

- Take the inverse Fourier transform $\mathcal{F}^{-1}f$ and ask what happens if the sign of the argument is reversed

$$\mathcal{F}^{-1}f(t) \equiv \int_{-\infty}^{\infty} f(s) e^{2\pi i s t} ds$$

$$\mathcal{F}^{-1}f(-t) = \int_{-\infty}^{\infty} f(s) e^{2\pi i s (-t)} ds$$

$$= \int_{-\infty}^{\infty} f(s) e^{-2\pi i s t} ds$$

$$= \mathcal{F}f(t)$$

or removing the explicit statement of the independent variable

$$\mathcal{F}^{-1}f^- = \mathcal{F}f$$

- Because this holds for $f(t)$ and tempered distributions can be obtained from f by

$\mathcal{T}f$ and $\lim_{\alpha \rightarrow 0} \mathcal{T}_{f_\alpha}$ it holds for distributions

$$(\mathcal{F}^{-1}\mathcal{T})^- = \mathcal{F}\mathcal{T} \quad \checkmark$$

[see Osgood p 82-85 d 179-182]