Discontinuous Functions - Motivation

Fielding a dynamic system. E.g. operator pushes a button, defining t=0.
This triggers a pre-planned sequence of commands that are sent to the
system.



- Designing a dynamic system. You may be responsible for designing the input function to meet motion requirements.
 - Represent the input mathematically
 - Calculate or simulate the system response, iterate as needed

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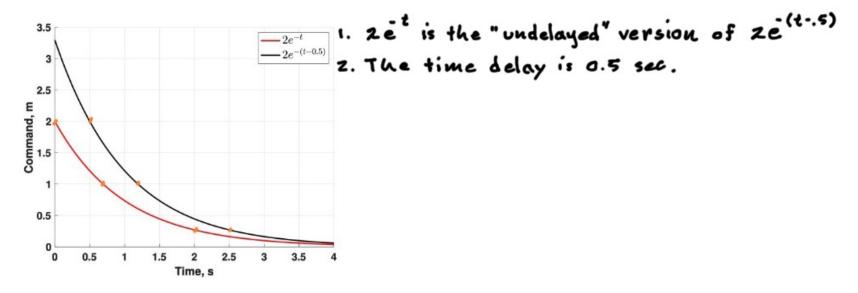
Skills

- Identify time delayed functions
- 2. Given a discontinuous function equation, sketch it.
- 3. Given a discontinuous function **sketch**, create its equation
- 4. Write and use the definition of the **impulse**, **step** and **ramp** functions
- Given a MATLAB dynamic system model create its step and impulse responses

Terminology

Unit, Unity: Another way of saying "one," e.g. unit step, unity gain.

Time Delayed Functions



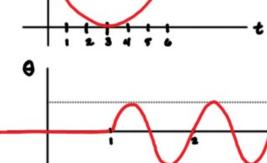
Identify Time-Delayed Functions - Examples

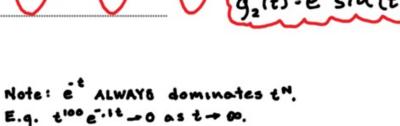
$$y = (t-3)^2$$

$$\theta = \begin{cases} 0 & t < 1 \end{cases}$$

 $\theta = \begin{cases} 0 & t < 1 \\ \sin\left(2\pi(t-1)\right) & t \ge 1 \end{cases}$

 $r = \begin{cases} 0 & t < 4 \\ 3te^{-(t-4)} & t \geq 4 \end{cases}$





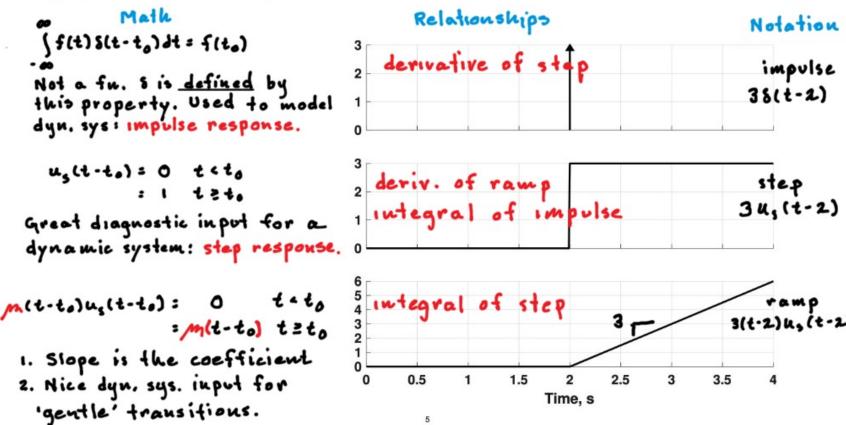
All occurrence of t

 $g_{i}(t) = e^{-(t-4)} \sin(t-4)$ $vs. e^{-t} \sin(t-4)$

The undelayed cousin' ... replace t-T with t.

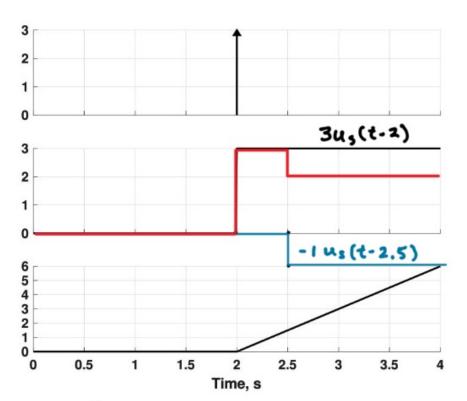
appear as t-T.

Impulse, Step and Ramp Functions



Impulse, Step and Ramp Functions

create exotic fus by adding steps & ramps.

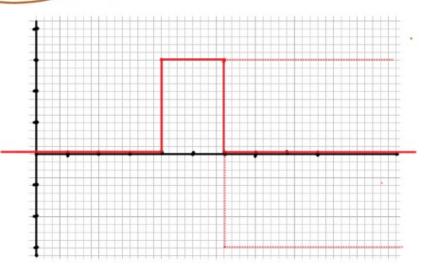


MATLAB and Simulink

- The step and impulse commands create step and impulse responses of a dynamic system object
- The heaviside function (named for Oliver Heaviside, 1850-1925, UK) can be used for symbolic operations, or to create an array of numeric step data. By default, heaviside(0) = 0.5. It really doesn't matter what value you assign it at t=0.
- The dirac function (named for Paul Dirac, 1902-1984, UK) is mostly used for symbolic work.
- The Simulink Library Browser, Sources folder has both step and ramp blocks. Clever addition and multiplication of these, with other blocks, can make exotic inputs.

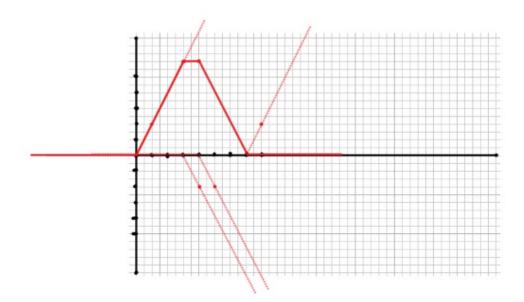
Sketch the function below and model it in Simulink.

$$g(t) = 3u_s(t-4) - 3u_s(t-6)$$

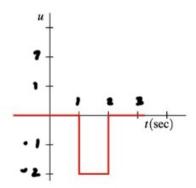


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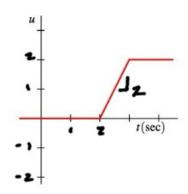
Sketch the function: $y(t) = 2tu_s(t) - 2(t-3)u_s(t-3) - 2(t-4)u_s(t-4) + 2(t-7)u_s(t-7)$



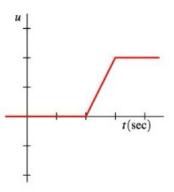
Write an expression for the function shown at right.



Write an expression for the function shown at right and model it in Simulink.



Write an expression for the function shown at right and model it in Simulink.



Given a MATLAB dynamic system, create its impulse and step responses. For now, you don't need to know how to create the MATLAB dynamic system - assume it's given.

```
>> my sys : tf(7,[1 1 f]);
>> figure(1); impulse(my sys); grid
>> figure(2); step(my sys); grid
```

Summary

- Recognize time-delayed functions, and when possible, extract out the "undelayed" function
- Use the definition of step and ramp functions to create and/or sketch complicated discontinuous functions
- Model discontinuous functions in Simulink
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