

- Take the Fourier transform $\mathcal{F}f$ and ask what happens if the sign of its argument is reversed

$$\mathcal{F}f(s) \equiv \int_{-\infty}^{\infty} f(t) e^{-2\pi i s t} dt$$

$$\Rightarrow \mathcal{F}f(-s) = \int_{-\infty}^{\infty} f(t) e^{-2\pi i (-s) t} dt$$

$$= \int_{-\infty}^{\infty} f(t) e^{2\pi i s t} dt$$

$$= \mathcal{F}^{-1}f(s)$$

or removing the explicit statement of the independent variable

$$(\mathcal{F}f)^{-} = \mathcal{F}^{-1}f$$

- Because this holds for $f(t)$ and tempered distributions can be obtained from f by

\mathcal{F}_f and $\lim_{\alpha \rightarrow 0} \mathcal{F}_{f_\alpha}$ it also holds for distributions

$$(\mathcal{F}\mathcal{T})^{-} = \mathcal{F}^{-1}\mathcal{T} \quad \checkmark$$

[see Osgood p82-85 & 179-182]