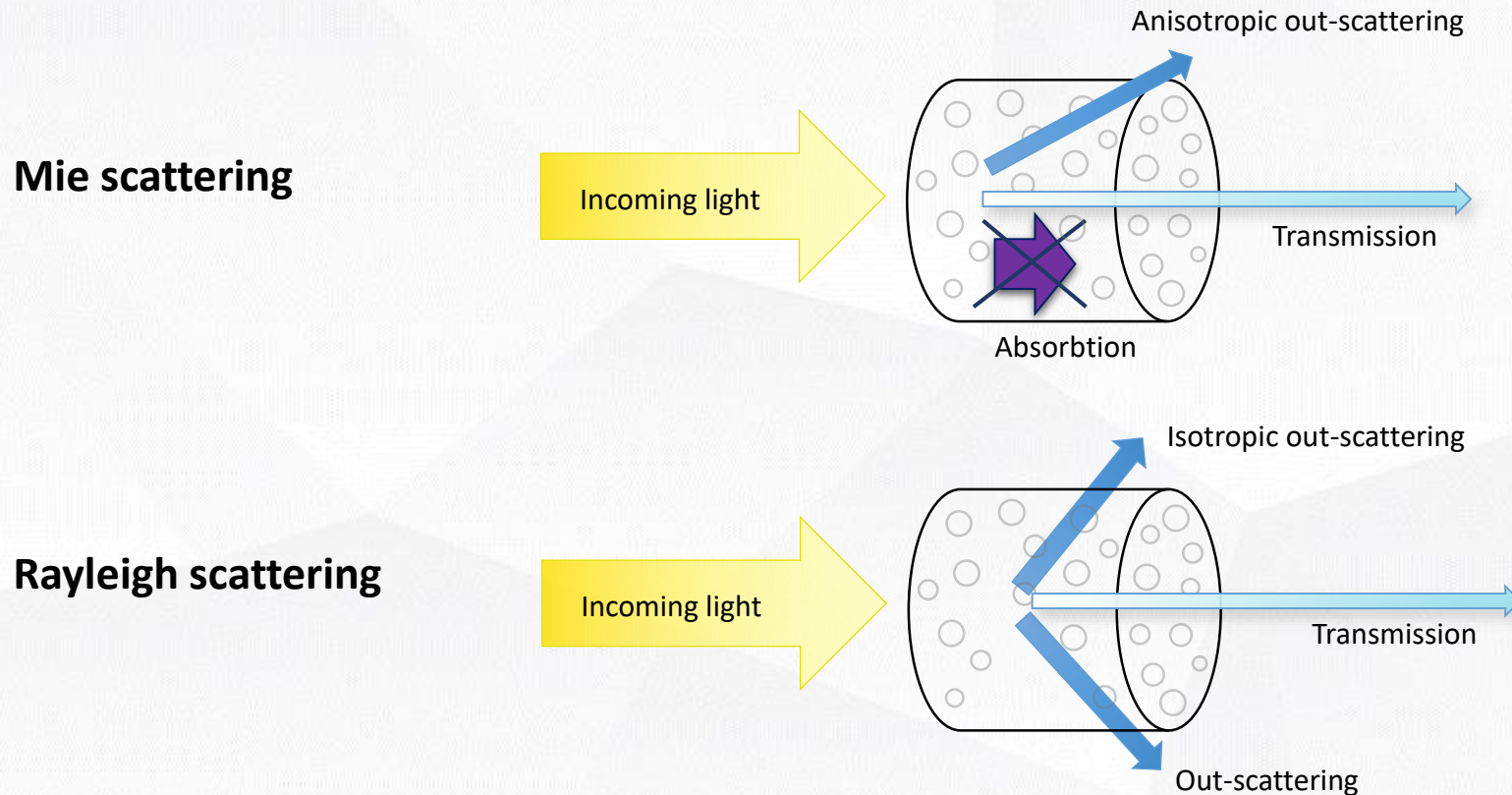
# Scattering Principles. Beer-Lambert Law



$$T(A \rightarrow B) = e^{-\int_A^B \beta e(x) dx}$$

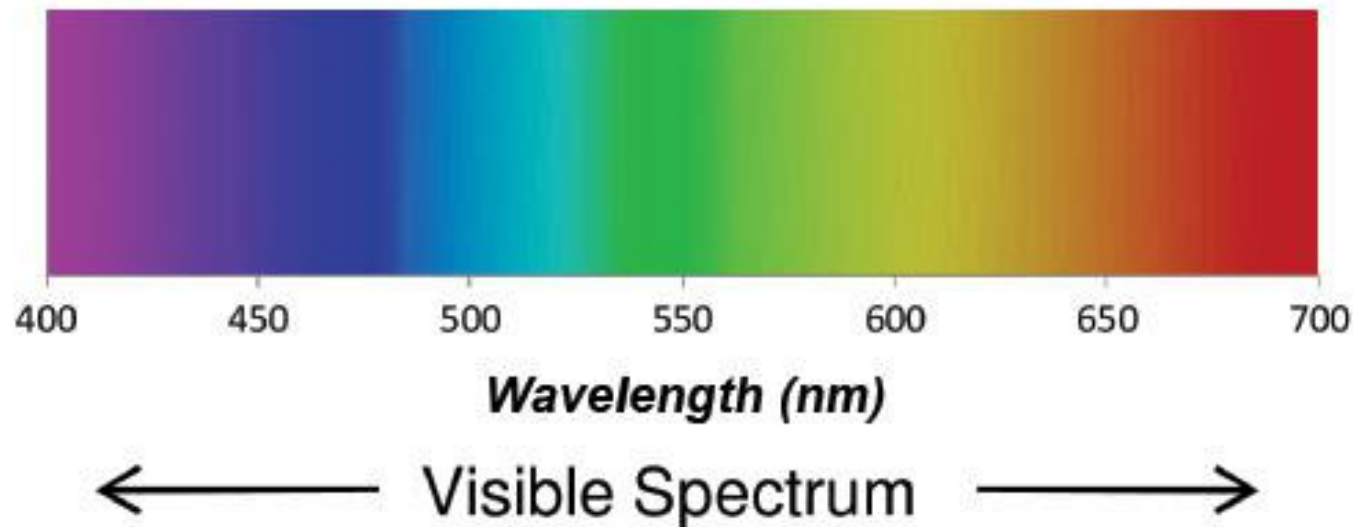
# Rayleigh and Mie Scattering

- Different particles scatter light in different ways.
- Most common types of scattering: **Rayleigh** and **Mie** scattering



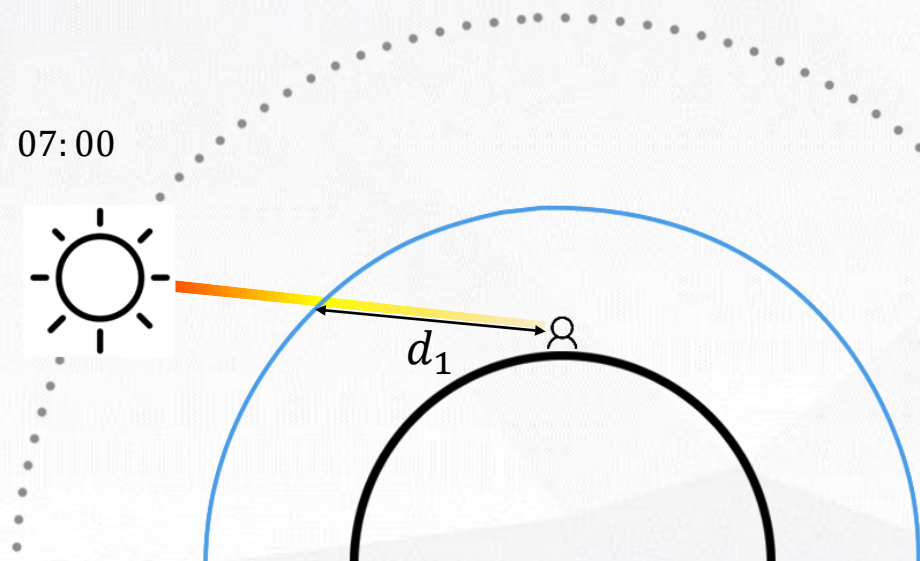
# Rayleigh Scattering

- Caused by small molecules in the air
- Scatters more heavily at shorter wavelengths (blue first, then green and finally red)
- Why is the sky blue then? Why is it red at sunset?

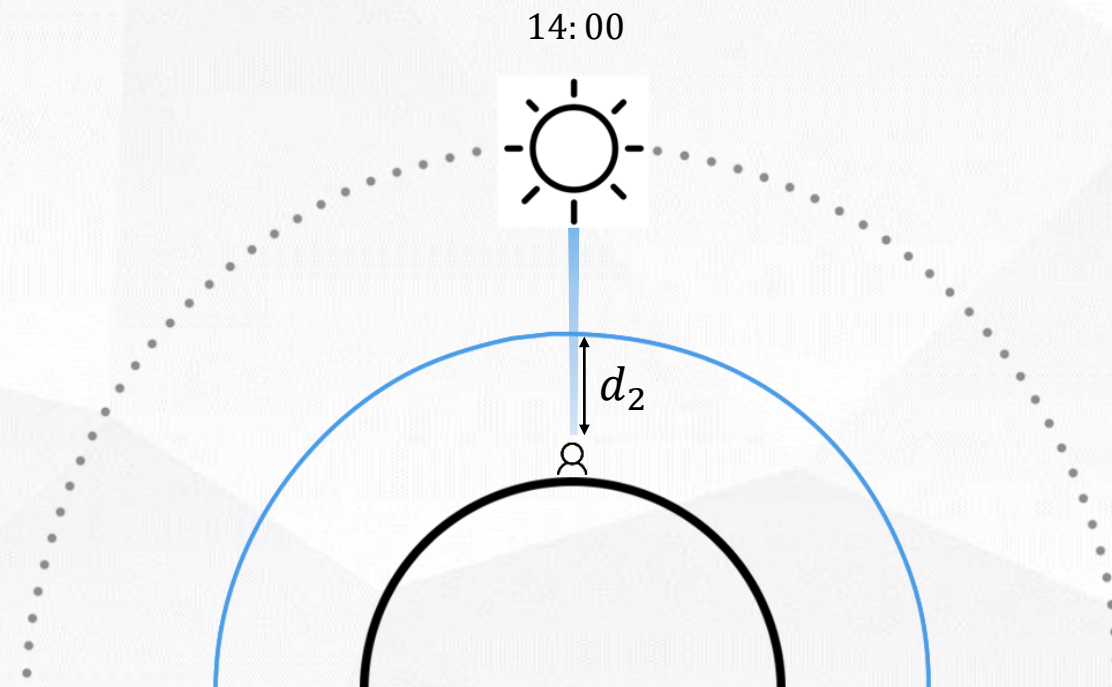




## Dawn & dusk



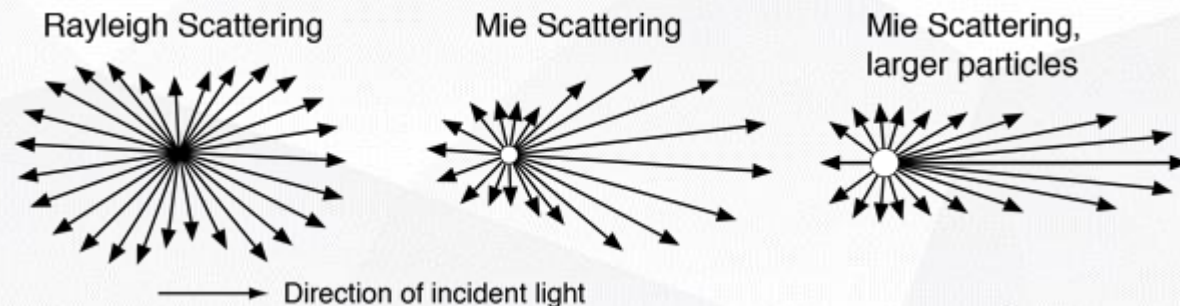
## Middle of day



$$d_1 \gg d_2$$

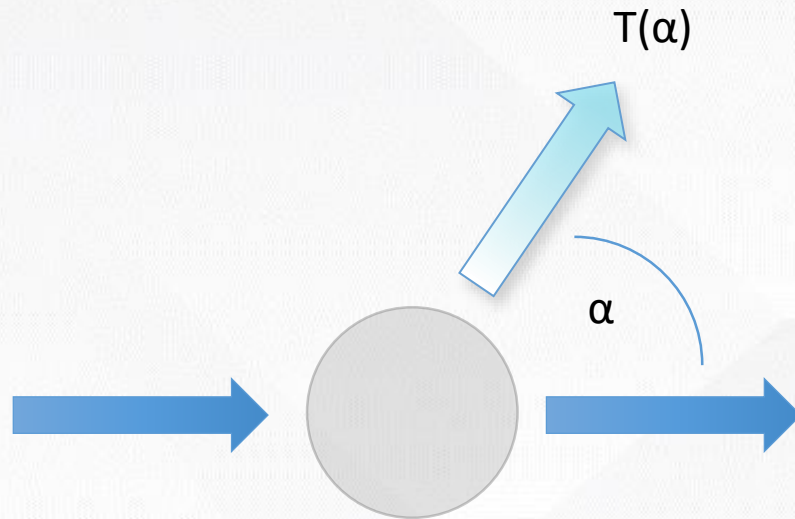
# Mie Scattering

- Caused by larger particles called aerosols (such as dust and pollution)
- Tends to scatter all wavelengths equally
- Highly directional on forward lobe (anisotropic)
- High absorption proportion
- Produces halo on sun on hazy days



# The phase function

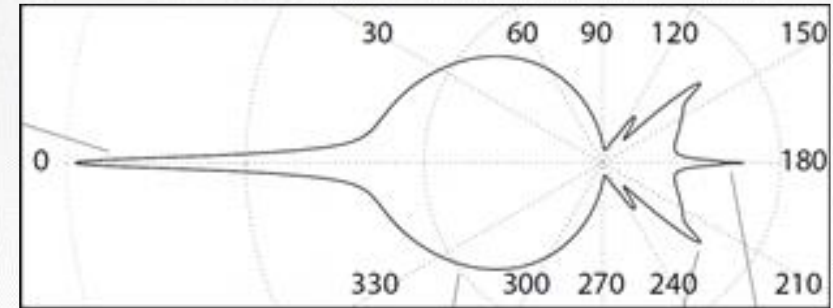
- **Describes how much light is scattered toward all directions**, in the analytical version it depends on angle and a constant  $g$  (for directionality)



Light scattered in direction  $T(\alpha)$

Energy conserving

$$\int_0^{2\pi} \int_0^\pi P(\theta) d\theta d\varphi = 1$$



Phase functions can be very complex

Example: clouds phase function

Source: Bouthors et al, "Real-time realistic illumination and shading of stratiform clouds"



# Analytical phase function

$$F(\theta, g) = \frac{3 \times (1 - g^2)}{2 \times (2 + g^2)} \times \frac{1 + \cos^2 \theta}{(1 + g^2 - 2 \times g \times \cos \theta)^{\frac{3}{2}}}$$

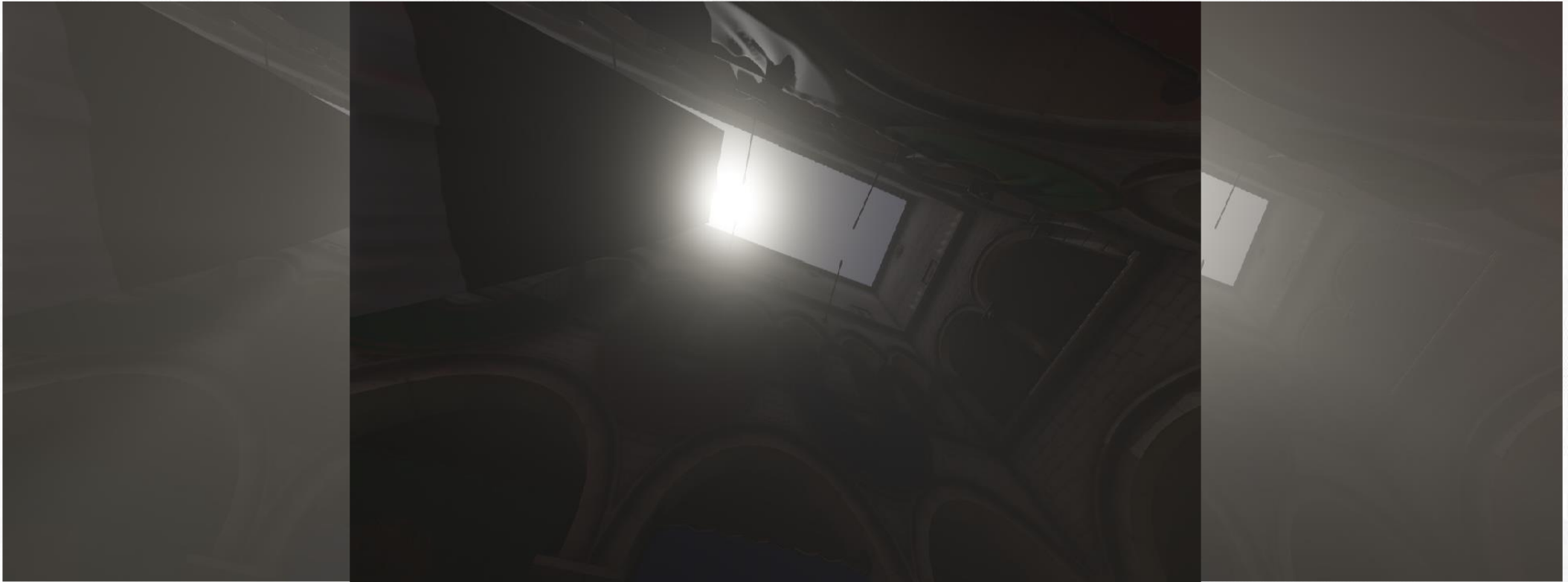
Adaptation of the **Henyeey-Greenstein** function used in Nishita et al. 1993.

***g*** is the anisotropy factor, for defining directionality of scattering

**Rayleigh Scattering:** ***g*** = 0 (Reduces complexity, makes it simetrical)

**Mie Scattering:** ***g*** = [-0.75, -0.99] (Scatters more light in forward direction)

# Scattering anisotropy



$g = 0$

$g = 0.9$

$g = 0.3$

**Negative  $g$  values** scatter more light in the **forward direction**  
**Positive  $g$  values** scatter more light toward the **light source**

# The Out-Scattering equation

- Determines **how much light gets scattered away** from the ray **by the particles** it passes

$$t(P_a P_b, \lambda) = 4\pi \times K(\lambda) \times \int_{P_a}^{P_b} \exp\left(\frac{-b}{H_0}\right) ds$$

**Wavelength**  
(or color) of light

**Scattering constant**  
(Rayleigh, Mie scattering)

**Optical Depth or Optical Thickness**  
**Average atmospheric density** across the ray  
from  $P_a$  to  $P_b$  (**quantity of particles**)



# Out-Scattering->Optical Depth. In detail

- Think of it as a weighting factor based on how many air particles are in the path of the light along the ray

$$\text{Optical Depth} = \int_{P_a}^{P_b} \exp\left(\frac{-h}{H_o}\right) ds$$

- Will be calculated by broken up the integral into segments
- Exponential evaluated at each sample point ***h*** is the height of the sample point (In this implementation ***h* = 0** is sea level and ***h* = 1** is top of the atmosphere)
- ***H<sub>o</sub>*** is the scale height, height at which the atmosphere average density is found. In implementation = **0.25**, 25% on the way up from ground to top of atmosphere

# The In-Scattering equation

- Determines **how much light is added to a ray** through the atmosphere due to light scattering from the sun
- Main computation for determining sky colour

$$I_v(\lambda) = I_s(\lambda) \times K(\lambda) \times F(\theta, g) \times \int_{P_s}^{P_e} \left( \exp\left(\frac{-b}{H_0}\right) \times \exp(-t(P P_c, \lambda) - t(P P_a, \lambda)) \right) ds$$

## *Light scaling functions*

Light that travessed the atmosphere is scaled by this functions

## *Light that travessed the atmosphere*

Final light that gets into the camera after scattering events inside atmosphere

# In-Scattering->Integral. In Detail

**A**

$$I_s(\lambda) = I_i(\lambda) \times K(\lambda) \times F(\theta, g) \times \int_{P_s}^{P_b} \left( \exp\left(\frac{-b}{H_0}\right) \times \exp(-t(P P_c, \lambda) - t(P P_a, \lambda)) \right) ds$$

**Integral that travesses the ray**

$P_a$  starting entry point to atmosphere,  
 $P_b$  ending entry point from atmosphere

**Transmittance (light outscattering)**

Proportion of light transported through medium to  
 incoming light from given direction

$$A = \int_{P_a}^{P_b} \left( \exp\left(\frac{-b}{H_0}\right) \times \exp(-t(P P_c, \lambda) - t(P P_a, \lambda)) \right) ds$$

Light that travessed  
 the armosphere

**Optical Depth**

Particle density in ray  
 traversing atmosphere  
 (NESTED INTEGRAL)

**out – scattering point to sun**  
 Light scattered out of ray from point to sun

**out – scattering point to camera**  
 Light scattered out of ray from point to camera



# In-Scattering->Scaling light. In Detail

$$I_s(\lambda) = \overset{B}{I_s(\lambda) \times K(\lambda) \times F(\theta, g)} \times \int_{p_s}^{p_r} \left( \exp\left(\frac{-b}{H_0}\right) \times \exp(-t(Pp_c, \lambda) - t(Pp_a, \lambda)) \right) ds$$

$$\overset{B}{B} = I_s(\lambda) \times K(\lambda) \times F(\theta, g)$$

**Sunlight intensity**  
scaling the incoming light by  
the sun intensity (*depending  
of wavelength for snazzy alien  
effects*)

**Scattering constant**  
scaling the incoming light by  
the scattering constants  
(Rayleigh & Mie)

**Phase Function**  
Directionality of the final  
light going to camera

# The In-Scattering equation. Complete

The diagram illustrates the components of the In-Scattering equation, which calculates the total light intensity  $I_e(\lambda)$  at a point in the atmosphere. The equation is presented as a product of several terms, each with a descriptive annotation and a red arrow pointing to it. The equation is: 
$$I_e(\lambda) = I_s(\lambda) \times K(\lambda) \times F(\theta, g) \times \int_{P_a}^{P_b} \left[ \exp\left(\frac{-b}{H_0}\right) \times \exp\left(-t(P P_c, \lambda) - t(P P_a, \lambda)\right) \right] ds$$
 The annotations are as follows: 

- Sunlight intensity**: scaling the incoming light by the sun intensity (depending of wavelength for snazzy alien effects). This points to  $I_s(\lambda)$ .
- Scattering constant**: scaling the incoming light by the scattering constants (Rayleigh & Mie). This points to  $K(\lambda)$ .
- Phase Function**: Directionality of the final light going to camera. This points to  $F(\theta, g)$ .
- optical depth**: Particle density in ray traversing atmosphere (NESTED INTEGRAL). This points to the integral term  $\int_{P_a}^{P_b}$ .
- Transmittance (light outscattering)**: Proportion of light transported through medium to incoming light from given direction. This points to the entire integral term.
- out – scattering point to sun**: Light scattered out of ray from point to sun. This points to  $t(P P_c, \lambda)$  inside the integral.
- out – scattering point to camera**: Light scattered out of ray from point to camera. This points to  $t(P P_a, \lambda)$  inside the integral.

 Additionally, a note above the integral term states: **Integral that travesses the ray**  $P_a$  starting entry point to atmosphere,  $P_b$  ending entry point from atmosphere.

**Integral that travesses the ray**  
 $P_a$  starting entry point to atmosphere,  
 $P_b$  ending entry point from atmosphere

**Transmittance (light outscattering)**  
Proportion of light transported through medium to  
incoming light from given direction

**Sunlight intensity**  
scaling the incoming  
light by the sun  
intensity (depending of  
wavelength for snazzy  
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**Scattering constant**  
scaling the incoming light by  
the scattering constants  
(Rayleigh & Mie)

**Phase Function**  
Directionality of the  
final light going to  
camera

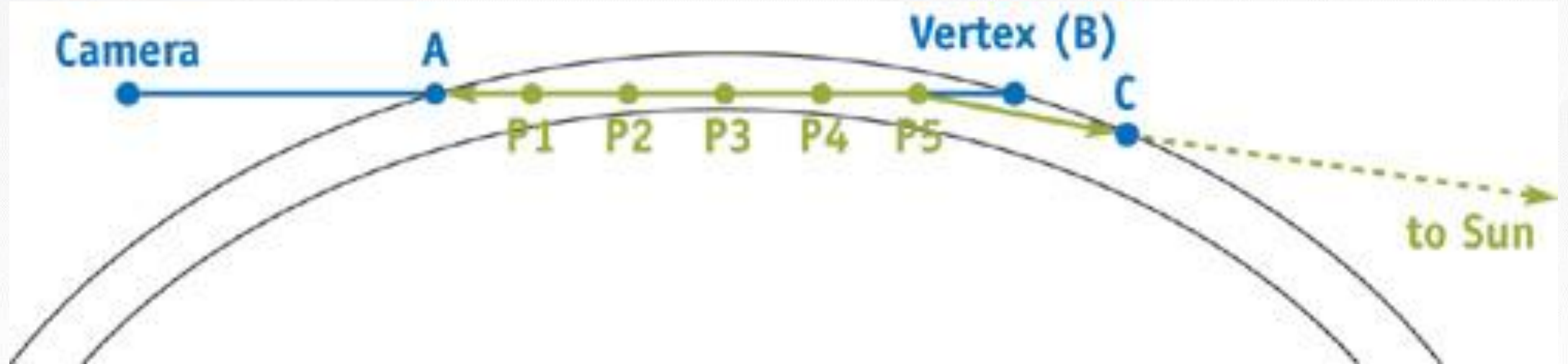
**optical depth**  
Particle density in ray  
traversing atmosphere  
(NESTED INTEGRAL)

**out – scattering point to sun**  
Light scattered out of ray from point to sun

**out – scattering point to camera**  
Light scattered out of ray from point to camera

$$I_e(\lambda) = I_s(\lambda) \times K(\lambda) \times F(\theta, g) \times \int_{P_a}^{P_b} \left[ \exp\left(\frac{-b}{H_0}\right) \times \exp\left(-t(P P_c, \lambda) - t(P P_a, \lambda)\right) \right] ds$$

# Visual Representation





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CAVEATS OF NAIVE IMPLEMENTATION

- Naive Implementation
- Making it Real Time

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# Naive Implementation (1)

## For example:

- 5 sample points in the in-scattering equation
- 5 sample points for each of the integrals to compute out-scattering equations

$$I_v(\lambda) = I_s(\lambda) \times k(\lambda) \times F(\theta, \lambda) \times \sum_{i=0}^{N=5} \left( \exp\left(\frac{-h}{H_o}\right) \times \exp(-t(PP_c, \lambda) - t(PP_a, \lambda)) \right) ds$$

$$t(P_a P_b, \lambda) = 4\pi \times k(\lambda) \times \sum_{i=0}^{N=5} \exp\left(\frac{-h}{H_o}\right) ds$$

$N_{operations} \approx 5 \times (5 + 5)$  samples => To evaluate at every vertex (doing it in vertex shader pass)

- Two types of scattering, Rayleigh and Mie
- Each one of the different wavelengths of each color channel (RGB)

SO...

# Naive Implementation (2)

$$N_{operations} \approx 2 \times 3 \times 5 \times (5 + 5) = 300 \text{ computations per vertex}$$



Five samples is not enough. Low quality. O'Neil uses **50 samples for inner integral** and **5 samples for outer integral**

$$N_{operations} \approx 2 \times 3 \times 5 \times (50 + 50) = 3000 \text{ computations per vertex!!!}$$





# Making it Real-Time

- To cut number of calculations O'Neill proposed a **2D lookup table** where the **results of both integrals are stored** using 50 samples for each. Calculated beforehand on CPU
- A lookup table is a texture used to save data that can be fetched in a shader instead of doing the same calculation in the shader pass
- The lookup table permits to cut number of calculations to:  $2 \times 3 \times 5 \times (1 + 1) = 60$
- Enough for 60 to 100 frames per second by 2007 standards



# Making it Real-Time

- O'Neil wants to eliminate the sampling of textures in vertex shader
- Eliminate the 2D lookup table by finding heuristic equations that approximate the results of the integral
- Finds the heuristic by analyzing the results of the lookup table integrals.

- *First approximation :*

**Optical Depth at point** approximated by using  $\exp(-4h)$  instead of  $\exp\left(\frac{-h}{H_o}\right)$

- *Second approximation :*

**Optical Depth integral approximated** by using a **special scale function** that uses a polynomial. This function obliges use to have the atmosphere be 2.5% of the planet's radius, and the scale height (height where the atmosphere's average density is found) = 0.25



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**ACTUAL IMPLEMENTATION**

- Geometry
- Vertex Shader
- Fragment Shader

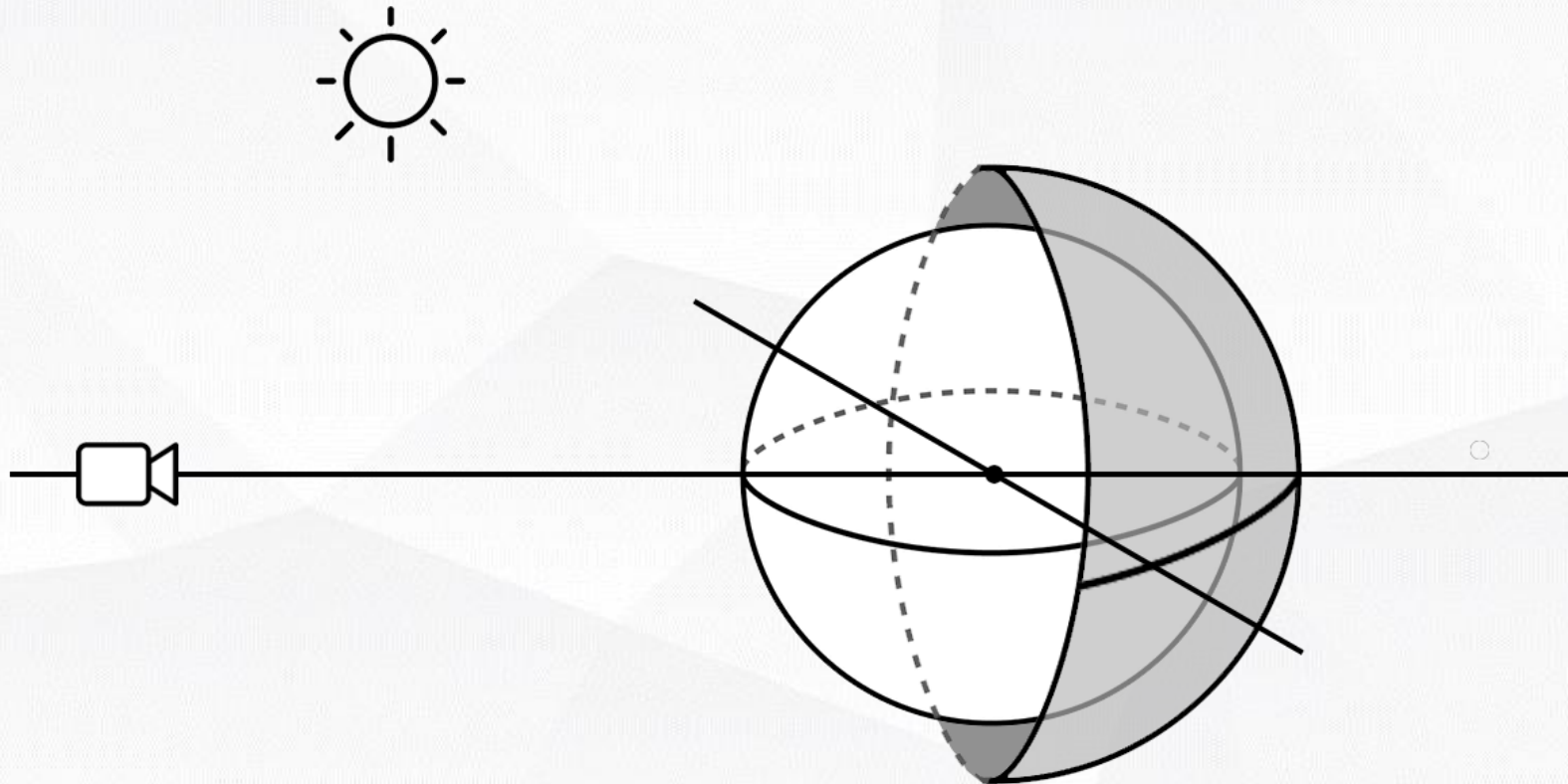
DEMO

CONCLUSIONS AND FUTURE WORK

REFERENCES

# Geometry

- Two spheres, atmosphere and planet
- Atmosphere is sphere only showing the back faces. (Culling to remove front faces)
- Free floating camera. Vector defining position of sun in world space



# Vertex Shader

- Majority of calculations done in vertex shader pass
- Some calculations done at fragment shader pass to avoid artifacts. (Phase function)

## UNIFORMS:

- Kr rayleigh scattering constant
- Km mie scattering constant
- Esun is the brightness of the sun
- Rayleigh scatters different wavelengths at different ratios, ratio =  $1/\text{wavelength}^4$



# Vertex Shader. SkyFromAtmosphere-vs

```
attribute vec3 aVertexPosition;

varying vec3 v3Direction;
varying vec3 frontColor;
varying vec3 frontSecondaryColor;

varying vec3 debugColor;

uniform mat4 uModelMatrix;
uniform mat4 uViewMatrix;
uniform mat4 uProjectionMatrix;

uniform vec3 v3CameraPos;           // The camera's current position

uniform vec3 v3LightPos;           // The direction vector to the light source
uniform vec3 v3InvWavelength;      // 1 / pow(wavelength, 4) for the red, green, and blue channels
uniform float fCameraHeight;       // The camera's current height

uniform float fCameraHeight2;      // fCameraHeight^2
uniform float fOuterRadius;        // The outer (atmosphere) radius
uniform float fOuterRadius2;       // fOuterRadius^2

uniform float fInnerRadius;        // The inner (planetary) radius
uniform float fInnerRadius2;       // fInnerRadius^2
uniform float fKrESun;             // Kr * ESun

uniform float fKmESun;             // Km * ESun
uniform float fKr4PI;              // Kr * 4 * PI
uniform float fKm4PI;              // Km * 4 * PI

uniform float fScale;              // 1 / (fOuterRadius - fInnerRadius)
uniform float fScaleDepth;         // The scale depth (i.e. the altitude at which the atmosphere's average density is found)
uniform float fScaleOverScaleDepth; // fScale / fScaleDepth

uniform sampler2D uTextureDebug;
uniform sampler2D uOpticalDepthLUT;

#define nSamples 2

//const int nSamples = 2;
```

```

#define nSamples 2

//const int nSamples = 2;
const float fSamples = 2.0;

float scale(float fCos)
{
    float x = 1.0 - fCos;
    return fScaleDepth * exp(-0.00287 + x*(0.459 + x*(3.83 + x*(-6.80 + x*5.25))));
}

void main(void)
{
    // Get the ray from the camera to the vertex and its length
    vec4 aux = uModelMatrix * vec4(aVertexPosition, 1.0);
    vec3 v3Pos = aux.xyz;
    vec3 v3Ray = v3Pos - v3CameraPos;
    float fFar = length(v3Ray);
    v3Ray /= fFar;

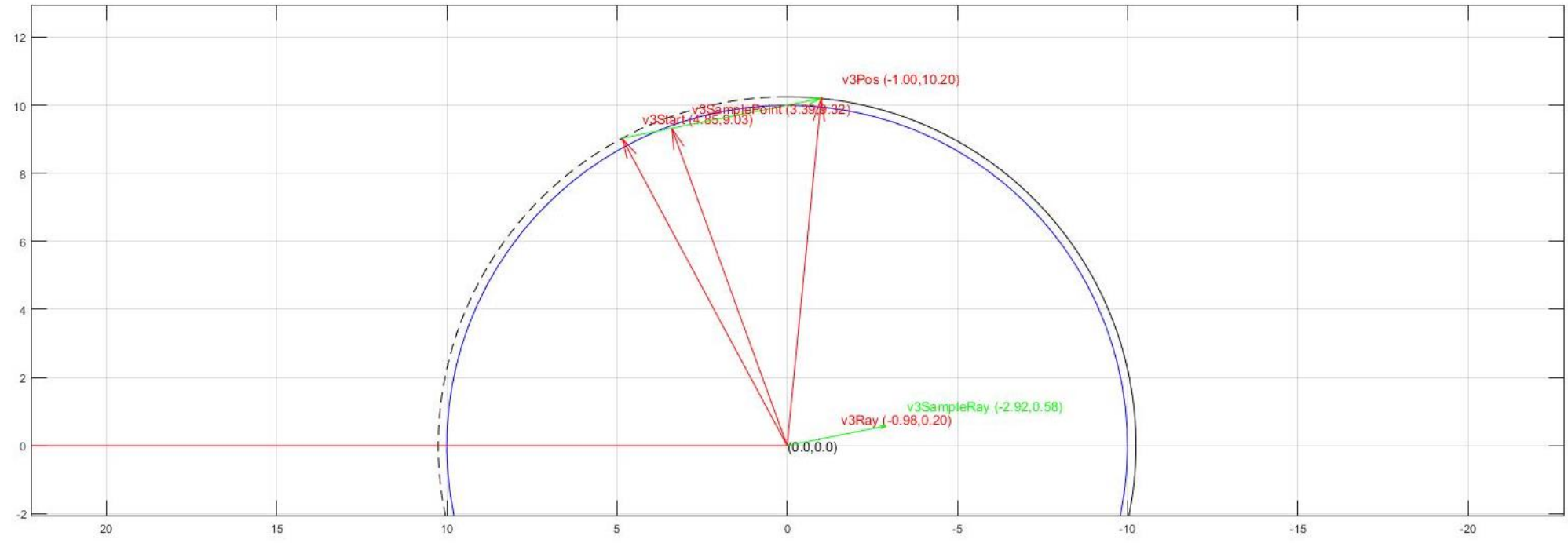
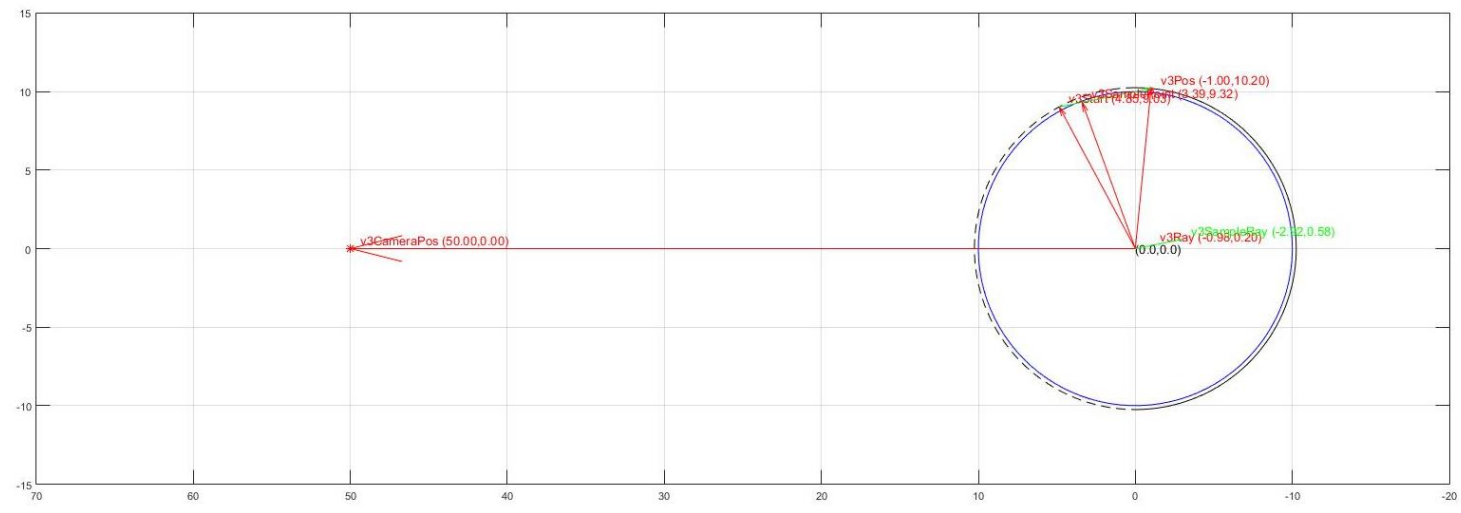
    // Calculate the ray's starting position, then calculate its scattering offset
    vec3 v3Start = v3CameraPos;
    float fHeight = length(v3Start);
    float fDepth = exp(fScaleOverScaleDepth * (fInnerRadius - fCameraHeight));

    float fStartAngle = dot(v3Ray, v3Start) / fHeight;
    float fStartOffset = fDepth * scale(fStartAngle);

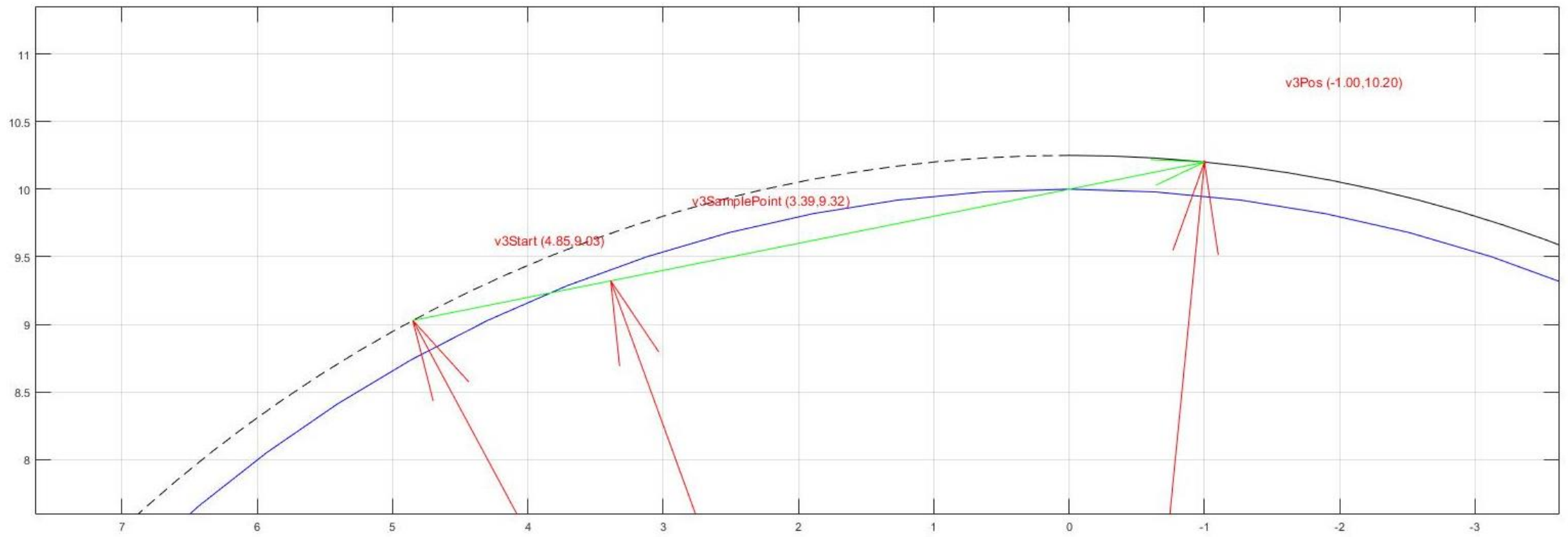
    vec4 v4LightDepth;
    vec4 v4SampleDepth;

    // Initialize the scattering loop variables
    vec3 v3RayleighSum = vec3(0.0,0.0,0.0);
    vec3 v3MieSum = vec3(0.0,0.0,0.0);
    vec3 v3Attenuation;
    float fSampleLength = fFar / fSamples;
    float fScaledLength = fSampleLength * fScale;
    vec3 v3SampleRay = v3Ray * fSampleLength;
    vec3 v3SamplePoint = v3Start + v3SampleRay * 0.5;

```







```
vec3 v3SamplePoint = v3Start + v3SampleRay * 0.5;
```

```
// Now loop through the sample rays
```

```
vec3 v3FrontColor = vec3(0.0, 0.0, 0.0);
```

```
for (int i=0; i<nSamples; i++)
```

```
{
```

```
    float fHeight = length(v3SamplePoint);
```

```
    float fDepth = exp(fScaleOverScaleDepth * (fInnerRadius - fHeight));
```

```
    float fLightAngle = dot(v3LightPos, v3SamplePoint) / fHeight;
```

```
    float fCameraAngle = dot(v3Ray, v3SamplePoint) / fHeight;
```

```
    float fScatter = (fStartOffset + fDepth*(scale(fLightAngle) - scale(fCameraAngle)));
```

```
    vec3 v3Attenuate = exp(-fScatter * (v3InvWavelength * fKr4PI + fKm4PI));
```

```
    v3FrontColor += v3Attenuate * (fDepth * fScaledLength);
```

```
    v3SamplePoint += v3SampleRay;
```

```
}
```

```
debugColor = v3FrontColor * (v3InvWavelength * fKrESun);
```

```
// Finally, scale the Mie and Rayleigh colors and set up the varying variables for the pixel shader
```

```
frontSecondaryColor.rgb = v3FrontColor * fKmESun; // MieColour
```

```
frontColor.rgb = v3FrontColor * (v3InvWavelength * fKrESun); // RayleighColour
```

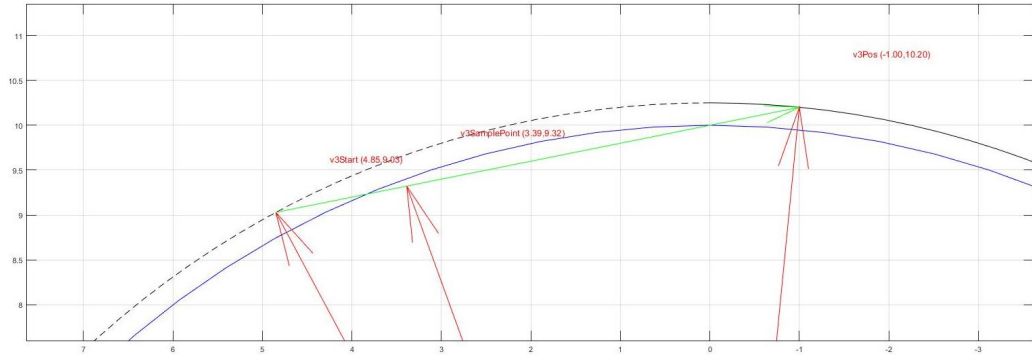
```
gl_Position = uProjectionMatrix * uViewMatrix * uModelMatrix * vec4(aVertexPosition, 1.0);
```

```
v3Direction = v3CameraPos - v3Pos;
```

```
}
```

Midpoint rule integral approximation

$|v3SamplePoint|$



```
for (int i=0; i<nSamples; i++)
{
    float fHeight = length(v3SamplePoint);
    float fDepth = exp(fScaleOverScaleDepth * (fInnerRadius - fHeight));
}
```

$$fScaleOverScaleDepth = \frac{fScale}{fScaleDepth}$$

$$fDepth = \frac{\frac{(fOuterRadius - fInnerRadius)}{0.25}}{1} \times (fInnerRadius - fHeight) = \exp(-4h)$$

From first approximation



```
float fLightAngle = dot(v3LightPos, v3SamplePoint) / fHeight;  
float fCameraAngle = dot(v3Ray, v3SamplePoint) / fHeight;
```

$$u \cdot v = |\vec{u}| \times |\vec{v}| \times \cos \alpha \Rightarrow \cos \alpha = \frac{u \cdot v}{|\vec{u}| \times |\vec{v}|}$$

*v3LightPos* is actually the direction of light (normalized),  
*v3Ray* is also normalized

### Out-scattering

$$t(P_a P_b, \lambda) = 4\pi \times k(\lambda) \times \sum_{i=0}^N \exp\left(\frac{-h}{H_o}\right) ds$$

```
float fScatter = (fStartOffset + fDepth*(scale(fLightAngle) - scale(fCameraAngle)));
```

$$fScatter = \sum_P^{P_c} \exp\left(\frac{-h}{H_o}\right) ds + \sum_P^{P_a} \exp\left(\frac{-h}{H_o}\right) ds$$

### Out-scattering

$$t(P_a P_b, \lambda) = 4\pi \times k(\lambda) \times \sum_{i=0}^N \exp\left(\frac{-h}{H_o}\right) ds$$

### In-scattering

$$I_v(\lambda) = I_s(\lambda) \times k(\lambda) \times F(\theta, \lambda) \times \sum_{i=0}^N \left( \exp\left(\frac{-h}{H_o}\right) \times \exp(-t(P P_c, \lambda) - t(P P_a, \lambda)) \right) ds$$

```
vec3 v3Attenuate = exp(-fScatter * (v3InvWavelength * fKr4PI + fKm4PI));
```

$$\sum_P^{P_c} \exp\left(\frac{-h}{H_o}\right) ds + \sum_P^{P_a} \exp\left(\frac{-h}{H_o}\right) ds$$

**Rayleigh scattering  
coefficient**, dependent  
on wavelength

**Mie scattering  
coefficient**



$$v3FrontColor = \sum_{i=0}^N \left( \underbrace{\exp\left(\frac{-h}{H_o}\right)}_{\text{v3Attenuate}} \times \underbrace{\exp(-t(PP_c, \lambda) - t(PP_a, \lambda))}_{\text{fDepth * fScaledLength}} \right) ds$$

```

v3FrontColor += v3Attenuate * (fDepth * fScaledLength);

v3SamplePoint += v3SampleRay;
}

```

Length of the  
sampled segment,  
*midpoint rule*

Move towards the  
next sample point

# Finally...

```
// Finally, scale the Mie and Rayleigh colors and set up the varying variables for the pixel shader  
frontSecondaryColor.rgb = v3FrontColor * fKmESun; // MieColour  
frontColor.rgb = v3FrontColor * (v3InvWavelength * fKrESun); // RayleighColour  
  
gl_Position = uProjectionMatrix * uViewMatrix * uModelMatrix * vec4(aVertexPosition, 1.0);  
v3Direction = v3CameraPos - v3Pos;  
}
```

# Fragment Shader

- Phase function multiplication by varying Rayleigh and Mie colors outputted from vs



# Fragment Shader. SkyFromAtmosphere-fs

```
precision mediump float;

uniform vec3 v3LightPos;
uniform float g;
uniform float g2;

uniform sampler2D uTextureDebug;

varying vec3 v3Direction;
varying vec3 frontColor;
varying vec3 frontSecondaryColor;

varying vec3 debugColor;

float GetMiePhase(float fCos, float fCos2, float g, float g2);
float GetRayleighPhase(float fCos2);

void main(void)
{
    //gl_FragColor = vec4(0.98, 0.54, 0.035, 1.0); return;
    float fCos = dot(v3LightPos, v3Direction) / length(v3Direction);
    float fCos2 = fCos*fCos;

    vec3 col = GetRayleighPhase(fCos2) * frontColor + GetMiePhase(fCos, fCos2, g, g2) * frontSecondaryColor;

    gl_FragColor = vec4(col, 1.0); return;
}

float GetMiePhase(float fCos, float fCos2, float g, float g2)
{
    return 1.5 * ((1.0 - g2) / (2.0 + g2)) * (1.0 + fCos2) / pow(1.0 + g2 - 2.0*g*fCos, 1.5);
}

float GetRayleighPhase(float fCos2)
{
    return 0.75 + 0.75 * fCos2;
}
```

# OUTLINE

BASICS

SCATTERING THEORY

CAVEATS OF NAIVE IMPLEMENTATION

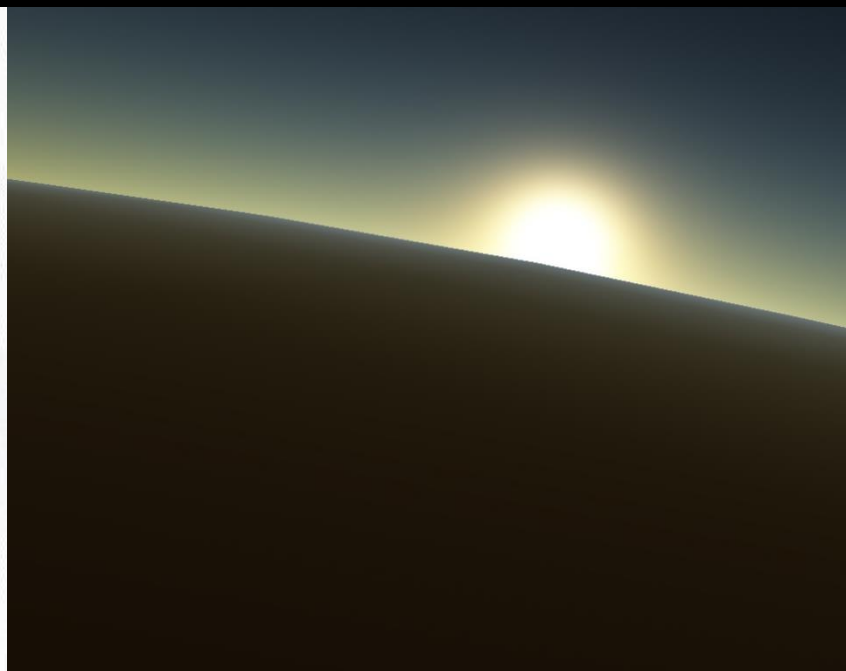
ACTUAL IMPLEMENTATION

**DEMO**

CONCLUSIONS AND FUTURE WORK

REFERENCES

Q2.58FPS  
Samples (+/-): 3  
Kr (1/Shift+1): 0.0025  
Km (2/Shift+2): 0.0010  
z (3/Shift+3): -0.998  
Esun (4/Shift+4): 20.0  
Red (5/Shift+5): 0.650  
Green (6/Shift+6): 0.570  
Blue (7/Shift+7): 0.475  
Exposure (8/Shift+8): 0.8





# OUTLINE

INTRODUCTION

BASICS

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ACTUAL IMPLEMENTATION

DEMO

CONCLUSIONS AND FUTURE WORK

REFERENCES

# Conclusions and Future Work

- Gets results and its fast, could be rendered at a full screen quad instead of sphere, super optimal.
  - Caveat of the approximations used, cannot change the atmosphere or density at will
- 
- Add multiple scattering, multiple scattering makes the sky more real
  - Remove exponential decrease of atmospheric density approximation
  - Scattering from the moon
  - Add Atmospheric Perspective
  - etc...

# OUTLINE

BASICS

SCATTERING THEORY

CAVEATS OF NAIVE IMPLEMENTATION

ACTUAL IMPLEMENTATION

DEMO

CONCLUSIONS AND FUTURE WORK

REFERENCES



# References

- [REF1]

<http://citeseerx.ist.psu.edu/viewdoc/download?doi=10.1.1.75.5595&rep=rep1&type=pdf>

- [REF2]

[https://developer.nvidia.com/gpugems/GPUGems2/gpugems2\\_chapter16.html](https://developer.nvidia.com/gpugems/GPUGems2/gpugems2_chapter16.html)

- <https://github.com/Scrawk/Brunetons-Improved-Atmospheric-Scattering>
- <https://www.gamedev.net/articles/programming/graphics/real-time-atmospheric-scattering-r2093/>

# Thank you!



<https://github.com/graushf/AtmosphericScatteringWebGL.git>

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