# Title

Antoine Gréa

# **Abstract**

# **Table of Content**

Α	ckno	wledg	ements	7
ln	trod	uction		8
	0.1	Thesis	Context	8
	0.2	Motiva	ations	8
		0.2.1	Observation	8
		0.2.2	Abstraction	8
		0.2.3	Cognition	8
	0.3	Issues		8
	0.4	Contri	butions	8
	0.5	Plan .		8
1	Kna	wlede	ge representation	9
_			•	10
	1.1			10
		1.1.1		10
			<u> </u>	10
			•	10
			e	13
				13 14
				14 14
			_	14 15
		117		
	1 2			16 17
	1.2			
		1.2.1		17
				18
		4 2 2	' '	18
			<b>,</b>	20
		1.2.3	- J	21
				22
				23
			· · · · · · · · · · · · · · · · · · ·	23
		1.2.4	<b>F</b>	24
			1.2.4.1 Naming and Scope	
				25
		1.2.5		25
			•	25
			0 1 1	27
		1.2.6	Extended Inference Mechanisms	27
			1.2.6.1 Type inference	28
			1.2.6.2 Instanciation	วฉ

1.3.2 Advanced Inference 1.3.3 Querries 31 2 General Planning Framework 2.1 Existing Languages and Frameworks 2.2 Taxonomy 3.2.2.1 Action type 3.2.2.2 Plan type 3.2.2.3 Problem type 3.2.3 Color 3. Online and Flexible Planning Algorithms 3.1 Existing Algorithms 3.2 Lollipop 3.2.1 Operator Graph 3.2.2 Negative Refinements 3.2.3 Usefullness Heuristic 3.2.4 Algorithm 3.2.5 Theoretical and Empirical Results 3.3 HEART 3.3.1 Domain Compilation 3.3.2.2 Abstraction in POP 3.3.3.3 Planning in cycle 3.3.4 Properties of Abstract Planning 3.4.4 Heuristics using Semantics 3.4.4 Macro-Action learning 3.5.5 Recognition 3.5.1 Existing approcahes 3.5.1 Existing approcahes 3.5.2 Rico 3.5.2.1 Probabilities and approximations 3.5.2 Rico 3.5.2.1 Probabilities and approximations 3.5.3 Apendix		1.3	Perpectives	 28
1.3.3 Querries			1.3.1 Literal definition using Peano's axioms	 29
2 General Planning Framework       3         2.1 Existing Languages and Frameworks       3         2.2 Taxonomy       3         2.2.1 Action type       3         2.2.2 Plan type       3         2.2.3 Problem type       3         2.3 Color       3         3 Online and Flexible Planning Algorithms       3         3.1 Existing Algorithms       3         3.2 Lollipop       3         3.2.1 Operator Graph       3         3.2.2 Negative Refinements       3         3.2.3 Usefullness Heuristic       3         3.2.4 Algorithm       3         3.2.5 Theoretical and Empirical Results       3         3.3 HEART       3         3.3.1 Domain Compilation       3         3.3.2 Abstraction in POP       3         3.3.3 Planning in cycle       3         3.3.4 Properties of Abstract Planning       3         3.4.2 Macro-Action learning       3         3.4.2 Macro-Action learning       3         3.5.1 Existing approcahes       3         3.5.2 Rico       3         3.5.1 Existing approcahes       3         3.5.2.1 Probabilities and approximations       3         4 Conclusion       3 <th></th> <th></th> <th>1.3.2 Advanced Inference</th> <th> 30</th>			1.3.2 Advanced Inference	 30
2.1 Existing Languages and Frameworks       3         2.2 Taxonomy       3         2.2.1 Action type       3         2.2.2 Plan type       3         2.2.3 Problem type       3         2.3 Color       3         3 Online and Flexible Planning Algorithms       3         3.1 Existing Algorithms       3         3.2 Lollipop       3         3.2.1 Operator Graph       3         3.2.2 Negative Refinements       3         3.2.3 Usefullness Heuristic       3         3.2.4 Algorithm       3         3.2.5 Theoretical and Empirical Results       3         3.3 HEART       3         3.3.1 Domain Compilation       3         3.3.2 Abstraction in POP       3         3.3.3 Planning in cycle       3         3.3.4 Properties of Abstract Planning       3         3.4.1 Heuristics using Semantics       3         3.4.2 Macro-Action learning       3         3.5.1 Existing approcahes       3         3.5.2 Rico       3         3.5.2.1 Probabilities and approximations       3         4 Conclusion       3			1.3.3 Querries	 30
2.2.1 Action type       3         2.2.2 Plan type       3         2.2.3 Problem type       3         2.3 Color       3         3 Online and Flexible Planning Algorithms       3         3.1 Existing Algorithms       3         3.2 Lollipop       3         3.2.1 Operator Graph       3         3.2.2 Negative Refinements       3         3.2.3 Usefullness Heuristic       3         3.2.4 Algorithm       3         3.2.5 Theoretical and Empirical Results       3         3.3 HEART       3         3.3.1 Domain Compilation       3         3.3.2 Abstraction in POP       3         3.3.3 Planning in cycle       3         3.3.4 Properties of Abstract Planning       3         3.3.5 Computational Profile       3         3.4.1 Heuristics using Semantics       3         3.4.2 Macro-Action learning       3         3.5.1 Existing approcahes       3         3.5.2 Rico       3         3.5.2.1 Probabilities and approximations       3         4 Conclusion       3	2	Ger	neral Planning Framework	31
2.2.1 Action type       3         2.2.2 Plan type       3         2.2.3 Problem type       3         2.3 Color       3         3 Online and Flexible Planning Algorithms       3         3.1 Existing Algorithms       3         3.2 Lollipop       3         3.2.1 Operator Graph       3         3.2.2 Negative Refinements       3         3.2.3 Usefullness Heuristic       3         3.2.4 Algorithm       3         3.2.5 Theoretical and Empirical Results       3         3.3 HEART       3         3.3.1 Domain Compilation       3         3.3.2 Abstraction in POP       3         3.3.3 Planning in cycle       3         3.3.4 Properties of Abstract Planning       3         3.4.1 Heuristics using Semantics       3         3.4.2 Macro-Action learning       3         3.5.1 Existing approcahes       3         3.5.2 Rico       3         3.5.2.1 Probabilities and approximations       3         4 Conclusion       3		2.1	Existing Languages and Frameworks	 31
2.2.2 Plan type       3         2.2.3 Problem type       3         2.3 Color       3         3 Online and Flexible Planning Algorithms       3         3.1 Existing Algorithms       3         3.2 Lollipop       3         3.2.1 Operator Graph       3         3.2.2 Negative Refinements       3         3.2.3 Usefullness Heuristic       3         3.2.4 Algorithm       3         3.2.5 Theoretical and Empirical Results       3         3.3 HEART       3         3.3.1 Domain Compilation       3         3.3.2 Abstraction in POP       3         3.3.3 Planning in cycle       3         3.3.4 Properties of Abstract Planning       3         3.4.1 Heuristics using Semantics       3         3.4.2 Macro-Action learning       3         3.5.1 Existing approcahes       3         3.5.2 Rico       3         3.5.2.1 Probabilities and approximations       3         4 Conclusion       3		2.2	Taxonomy	 31
2.2.3 Problem type       3         2.3 Color       3         3 Online and Flexible Planning Algorithms       3         3.1 Existing Algorithms       3         3.2 Lollipop       3         3.2.1 Operator Graph       3         3.2.2 Negative Refinements       3         3.2.3 Usefullness Heuristic       3         3.2.4 Algorithm       3         3.2.5 Theoretical and Empirical Results       3         3.3 HEART       3         3.3.1 Domain Compilation       3         3.3.2 Abstraction in POP       3         3.3.3 Planning in cycle       3         3.3.4 Properties of Abstract Planning       3         3.4.1 Heuristics using Semantics       3         3.4.2 Macro-Action learning       3         3.5.1 Existing approcahes       3         3.5.2 Rico       3         3.5.2.1 Probabilities and approximations       3         4 Conclusion       3         Apendix       3			2.2.1 Action type	 31
2.3 Color       3         3 Online and Flexible Planning Algorithms       3         3.1 Existing Algorithms       3         3.2 Lollipop       3         3.2.1 Operator Graph       3         3.2.2 Negative Refinements       3         3.2.3 Usefullness Heuristic       3         3.2.4 Algorithm       3         3.2.5 Theoretical and Empirical Results       3         3.3 HEART       3         3.3.1 Domain Compilation       3         3.3.2 Abstraction in POP       3         3.3.3 Planning in cycle       3         3.3.4 Properties of Abstract Planning       3         3.4.2 Heuristics using Semantics       3         3.4.1 Heuristics using Semantics       3         3.4.2 Macro-Action learning       3         3.5.1 Existing approcahes       3         3.5.2 Rico       3         3.5.2.1 Probabilities and approximations       3         4 Conclusion       3         Apendix       3			2.2.2 Plan type	 31
3 Online and Flexible Planning Algorithms       3:         3.1 Existing Algorithms       3:         3.2 Lollipop       3:         3.2.1 Operator Graph       3:         3.2.2 Negative Refinements       3:         3.2.3 Usefullness Heuristic       3:         3.2.4 Algorithm       3:         3.2.5 Theoretical and Empirical Results       3:         3.3 HEART       3:         3.3.1 Domain Compilation       3:         3.3.2 Abstraction in POP       3:         3.3.3 Planning in cycle       3:         3.3.4 Properties of Abstract Planning       3:         3.4.1 Heuristics using Semantics       3:         3.4.2 Macro-Action learning       3:         3.5.1 Existing approcahes       3:         3.5.2 Rico       3:         3.5.2.1 Probabilities and approximations       3:         4 Conclusion       3:         Apendix       3:			2.2.3 Problem type	 31
3.1 Existing Algorithms       3         3.2 Lollipop       3         3.2.1 Operator Graph       3         3.2.2 Negative Refinements       3         3.2.3 Usefullness Heuristic       3         3.2.4 Algorithm       3         3.2.5 Theoretical and Empirical Results       3         3.3 HEART       3         3.3.1 Domain Compilation       3         3.3.2 Abstraction in POP       3         3.3.3 Planning in cycle       3         3.3.4 Properties of Abstract Planning       3         3.4.1 Heuristics using Semantics       3         3.4.2 Macro-Action learning       3         3.5 Recognition       3         3.5.1 Existing approcahes       3         3.5.2 Rico       3         3.5.2.1 Probabilities and approximations       3         4 Conclusion       3         Apendix       3		2.3	Color	 31
3.2 Lollipop       3.         3.2.1 Operator Graph       3.         3.2.2 Negative Refinements       3.         3.2.3 Usefullness Heuristic       3.         3.2.4 Algorithm       3.         3.2.5 Theoretical and Empirical Results       3.         3.3 HEART       3.         3.3.1 Domain Compilation       3.         3.3.2 Abstraction in POP       3.         3.3.3 Planning in cycle       3.         3.3.4 Properties of Abstract Planning       3.         3.4.1 Heuristics of Abstract Planning       3.         3.4.2 Macro-Action learning       3.         3.4.2 Macro-Action learning       3.         3.5.1 Existing approcahes       3.         3.5.2 Rico       3.         3.5.2.1 Probabilities and approximations       3.         4 Conclusion       3.         Apendix       3.	3	Onl	line and Flexible Planning Algorithms	32
3.2.1 Operator Graph       3.         3.2.2 Negative Refinements       3.         3.2.3 Usefullness Heuristic       3.         3.2.4 Algorithm       3.         3.2.5 Theoretical and Empirical Results       3.         3.3 HEART       3.         3.3.1 Domain Compilation       3.         3.3.2 Abstraction in POP       3.         3.3.3 Planning in cycle       3.         3.3.4 Properties of Abstract Planning       3.         3.3.5 Computational Profile       3.         3.4.1 Heuristics using Semantics       3.         3.4.2 Macro-Action learning       3.         3.5 Recognition       3.         3.5.1 Existing approcahes       3.         3.5.2 Rico       3.         3.5.2.1 Probabilities and approximations       3.         4 Conclusion       3.         Apendix       3.		3.1	Existing Algorithms	 32
3.2.2 Negative Refinements       3         3.2.3 Usefullness Heuristic       3         3.2.4 Algorithm       3         3.2.5 Theoretical and Empirical Results       3         3.3 HEART       3         3.3.1 Domain Compilation       3         3.3.2 Abstraction in POP       3         3.3.3 Planning in cycle       3         3.3.4 Properties of Abstract Planning       3         3.3.5 Computational Profile       3         3.4 Planning Improvements       3         3.4.1 Heuristics using Semantics       3         3.4.2 Macro-Action learning       3         3.5 Recognition       3         3.5.1 Existing approcahes       3         3.5.2 Rico       3         3.5.2.1 Probabilities and approximations       3         4 Conclusion       3         Apendix       3		3.2	Lollipop	 32
3.2.3       Usefullness Heuristic       3.         3.2.4       Algorithm       3.         3.2.5       Theoretical and Empirical Results       3.         3.3       HEART       3.         3.3.1       Domain Compilation       3.         3.3.2       Abstraction in POP       3.         3.3.3       Planning in cycle       3.         3.3.4       Properties of Abstract Planning       3.         3.3.5       Computational Profile       3.         3.4       Planning Improvements       3.         3.4.1       Heuristics using Semantics       3.         3.4.2       Macro-Action learning       3.         3.5       Recognition       3.         3.5.1       Existing approcahes       3.         3.5.2.1       Probabilities and approximations       3.         4       Conclusion       3.         Apendix       3.			3.2.1 Operator Graph	 32
3.2.4 Algorithm       3         3.2.5 Theoretical and Empirical Results       3         3.3 HEART       3         3.3.1 Domain Compilation       3         3.3.2 Abstraction in POP       3         3.3.3 Planning in cycle       3         3.3.4 Properties of Abstract Planning       3         3.4.1 Planning Improvements       3         3.4.1 Heuristics using Semantics       3         3.4.2 Macro-Action learning       3         3.5.1 Existing approcahes       3         3.5.2 Rico       3         3.5.2.1 Probabilities and approximations       3         4 Conclusion       3         Apendix       3			3.2.2 Negative Refinements	 32
3.2.5 Theoretical and Empirical Results       3         3.3 HEART       3         3.3.1 Domain Compilation       3         3.3.2 Abstraction in POP       3         3.3.3 Planning in cycle       3         3.3.4 Properties of Abstract Planning       3         3.3.5 Computational Profile       3         3.4 Planning Improvements       3         3.4.1 Heuristics using Semantics       3         3.4.2 Macro-Action learning       3         3.5 Recognition       3         3.5.1 Existing approcahes       3         3.5.2 Rico       3         3.5.2.1 Probabilities and approximations       3         4 Conclusion       3         Apendix       3			3.2.3 Usefullness Heuristic	 32
3.3 HEART       3.3.1 Domain Compilation       3.3.2 Abstraction in POP       3.3.3 Planning in cycle       3.3.3 Planning in cycle       3.3.4 Properties of Abstract Planning       3.3.5 Computational Profile       3.3.5 Computational Profile       3.3.4 Planning Improvements       3.3.4.1 Heuristics using Semantics       3.3.4.1 Heuristics using Semantics       3.3.5 Recognition       3.3.5 Recognition       3.3.5 Recognition       3.3.5.1 Existing approcahes       3.3.5.2 Rico       3.3.5.2 Rico       3.3.5.2.1 Probabilities and approximations       3.3.5.2 Rico       3.3.5.2.1 Probabilities and approximations       3.3.5.2 Rico       3.3.5 Rico </th <th></th> <th></th> <th>3.2.4 Algorithm</th> <th> 32</th>			3.2.4 Algorithm	 32
3.3.1 Domain Compilation       3         3.3.2 Abstraction in POP       3         3.3.3 Planning in cycle       3         3.3.4 Properties of Abstract Planning       3         3.3.5 Computational Profile       3         3.4 Planning Improvements       3         3.4.1 Heuristics using Semantics       3         3.4.2 Macro-Action learning       3         3.5 Recognition       3         3.5.1 Existing approcahes       3         3.5.2 Rico       3         3.5.2.1 Probabilities and approximations       3         4 Conclusion       3         Apendix       3			3.2.5 Theoretical and Empirical Results	 32
3.3.2 Abstraction in POP       3         3.3.3 Planning in cycle       3         3.3.4 Properties of Abstract Planning       3         3.3.5 Computational Profile       3         3.4 Planning Improvements       3         3.4.1 Heuristics using Semantics       3         3.4.2 Macro-Action learning       3         3.5 Recognition       3         3.5.1 Existing approcahes       3         3.5.2 Rico       3         3.5.2.1 Probabilities and approximations       3         4 Conclusion       3         Apendix       3		3.3	HEART	 32
3.3.3 Planning in cycle       3         3.3.4 Properties of Abstract Planning       3         3.3.5 Computational Profile       3         3.4 Planning Improvements       3         3.4.1 Heuristics using Semantics       3         3.4.2 Macro-Action learning       3         3.5 Recognition       3         3.5.1 Existing approcahes       3         3.5.2 Rico       3         3.5.2.1 Probabilities and approximations       3         4 Conclusion       3         Apendix       3			3.3.1 Domain Compilation	 32
3.3.4 Properties of Abstract Planning       3.         3.3.5 Computational Profile       3.         3.4 Planning Improvements       3.         3.4.1 Heuristics using Semantics       3.         3.4.2 Macro-Action learning       3.         3.5 Recognition       3.         3.5.1 Existing approcahes       3.         3.5.2 Rico       3.         3.5.2.1 Probabilities and approximations       3.         4 Conclusion       3.         Apendix       3.			3.3.2 Abstraction in POP	 32
3.3.5 Computational Profile  3.4 Planning Improvements  3.4.1 Heuristics using Semantics  3.4.2 Macro-Action learning  3.5 Recognition  3.5.1 Existing approcahes  3.5.2 Rico  3.5.2.1 Probabilities and approximations  4 Conclusion  3.5.2 Apendix			3.3.3 Planning in cycle	 32
3.4 Planning Improvements       3.         3.4.1 Heuristics using Semantics       3.         3.4.2 Macro-Action learning       3.         3.5 Recognition       3.         3.5.1 Existing approcahes       3.         3.5.2 Rico       3.         3.5.2.1 Probabilities and approximations       3.         4 Conclusion       3.         Apendix       3.			3.3.4 Properties of Abstract Planning	 32
3.4.1 Heuristics using Semantics       3.3.3.4.2 Macro-Action learning       3.5.3.5 Recognition       3.5.5.1 Existing approcahes       3.5.2 Rico       3.5.2.1 Probabilities and approximations       3.5.2.1 Probabilities approximations       3.5.2.1 Probabilitie			3.3.5 Computational Profile	 32
3.4.2 Macro-Action learning       3.5.2 Recognition         3.5.1 Existing approcahes       3.5.2 Rico         3.5.2.1 Probabilities and approximations       3.5.2.1 Probabilities and approximations         4 Conclusion       3.5.2.1 Appendix		3.4	Planning Improvements	 32
3.5       Recognition       3.         3.5.1       Existing approcahes       3.         3.5.2       Rico       3.         3.5.2.1       Probabilities and approximations       3.         4       Conclusion       3.         Apendix       3.			3.4.1 Heuristics using Semantics	 32
3.5.1 Existing approcahes			3.4.2 Macro-Action learning	 32
3.5.2 Rico		3.5	Recognition	 32
3.5.2.1 Probabilities and approximations			3.5.1 Existing approcahes	 32
4 Conclusion 34 Apendix 35			3.5.2 Rico	 32
Apendix 3			3.5.2.1 Probabilities and approximations	 32
•	4	Cor	nclusion	34
	Αı	oend	dix	35
	•			36

# Acknowledgements

## Introduction

- 0.1 Thesis Context
- 0.2 Motivations
- 0.2.1 Observation
- 0.2.2 Abstraction
- 0.2.3 Cognition
- 0.3 Issues
- 0.4 Contributions
- 0.5 Plan

## 1 Knowledge representation

Knowledge representation is at the intersection of maths, logic, language and computer sciences. Its research begins in the end of the 19<sup>th</sup> century, with Cantor inventing set theory (Cantor 1874). Then after a crisis in the begining of the 20<sup>th</sup> century with Russel's paradox and Gödel's incompletude theorem, revised versions of the set theory become one of the fundations of mathematics. The most accepted version is the Zermelo–Fraenkel axiomatic set theory with the axiom of Choice (ZFC) (Fraenkel *et al.* 1973, vol. 67; Ciesielski 1997). This effort lead to a formalization of mathematics itself, at least to a certain degree.

Knowledge description systems rely on a syntax to interoperate systems and users to one another. The base of such languages comes from the formalization of automated grammars by Chomsky (1956). It mostly consist in a set of hierarchical rules aiming to deconstruct an input string into a sequence of terminal symbols. This deconstruction is called parsing and is a common operation in computer science. More tools for the formalization of computer language emerged soon after thanks to Backus (1959) while working on a programming language at IBM. This is how the Backus–Naur Form (BNF) meta-language was created ontop of Chomsky's formalization.

A similar process happened in the 1970's, when logic based knowledge representation gained popularity among computer scientists (Baader 2003). Systems at the time explored notions such as rules and networks to try and organize knowledge into a rigourous structure. At the same time other systems were built arround First Order Logic (FOL). Then, around the 1990's, the research began to merge in search of common semantics in what led to the developpement of Description Logics (DL). This domain is expressing knowledge as a hierarchy of classes containing individuals.

From there and with the advent of the world wide web, engineers were on the lookout for standardization and interoperability of computer systems. One such standardization took the name of "semantic web" and aimed to created a widespread network of connected services sharing knowledge between one another in a common language. At the begining of the 21<sup>st</sup> century, several languages were created, all based around World Wide Web Consortium (W3C) specifications called Resource Description Framework (RDF) (Klyne and Carroll 2004). This language is based around the notion of statements as triples. Each can express a unit of knowledge. All the underlying theoritical work of DL continued with it and created more expressive derivatives. One such derivative is the family of languages called Web Ontology Language (OWL) (Horrocks *et al.* 2003). Ontologies and knowledge graphs are more recent names for the representation and definition of categories (DL classes), properties and relation between concepts, data and entities.

All these tools are the base for all modern knowledge representations. In the rest of this chapter, we discuss the fundamentals of each of the aspects of knowledge description, then we propose a knowledge description framework that is able to adapt to its usage.

## 1.1 Fundamentals

First and foremost, we present the list of notations in this document. While trying to stick to traditional notations, we also aim for an unambiguious notation across several domains while remaining concise and precise. In table 1.1 we present the list of all symbols and relations. When possible we use the classical mathematical notations and we prefer lower case greek letters for relations. Table 1.2 lists all important sets that we represent with uppercase letters.

## 1.1.1 Fundation of maths and logic systems

In order to understand knowledge representation, some mathematical and logical tools need to be presented.

## 1.1.1.1 Fisrt Order Logic

The first mathematical notion we define is logic. More precisely First Order Logic (FOL) in the context of DL. FOL is based on boolean logic with the two values  $\top$  *true* and  $\bot$  *false* along with the classical boolean operators  $\neg$  *not*,  $\land$  *and* and  $\lor$  *or*. These are defined the following way:

```
• \neg T = \bot
• a \land b \models (a = b = T)
```

•  $\neg (a \lor b) \models (a = b = \bot)$ 

With  $a \models b$  being the logical implication also called entailement. To that, FOL adds a handfull of quantifiers:

- The universal quantifier ∀ meaning "for all".
- The existential quantifier ∃ meaning "it exists".
- The uniqueness quantifier !\(\frac{1}{2}\) meaning "it exists a unique".
- The solution quantifier § meaning "those" (Hehner 2012).

The last two quantifiers are optional in FOL but will be useful later on. It is interesting to note that most quantified expression can be express using the set builder notation discussed in the following section.

## 1.1.1.2 Set theory

Since we need to represent knowledge, we will handle more complex data than simple booleans. At the begining of his funding work on set theory, Cantor wrote:

A set is a gathering together into a whole of definite, distinct objects of our perception or of our thought—which are called elements of the set. – George Cantor (1895)

For Cantor, a set is a collection of concepts and percepts. In the rest of the document, we then define a set the following way:

**Definition 1** (Set). A collection of *distinct* objects, considered as an object in its own right. We define a set one of two way (always using braces):

- In extension by listing all the elements in the set:  $\{1, 2, 4\}$
- In intension by specifying the rule that all elements follow:  $\{n:n\in\mathbb{N}\land(n\mod 2=0)\}$

The member relation is noted  $e \in \mathcal{S}$  to indicate that e is an element of  $\mathcal{S}$ . We note  $\mathcal{S} \subset \mathcal{T} \models ((e \in \mathcal{S} \models e \in \mathcal{T}) \land \mathcal{S} \neq \mathcal{T})$ , that a set  $\mathcal{S}$  is a proper subset of a more general set  $\mathcal{T}$ .

Table 1.1: List of symbols and relations. The symbol  $\pm$  shows when the notation has signed variants.

Symbol	Description
var : exp	The colon is a separator to be read as "such that".
[exp]	Iverson's brackets: $[false] = 0 \land [true] = 1$ .
$\{e: exp(e)\}$	Set builder notation, all $e$ such that $exp(e)$ is true.
∀,∃,!,§	Universal, existential, uniqueness and solution quantifiers.
$\langle e_1, e_2, e_n \rangle$	n-Tuple of various elements.
$e_s \xrightarrow{e_p} e_o$	Link or edge from $e_s$ to $e_o$ having $e_p$ .
$l \downarrow a$	Link $l$ partially supports step $a$ .
$\pi \Downarrow a$	Plan $\pi$ fully supports $a$ .
Ø	Empty set, also notted {}.
$\subset$ , $\cup$ , $\cap$ , $\setminus$	Set inclusion, union, intersection and difference.
$e \in E$	Element $e$ belongs in set $E$ also called choice operator.
=,≠	Equal and not equal.
$\neg, \land, \lor$	Negation (not), conjonction (and), disjonction (logical or).
E	Cardinal of set $E$ .
	Subsumption relation used for types.
<	Precedance relation used for order.
Τ,⊥	Top and bottom symbols used as true and false respectively.
F	Entails, used for logical implication.
$f \circ g$	Function composition.
$\otimes$	Flaws in a partial plan. Several variants:
$\otimes_{\ddagger}$	<ul> <li>unsupported subgoal.</li> </ul>
$\otimes_{\dagger}$	<ul> <li>causal threat to an existing causal link.</li> </ul>
⊗♂	• cycle in the plan.
$\otimes_*$	<ul> <li>decomposition of a compound action.</li> </ul>
$\otimes_{\leadsto}$	<ul> <li>alternative to an existing action.</li> </ul>
$\otimes_{\odot}$	• orphan action in the plan.
$\oplus$ , $\ominus$	Positive and negative resolvers.
¢	Cost of an action.
i, g	Initial and Goal step.
$\mathbb{P}(E)$	Powerset, set of all subsets of $E$ .
$\mathcal{P}(X)$	Probability of event X.
pre, eff	Preconditions and effects of an action.
δ	Duration of an action.
$\mu^{\pm}(e)$	Signed meta-relation. $\mu^+$ abstracts and $\mu^-$ reifies.
(.)	$\mu$ alone gives the abstraction level.
ν(e)	Name of entity <i>e</i> .
$\pi$	Plan or method of compound action.
$\rho(e)$	Parameters of entity e.
$\tau(e)$	Type of entity e.
$\phi^{\pm}(e)$	Signed incidence (edge) and adjacence (vertice) function for graphs.
	$\phi^-$ gives the anterior (subject), $\phi^+$ the posterior (object) and $\phi^0$ gives the property of statement or cause of a causal link.
v*(a)	φ alone gives a triple corresponding to the edge.  Transitive cover of graph g
$\chi^*(g)$	Transitive cover of graph $g$ .

Table 1.2: List of important named sets.

Name	Description
$\overline{A}$	Actions.
C	Causal links.
D	Domain of knowledge.
E	Entities.
$\mathcal{E}$	Edges of a graph.
F	Fluents.
L	Literals.
0	Observations.
P	Properties.
Q	Quantifiers.
$\boldsymbol{S}$	Statements.
T	Types.
V	Vertex of a graph.
П	Plans or method of compound action.

We also define the union, intersection and difference as following:

```
    S∪T = {e : e ∈ S ∨ e ∈ T}
    S∩T = {e : e ∈ S ∧ e ∈ T}
    S\T = {e : e ∈ S ∧ e ∉ T}
```

The most common axiomatic set theory is ZFC. In that definition of sets there are a few notions that comes from its axioms. By being able to distinguish elements in the set from one another we assert that elements have an identity and we can derive equality from there:

```
Axiom (Extensionality). \forall \mathcal{S} \forall \mathcal{T} : \forall e (e \in \mathcal{S} \Leftrightarrow e \in \mathcal{T}) \models \mathcal{S} = \mathcal{T}
```

Another axiom of ZFC that is crucial in avoiding Russel's paradox ( $S \in S$ ) is the following: **Axiom** (Fondation).  $\forall S : (S \neq \emptyset \models \exists \mathcal{F} \in S, (\mathcal{F} \cap S = \emptyset))$ 

This axiom uses the empty set  $\emptyset$  (also noted  $\{\}$ ) as the set with no elements. Since two sets are equals if and only if they have precisely the same elements, the empty set is unique.

The definition by intention uses  $set\ builder\ notation\ to\ define\ a\ set.$  It is composed of an expression and a predicate p that will make any element e in a domain  $set\ D$  satisfying it part of the resulting  $set\ \mathcal{S}$ , or as formulated in ZFC:

```
Axiom (Specification). \forall p \forall D \exists S : (\forall e \in S : (e \in D \land p(e)))
```

The last axiom of ZFC we use is to define the power set  $\mathbb{P}(\mathcal{S})$  as the set containing all subsets of a set  $\mathcal{S}$ : Axiom (Power set).  $\mathbb{P}(\mathcal{S}) = \{\mathcal{T} : \mathcal{T} \subseteq \mathcal{S}\}$ 

With the symbol  $\mathcal{S} \subseteq \mathcal{T} \models (\mathcal{S} \subset \mathcal{T} \lor \mathcal{S} = \mathcal{T})$ . These symbols have an interesting property as they are often used as a partial order over sets.

## 1.1.1.3 Graphs

Next in line, we need to define a few notion of graph theory.

**Definition 2** (Graph). A graph is a mathematical structure  $g=(V,\mathcal{E})$  consisting of vertices V (also called nodes) and edges  $\mathcal{E}$  (arcs) that links two vertices together. Each edge is basically a pair of vertices ordered or not depending if the the graph is directed or not.

From that definition, some other relations are needed to express most properties of graphs. In the following, the signed symbols only applies to directed graphs.

We provide graphs with an adjacence function  $\phi$  over any vertex  $v \in V$  such that:

```
• \phi(v) = \{e \in \mathcal{E} : v \in e\}

• \phi^+(v) = \{\langle v, v' \rangle \in \mathcal{E} : v' \in V\}

• \phi^-(v) = \{\langle v', v \rangle \in \mathcal{E} : v' \in V\}
```

This relation gives the set of incoming or outgoing edges from any vertex. In non directed graphs, the relation gives edges adjacent to the vertex. Using types, it is possible to reuse the same symbol to define an incidence function over any edges  $e = \langle v, v' \rangle \in \mathcal{E}$  such that:

```
    φ(e) = ⟨v, v'⟩
    φ<sup>-</sup>(e) = v
    φ<sup>+</sup>(e) = v'
```

Most of the intrisic information of a graph is conatined within its structure. Exploring its properties require to study the "shape" of a graph and to find relationships between vertices. That is why graphs properties are easier to explain using the *transitive cover*  $\chi^*$  of any graph  $g = (V, \mathcal{E})$  defined as follow:

```
 \begin{array}{l} \bullet \ \chi(g) = (V,\mathcal{E}') : \mathcal{E}' = \mathcal{E} \cup \{\langle v_1,v_3 \rangle : \{\langle v_1,v_2 \rangle, \langle v_2,v_3 \rangle\} \subset \mathcal{E}\} \\ \bullet \ \chi^2 = \chi \circ \chi \\ \bullet \ \chi^n = \bigcirc_{i=0}^n \chi \\ \bullet \ \chi^* = \bigcirc^\infty \chi \\ \end{array}
```

This transitive cover will create another graph in which two vertices are connected through an edge if and only if it exists a path between them in the original graph g.

**Definition 3** (Path). We say that vertices  $v_1$  and  $v_2$  are *connected* if it exists a path from one to the other. Said otherwise, there is a path from  $v_1$  to  $v_2$  if and only if  $\langle v_1, v_2 \rangle \in \mathcal{E}_{\chi^*(g)}$ .

Similarly we define *cycles* as the existence of a path from a given vertex to itself. Some graphs can be strictly acyclical, enforcing the absence of cycles.

TODO: Needs diagrams

## 1.1.1.4 Hypergraphs

A generalization of graphs are **hypergraphs** where the edges are allowed to connect to more than two vertices. An hypergraph is n-uniform if the edges are restricted to connect to only n vertices together. In that regard, classical graphs are 2-uniform hypergraphs.

TODO: Diagram of hypergraph

Hypergraphs have a special case where  $\mathcal{E} \subset V$ . This means that edges are allowed to connect to other edges. Informations about these kind of structures for knowledge are hard to come by and rely mostly on a form of "folk wisdom" within the mathematics community where knowledge is rarely published and mostly transmitted orally during lessons. One of the closest information available is this forum post (Kovitz 2018) that associated this type of graph to port graphs (Silberschatz 1981). Additional information was found in the form of a contribution of Vepstas (2008) on an encyclopedia article about hypergraphs. In that contribution, he says that a generalization of hypergraph allowing for edge-to-edge connections violates the axiom of Fondation of ZFC by allowing edge-loops.

TODO: Diagram of edge-loops

This shows the limits of standard mathematics especially on the field of knowledge representation. Some structures needs higher dimensions than allowed by the one dimensional structure of ZFC and FOL. However, it is important to not be mistaken: such non-standard set theories are more general than ZFC and therefore contains ZFC as a special case. All is a matter of restrictions.

### 1.1.1.5 Sheaf

In order to understand sheaves, we need to present a few auxiliary notions. Most of these definitions are adapted from (Vepštas 2008). The first of which is a seed.

**Definition 4** (Seed). A seed correspond to a vertex along with the set of adjacent edges. Formally we note a seed  $(v, \phi_g(v))$  that means that a seed build from vertex v in the graph g contains a set of adjacent edges  $\phi_g(v)$ . We call the vertex v the germ of the seed. The edges does not connect to the other vertices but keep the information and are able to match the correct vertices through typing (often a type of a single individual). We call the edges in a seed connectors.

Now we can build a kind of partial graphs from seeds called sections.

**Definition 5** (Section). A section is a set of seeds that have their common edges connected. This means that if two seeds have an edge in common connecting both germs, then the seeds are connected in the section and the edges are merged.

This tool was originally mostly meant for big data and categorization over large graphs. This is the reason for the next notion.

**Definition 6** (Graph Quotient). A quotient over a graph is the act of reducing a subgraph into a node while preserving the external connections. All internal structure becomes ignored and the subgraph now acts like a regular node.

Porting that notion to sections instead of graphs allows us to define stalks.

**Definition 7** (Stalk). Given a projection  $p:V\to V'$  over the germs of a section s, the stalk above the vertex  $v'\in V'$  is the quotient of all seeds that have their germ follow p(v)=v'.

Now we can add the final definition of sheaves.

**Definition 8** (Seaf). A seaf is a collection of sections, together with a projection function p and gluing axioms that the projection should respect depending on the application.

TODO: Diagrams and examples all the way.

## 1.1.1.6 Grammar and Parsing

Grammar is an old tool that used to be dedicated to liguists. With the funding works of Chomsky and his Contex-Free Grammars (CFG), these tools became available to mathematicians and shortly after to computer scientists.

A CFG is a formal grammar that aims to generate a formal language given a set of hierarchical rules. Each rule is given a symbol as a name. From any finite input of text in a given alphabet, the grammar should be able to determine if the input is part of the language it generates.

In computer science, popular meta-language called BNF was created shortly after Chomsky's work on CFG. The syntax is of the following form:

```
1 <rule> ::= <other_rule> | <terminal_symbol> | "literals"
```

A terminal symbol is a rule that does not depend of any other rule. It is possible to use recursion, meaning that a rule will use itself in its definition. This actually allows for infinite languages. Despite its expressive power, BNF is often used in one of its extended form.

In this context, we present a widely used form of BNF syntax that is meant to be human readable despite not being very formal. We add the repetition operators \* and + that respectively repeat 0 and 1 times or more the preceding expression. We also add the negation operator ~ that matches only if the following expression does not match. We also add parentesis for grouping expression and brackets to group literals.

A regular grammar is static, it is set once and for all and will always produce the same language. In order to be more flexible we need to talk about dynamic grammars and their associated tools.

One of the main tool for both static and dynamic grammar, is a parser. It is the program that will interprete the input into whatever usage it is meant for. Most of the time, a parser will transform the input into another similarily structured language. It can be a storage inside objects or memory, or compiled into another format, or even just for syntax coloration. Since a lot of usage requires the same kind of function, a new kind of tool emerged to make the creation of a parser simpler. We call those tools parser or compiler generators (Paulson 1982). They take a grammar description as input and gives the program of a parser of the generated language as an output.

For dynamic grammar, these tools can get more complicated. There are a few ways a grammar can become dynamic. The most straight-forward way to make a parser dynamic is to introduce code in the rule handling that will tweak variables affecting the parser itself (Souto *et al.* 1998). This allows for handling context in CFG without needing to rewrite the grammar.

Another kind of dynamic grammar are grammar that can modify themselves. In order to do this a grammar is valuated with reified objects representing parts of itself (Hutton and Meijer 1996). These parts can be modified dynamically by rules as the input gets parsed (Renggli *et al.* 2010; Alessandro and Piumarta 2007). This approach uses Parsing Expression Grammars (PEG)(Ford 2004) with Packrat parsing that Packrat parsing backtracks by ensuring that each production rule in the grammar is not tested more than once against each position in the input stream (Ford 2002). While PEG are easier to implement and more efficient in practice than their classical conterparts (Loff *et al.* 2018; Henglein and Rasmussen 2017), it offset the computation load in memory making it actually less efficient in general (Becket and Somogyi 2008).

Some tools actually just infer entire grammars from inputs and softwares (Höschele and Zeller 2017; Grünwald 1996). However, these kind of approaches require a lot of input data to perform well. They also simply provide the grammar after expensive computations.

## 1.1.1.7 Description Logics

On of the most standard and flexible way of representing knowledge for databases is by using ontologies. They are based mostly on the formalism of Description Logics (DL). It is based on the notion of classes (or types) as a way to make the knowledge hierarchically structured. A class is a set of individuals that are called instances of the classes. Classes got the same basic properties as sets but can also be constrained with logic formula. Constraints can be on anything about the class or its individuals. Knowledge is also encoded in relations that are predicates over attributes of individuals.

It is common when using DLs to store statements into three boxes (Baader 2003):

The TBox for terminology (statements about types)

- The RBox for rules (statements about properties) (Bürckert 1994)
- The ABox for assertions (statements about individual entities)

These are used mostly to separate knowledge about general facts (intentional knowledge) from specific knowledge of individual instances (extensional knowledge). The extra RBox is for "knowhow" or knowledge about entities behaviour. It restrict usages of roles (properties) in the ABox. The terminology is often hierarchically ordered using a subsumption relation noted □. If we represent classes or type as a set of individuals then this relation is akin to the subset relation of set theory.

There are several versions and extensions of DL. They all varies in expressivity. Improving the expressivity of DL system often comes at the cost of less efficient inference engines that can even become undecidable for some extensions of DL.

## 1.1.2 Ontologies and their Languages

Most AI problems needs a way to represent data. The classical way to represent knowledge has been more and more specialized for each AI community. Each their Domain Specific Language (DSL) that neatly fit the specific use it is intended to do. There was a time when the branch of AI wanted to unify knowledge description under the banner of the "semantic web". From numerous works, a repeated limitation of the "semantic web" seems to come from the languages used. In order to guarantee performance of generalist inference engines, these languages have been restricted so much that they became quite complicated to use and quickly cause huge amounts of recurrent data to be stored because of some forbidden representation that will push any generalist inference engine into undecidability.

The most basic of these language is perhaps RDF Turtle (Beckett and Berners-Lee 2011). It is based on tripples with an XML syntax and has a graph as its knowledge structure (Klyne and Carroll 2004). A RDF graph is a set of RDF triples  $\langle sub, pro, obj \rangle$  which fields are respectively called subject, property and object. It can also be seen as a partially labeled directed graph  $(N,\mathcal{E})$  with N being the set of RDF nodes and  $\mathcal{E}$  being the set edges. This graph also comes with an incomplete  $label: (N \cup \mathcal{E}) \to URI$  relation. Nodes without an URI are called blank nodes. It is important that, while not named, blank nodes have a distinct internal identifier from one another that allows to differentiate them.

Built on top of RDF, the W3C recommended another standard called OWL. I adds the ability to have hierarchical classes and properties alog with more advanced description of their arrity and constraints. OWL is, in a way, more expressive than RDF (Van Harmelen *et al.* 2008, vol. 1 p825). It adds most formalisms used in knowledge representation and is widely used and interconnected. OWL comes in three versions: OWL Lite, OWL DL and OWL Full. The lite version is less advanced but its inference is decidable, OWL DL contains all notions of DL and the full version contains all features of OWL but is strongly undecidable.

Expressivity can also come from a lack of restriction. If we allow some freedom of expression in RDF statements, its inference can quickly become undecidable (Motik 2007). This kind of extremely permissive language are better suited for specific usage for other branches of AI. Even with this expressivity, several works still deems existing ontology system as not expressive enough, mostly due to the lack of classical constructs like lists, parameters and quantifiers that don't fit the triple representation of RDF.

One of the ways which have been explored to overcome these limitations is by adding a 4<sup>th</sup> field in RDF. This field is meant for context and anotations. This field is used for informations about any statement represented as a triple, such as access rights, belief and probabilities, or most of the time the source of the data (Tolksdorf *et al.* 2004). One of the other use of the fourth field of RDF is to reify statements

(Hernández *et al.* 2015). Indeed by identifying each statement, it becomes possible to efficiently for statements about statements.

A completely different approach is done by Hart and Goertzel (2008) in his framework for Artificial General Intelligence (AGI) called OpenCog. The structure of the knowledge is based on a rhizome, a collection of trees, linked to one another. This structure is called Atomspace. Each vertex in the tree is an atom, leaf-vertexes are nodes, the others are links. Atoms are immutable, indexed objects. They can be given values that can be dynamical and, since they are not part of the rhizome, are an order of magnitude faster to access. Atoms and values alike are typed.

The goal of such a structure is to be able to merge concepts from widely different domains of AI. The major drawback being that the whole system is very slow compared to pretty much any domain specific software.

## 1.2 **Self**

As we have seen, most existing knowledge description systems have a common drawback: they are static. This means that they are either too inefficient or too specific. To fix this issue, a new knowledge representation system must be presented. The goal is to make a minimal language framework that can adapt to its use to become as specific as needed. If it becomes specific is must start from a generic base. Since that base language must be able to evolve to fit the most cases possible, it must be neutral and simple.

To summarize, that framework must maximize the following criteria:

- 1. Neutral: Must be independent from preferences and be localization.
- 2. Permissive: Must allow as many data representation as possible.
- 3. Minimalist: Must have the minimum amount of base axioms and as little native notions as possible.
- 4. Adaptive: Must be able to react to user input and be as flexible as possible.

In order to respect these requirements, we developed a framework for knowledge description. This Structuraly Expressive Language Framework (SELF) is our answer to these criteria. SELF is inspired by RDF Turtle and Description Logic.

## 1.2.1 Knowledge Structure

SELF extends the RDF graphs by adding another label to the edges of the graph to uniquely identify each statement. This basically turns the system into a quadruple storage even if this forth field is transparent to the user.

**Axiom** (Structure). A SELF graph is a set of statements that transparently include their own identity. The closest representation of the underlying structure of SELF is as follow:

$$W = (E, S) : S = \left\{ s = \left\langle e_{sub}, e_{pro}, e_{obj} \right\rangle : s \in D \models s \land D \right\}$$

with:

- $e_{sub}, e_{obj} \in E$  being entities representing the subject and object of the statement s,
- $e_{pro} \in P$  being the *property* of the statement s,
- $D \subset S$  is the domain of the world W,
- $S, P \subset E$  with S the set of statements and P the set of properties,

This means that the world W is a graph with the set of entities E as vertices and the set of statements S as edges. This model also suppose that every statement S must be true if they belong to the domain D. This graph is a directed 3-uniform hypergraph.

Since sheaves are a representation of hypergraphs, we can encode the structure of SELF into a sheaf-like form. Each seed is a statement, the germ being the statement vertex. It always is accompagnied of an incomming connector (its subject), an outgoing connector (its object) and an non dirrected connector (its property). The sections are domains and must be coherent. Each statement, along with its property, makes a stalk.

The difference with a sheaf is that the projection function is able to map the pair statement-property into a labelled edge in its projection space. We map this pair into a classical labeled edge that connects the subject to the object of the statement in a dirrected fashion. This results in the projected structure being a correct RDF graph.

TODO diagram

## 1.2.1.1 Consequences

The base knowledge structure is more than simply convenience. The fact that statements have their own identity, changes the degrees of freedom of the representation. RDF has a way to represent reified statements that are basically blank nodes with properties that are related to information about the subject, property and object of a designated statement. The problem is that, such statements are very differently represented and need 3 regular statements just to define. Using the forth field, it becomes possible to make statements about *any* statements. It becomes also possible to express modal logic about statements or to express, various traits like the probability or the access rights of a statements.

The knowledge structure holds several restrictions on the way to express knowledge. As a direct consequence, we can add several theorems to the logic system underlying SELF. The axiom of Structure is the only axiom of the system.

**Theorem 1 (Identity).** Any entity is uniquely distinct from any other entity.

This theorem comes from the axiom of Extensionality of ZFC. Indeed it is stated that a set is a unordered collection of distinct objects. Distinction is possible if and only if intrinsic identity is assumed. This notion of identity entails that a given entity cannot change in a way that would alter its identifier.

**Theorem 2 (Consistency).** Any statement in a given domain is consistent with any other statements of this domain.

Consistency comes from the need for a coherent knowledge database and is often a requirement of such constructs. This theorem also is a consequence of the axiom of Structure:  $s \in D \models s \land D$ .

Theorem 3 (Uniformity). Any object in SELF is an entity. Any relations in SELF are restricted to E.

This also means that all native relations are closed under E. This allows for a uniform knowledge database.

## 1.2.1.2 Native properties

Theorem 1 leads to the need for two native properties in the system: equality and name.

The **equality relation** = :  $E \rightarrow E$ , behaves like the classical operator. Since the knowledge database will be expressed through text, we also need to add an explicit way to identify entities. This identification is

done through the **name relation**  $\nu: E \to String$  that affects a string literal to some entities. This lead us to introduce literals into SELF that are also entities that have a native value (more on literal **LATER**).

The axiom of Structure puts a type restriction on property. Since it compartments E using various named subsets, we must adequately introduce an explicit type system into SELF. That type system requires a **type relation**  $\tau: E \to T$ . That relation is complete as all entities have a type. Theorem 3 causes the set of entities to be universal. Type theory, along with Description Logic (DL), introduce a **subsumption relation**  $\prec: T \to T$  as a partial ordering relation to the types. In our case, the entity type is the greatest element of the lattice formed by the set of types with the subsumption relation  $(T, \prec)$ .

The theorem 3 also allows for some very interesting meta-constructs. That is why we also introduce a **meta relation**  $\mu^{\pm}: E \rightleftharpoons_{-}^{+} D$ . This allows to create domain from certain entities and to encapsulate domains into entities.  $\mu^{-}$  is for reification and  $\mu^{+}$  is for abstraction. This meta relation also allows to express value of entities, like lists or various containers.

To fullfil the principle of adaptability and in order to make the type system more useful, we introduce the **parameter relation**  $\rho: E \to E$ . This relation affects a list of parameters, using the meta relation, to some parameterized entities. This also allows for variables in statements.

Since axiom of Structure gives the structure of SELF a hypergraph shape, we must port some notions of graph theory into our framework. Introducing the **statement relation**  $\phi:S\to E$  reusing the same symbol as for the adjacency and incidency relation of graphs. This isn't a coincidence as this relation has the same properties. For example  $\phi^-(s)$  gives the subject of a statement s. Respectively,  $\phi^+$  and  $\phi^0$  give the object and property of any statement. For adjacency,  $\phi^-$  and  $\phi^+$  can give the set of statements any entity is respectively the object and subject of. For any property  $p\in P$ , the notation  $\phi^0(p)$  gives the set of statements using this property. This allows us to port all the other notions of graphs using this relation as a base.

In figure 1.1, we present all the native relations along with their domains and most subsets of E.

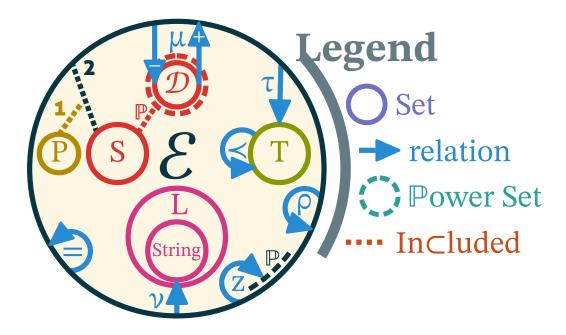


Figure 1.1: Venn diagram of subsets of E along with their relations. Dotted lines means that the sets are defined a subsets of the wider set.

## 1.2.2 Syntax

Since we need to respect the requirements of the problem, the RDF syntax cannot be used to express the knowledge. Indeed, RDF states native properties as English nodes with a specific URI that isn't neutral. It also isn't minimalist since it uses an XML syntax so verbose that it is not used for most examples in the documents that defines RDF because it is too confusing and complex (W3C 2004a; W3C 2004b). The XML syntax is also quite restrictive and cannot evolve dynamically to adapt to the usage.

So we need to define a new language that is minimalist and neutral. At the same time the language must be permissive and dynamical. These two goals are incompatible and will end up needing different solutions. So the solution to the problem is to actually define two languages that fit the criteria: one minimalist and one adaptive. The issue is that we need not make a user learn two languages and the second kind of language must be very specific and that violates the principle of neutrality we try to respect.

The only solution is to make a mechanism to adapt the language as it is used. We start off with a simple framework that uses a grammar noted  $g_0$ .

The description of  $g_0$  is pretty straightforward: it mostly is just a triple representation separated by whitespaces. The goal is to add a minimal syntax consistent with the axiom of Structure. In listing 1.1, we give a simplified version of  $g_0$ . It is written in a pseudo-BNF fashion, which is extended with the classical repetition operators  $\ast$  and + along with the negation operator  $\sim$ . All tokens have names in uppercase. We also add the following rule modifiers:

- <~name> are ignored for the parsing. However, the tokens are consumed and therefore acts like separators for the other rules.
- <?name> are inferred rules and tokens. They play a key role for the process of derivation explained in section 1.2.3.

Listing 1.1: Simplified pseudo-BNF description for basic SELF.

In order to respect the principle of neutrality, the language must not suppose of any regional predisposition of the user. There are few exceptions for the sake of convenience and performance. The first exception is that the language is meant to be read from left to right and have an occidentally biased subject verb object triple description. Another exception is for literals that use the same grammar as

in classical Java. This means that the decimal separator is the dot (.). This could be fixed in later version using dynamical definitions (see section 1.3.1).

Even if sticking to the ASCII subset of characters is a good idea for efficiency, SELF can work with UTF-8 and exploits the Unicode Character Database (UCD) for its token definitions (Unicode Consortium 2018a). This means that SELF comes keyword free and that the definition of each symbol is left to the user. Each notion and symbol is inferred (with the exception of the first statement which is closer to an imposed configuration file).

In  $g_0$ , the first two token definitions are ignored. This means that comments and white-spaces will act as separation and won't be interpreted. Comments are there only for convenience since they do not serve any real purpose in the language. It was arbitrarily decided to use Java style comments. White-spaces are defined against UCD's definition of the separator category  $\mathbb{Z}$  (see Unicode Consortium 2018b, chap. 4).

Line 4 uses the basic Java definition for literals. In order to keep the independence from any natural language, boolean literals are not natively defined (since they are English words).

Another aspect of that language independence is found starting at line 5 where the definitions of <uppercase, <lowercase, <lowercase, <lowercase, <lowercase, <lowercase, <lowercase, <lowercase and <ul>Lu, Ll, L&, Nd). This means that any language's upper case can be used in that context. For performance and simplicity reasons we will only use ASCII in our examples and application.

The rule at line 1 is used for the definition of three tokens that are important for the rest of the input. <EQUAL> is the symbol for equality and <SOLVE> is the symbol for the solution quantifier (and also the language pendant of  $\mu^-$ ). The most useful token <EOS> is used as a statement delimiter. This rule also permits the inclusion of other files if a string literal is used as subject. The underlying logic of this first statement will be presented in section 1.2.5.1.

At line 11, we can see one of the most defining feature of  $g_0$ : statements. The input is nothing but a set of statements. Each components of the statements are entities. We defined two specific rules for the subject and object to allow for eventual run-time modifications. The property rule is more restricted in order to guarantee the non-ambiguity of the grammar.

## 1.2.3 Dynamic Grammar

The syntax we described is only valid for  $g_0$ . As long as the input is conforming to these rules, the framework keeps the minimal behavior. In order to access more features, one need to break a rule. We add a second outcome to handling with violations: **derivation**. There are several kind of possible violations that will interrupt the normal parsing of the input:

- Violations of the <first> statement rule : This will cause a fatal error.
- Violations of the <statement> rule: This will cause a derivation if an unexpected additional token is found instead of <EOS>. If not enough tokens are present, a fatal error is triggered.
- Violations of the secondary rules (<subject>, <entity>, ...): This will give a fatal error except if there is also an excess of token in the current statement which will cause derivation to happen.

Derivation will cause the current input to be analyzed by a set of meta-rules. The main restriction of these rules is given in  $g_0$ : each statement must be expressible using a triple notation. This means that the goal of the meta-rules is to find an interpretation of the input that is reducible to a triple and to augment  $g_0$  by adding an expression to any <meta\_\*> rules. If the input has less than 3 entities for

a statement then the parsing fails. When there is extra input in a statement, there is a few ways the infringing input can be reduced back to a triple.

## 1.2.3.1 Containers

The first meta-rule is to infer a container. A container is delimited by at least a left and right delimiter (they can be the same symbol) and an optional middle delimiter. We infer the delimiters using the algorithm 1.

#### Algorithm 1 Container meta-rule 1 function container(Token current) 2 lookahead(current, EOS) ▶ Populate all tokens of the statement 3 for all token in horizon do if token is a new symbol then delimiters.append(token) 5 if length(delimiters) < 2 then if coherentDelimiters(horizon, delimiters[0]) then 6 inferMiddle(delimiters[0]) ▶ New middle delimiter in existing container 8 return Success return Failure 10 while length(delimiters) > 0 do for all (left, middle, right) in sortedDelimiters(delimiters) do 11 12 if coherentDelimiters(horizon, left, middle, right) then inferDelimiter(left, right) 13 14 inferMiddle(middle) ▶ Ignored if null 15 delimiters.remove(left, middle, right) 16 if length(delimiters) stayed the same then return Success 17

The function sortedDelimiters at line 11 is used to generate every ordered possibility and sort them using a few criteria. The default order is possibilities grouped from left to right. All coupled delimiters that are mirror of each other following the UCD are preferred to other possibilities.

Checking the result of the choice is very important. At line 12 a function checks if the delimiters allows for triple reduction and enforce restrictions. For example, a property cannot be wrapped in a container (except if part of parameters). This is done in order to avoid a type mismatch later in the interpretation.

Once the inference is done, the resulting calls to inferDelimiter will add the rules listed in listing 1.2 to  $g_0$ . This function will create a <code><container></code> rule and add it to the definition of <code><meta\_entity></code>. Then it will create a rule for the container named after the UCD name of the left delimiter (searching in the <code>NamesList.txt</code> file for an entry starting with "left" and the rest of the name or defaulting to the first entry). Those rules are added as a conjunction list to the rule <code><container></code>. It is worthy to note that the call to inferMiddle will add rules to the token <code><MIDDLE></code> independently from any container and therefore, all containers share the same pool of middle delimiters.

```
1 <meta_entity> ::= <container>
2 <container> :: = <parentesis> | ...
3 <parentesis> ::= "(" [<naked_entity>] (<?MIDDLE> <naked_entity>)* ")"
4 <naked_entity> ::= <statement> | <entity>
```

Listing 1.2: Rules added to the current grammar for handling new container for parenthesis

18

return Success

The rule at line 4 is added once and enables the use of meta-statements inside containers. It is the language pendant of the  $\mu^+$  relation, allowing to wrap abstraction in a safe way.

### 1.2.3.2 Parameters

If the previous rule didn't fix the parsing of the statement, we continue with the following meta-rule. Parameters are extra containers that are used after an entity. Every container can be used as parameters. We detail the analysis in algorithm 2.

## Algorithm 2 Parameter meta-rule

```
1 function parameter(Entity[] statement)
      reduced = statement
 3
      while length(reduced) >3 do
 4
          for i from 0 to length(reduced) - 1 do
             if name(reduced[i]) not null and
 6 type(reduced[i+1]) = Container and
 7 coherentParameters(reduced, i) then
                param = inferParameter(reduced[i], reduced[i+1])
9
                reduced.remove(reduced[i], reduced[i+1])
10
                reduced.insert(param, i)
                                                                                          ▶ Replace parameterized entity
11
                break
         if length(statement) stayed the same then return Success
12
13
      return Failure
```

The goal is to match extra containers with the preceding named entity. The container is then combined with the preceding entity into a parameterized entity.

The call to inferParameter will add the rule in listing 1.3, replacing <?container> with the name of the container used (for example <parenthesis>).

```
1 <meta_entity> ::= <ID> <?container>
2 <meta_property> ::= <ID> <?container>
```

Listing 1.3: Rules added to the current grammar for handling parameters

## 1.2.3.3 Operators

A shorthand for parameters is the operator notation. It allows to affect a single parameter to an entity without uing a container. It is most used for special entities like quantifiers or modificators. This is why once used the parent entity take a polymorphic type, meaning that type inference will not issue errors for any usage of them. Details of the way the operators are reduced is exposed in algorithm 3.

From the call of inferOperator, comes new rules explicated in listing 1.4. The call also add the operator entity to an inferred token <0P>.

```
1 <meta_entity> ::= <?OP> <ID>
2 <meta_property> ::= <?OP> <ID>
```

Listing 1.4: Rules added to the current grammar for handling operators

If all meta-rules fail, then the parsing fails and returns an error to the user.

#### Algorithm 3 Operator meta-rule 1 function operator(Entity[] statement) reduced = statement 3 while length(reduced) >3 do 4 for i from 0 to length(reduced) - 1 do if $\nu$ (reduced[i]) not null and 6 ν(reduced[i+1]) not null and 7 ( $\nu$ (reduced[i]) is a new symbol or 8 reduced[i] has been parameterized before) and 9 coherentOperator(reduced, i) then op = inferOperator(reduced[i], reduced[i+1]) 10 reduced.remove(reduced[i], reduced[i+1]) 11 12 reduced.insert(op, i) ▶ Replace parameterized entity 13 if length(statement) stayed the same then return Success 14 15 return Failure

## 1.2.4 Contextual Interpretation

While parsing another important part of the processing is done after the success of a grammar rule. The grammar in SELF is valuated, meaning that each rule has to return an entity. A set of functions are used to then populate the database with the right entities or retrieve an existing one that correspond to what is being parsed.

## 1.2.4.1 Naming and Scope

When parsing an entity by name, the system will first request for an existing entity with the same name. If such an entity is retrieved it is returned instead of creating a new one. The validity of a name is limited by the notion of scope.

A scope is the reach of an entity's dirrect influence. It affects the naming relation by removing variable's names. Scopes are delimited by containers and statements. This local context is useful when wanting to restrict the scope of the declaration of an entity. The main goal of such restriction is to allow for a similar mechanism as the RDF namespaces. This also makes the use of variable (RDF blank nodes) possible.

The scope of an entity have three special values:

- · Variable: This scope restricts the scope of the entity to only the other entities in its scope.
- Local: This scope means that the parsing is still populating the scope of the entity. Its scope is limited to the currently parsing statement.
- Global: This scope means the name has no scope limitation.

The scope of an entity also contains all its parent entities, meaning all container or statement the entity is part of. This is used when chosing between the special values of the scope. The process is detailed in algorithm 4.

The process happens for each entity created or requested by the parser. If a given entity is part of any other entity, the enclosing entity is added to its scope. When an entity is enclosed in any entity while

## Algorithm 4 Determination of the scope of an entity

```
1 function inferScope(Entity e)
        Entity[] reach = []
 3
        if \tau(e) = S then
 4
          for all i \in \phi(e) do reach.append(inferVariable(i))
                                                                                                          ▶ Adding scopes nested in statement e
 5
        for all i \in \mu^-(e) do reach.append(inferVariable(i))
                                                                                                          ▶ Adding scopes nested in container e
 6
        if \exists \rho(e) then
            Entity[] param = inferScope(\rho(e))
 7
 8
            for all i \in \text{param } do \text{ param.remove}(\text{inferScope}(i))
                                                                                                   ▶ Remove duplicate scopes from parameters
            for all i \in \text{param do reach.append(inferVariable}(i))
                                                                                                            ▶ Adding scopes from paramters of e
10
        scope(e) \leftarrow reach
        \textbf{if} \ \mathsf{GLOBAL} \not\in \mathsf{scope}(e) \ \textbf{then} \ \mathsf{scope}(e) \leftarrow \mathsf{scope}(e) \cup \{\mathsf{LOCAL}\}
    return reach
12 function inferVariable(Entity e)
13
        Entity[] reach = []
14
        if LOCAL \in scope(e) then
15
            for all i \in \text{scope}(e) do
16
                if \exists p \in E : \rho(p) = i then
                                                                                                 \triangleright e is already a parameter of another entity p
17
                     scope(e) \leftarrow scope(e) \setminus \{LOCAL\}
                     scope(p) \leftarrow scope(p) \cup scope(e)
19
                     scope(e) \leftarrow scope(e) \cup \{VARIABLE, p\}
20
            reach.append(e)
            reach.append(scope(e))
    return reach
```

already being a parameter of another entity, it becomes a variable.

## 1.2.4.2 Instanciation identification

When a parameterized entity is parsed, another process starts to identify if a compatible instance already exists. From theorem 1, it is impossible for two entity to share the same identifier. This makes mandatory to avoid creating an entity that is equal to an existing one. Given the order of which parsing is done, it is not always possible to determine the parameter of an entity before its creation. In that case a later examination will merge the new entity onto the older one and discard the new identifier.

## 1.2.5 Structure as a Definition

The derivation feature on its own does not allow to define most of the native properties. For that, one need a light inference mechanism. This mecanism is part of the default inference engine. This engine only works on principle of structure as a definition. Since all names must be neutral from any language, that engine cannot rely on regular mechanism like configuration files with keys and values or predefined keywords.

To use correctly SELF, one muist be familiar with the native properties and their structure or implement their own inference engine to override the default one.

## 1.2.5.1 Quantifiers

What are quantifiers? In SELF they differs from their mathematical counterparts. Quantifiers are special entities that are meant to be of a generic type that matches any entities including quantifiers. There

are infinitely many quantifiers in SELF but they are all derived from a special one called the solution quantifier. We mentioned it briefly durring the definition of the grammar  $g_0$ . It is the language pendant of  $\mu^-$  and is used to extract and evaluate reified knowledge.

For example, the statement bob is <SOLVE>(x) will give either a default container filled with every value that the variable x can take or if the value is unique, it will take that value. If there is no value it will default to <NULL>, the exclusion quantifier.

How are these other quantifiers defined? We use a definition akin to Lindstöm quantifiers (1966) which is a generalization of counting quantifiers (Gradel *et al.* 1997). Meaning that a quantifier is defined as a constrained range over the quantified variable. We suppose five quantifiers as existing in SELF as native entities.

- The **solution quantifier** <**SOLVE**> noted § in classical mathematics, makes a querry that turn the expression into the possible range of its variable.
- The universal quantifier <ALL> behaves like ∀ and forces the expression to affect every possible value of its variable.
- The existential quantifier <SOME> behaves like  $\exists$  and forces the expression to match at least one value for its variable.
- The uniqueness quantifier < ONE> behaves like ! and forces the expression to match exactly one value for its variable.
- The **exclusion quantifier** <NULL> behaves like ¬∃ and forces the expression to match none of the value of its variable.

The four last quantifiers are inspired from Aristotle's square of opposition (D'Alfonso 2011).

In SELF, quantifier are not always followed by a quantified variable and can be used as a value. In that case the variable is simply anonymous. We use the exclusion quantifier as a value to indicate that there are no value, sort of like null or nil in programming languages.

In listing 1.5, we present an example file that is meant to define most of the useful native properties along with default quantifiers.

```
1 * = ? ;
2 ?(x) = x; //Optional definition
3 ?~ = { };
4 ?_ ~(=) ~;
5 ?!_ = {_};
7 (*e, !T) : (e :: T); *T : (T :: Type);
8 *T : (Entity / T);
10 :: :: Property(Entity, Type);
11 (___) :: Statement;
12 (~, !, _, *) :: Quantifier;
13 ( )::Group;
14 { }::Set;
15 [ ]::List;
16 < >::Tuple;
17 Collection/(Set,List,Tuple);
18 0 :: Integer; 0.0::Float;
19 '\0'::Character; ""::String;
20 Literal/(Boolean, Integer, Float, Character, String);
```

```
22 (*e, !(s::String)) : (e named s);
23 (*e(p), !p) : (e param p);
24 *(s p o):(((s p o) subject s),((s p o) property p),((s p o) object o));
```

Listing 1.5: The default lang.w file.

At line 1, we give the first statement that defines the solution quantifier's symbol. The reason this first statement is shaped like this is that global statements are always evaluated to be a true statement. This means that anything equaling the solution quantifier at this level will be evaluated as a domain. If it is a string literal, then it must be either a file path or URL or a valid SELF expression. If it is a single entity then it becomes synonymous to the entire SELF domain and therefore contains everything. We can infer that it becomes the universal quantifier.

All statements up to line 5 are quantifiers definitions. On the left side we got the quantifier symbol used as a parameter to the solution quantifier using the operator notation. On the right we got the domain of the quantifier. The exclusive quantifier has as a range the empty set. For the existantial quantifier we have only a restriction of it not having an empty range. At last, the uniqueness quantifier got a set with only one element matching its variable (noting that anonymous variables doesn't match necessarily other anonymous variables in the same statement).

## 1.2.5.2 Infering native properties

All native propserties can be infered by structure using quantified statements. Here is the structural definition for each of them:

- = (at line 1) is the equality relation given in the first statement.
- < (at line 8) is the first property to relate a particuliar type relative to all types. That type becomes the entity type.
- $\mu^-$  (at line 1) is the solution quantifier discussed above given in the first statement.
- $\mu^+$  is represented using containers.
- $\nu$  (at line 22) is the first property affecting a string literal uniquely to each entity.
- $\rho$  (at line 23) is the first property to affect to all entity a possible parameter list.
- $\tau$  (at line 7) is the first property that matches every entity to a type.
- $\phi$  (at line 24) is the first property to match for all statements:
  - $\phi^-$  its subject,
  - $-\phi^0$  its property,
  - $\phi^+$  its object.

We limit the inference to one symbol to make it much simpler to implement and to retrieve but, except for false positives, there are no reason it should not be possible to define several notations for each relation.

## 1.2.6 Extended Inference Mechanisms

In this section we present the default inference engine. It has only a few functionalities. It isn't meant to be universal and the goal of SELF is to provide a framework that can be used by specialists to define and code exactly what tools they need.

Inference engines need to create new knowledge but this knowledge shouldn't be simply merged with the explicit domain. Since this knowledge is infered, it is not exactly part of the domain but must remain consistent with it. This knowledge is stored in a special scope dedicated to each inference engine.

This way, inference engines can use defeasable logic or have dynamic inference from any knowledge insertion in the system.

## 1.2.6.1 Type inference

Type inference works on matching types in statements. The main mechanism consist in infering the type of properties in a restrictive way. Properties have a parameterized type with the type of their subject and object. The goal is to make that type match the inputed subject and object.

For that we start by trying to match the types. If the types differs the process tries to reduce the more general type against the lesser one (subsumption wise). If they are incompatible, the inference uses some light defeasable logic to undo previous inferences. In that case the types are changed to the last common type in the subsumption tree.

However, this may not always be possible. Indeed, types can be explicitely specified as a safeguard against mistake. If that's the case, an error is raised and the parsing or knowledge insertion is interrupted.

### 1.2.6.2 Instanciation

Another inference tool is instanciation. Since entities can be parameterized, they can also be defined against their parameters. When those parameters are variables, it allows entities to be instanciated later.

This is a complicated process because entities are imutable. Indeed, parsing happens from left to right and therefore an entity is often created before all the instanciation informations are available. Even harder are completion of definition in several separate statements. In all case, a new entity is created and then the inference realize that it is either matching a previous definition and will need to be merged with the older entity or it is a new instance and need all properties duplicated and instanciated.

This gives us two mechanism to take into account: merging and instanciating.

Merging is pretty straightforward: the new entity is replaced with the old one in all of the knowledge graph. containers, parameterized entities, quantifiers and statements must be duplicated with the correct value and the original destroyed. This is a heavy and complicated process but seemingly the only way to implement such a case with immutable entities.

Instanciating is similar to merging but even more complicated. It starts with computing a relation that maps each variable that needs replacing with their grounded value. Then it duplicate all knowledge about the parent entity while applying the replacement map.

## 1.3 Perpectives

Listing the contributions there are a couple that didn't made the cut. It is mainly ideas or projects that were too long to check or implement and needed more time to complete. SELF is still a prototype, and even if the implementation seemed to perform well on a simple example, no benchmarks have been done on it. It might be good to make a theoritical analysis of OWL compared to SELF along with some benchmark results.

On the theoritical parts there are some works that seems worthy of exposure even if unfinished.

## 1.3.1 Literal definition using Peano's axioms

The only real exceptions to the axioms and criterias are the first statement, the comments and the literals.

For the first statement, there is yet to find a way to express both inclusion, the equality relation and solution quantifier. If such a convinient expression exists, then the language can become almost entirely self described.

Comments can be seen as a special kind of containers. The difficult part is to find a clever way to differentiate them from regular containers and to ignore their content in the regular grammar. It might be possible to at first describe their structure but then they become parseable entities and fails at their purpose.

Lastly and perhaps the most complicated violation to fix: literals. It is quite possible to define literals by structure. First we can define boolean logic quite easily in SELF as demonstrated by listing 1.6.

```
1 ~(false) = true;
2 ( false , true ) :: Boolean;
3 true = ?; //conflicts with first statement !
4 *a : ((a | true) = true);
5 *a : ((false | a) = a);
6 *a : ((a & false) = false);
7 *a : ((true & a) = a);
```

Listing 1.6: Possible definition of boolean logic in SELF.

Starting with line 1, we simply define the negation using the exclusive quantifier. From there we define the boolean type as just the two truth values. And now it gets complicated. We could either arbitrarily say that the false literal is always parameter of the exclusion quantifier or that it comes first on either two first statements but that would just violates minimalism even more. We could use the solution quantifier to define truth but that colide with the first statement definition. There doesn't seem to be a good answer for now.

From line 4 going on, we state the definition of the logical operators  $\land$  and  $\lor$ . The problem with this is that we either need to make a native property for those operator or the inference to compute boolean logic will be terribly ineficient.

We can use Peano's axioms (1889) to define integers in SELF. The attempt at this definition is presented in listing 1.7.

```
1 0 :: Integer;
2 *n : (++(n) :: Integer);
3 (*m, *n) : ((m=n) : (++m = ++n));
4 *n : (++n ~= 0);
5 *n : ((n + 0) = n);
6 (*n, *m) : ((n + ++m) = ++(n + m));
7 *n : ((n × 0) = 0);
8 (*n, *m) : ((n × ++m) = (n + (n × m)));
```

Listing 1.7: Possible integration of the Peano axioms in SELF.

We got several problems doing so. The symbols \* and / are already taken in the default file and so would need replacement or we should use the non ASCII  $\times$  and  $\div$  symbols for multiplication and division. Another

more fundamental issue is as previously discussed for booleans: the inference would be excrutiatingly slow or we should revert to a kind of parsing similar to what we have already under the hood. The last problem is the definition of digits and bases that would quickly become exceedingly complicated and verbose.

For floating numbers this turns out even worse and complicated and such a description wasn't even attempted for now.

The last part concerns textual literals. The issue is the same as the one with comments but even worse. We get to interprete the content as literal value and that would necessitate a similar system as we already have and wouldn't improve the minimalist aspect of things much. Also we should define ways to escape characters and also to input escape sequences that are often needed in such case. And since SELF isn't meant for programming that can become very verbose and complex.

## 1.3.2 Advanced Inference

The inference in SELF is very basic. It could be improved a lot more by simply checking the consistency of the database on most aspect. However, such a task seems to be very difficult or very slow. Since that kind of inference is undecidable in SELF, it would be all a research problem just to find a performant inference algorithm.

Other kind of inference are more about convinience. For example one can erase singlets (containers with a single value) to make the database lighter and easier to maintain and query.

## 1.3.3 Querries

We haven't really discussed querries in SELF. They can be made using the main syntax and the solution quantifiers but efficiency of such querries is unknown. Making an efficient query engine is a big research project on its own.

For now a very simplified query API exists in the prototype and seems to perform well but further tests are needed to assess its scalability capacities.

# 2 General Planning Framework

## 2.1 Existing Languages and Frameworks

État de l'art

## 2.2 Taxonomy

## 2.2.1 Action type

(Définition)

## 2.2.2 Plan type

(Définition)

## 2.2.3 Problem type

(Définition)

## 2.3 Color

(Framework)

# 3 Online and Flexible Planning Algorithms

## 3.1 Existing Algorithms

État de l'art

## 3.2 Lollipop

- 3.2.1 Operator Graph
- 3.2.2 Negative Refinements
- 3.2.3 Usefullness Heuristic
- 3.2.4 Algorithm
- 3.2.5 Theoretical and Empirical Results

## 3.3 HEART

- 3.3.1 Domain Compilation
- 3.3.2 Abstraction in POP
- 3.3.3 Planning in cycle
- 3.3.4 Properties of Abstract Planning
- 3.3.5 Computational Profile

## 3.4 Planning Improvements

- 3.4.1 Heuristics using Semantics
- 3.4.2 Macro-Action learning

## 3.5 Recognition

- 3.5.1 Existing approcahes
- 3.5.2 Rico

## 3.5.2.1 Probabilities and approximations

We define a probability distribution over dated states of the world. That distribution is in part given and fixed and the rest needs computation. **TODO: that's super bad...** 

Here is the list of given prior probabilities and asumptions:

- $P(O) = \prod_{o \in O} P(o)$   $P(\mathcal{G}) = \sum_{G \in \mathcal{G}} P(G) = 1$  since we assume that the agent must be pursuing one of the goals.  $P(G|\pi) = 1$  for a plan  $\pi$  appliable in I that achieves G.

From dirrect application of Bayes theorem and the previous assomptions, we have:

$$P(\pi|O) = \frac{P(O|\pi)P(\pi)}{P(O)} = \frac{P(O|\pi)P(\pi|G)P(G)}{P(O)}$$
(3.1)

$$P(G|O) = \frac{P(O|G)P(G)}{P(O)}$$
(3.2)

From the total probability formula:

$$P(O|G) = \sum_{\pi \in \Pi_G} P(O|\pi)P(\pi|G)$$
(3.3)

$$P(O|G) = \sum_{\pi \in \Pi_G} P(O|\pi)P(\pi|G) \tag{3.4}$$

# 4 Conclusion

# **Apendix**

## References

## Alessandro, W., and I. Piumarta

**OMeta:** An object-oriented language for pattern matching, *Proceedings of the 2007 symposium on Dynamic languages*, **2007**.

## Baader, F.

The description logic handbook: Theory, implementation and applications, Cambridge university press, 2003.

### Backus, J. W.

The syntax and semantics of the proposed international algebraic language of the Zurich ACM-GAMM conference, *Proceedings of the International Comference on Information Processing*, 1959, 1959.

### Becket, R., and Z. Somogyi

DCGs+ memoing= packrat parsing but is it worth it?, International Symposium on Practical Aspects of Declarative Languages, Springer, 2008, 182–196.

## Beckett, D., and T. Berners-Lee

Turtle - Terse RDF Triple Language, W3C Team Submission W3C, March 2011.

### Bürckert, H.-J

Terminologies and rules, Workshop on Information Systems and Artificial Intelligence, Springer, 1994, 44–63.

## Cantor, G.

On a Property of the Class of all Real Algebraic Numbers., *Crelle's Journal for Mathematics*, 77, 258–262, 1874.

### Cantor, G.

Beiträge zur Begründung der transfiniten Mengenlehre, Mathematische Annalen, 46 (4), 481–512, 1895.

### Chomsky, N.

Three models for the description of language, IRE Transactions on information theory, 2 (3), 113–124, 1956.

### Ciesielski, K.

Set Theory for the Working Mathematician, Cambridge University Press, August 1997.

## D'Alfonso, D.

Generalized Quantifiers: Logic and Language, 2011.

### Ford, B.

Packrat parsing:: Simple, powerful, lazy, linear time, functional pearl, ACM SIGPLAN Notices, ACM, 2002, 37,36–47.

## Ford, B.

Parsing expression grammars: A recognition-based syntactic foundation, ACM SIGPLAN Notices, ACM,

2004, 39,111-122.

Fraenkel, A. A., Y. Bar-Hillel, and A. Levy

Foundations of set theory, vol. 67Elsevier, 1973.

Gradel, E., M. Otto, and E. Rosen

Two-variable logic with counting is decidable, Logic in Computer Science, 1997. LICS'97. Proceedings., 12th Annual IEEE Symposium on, IEEE, 1997, 306–317.

Grünwald, P.

A minimum description length approach to grammar inference, in S. Wermter, E. Riloff, and G. Scheler (eds.), Connectionist, Statistical and Symbolic Approaches to Learning for Natural Language Processing, Lecture notes in computer science; Springer Berlin Heidelberg, 1996, 203–216.

Hart, D., and B. Goertzel

Opencog: A software framework for integrative artificial general intelligence, AGI, 2008, 468–472.

Hehner, E. C.

A practical theory of programming, Springer Science & Business Media, 2012.

Henglein, F., and U. T. Rasmussen

PEG parsing in less space using progressive tabling and dynamic analysis, *Proceedings of the 2017 ACM SIGPLAN Workshop on Partial Evaluation and Program Manipulation*, ACM, 2017, 35–46.

Hernández, D., A. Hogan, and M. Krötzsch

Reifying RDF: What works well with wikidata?, SSWS@ ISWC, 1457, 32-47, 2015.

Horrocks, I., P. F. Patel-Schneider, and F. V. Harmelen

From SHIQ and RDF to OWL: The Making of a Web Ontology Language, *Journal of Web Semantics*, 1, 2003, 2003.

Höschele, M., and A. Zeller

**Mining input grammars with AUTOGRAM**, *Proceedings of the 39th International Conference on Software Engineering Companion*, **IEEE Press**, **2017**, **31–34**.

Hutton, G., and E. Meijer

Monadic parser combinators, 1996.

Klyne, G., and J. J. Carroll

Resource Description Framework (RDF): Concepts and Abstract Syntax, Language Specification. Ed. B. McBride W3C, 2004.

Kovitz, B.

Terminology - What do you call graphs that allow edges to edges?, *Mathematics Stack Exchange*, January 2018.

Lindström, P.

First Order Predicate Logic with Generalized Quantifiers, 1966.

Loff, B., N. Moreira, and R. Reis

**The Computational Power of Parsing Expression Grammars,** *International Conference on Developments in Language Theory*, **Springer**, **2018**, **491–502**.

Motik, B.

On the properties of metamodeling in OWL, Journal of Logic and Computation, 17 (4), 617–637, 2007.

#### Paulson, L.

A semantics-directed compiler generator, *Proceedings of the 9th ACM SIGPLAN-SIGACT symposium on Principles of programming languages - POPL '82*, Albuquerque, Mexico: ACM Press, 1982, 224–233. doi:10.1145/582153.582178.

## Peano, G.

Arithmetices principia: Nova methodo exposita, Fratres Bocca, 1889.

## Renggli, L., S. Ducasse, T. Gîrba, and O. Nierstrasz

Practical Dynamic Grammars for Dynamic Languages, Workshop on Dynamic Languages and Applications, Malaga, Spain, 2010, 4.

### Silberschatz, A.

Port directed communication, The Computer Journal, 24(1), 78–82, January 1981. doi:10.1093/comjnl/24.1.78.

## Souto, D. C., M. V. Ferro, and M. A. Pardo

Dynamic Programming as Frame for Efficient Parsing, *Proceedings SCCC'98. 18th International Conference of the Chilean Society of Computer Science (Cat. No.98EX212)(SCCC)*, **November 1998, 68.** doi:10.1109/SCCC.1998.730784.

Tolksdorf, R., L. Nixon, F. Liebsch, Minh NguyenD., and Paslaru BontasE.

Semantic web spaces, 2004.

### **Unicode Consortium**

Unicode Character Database, About the Unicode Character Database, https://www.unicode.org/ucd/#Latest, June 2018a.

## **Unicode Consortium**

The Unicode Standard, Version 11.0, Core specification 11.0Mountain View, CA, June 2018b.

## Van Harmelen, F., V. Lifschitz, and B. Porter

Handbook of knowledge representation, vol. 1Elsevier, 2008.

## Vepstas, L.

Hypergraph edge-to-edge, Wikipedia, May 2008.

## Vepštas, L.

Sheaves: A Topological Approach to Big Data, 2008.

## W3C

RDF Semantics, W3C, 2004a.

### W3C

RDF Vocabulary Description Language 1.0: RDF Schema http://www.w3.org/TR/rdf-schema/, February 2004b.