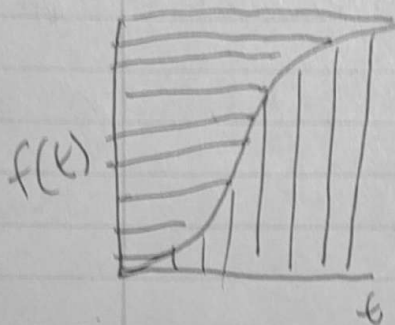


July 17<sup>th</sup>

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# CS 488 Animation

Velocity Curve



## Key-Frame Systems

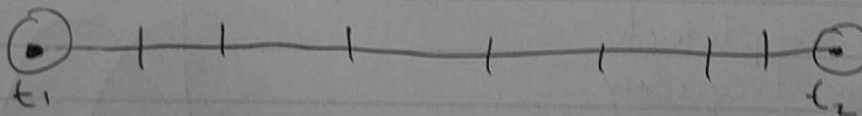
we generate a set of in-between frames from the specification of two or more frames.

Example: Simulating Accelerations: (Hearn & Baker 2nd Ed)

- a) constant speed (Zero acceleration)  
 - equal time intervals, for the in-betweens (IBs)

$$\Delta t = \frac{t_2 - t_1}{n+1} \quad n \text{ IBs for key frames at } t_1 \text{ and } t_2$$

$n+1$  intervals.



### b) Positive Acceleration

- increase interval size  $(1 - \cos \theta)$ ,  $0 < \theta < \frac{\pi}{2}$

$$tIB_j = t_1 + \Delta t \left[ 1 - \cos \left( \frac{j\pi}{2(n+1)} \right) \right] \quad j = 1, 2, \dots, n$$

### c) Negative Acceleration

- reduce interval size,  $\sin \theta$ ,  $0 < \theta < \frac{\pi}{2}$

$$tIB_j = t_1 + \Delta t \sin \left( \frac{j\pi}{2(n+1)} \right) \quad j = 1, 2, \dots, n$$

### d) Combining Both Cases

$$tIB_j = t_1 + \Delta t \left\{ \frac{1 - \cos \left[ \frac{j\pi}{2(n+1)} \right]}{2} \right\} \quad j = 1, 2, \dots, n$$

## Direct Motion Specification

Ex. Bouncing ball:

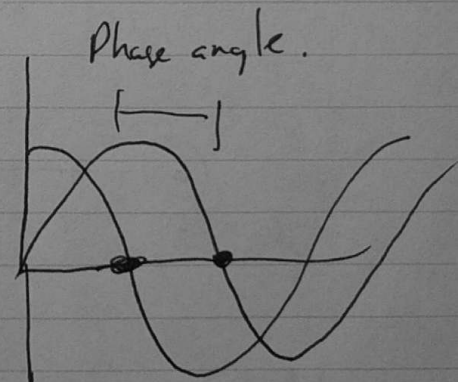
$$y(x) = A |\sin(\omega x + \theta_0)| e^{-kx}$$

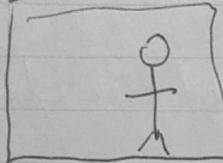
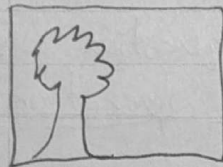
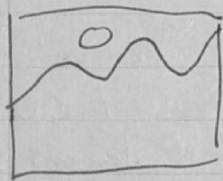
$A$  = initial amplitude

$\omega$  = angular frequency

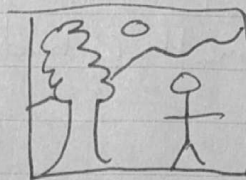
$\theta_0$  = phase angle

$k$  = damping constant.





Cell shading



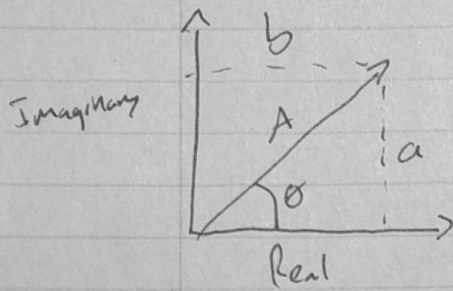
## Classic Techniques

1. Squash and Stretch
2. Timing
3. Anticipation
4. Staging
5. Follow through and overlapping action
6. Straight Ahead and Pose to Pose Action
7. slow in, slow out
8. Arcs
9. Exaggeration
10. Secondary action
11. Appeal.

All of these are used to convey personality.



# Quaternions



- Iso topic
- inverse problems easy
- ai is easier
- math is harder

- just know pros & cons of Euler vs Quaternions

★  
- no question about  
Quaternion operation on Exam

## Demo sign up

- |                   |                       |                 |
|-------------------|-----------------------|-----------------|
| - Tuesday morning | - Wednesday 8pm       | on of fire door |
| Thursday          | Morning 9-12          | 15 min slots    |
| - Thursday        | Afternoon 2:30 - 5:30 |                 |

July 19<sup>th</sup>  
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# CS488 Animation

## Goal Directed Systems

Kinematics and Dynamics

### Forward kinematics (eg. Human motion)

- specify the animation by given motion parameters (eg, position, velocity, acceleration)

### Inverse kinematics

Dynamics: Forces (physically - based modeling)

Examples: electromagnetic, gravitational, friction, Newton's laws, Motion for gravitational or friction processes. Maxwell's law for electromagnetic forces Euler or Navier Stokes for fluids

→ Application of Numerical Methods → Initial values  
→ Boundary Conditions.

Hilroy