## L2: Basic Cryptography

Hui Chen, Ph.D.

Dept. of Engineering & Computer Science

Virginia State University

Petersburg, VA 23806

#### Acknowledgement

- Many slides are from or are revised from the slides of the author of the textbook
  - Matt Bishop, Introduction to Computer Security, Addison-Wesley Professional, October, 2004, ISBN-13: 978-0-321-24774-5. <u>Introduction to Computer Security @ VSU's Safari Book Online subscription</u>
  - http://nob.cs.ucdavis.edu/book/book-intro/slides/

#### Overview

- Cryptography as mechanism to enforce security policies
- Concepts
  - Cryptography, cryptanalysis
- Basic Cryptography
  - Classical Cryptography
  - Public Key Cryptography
  - Cryptographic Checksums

#### Overview

- Classical Cryptography
  - Caesar cipher
  - Vigènere cipher
  - DES
- Public Key Cryptography
  - Diffie-Hellman
  - RSA
- □ Cryptographic Checksums
  - HMAC

## Security Policy and Mechanism

- Security policy
  - A statement of what is allowed and what is not allowed
  - Example
    - A student may not copy another student's homework
  - Can be informal or highly mathematical
- Security mechanism
  - A method, tool, or procedure for enforcing security policy
  - Technical and non-technical
    - □ A homework electronic submission system (e.g., Blackboard) enforces who may read a homework submission

## Security Mechanisms

- □ Cryptographic mechanisms
- Non-cryptographic mechanisms

6

## Cryptography

- Word Origin
  - Greek words
  - "secrete writing"
- □ Art & science of concealing meaning

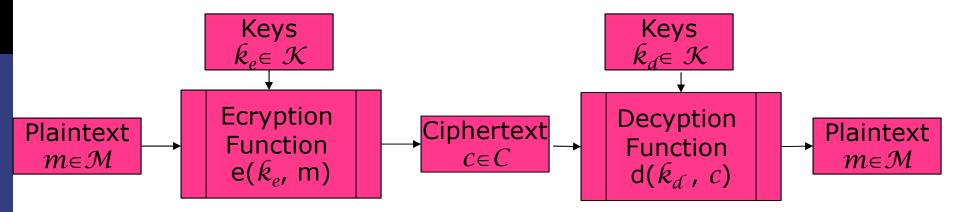
## Cryptanalysis

- Breaking of codes
- Application
  - World War II
- □ Further Reading
  - W. Diffie and M. Hellman. 2006. New directions in cryptography. *IEEE Trans. Inf. Theor.* 22, 6 (September 2006), 644-654. DOI=10.1109/TIT.1976.1055638 http://dx.doi.org/10.1109/TIT.1976.1055638

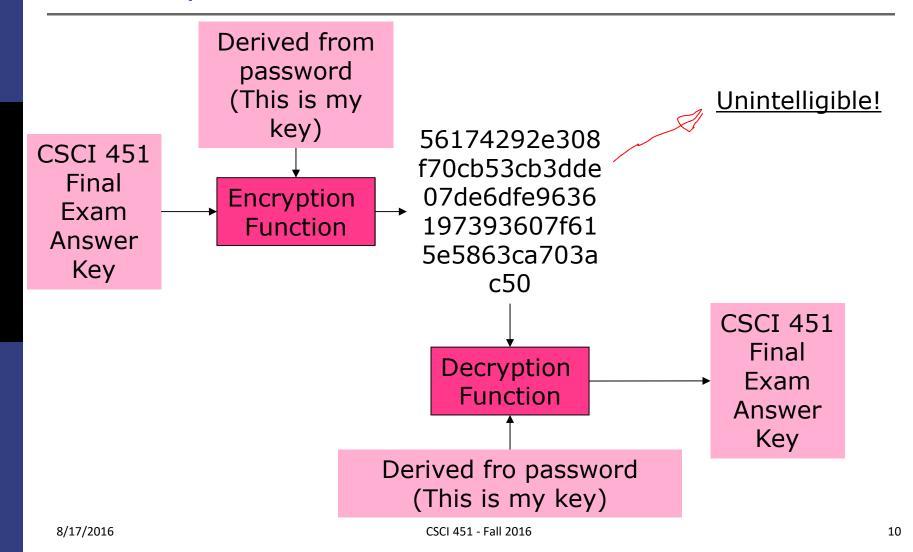
8

#### Cryptosystem

- $\square$  Quintuple or 5-tuple ( $\mathcal{E}$ ,  $\mathcal{D}$ ,  $\mathcal{M}$ ,  $\mathcal{K}$ ,  $\mathcal{C}$ )
  - lacksquare  $\mathcal M$  set of plaintexts
  - lacksquare  $\mathcal K$  set of keys
  - C set of ciphertexts
  - $\mathcal{E}$  set of encryption functions  $e: \mathcal{M} \times \mathcal{K} \rightarrow \mathcal{C}$
  - $\mathcal{D}$  set of decryption functions  $d: C \times \mathcal{K} \rightarrow \mathcal{M}$



#### Example



# Example: NotePad++ NPPCrypt Plugin



```
<nppcrypt version="101">
<encryption cipher="aes256" mode="cbc" encoding="base16" />
<random iv="atuPGKigDnTy46fHBPM1vA==" salt="wOiEp1afVtXebE4kMSliFg==" />
<key algorithm="pbkdf2" hash="md5" iterations="1000" />
</nppcrypt>
56174292e308f70cb53cb3dde07de6dfe9636197393607f615e5863ca703ac50
```

## Classical Cryptography

- Sender, receiver share common key
  - Keys may be the same, or trivial to derive from one another
  - Sometimes called symmetric cryptography
- Two basic types
  - Transposition ciphers
    - Example: Rail Fence Cipher
  - Substitution ciphers
    - Example: Caesar Cipher
  - Combinations are called product ciphers

#### Transposition Cipher

- □ Rearrange letters in plaintext to produce ciphertext
- **□** Example
  - Rail-Fence Cipher
  - Example
    - □ HELLO WORLD becomes HLOOL ELWRD

#### Rail-Fence Cipher

#### **□** Encryption

- Writing the plaintext in two rows, proceeding down, then across
- Reading the ciphertext across, then down.

#### Rail-Fence Cipher

- □ Plaintext is HELLO WORLD
  - Rearrange as

HLOOL

ELWRD

- Cipher-text is HLOOL ELWRD
- Mathematically, the key to a transposition cipher is a permutation function.

#### Attacking Transposition Cipher

- Mathematically, the key to a transposition cipher is a permutation function.
- Observation: the permutation does not alter the frequency of plaintext characters
- Detecting the cipher by comparing character frequencies with a model of the language
  - Anagramming

#### Anagramming Attack

- □ Language Model: tables of n-gram frequencies Input: Cipher-text
- Method:
  - If 1-gram frequencies match English frequencies, but other n-gram frequencies do not, probably transposition
  - Let n := 1
  - Do
    - □ n := n + 1
    - □ Rearrange letters to form *n*-grams with highest frequencies
  - Until the transposition pattern is found

#### Example

- Konheim's diagram table
- □ Cipher-text: HLOOLELWRD
- □ Frequencies of 2-grams beginning with H
  - HE 0.0305
  - HO 0.0043
  - HL, HW, HR, HD < 0.0010</p>
- □ Frequencies of 2-grams ending in H
  - WH 0.0026
  - EH, LH, OH, RH, DH ≤ 0.0002
- □ Implies E follows H

#### Example

■ Since "E" follows "H", we arrange the letters so that each letter in the first block of five letters is adjacent to the corresponding letters in the 2<sup>nd</sup> block of five letters

- HLOOL ELWRD
- HE
- LL
- OW
- OR
- LD

#### Substitution Ciphers

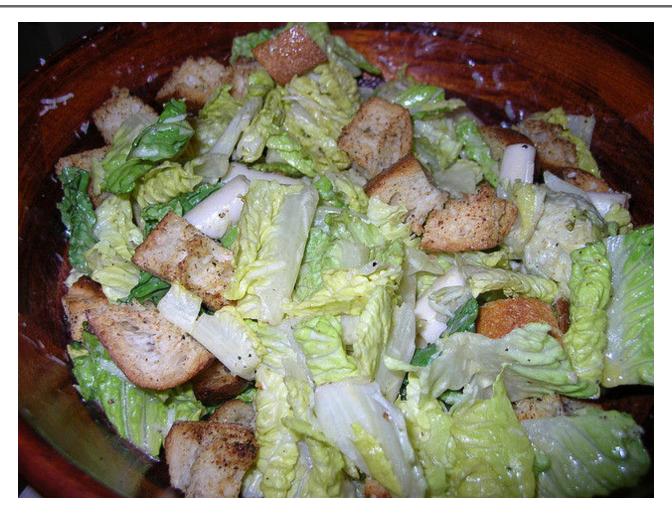
- □ Change characters in plaintext to produce ciphertext
- Example
  - Caesar cipher
    - □ Plaintext is HETALO WORTAD
    - □ Change each letter to the third letter following it (X goes to A, Y to B, Z to C)
      - Key is 3, usually written as letter 'D'
    - □ Ciphertext is KHOOR ZRUOG
- More details follow

## Caesar Cipher

- □ Gaius Julius Caesar(July 100 BC 15March 44 BC)
- "If he had anything confidential to say, he wrote it in cipher..."



#### Did he invent this also?



#### Caesar Cipher

- $\square \mathcal{M} = \{ \text{ sequences of letters } \}$ 
  - The alphabet has N letters
- $\square \mathcal{K} = \{ i \mid i \text{ is an integer and } 0 \le i \le \mathbb{N} 1 \}$
- $\square \mathcal{E} = \{ E_k \mid k \in \mathcal{K} \text{ and for all letters } m, E_k(m) = (m + k)$  mod N \}
- $\square \mathcal{D} = \{ D_k \mid k \in \mathcal{K} \text{ and for all letters } c, \ D_k(c) = (N + c k) \text{ mod } N \}$
- $\Box C = \mathcal{M}$

#### A Caesar Cipher

- $\square \mathcal{M} = \{0, 1, 2, ..., 25\}$ 
  - Assume English alphabet. The alphabet has N = 26 letters,
     representing each letter by its position in the alphabet
- $\Box$  Choose k = 3
- $\Box$  E<sub>3</sub>(m) = (m + k) mod 26
- $\Box$  D<sub>3</sub>(c) = (26 + c k) mod 26
- $\Box C = \mathcal{M}$

#### Example: Encryption

- □ Plaintext = "HELLO", i.e.,
  - **7** 4 11 11 14
- $\square$  k = 3
- □ Compute ciphertext
  - 7 + 3 mod 26 = 10
  - $4 + 3 \mod 26 = 7$
  - 11 + 3 mod 26 = 14
  - 11 + 3 mod 26 = 14
  - 14 + 3 mod 26 = 17
  - **10** 7 14 14 17

## Example

- □ Convert the integers back to letters
  - **10** 7 14 14 17
- □ Ciphertext = "KHOOR"

#### Example: Decryption

- □ Ciphertext = "KHOOR", i.e.,
  - **10** 7 14 14 17
- $\square$  k = 3
- □ Compute plaintext
  - $26 + 10 3 \mod 26 = 7$
  - $26 + 7 3 \mod 26 = 4$
  - 26 + 14 3 mod 26 = 11
  - 26 + 14 3 mod 26 = 11
  - 26 + 17 3 mod 26 = 14
  - **7** 4 11 11 14

## Example

- □ Convert the integers back to letters
  - **7** 4 11 11 14
- □ Ciphertext = "HELLO"

#### Attacking the Cipher

- Exhaustive search
  - If the key space is small enough, try all possible keys until you find the right one
  - Caesar cipher has only 26 possible keys (assuming English alphabet)
    - Exhaustive search is feasible
- Statistical analysis
  - Compare to 1-gram model of English

#### Exercise L2-1

- $\Box$  Use Caesar Cipher with k = 9, and compute ciphertext for the message below,
  - TROJAN

#### Exercise L2-2

- Assume Caesar Cipher, use exhaustive search to find the key for the ciphertext below
  - XUW
- To determine if your key is correct, read the plaintext using the key guessed to see if it is intelligible.

#### Exercise L2-3

■ Write a program that computes ciphertext letter from a plaintext letter using Caesar cipher with a given key k, and a program that computes plaintext letter from a giver ciphertext letter using Caesar cipher with a given key k.

#### Statistical Attack

□ Compute frequency of each letter in ciphertext:

G 0.1 H 0.1 K 0.1 O 0.3

R 0.2 U 0.1 Z 0.1

- □ Apply 1-gram model of English
  - Frequency of characters (1-grams) in English is on next slide

8/17/2016 CSCI 451 - Fall 2016 33

## English Letter Frequencies

Letter	Frequency	Letter	Frequency	Letter	Frequency	Letter	Frequency
a	0.080	h	0.060	n	0.070	t	0.090
b	0.015	i	0.065	O	0.080	u	0.030
c	0.030	j	0.005	p	0.020	V	0.010
d	0.040	k	0.005	q	0.002	W	0.015
e	0.130	1	0.035	r	0.065	X	0.005
f	0.020	m	0.030	S	0.060	У	0.020
g	0.015					Z	0.002

#### Statistical Analysis

- $\Box$  f(c): frequency of character c in ciphertext
- $\mathbf{d}(k_d,c)$ : decryption function on ciphertext character  $\mathbf{c}$  with key  $k_d$
- $\Box \varphi(k_d) = \sum_{0 \le c \le 25} f(c)p(d(k_d, c))$ : correlation of frequency of letters in ciphertext with corresponding letters in English
  - key is  $k_d$
  - p(x) is frequency of character x in the language
- ☐ This correlation should be a maximum when the key *k* translates to the ciphertext into English, i.e.,
  - $\blacksquare$  argmax  $_{kd}$   $\varphi(k_d)$

## Statistical Analysis on Caesar Cipher

- $\Box$  f(c): frequency of character c in ciphertext
- Considering the Caesar Cipher and English, decryption function is
  - $d_i(c) = 26 + c i \mod 26$
- □ Correlation of frequency of letters in ciphertext with corresponding letters in English becomes
  - $\phi(i) = \sum_{0 \le c \le 25} f(c)p(26 + c i \mod 26)$
  - p(x) is frequency of character x in English
- $\Box$  Find key *i* such that  $\varphi(i)$  is a maximum for all *i*

### Statistical Analysis

- □ Consider the ciphertext KHOOR ZRUOG
- $\Box$  f(c): frequency of character c in ciphertext

c	f(c)	c	f(c)	c	f(c)	c	c
0	0	7	0.1	13	0	19	0
1	0	8	0	14	0.3	20	0.1
2	0	9	0	15	0	21	0
3	0	10	0.1	16	0	22	0
4	0	11	0	17	0.2	23	0
5	0	12	0	18	0	24	0
6	0.1					25	0

8/17/2016 CSCI 451 - Fall 2016

37

#### Statistical Analysis

- □ Consider the ciphertext KHOOR ZRUOG
- $\Box$  f(c): frequency of character c in ciphertext
- - □ For the cipher text

$$\varphi(i) = 0.1p(26 + 6 - i \mod 26) + 0.1p(26 + 7 - i \mod 26) + 0.1p(26 + 10 - i \mod 26) + 0.3p(26 + 14 - i \mod 26) + 0.2p(26 + 17 - i \mod 26) + 0.1p(26 + 20 - i \mod 26) + 0.1p(26 + 25 - i \mod 26)$$

- p(x) is frequency of character x in English
- Compute  $\varphi(i)$  for all i,  $0 \le i \le 25$
- Find key *i* such that  $\varphi(i)$  is *large* and decrypted text is *intelligible*

8/17/2016

# Correlation: $\varphi(i)$ for $0 \le i \le 25$

i	$\varphi(i)$	i	$\varphi(i)$	i	$\varphi(i)$	i	$\varphi(i)$
0	0.0482	7	0.0442	13	0.0520	19	0.0315
1	0.0364	8	0.0202	14	0.0535	20	0.0302
2	0.0410	9	0.0267	15	0.0226	21	0.0517
3	0.0575	10	0.0635	16	0.0322	22	0.0380
4	0.0252	11	0.0262	17	0.0392	23	0.0370
5	0.0190	12	0.0325	18	0.0299	24	0.0316
6	0.0660					25	0.0430

#### Result of Statistical Analysis

- Most probable keys, based on φ:
  - i = 6,  $\varphi(i) = 0.0660$ 
    - □ plaintext EBIIL TLOLA
  - $i = 10, \varphi(i) = 0.0635$ 
    - □ plaintext AXEEH PHKEW
  - $i = 3, \varphi(i) = 0.0575$ 
    - □ plaintext HELLO WORLD
  - i = 14,  $\varphi(i) = 0.0535$ 
    - □ plaintext WTAAD LDGAS
- $\Box$  Only English phrase is for i = 3
  - That's the key (3 or 'D')

#### Problem with Caesar Cipher

- Key is too short
  - Can be found by exhaustive search
  - Statistical frequencies not concealed well
    - They look too much like regular English letters
- So make it longer: long key may obscure the statistics
  - Multiple letters in key
  - Idea is to smooth the statistical frequencies to make cryptanalysis harder

### Vigenère Cipher

- ☐ Giovan Battista Bellaso, 1553
- Use phrase as the key
- Similar to Caesar cipher, but use each letter from the key to encipher
- Example
  - Message: THE BOY HAS THE BALL
  - **Key**: VIG
  - Encipher using Caesar cipher for each letter:

```
key VIGVIGVIGVIGV
```

plain THEBOYHASTHEBALL

cipher OPKWWECIYOPKWIRG

### Table-Lookup Approach

- Trade memory for efficiency
- Store pre-calculated ciphertext for each letter using each possible key letter
  - 26 letters
  - 26 possible keys
  - Table of 26 × 26

### Vigenère Tableau

```
A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B D D E F G H I J K L M N O P Q R S T U V W X Y Z A B D D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I J K L M N O P Q R S T U V W X Y Z A B C D E F G H I
```

#### **Generate the table**

```
In C++

for (int key = 0; key < KEY_SPACE_SIZE; key ++)
{
  cout << char(key + 'A') << ' ';
  for (int letter = 0; letter < ALPHABET_SIZE; letter ++)
  {
   int ciphertext = (letter + key) % ALPHABET_SIZE;
   cout << char(ciphertext + 'A') << ' ';
  }
  cout << endl;
}</pre>
```

#### Relevant Parts of Tableau

	G	$\mathcal{I}$	V
A	G	I	V
В	Н	J	M
E	L	M	Z
Н	N	P	C
$\mathcal{L}$	R	${ m T}$	G
0	U	M	J
S	Y	A	N
T	Z	В	0
Y	E	Η	Τ

- Tableau shown has relevant rows, columns only
- **□** Example encipherments:
  - key V, letter T: follow V column down to T row (giving "O")
  - Key I, letter H: follow I column down to H row (giving "P")

#### **Useful Terms**

- □ *period*: length of key
  - In earlier example, period is 3
- □ tableau: table used to encipher and decipher
  - Vigenère cipher has key letters on top, plaintext letters on the left
- polyalphabetic: the key has several different letters
  - Caesar cipher is monoalphabetic

### Attacking Vigenère Cipher

- Approach
  - Establish period; call it n
  - Break message into n parts, each part being enciphered using the same key letter
  - Solve each part
    - You can leverage one part from another
- We will show each step

### Target Ciphertext

■ We want to break the Vigenère cipher using the ciphertext:

```
ADQYS MIUSB OXKKT MIBHK IZOOO
EQOOG IFBAG KAUMF VVTAA CIDTW
MOCIO EQOOG BMBFV ZGGWP CIEKQ
HSNEW VECNE DLAAV RWKXS VNSVP
HCEUT QOIOF MEGJS WTPCH AJMOC
HIUIX
```

#### Establish Period

- ☐ The key is to establish the period
- Method
  - Using Kasiski method establish initial guesses
  - Using index of coincidence to confirm the guesses

#### Establish Period: Kasiski

- ☐ Friedrich W. Kasiski: a Prussian cavalry officer
  - repetitions in the ciphertext occur when characters of the key appear over the same characters in the plaintext (Kasiski, 1863)
- **□** Example:

key **VIGV**IGVIGVIGV

plain THEBOYHASTHEBALL

cipher **OPKW**WECIY**OPKW**IRG

Counting distance 0123456789

Note the key and plaintext line up over the repetitions (underlined). As distance between repetitions is 9, the period is a factor of 9 (that is, 1, 3, or 9)

## Repetitions in Example

Letters	Start	End	Distance	Factors
MI	5	15	10	2, 5
00	22	27	5	5
OEQOOG	24	54	30	2, 3, 5
FV	39	63	24	2, 2, 2, 3
AA	43	87	44	2, 2, 11
MOC	50	122	72	2, 2, 2, 3, 3
QO	56	105	49	7, 7
PC	69	117	48	2, 2, 2, 2, 3
NE	77	83	6	2, 3
SV	94	97	3	3
СН	118	124	6	2, 3

■ Note that the program counts from 1 and we count from 0 in previous example

# Looking For Repetition using Provided Program

#### □ Note that the program counts from 1; however, we count from 0 in previous example

octave>

findcommonsubstrings('ADQYSMIUSBOXKKTMIBHKIZOOOEQOOGIFBAGKAUMFVVTAACIDTWMOCIOEQOOGBMBFVZGGWPCIEKQHSNEWVEC NEDLAAVRWKXSVNSVPHCEUTQOIOFMEGJSWTPCHAJMOCHIUIX', 'v');

Start	End	Len	Gap	Letters
6	16	2	10	MI
7	127	2	120	IU
23	28	2	5	00
23	58	2	35	00
24	28	2	4	00
24	58	2	34	00
27	106	2	79	QO
25	55	6	30	OEQOOG
40	64	2	24	FV
44	88	2	44	AA
46	53	2	7	CI
46	71	2	25	CI
51	123	3	72	MOC
53	71	2	18	CI
54	108	2	54	IO
57	106	2	49	QO
70	118	2	48	PC
78	84	2	6	NE
95	98	2	3	SV
119	125	2	6	СН

octave>

#### Estimate of Period

- OEQOOG is probably not a coincidence
  - It is too long for that
  - Period may be 1, 2, 3, 5, 6, 10, 15, or 30
- Most others (7/10) have 2 in their factors
- □ Almost as many (6/10) have 3 in their factors
- $\blacksquare$  Begin with period of  $2 \times 3 = 6$

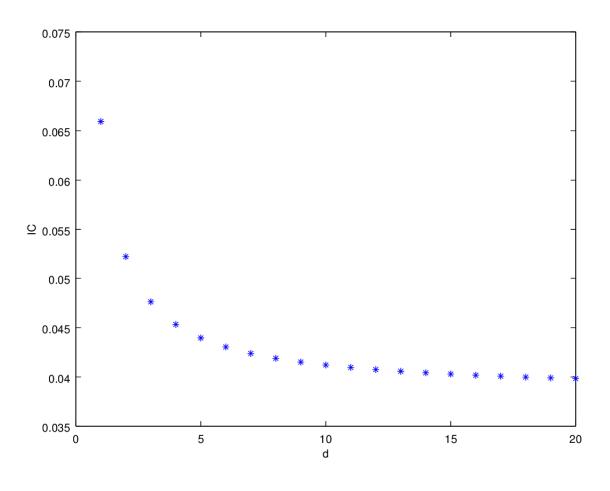
#### Checking on Period

- □ Index of coincidence is probability that two randomly chosen letters from ciphertext match
- Tabulated for different periods for English ciphertexts at different periods (d):

$$IC = 0.065933 / d + 0.038462 (d - 1) / d$$

Period	IC	Period	IC	Period	IC
1	0.066	3	0.047	5	0.044
2	0.052	4	0.045	10	0.041
Large	0.038				

# Index of Coincidence for English Ciphertext



#### Computing IC

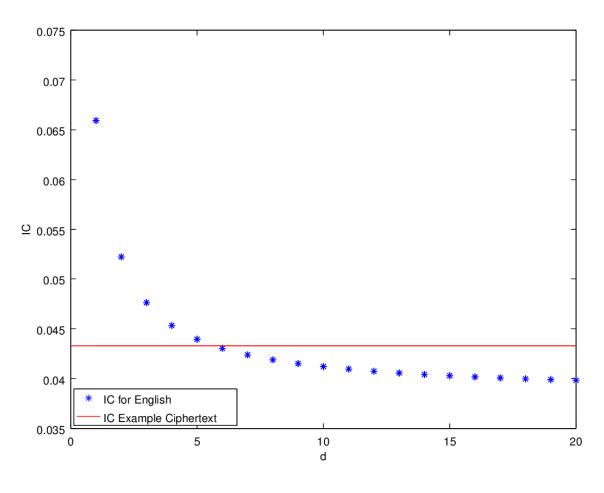
$$\square$$
 IC =  $[n (n-1)]^{-1} \sum_{0 \le i \le 25} [F_i (F_i - 1)]$ 

- where n is length of ciphertext and F<sub>i</sub> the number of times character i occurs in ciphertext
- □ Here, IC = 0.043
  - Indicates a key of slightly more than 5
  - A statistical measure, so it can be in error, but it agrees with the previous estimate (which was 6)

# Computing IC using Provided Program

```
octave> ciphertext =
'ADQYSMIUSBOXKKTMIBHKIZOOOEQOOGIFBAGK
AUMFVVTAACIDTWMOCIOEQOOGBMBFVZGGWPCIE
KQHSNEWVECNEDLAAVRWKXSVNSVPHCEUTQOIOF
MEGJSWTPCHAJMOCHIUIX';
octave> computeic(ciphertext)
ans = 0.043292
octave>
```

# Confirming Key Length



# Splitting Into Alphabets using Estimated Period (Period = 6)

#### Ciphertext

```
ADQYS MIUSB OXKKT MIBHK IZOOO EQOOG IFBAG
KAUMF VVTAA CIDTW MOCIO EQOOG BMBFV ZGGWP
CIEKQ HSNEW VECNE DLAAV RWKXS VNSVP HCEUT
QOIOF MEGJS WTPCH AJMOC HIUIX
```

alphabet 1: AIKHOIATTOBGEEERNEOSAI

alphabet 2: DUKKEFUAWEMGKWDWSUFWJU

alphabet 3: QSTIQBMAMQBWQVLKVTMTMI

alphabet 4: YBMZOAFCOOFPHEAXPQEPOX

alphabet 5: SOIOOGVICOVCSVASHOGCC

alphabet 6: MXBOGKVDIGZINNVVCIJHH

#### Checking on IC

```
alphabet 1: AIKHOIATTOBGEEERNEOSAI
```

alphabet 2: DUKKEFUAWEMGKWDWSUFWJU

alphabet 3: QSTIQBMAMQBWQVLKVTMTMI

alphabet 4: YBMZOAFCOOFPHEAXPQEPOX

alphabet 5: SOIOOGVICOVCSVASHOGCC

alphabet 6: MXBOGKVDIGZINNVVCIJHH

#### 

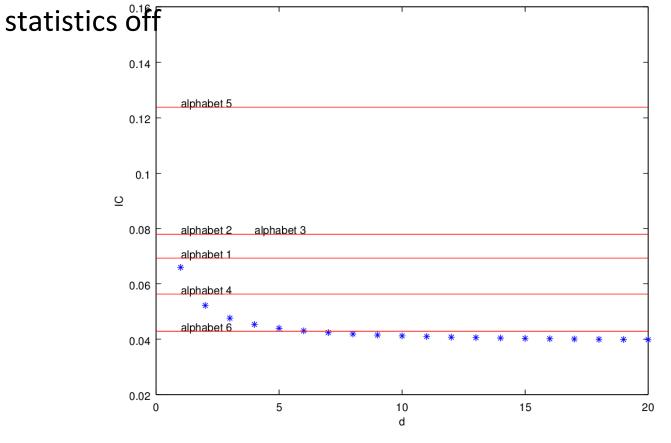
- #1, 0.069; #2, 0.078; #3, 0.078; #4, 0.056; #5, 0.124; #6, 0.043
- Indicate all alphabets have period 1, except #4 and #6; assume statistics off

# Computing IC using Provided Octave/Matlab Program

```
octave> alphabet1 = ciphertext(1:6:length(ciphertext))
alphabet1 = AIKHOIATTOBGEEERNEOSAI
octave > computeic(alphabet1)
ans = 0.069264
octave> alphabet2 = ciphertext(2:6:length(ciphertext))
alphabet2 = DUKKEFUAWEMGKWDWSUFWJU
octave > computeic(alphabet2)
ans = 0.077922
octave> alphabet3 = ciphertext(3:6:length(ciphertext))
alphabet3 = OSTIOBMAMOBWOVLKVTMTMI
octave> computeic(alphabet3)
ans = 0.077922
octave>
```

# Checking on IC

□ all alphabets have period 1, except #4 and #6; assume



#### Frequency Examination

```
ABCDEFGHIJKLMNOPQRSTUVWXYZ
```

- **1** 31004011301001300112000000
- **2** 10022210013010000010404000
- **3** 12000000201140004013021000
- 4 21102201000010431000000211
- **5** 10500021200000500030020000
- 6 01110022311012100000030101

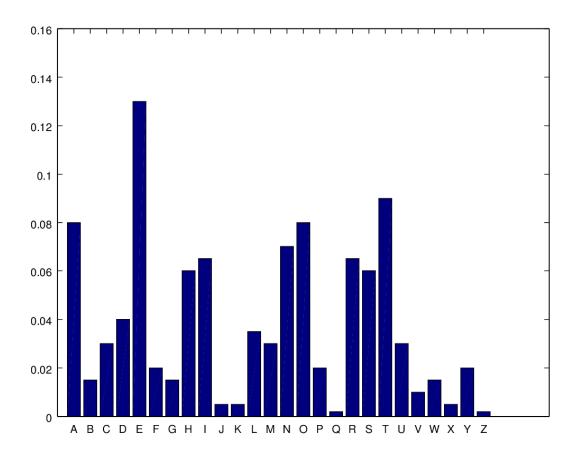
#### Letter frequencies are (H high, M medium, L low):

HMMMHHMMMHHMLHHHMLLLLL

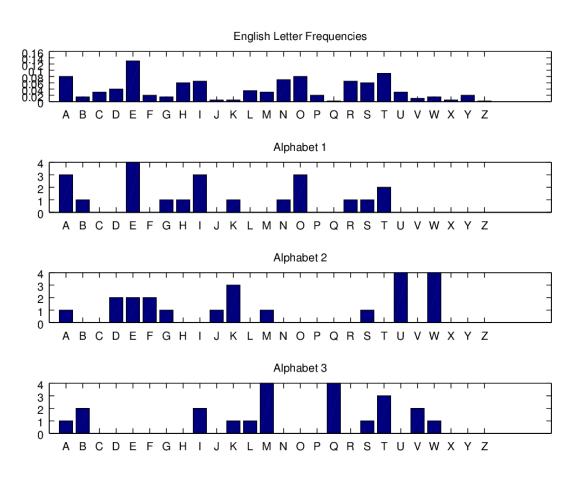
# English Letter Frequencies

Letter	Frequency	Letter	Frequency	Letter	Frequency	Letter	Frequency
a	0.080	h	0.060	n	0.070	t	0.090
b	0.015	i	0.065	O	0.080	u	0.030
c	0.030	j	0.005	p	0.020	V	0.010
d	0.040	k	0.005	q	0.002	W	0.015
e	0.130	1	0.035	r	0.065	X	0.005
f	0.020	m	0.030	S	0.060	У	0.020
g	0.015					Z	0.002

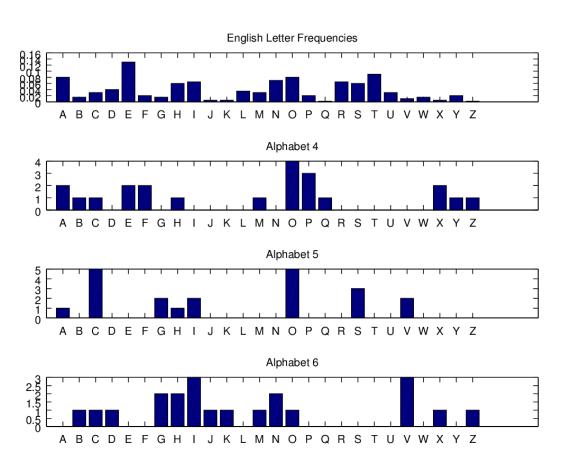
### English Letter Frequencies



### Guessing Key



## Guessing Key



#### Begin Decryption

- ☐ First matches characteristics of unshifted alphabet
- Third matches if I shifted to A
- □ Sixth matches if V shifted to A
- Substitute into ciphertext (bold are substitutions)

```
ADIYS RIUKB OCKKL MIGHK AZOTO EIOOL
```

IFTAG PAUEF VATAS CIITW EOCNO EIOOL

BMTFV EGGOP CNEKI HSSEW NECSE DDAAA

RWCXS ANSNP HHEUL QONOF EEGOS WLPCM

AJEOC MIUAX

#### Look For Clues

■ AJE in last line suggests "are", meaning second alphabet maps A into S:

```
ALIYS RICKB OCKSL MIGHS AZOTO
```

MIOOL INTAG PACEF VATIS CIITE

ECCNO MICOL BUTFY EGOOP CNESI

HSSEE NECSE LDAAA RECXS ANANP

HHECL QONON EEGOS ELPCM AREOC

MICAX

#### Next Alphabet

MICAX in last line suggests "mical" (a common ending for an adjective), meaning fourth alphabet maps O into A:

ALIMS RICKP OCKSL AIGHS ANOTO MICOL

INTOG PACET VATIS QIITE ECCNO MICOL

BUTTV EGOOD CNESI VSSEE NSCSE LDOAA

RECLS ANAND HHECL EONON ESGOS ELDCM

ARECC MICAL

#### Got It!

QI means that U maps into I, as Q is always followed by U:

ALIME RICKP ACKSL AUGHS ANATO MICAL INTOS PACET HATIS QUITE ECONO MICAL BUTTH EGOOD ONESI VESEE NSOSE LDOMA RECLE ANAND THECL EANON ESSOS ELDOM ARECO MICAL

# With Proper Spacing and Punctuation

□ A LIMERICK PACKS LAUGHS ANATOMICAL INTO SPACE THAT IS QUITE ECONOMICAL. BUT THE GOOD ONES I'VE SEEN SO SELDOM ARE CLEAN, AND THE CLEAN ONES SO SELDOM ARE COMICAL.

## Lessons Learned

- □ Vigenère cipher was once considered unbreakable
- □ It is easy to break by hand!
- Principles of attacks hold for more complex ciphers
  - WordPerfect: encipher a file with a password
    - Certain fields in the enciphered file contained information internal to WordPerfect
    - These fields could be predicted
- $\square$  Cycles of Attack  $\rightarrow$  Fix  $\rightarrow$  Attack  $\rightarrow$  Fix
- Stronger ciphers

## One-Time Pad

- A variant of Vigenère Cipher
  - The key string is chosen at random
  - The key string is at least as long as the message

#### Discussion on Attacks

- Opponent whose goal is to break cryptosystem is the adversary
  - Assume adversary knows algorithm used, but not key
- ☐ Three types of attacks:
  - ciphertext only: adversary has only ciphertext; goal is to find plaintext, possibly key
  - known plaintext: adversary has ciphertext, corresponding plaintext; goal is to find key
  - chosen plaintext: adversary may supply plaintexts and obtain corresponding ciphertext; goal is to find key
- Good cryptosystems protects against all 3 types of attacks

8/17/2016

#### Discussion on Attacks

- Mathematical attacks
  - Based on analysis of underlying mathematics
- Statistical attacks
  - Make assumptions about the distribution of letters, pairs of letters (digrams), triplets of letters (trigrams), etc.
    - Called models of the language
  - Examine ciphertext, correlate properties with the assumptions.

## Exercise L2-4

- Textbook exercise: Question 2 of Chapter 8 in the textbook
- You may use the provided program attackcaesar.m, but must explain your result

## Exercise L2-5

- Breaking two Vigenère ciphers
  - The ciphertext is in pg.txt and tc.txt
  - Use the programs (the example that breaks pg.txt follows and you will break tc.txt on your own)
- Disclaimer
  - All programs were tested in Octave, but not in Matlab although they should be mostly fine in Matlab

## Attacking Vigenère in Programs (1)

1. Read the ciphertext and find repeating substrings

```
octave> ciphertext = readline('pg.txt');
octave> computeletterfreq(ciphertext);
octave> [idx1st, idx2nd, lensubstr, gaps] =
findcommonsubstrings(ciphertext(1:1000), 'v');
octave> gaps(lensubstr > 6)
ans =
216    48    78    138    60    12
```

- 2. Let us now guess the period (the key length): 6
- 3. Confirm with index of coincidence

```
octave> computeic(ciphertext)
ans = 0.041854
```

# Attacking Vigenère in Programs (2)

#### 4. Now guess the letters in the key

```
octave> guesskey(ciphertext(1:6:end), 'v');
octave> guesskey(ciphertext(2:6:end), 'v');
octave> guesskey(ciphertext(1:6:end), 'v');
octave> guesskey(ciphertext(2:6:end), 'v');
octave> guesskey(ciphertext(3:6:end), 'v');
octave> guesskey(ciphertext(4:6:end), 'v');
octave> guesskey(ciphertext(5:6:end), 'v');
octave> guesskey(ciphertext(6:6:end), 'v');
```

The key appears to be ASIMOV.

## Attacking Vigenère in Programs (3)

#### 5. Decipher the ciphertext

```
octave:34> char(vigenere(ciphertext, 'ASIMOV', 'd'))
ans =
THEPROJECTGUTENBERGEBOOKOFMOBYDICKORTHEWHALEBYHERMANM.....
```

What if the result is not intelligible?

## Homework L2-1

- Breaking a Vigenère cipher. The ciphertext is in Exercise 8 of Chapter 8 in the textbook.
- ☐ Show steps, intermediate and final results

## Summary

- Classical Cryptography
  - Caesar cipher
  - Vigènere cipher
- Attack on Caesar cipher and Vigènere cipher
- Concepts of cryptanalysis
  - Simple cryptanalysis