

# Title

Antoine Gréa





## **Abstract**

# Table of Content

<b>Acknowledgements</b>	<b>8</b>
<b>Introduction</b>	<b>9</b>
0.1 Thesis Context . . . . .	9
0.2 Motivations . . . . .	9
0.2.1 Observation . . . . .	9
0.2.2 Abstraction . . . . .	9
0.2.3 Cognition . . . . .	9
0.3 Issues . . . . .	9
0.4 Contributions . . . . .	9
0.5 Plan . . . . .	9
<b>1 Knowledge Representation</b>	<b>10</b>
1.1 Fundamentals . . . . .	11
1.1.1 Foundation of maths and logic systems . . . . .	11
1.1.1.1 First Order Logic . . . . .	11
1.1.1.2 Set Theory . . . . .	12
1.1.1.3 Relational algebra . . . . .	13
1.1.1.4 Graphs . . . . .	14
1.1.1.5 Hypergraphs . . . . .	16
1.1.1.6 Sheaf . . . . .	18
1.1.2 Grammar and Parsing . . . . .	20
1.1.2.1 BNF . . . . .	20
1.1.2.2 Dynamic Grammar . . . . .	20
1.1.2.3 Description Logics . . . . .	21
1.1.3 Ontologies and their Languages . . . . .	21
1.2 Self . . . . .	22
1.2.1 Knowledge Structure . . . . .	23
1.2.1.1 Consequences . . . . .	23
1.2.1.2 Native properties . . . . .	24
1.2.2 Syntax . . . . .	26
1.2.3 Dynamic Grammar . . . . .	27
1.2.3.1 Containers . . . . .	28
1.2.3.2 Parameters . . . . .	29
1.2.3.3 Operators . . . . .	29
1.2.4 Contextual Interpretation . . . . .	30
1.2.4.1 Naming and Scope . . . . .	30
1.2.4.2 Instanciation identification . . . . .	31
1.2.5 Structure as a Definition . . . . .	31
1.2.5.1 Quantifiers . . . . .	31
1.2.5.2 Inferring Native Properties . . . . .	33

1.2.6	Extended Inference Mechanisms . . . . .	34
1.2.6.1	Type Inference . . . . .	35
1.2.6.2	Instanciation . . . . .	35
1.3	Perspectives . . . . .	35
1.3.1	Literal definition using Peano's axioms . . . . .	35
1.3.2	Advanced Inference . . . . .	37
1.3.3	Queries . . . . .	37
<b>2</b>	<b>General Planning Framework</b>	<b>38</b>
2.1	Illustration . . . . .	38
2.2	Formalism . . . . .	40
2.2.1	Planning domain . . . . .	41
2.2.1.1	Fluents . . . . .	41
2.2.1.2	Actions . . . . .	43
2.2.1.3	Domain . . . . .	43
2.2.2	Planning problem . . . . .	44
2.2.2.1	Solution . . . . .	44
2.2.2.2	Problem . . . . .	45
2.2.3	Planning algorithm . . . . .	45
2.2.3.1	Search space . . . . .	45
2.2.3.2	Diversity . . . . .	46
2.2.3.3	Temporality . . . . .	46
2.2.3.4	General planner . . . . .	46
2.3	Classical Formalisms . . . . .	47
2.3.1	State-transition planning . . . . .	48
2.3.2	Plan space planning . . . . .	48
2.3.3	Case based planning . . . . .	49
2.3.4	Probabilistic planning . . . . .	49
2.3.5	Hierarchical planning . . . . .	49
2.4	Existing Languages and Frameworks . . . . .	50
2.4.1	Classical . . . . .	50
2.4.2	Temporality oriented . . . . .	53
2.4.2.1	PDDL+ . . . . .	53
2.4.3	Probabilistic . . . . .	53
2.4.3.1	PPDDL . . . . .	54
2.4.3.2	RDDL . . . . .	54
2.4.4	Multi-agent . . . . .	55
2.4.4.1	MAPL . . . . .	55
2.4.4.2	MA-PDDL . . . . .	56
2.4.5	Hierarchical . . . . .	56
2.4.5.1	UMCP . . . . .	56
2.4.5.2	SHOP2 . . . . .	57
2.4.5.3	HDDL . . . . .	58
2.4.5.4	HPDDL . . . . .	59
2.4.6	Ontological . . . . .	59
2.4.6.1	WebPDDL . . . . .	59
2.4.6.2	OPT . . . . .	60

2.5	Color and general planning representation . . . . .	61
2.5.1	Framework . . . . .	61
2.5.2	Example domain . . . . .	62
2.5.3	Differences with PDDL . . . . .	62
<b>3</b>	<b>Online and Flexible Planning Algorithms</b>	<b>64</b>
3.1	Existing Algorithms . . . . .	64
3.1.1	Plan Space Planning . . . . .	64
3.1.1.1	Existing PSP planners . . . . .	64
3.1.1.2	Definitions . . . . .	65
3.1.2	Plan repair . . . . .	65
3.1.3	HTN . . . . .	65
3.2	Lollipop . . . . .	66
3.2.1	Operator Graph . . . . .	66
3.2.2	Negative Refinements . . . . .	67
3.2.3	Usefulness Heuristic . . . . .	69
3.2.4	Algorithm . . . . .	71
3.2.5	Theoretical and Empirical Results . . . . .	71
3.2.5.1	Proof of Soundness . . . . .	72
3.2.5.2	Proof of Completeness . . . . .	73
3.2.5.3	Experimental Results . . . . .	74
3.3	HEART . . . . .	76
3.3.1	Domain Compilation . . . . .	76
3.3.2	Abstraction in POP . . . . .	76
3.3.3	Planning in cycle . . . . .	77
3.3.4	Properties of Abstract Planning . . . . .	78
3.3.5	Computational Profile . . . . .	79
3.4	Planning Improvements . . . . .	81
3.4.1	Heuristics using Semantics . . . . .	81
3.4.2	Macro-Action learning . . . . .	81
3.5	Recognition . . . . .	81
3.5.1	Existing approaches . . . . .	81
3.5.2	Rico . . . . .	81
3.5.2.1	Probabilities and approximations . . . . .	81
<b>4</b>	<b>Conclusion</b>	<b>82</b>
	<b>Apendix</b>	<b>83</b>
	<b>References</b>	<b>84</b>

## **Acknowledgements**



# **Introduction**

## **0.1 Thesis Context**

## **0.2 Motivations**

### **0.2.1 Observation**

### **0.2.2 Abstraction**

### **0.2.3 Cognition**

## **0.3 Issues**

## **0.4 Contributions**

## **0.5 Plan**

# 1 Knowledge Representation

**SAMIR:**

- Cite slow start 1.2
- System : implmentation -> Model : theory
- Examples
- theorems or not
- $s : D \rightarrow D$  notation in table
- Double arrow too for  $\pm$
- to port : porter une notion in smth
- 1.2.2 : criterion
- Example of parsing
- 1.2.6.1 : light defeasible logic
- lacks properties and proofs: what are the advantages ?
- **TODO:** Chap 1 🕒

Knowledge representation is at the intersection of maths, logic, language and computer sciences. Its research starts at the end of the 19<sup>th</sup> century, with Cantor inventing set theory (Cantor [1874](#)). Then after a crisis in the beginning of the 20<sup>th</sup> century with Russel's paradox and Gödel's incompleteness theorem, revised versions of the set theory become one of the foundations of mathematics. The most accepted version is the Zermelo-Fraenkel axiomatic set theory with the axiom of Choice (ZFC) (Fraenkel *et al.* [1973](#), vol. 67; Ciesielski [1997](#)). This effort leads to a formalization of mathematics itself, at least to a certain degree.

Knowledge description systems rely on syntax to interoperate systems and users to one another. The base of such languages comes from the formalization of automated grammars by Chomsky ([1956](#)). It mostly consists of a set of hierarchical rules aiming to deconstruct an input string into a sequence of terminal symbols. This deconstruction is called parsing and is a common operation in computer science. More tools for the characterization of computer language emerged soon after thanks to Backus ([1959](#)) while working on a programming language at IBM. This is how the Backus-Naur Form (BNF) metalanguage was created on top of Chomsky's formalization.

A similar process happened in the 1970's, when logic based knowledge representation gained popularity among computer scientists (Baader [2003](#)). Systems at the time explored notions such as rules and networks to try and organize knowledge into a rigorous structure. At the same time other systems were built based on First Order Logic (FOL). Then, around the 1990's, the research began to merge in search of common semantics in what led to the development of Description Logics (DL). This domain is expressing knowledge as a hierarchy of classes containing individuals.

From there and with the advent of the world wide web, engineers were on the lookout for standardization and interoperability of computer systems. One such standardization took the name of "semantic web" and aimed to create a widespread network of connected services sharing knowledge between one another in a common language. At the beginning of the 21<sup>st</sup> century, several languages were created, all based on the World Wide Web Consortium (W3C) specifications called Resource Description Framework

Table 1.1: List of classical symbols for logic.

Symbol	Description
$=, \neq$	Equal and not equal.
$e : ?(e)$	The colon is a separator to be read as “such that”. Also used for typing.
$\top, \perp$	Top and bottom symbols used as true and false respectively.
$?(e)$	Predicate over $e$ .
$\neg, \wedge, \vee, \times$	Negation (not), conjunction (and), disjunction (logical or) and either.
$\vdash$	Entails, used for logical implication and consequence.
$\forall, \exists, \exists!, \nexists, \S$	Universal, existential, uniqueness, exclusive and solution quantifiers.
$[?(e)]$	Iverson’s brackets: $[\perp] = 0$ and $[\top] = 1$ .

(RDF) (Klyne and Carroll 2004). This language is based on the notion of statements as triples. Each can express a unit of knowledge. All the underlying theoretical work of DL continued with it and created more expressive derivatives. One such derivative is the family of languages called Web Ontology Language (OWL) (Horrocks *et al.* 2003). Ontologies and knowledge graphs are more recent names for the representation and definition of categories (DL classes), properties and relation between concepts, data and entities.

All these tools are the base for all modern knowledge representations. In the rest of this chapter, we discuss the fundamentals of each of the aspects of knowledge description, then we propose a knowledge description framework that is able to adapt to its usage.

## 1.1 Fundamentals

First, we present the list of notations in this document. While trying to stick to traditional notations, we also aim for an unambiguous symbols across several domains while remaining concise and precise.

### 1.1.1 Foundation of maths and logic systems

In order to understand knowledge representation, some mathematical and logical tools need to be presented.

#### 1.1.1.1 First Order Logic

The first mathematical notion we define is logic. More precisely First Order Logic (FOL) in the context of DL. All notations are presented in table 1.1. FOL is based on boolean logic with the two values  $\top$  *true* and  $\perp$  *false* along with the classical boolean operators  $\neg$  *not*,  $\wedge$  *and* and  $\vee$  *or*. These are defined in the following way :

- $\neg\top = \perp$ , not true is the same as false.
- $a \wedge b \vdash (a = b = \top)$ ,  $a$  and  $b$  is true when they are both simultaneously true.
- $\neg(a \vee b) \vdash (a = b = \perp)$ ,  $a$  or  $b$  is true if both variables are not false.

With  $\vdash$  being the logical implication also called entailment and  $=$  being the identity relation. When combining logical operators with boolean variables, we form *expressions* also called formulas. These expressions can be evaluated given an interpretation of the variable to return a boolean value. Any function that returns a boolean is called a *predicate* (noted  $?(e)$ ). Relations that takes an expression as parameter are called *modifiers*. FOL introduce a useful kind of modifier used to generalize expressions:

Table 1.2: List of classical symbols and syntax for sets.

Symbol	Description
$\emptyset$	Empty set, also noted $\{\}$ .
$e \in \mathcal{S}$	Element $e$ is a member of set $\mathcal{S}$ .
$\subset, \cup, \cap, \setminus, \times$	Set inclusion, union, intersection, difference and cartesian product.
$ \mathcal{S} $	Cardinal (number of elements) of set $\mathcal{S}$ .
$\{e : ?(e)\}$	Set builder notation, set of all $e$ such that $?(e)$ is true.
$\wp(\mathcal{S})$	Powerset: set of all subsets of $\mathcal{S}$ .

*quantifiers*. Quantifiers can specify restriction on a variable. These restrictions forces the expression to be true in specific cases depending on the quantifier used.

The classical quantifiers includes the following:

- The *universal quantifier*  $\forall$  meaning “for all”.
- The *existential quantifier*  $\exists$  meaning “it exists”.
- The *uniqueness quantifier*  $\exists!$  meaning “it exists a unique”.
- The *exclusive quantifier*  $\nexists$  meaning “it doesn’t exist”.
- The *solution quantifier*  $\S$  meaning “those” (Hegner 2012).

The last three quantifiers are optional in FOL but will be conducive later on. It is interesting to note that most quantified expression can be expressed using the set builder notation discussed in the following section.

### 1.1.1.2 Set Theory

Since we need to represent knowledge, we will handle more complex data than simple booleans. At the beginning of his funding work on set theory, Cantor wrote:

“A set is a gathering together into a whole of definite, distinct objects of our perception or of our thought—which are called elements of the set.”  
George Cantor (1895)

For Cantor, a set is a collection of concepts and percepts. We define a set using the notations in table 1.2.

**Definition 1 (Set).** A collection of *distinct* objects considered as an object in its own right. We define a set one of two ways (always using braces):

- In extension by listing all the elements in the set:  $\{0, 1, 2, 3, 4\}$
- In intension by specifying the rule that all elements follow:  $\{n : n \in \mathbb{N} \wedge (n \leq 4)\}$

The member relation is noted  $e \in \mathcal{S}$  to indicate that  $e$  is an element of  $\mathcal{S}$ . We note  $\mathcal{S} \subset \mathcal{T} \vdash ((e \in \mathcal{S} \vdash e \in \mathcal{T}) \wedge \mathcal{S} \neq \mathcal{T})$ , that a set  $\mathcal{S}$  is a proper subset of a more general set  $\mathcal{T}$ .

We also define the union, intersection and difference as following:

- $\mathcal{S} \cup \mathcal{T} = \{e : e \in \mathcal{S} \vee e \in \mathcal{T}\}$
- $\mathcal{S} \cap \mathcal{T} = \{e : e \in \mathcal{S} \wedge e \in \mathcal{T}\}$
- $\mathcal{S} \setminus \mathcal{T} = \{e : e \in \mathcal{S} \wedge e \notin \mathcal{T}\}$

An interesting way to visualize relationships with sets is by using Venn diagrams. In figure 1.1 we present the classical set operations.

These diagrams have a lack of expressivity regarding complex operations on sets. Indeed, from their planar form it is complicated to express numerous sets having intersection and disjunctions. One

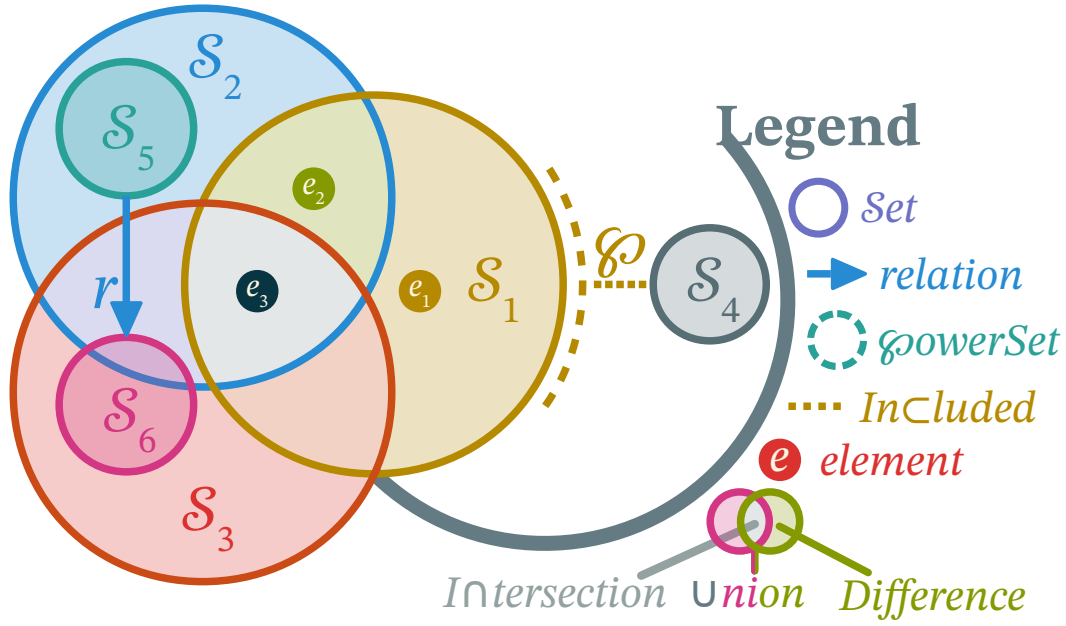


Figure 1.1: Example of Venn diagram to illustrate operations on sets.

example is the cartesian product that is defined as  $\mathcal{S} \times \mathcal{T} = \{\langle e_s, e_t \rangle : e_s \in \mathcal{S} \wedge e_t \in \mathcal{T}\}$ .

We can also define the set power recursively by  $\mathcal{S}^1 = \mathcal{S}$  and  $\mathcal{S}^n = \mathcal{S} \times \mathcal{S}^{n-1}$ .

The most common axiomatic set theory is ZFC. In that definition of sets there are a few notions that comes from its axioms. By being able to distinguish elements in the set from one another we assert that elements have an identity and we can derive equality from there:

**Axiom (Extensionality).**  $\forall \mathcal{S} \forall \mathcal{T} : \forall e ((e \in \mathcal{S}) = (e \in \mathcal{T})) \vdash \mathcal{S} = \mathcal{T}$

Another axiom of ZFC that is crucial in avoiding Russel's paradox ( $\mathcal{S} \in \mathcal{S}$ ) is the following:

**Axiom (Foundation).**  $\forall \mathcal{S} : (\mathcal{S} \neq \emptyset \vdash \exists \mathcal{T} \in \mathcal{S}, (\mathcal{T} \cap \mathcal{S} = \emptyset))$

This axiom uses the empty set  $\emptyset$  (also noted  $\{\}$ ) as the set with no elements. Since two sets are equals if and only if they have precisely the same elements, the empty set is unique.

The definition by intention uses *set builder notation* to define a set. It is composed of an expression and a predicate  $?$  that will make any element  $e$  in a set  $\mathcal{T}$  satisfying it part of the resulting set  $\mathcal{S}$ , or as formulated in ZFC:

**Axiom (Specification).**  $\forall ? \forall \mathcal{T} \exists \mathcal{S} : (\forall e \in \mathcal{S} : (e \in \mathcal{T} \wedge ?(e)))$

The last axiom of ZFC we use is to define the power set  $\wp(\mathcal{S})$  as the set containing all subsets of a set  $\mathcal{S}$ :

**Axiom (Power set).**  $\wp(\mathcal{S}) = \{\mathcal{T} : \mathcal{T} \subseteq \mathcal{S}\}$

With the symbol  $\mathcal{S} \subseteq \mathcal{T} \vdash (\mathcal{S} \subset \mathcal{T} \vee \mathcal{S} = \mathcal{T})$ . These symbols have an interesting property as they are often used as a partial order over sets.

### 1.1.1.3 Relational algebra

From set theory, it is possible to add relations between sets.

Table 1.3: List of classical symbols and syntax for relational algebra.

Symbol	Description
$f \circ g$	Function composition also noted $g(f(x))$
$\sigma, \pi$	Selection and projection of a relation.
$\langle e_1, e_2, e_n \rangle$	$n$ -uple also called a relation.
$\mathcal{S} \rightarrow \mathcal{S}$	Association relation. Used for graph edges and domain definition.
$e \mapsto f(e)$	Substitution relation.

Table 1.4: List of classical symbols and syntax for graphs.

Symbol	Description
$g = (V, E)$	Graph $g$ with set of vertices $V$ and edges $E$ .
$\phi^{\pm n *}(e v)$	Incidence (edge) and adjacence (vertex) function for graphs:
$\phi$	• A tuple or set representing the edge or all adjacent edges of a vertex.
$\phi^-$	• Source vertex (subject) or set of all incoming edges of a vertex.
$\phi^+$	• Target vertex (object) or set of all outgoing edges of a vertex.
$\phi^0$	• Label of edges and vertex : property of a statement or cause of a causal link.
$\chi(g)^+$	Transitive closure of graph $g$ .
$\div$	Graph quotient.

**Definition 2 (Relation).** A relation is effectively a subset of the cartesian product between several sets:  $r = \sigma_{\mathcal{G}}(\times_{i=1}^n \mathcal{S}_i)$  with  $\sigma$  being the selection relation and  $n$  being the *arity* of the relation  $r$ .

It can also be noted as a set of tuples each noted  $\langle e_1, e_2, e_n \rangle$ .

We need to define some special relations often used for set manipulation:

- The **substitution** that replace a variable in an expression  $e$  such that:  $(e \mapsto f(e))(e(e)) = e(f(e))$ . The substitution is often used for function definition.
- The **selection** that selects elements given a predicate  $?$  such that:  $\sigma_?(S) = \{e : ?(e) \wedge e \in S\}$ . The choice selection  $\sigma_i(S)$  is a non deterministic choice of one element in  $S$ .
- The **projection** that merges elements of a set given a filter  $f$  such that:  $\pi_f(S) = \{f(e) : e \in S\}$ . The default projection uses the identity relation  $=$  instead of  $f$ .

Functions are a special case of relations that takes as value the selected element of the last set. We note them  $f : (\times_{i=1}^{n-1} \mathcal{S}_i) \rightarrow \mathcal{S}_n$ . The set  $\times_{i=1}^{n-1} \mathcal{S}_i$  is called the *domain* of the function  $\mathcal{D}(f)$  and the set  $\mathcal{S}_n$  is called the *codomain*  $\mathcal{D}^{-1}(f)$ . The number  $n - 1$  is called the *degree* of the function.

We can combine functions using the *function composition operator*  $g \circ f = x \mapsto g(f(x))$ . The functional power of  $f$  noted  $f^n$  is defined recursively as :

- $f^0 = x \mapsto x, f^1 = x \mapsto f(x)$  and  $f^{-1} = f(x) \mapsto x$
- $f^n = f \circ f^{n+[n<0]-[n>0]}$  with  $[?(n)]$  being an Iverson bracket ( $[T] = 1$  and  $[F] = 0$ ).

#### 1.1.1.4 Graphs

Next in line, we need to define a few notions of graph theory.

**Definition 3 (Graph).** A graph is a mathematical structure  $g = (V, E)$  consisting of vertices  $V$  (also called nodes) and edges  $E$  (arcs) that links two vertices together. Each edge is basically a pair of vertices ordered or not depending on if the graph is directed or not. We can write  $E = \sigma_{\mathcal{G}}(V^2)$

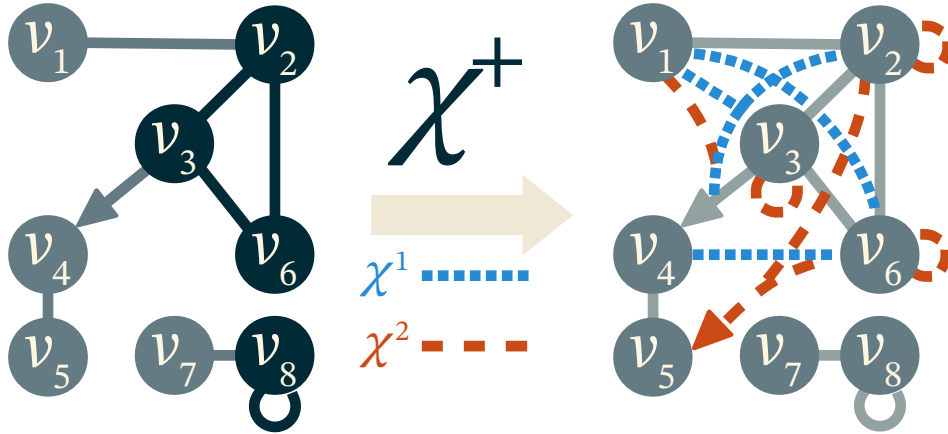


Figure 1.2: Example of the recursive application of the transitive cover to a graph.

A graph is often represented with lines or arrows linking points together like illustrated in figure 1.2. In that figure, the vertices  $v_1$  and  $v_2$  are connected through an undirected edge. Similarly  $v_3$  connects to  $v_4$  but not the opposite since they are bonded with a directed edge. The vertex  $v_8$  is also connected to itself.

From that definition, some other relations are needed to express most properties of graphs. In the following, the signed symbol only applies to directed graphs.

We provide graphs with an adjacence function  $\phi$  over any vertex  $v \in V$  such that:

- $\phi(v) = \{e : e \in E \wedge v \in e\}$
- $\phi^+(v) = \{\langle v \rightarrow v' \rangle \in E : v' \in V\}$  and  $\phi^-(v) = \{\langle v' \rightarrow v \rangle \in E : v' \in V\}$

This relation gives the set of incoming or outgoing edges from any vertex. In non directed graphs, the relation gives edges adjacent to the vertex. For example: in figure 1.2,  $\phi(v_1) = \{\langle v_1, v_2 \rangle\}$ . In that example, using directed graph notation we can note  $\phi^+(v_3) = \{\langle v_3 \rightarrow v_4 \rangle\}$ .

Using types, it is possible to reuse the same symbol to define an incidence function over any edges  $e = \langle v, v' \rangle$  such that:

- $\phi(e) = \langle v, v' \rangle$
- $\phi^-(e) = v$  and  $\phi^+(e) = v'$

Most of the intrinsic information of a graph is contained within its structure. Exploring its properties require to study the "shape" of a graph and to find relationships between vertices. That is why graph properties are easier to explain using the *transitive cover*  $\chi^+$  of any graph  $g = (V, e)$  defined as follows:

- $\chi(g) = (V, e') : e' = e \cup \{\langle v_1, v_3 \rangle : \{\langle v_1, v_2 \rangle, \langle v_2, v_3 \rangle\} \subset e\}$
- $\chi^+ = \chi^\infty$

This transitive cover will create another graph in which two vertices are connected through an edge if and only if it exists a path between them in the original graph  $g$ . We illustrate this process in figure 1.2. Note how there is no edge in  $\chi(g)$  between  $v_5$  and  $v_6$  and the one in  $\chi^2(g)$  is directed towards  $v_5$  because there is no path back to  $v_6$  since the edge between  $v_3$  and  $v_4$  is directed.

**Definition 4 (Path).** We say that vertices  $v_1$  and  $v_2$  are *connected* if it exists a path from one to the other. Said otherwise, there is a path from  $v_1$  to  $v_2$  if and only if  $\langle v_1, v_2 \rangle \in E_{\chi^+(g)}$ .

The notion of connection can be extended to entire graphs. An undirected graph  $g$  is said to be *connected* if and only if  $\forall e \in V^2 (e \in E_{\chi^+(g)})$ .

Similarly we define *cycles* as the existence of a path from a given vertex to itself. For example, in figure 1.2, the cycles of the original graph are colored in blue. Some graphs can be strictly acyclical, enforcing the absence of cycles.

A **tree** is a special case of a graph. A tree is an acyclical connected graph. If a special vertex called a *root* is chosen we call the tree a *rooted tree*. It can then be a directed graph with all edge pointing away from the root. When progressing away from the root, we call the current vertex *parent* of all exterior *children* vertices. Vertex with no children are called *leaves* of the tree and the rest are called *branches*.

An interesting application of trees to FOL is called *and/or trees* where each vertex has two sets of children: one for conjunction and the other for disjunction. Each vertex is a logic formula and the leaves are atomic logic propositions. This is often used for logic problem reduction. In figure 1.3 we illustrate how and/or trees are often depicted.

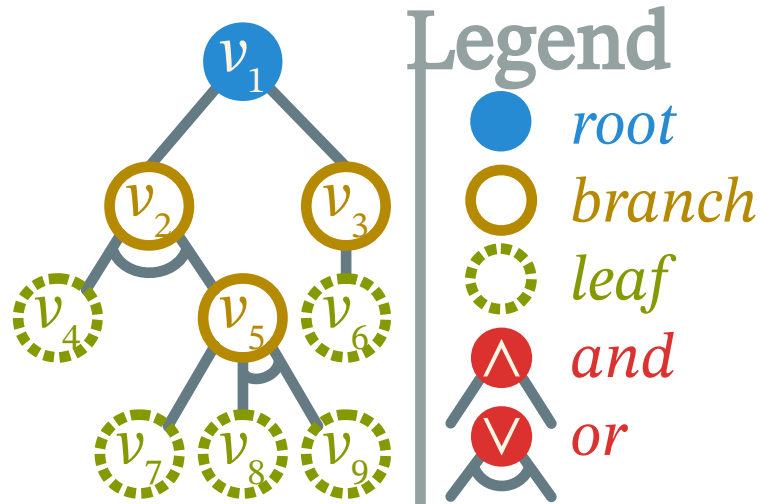


Figure 1.3: Example of and/or tree.

Another notion often used for reducing big graphs is the quotienting as illustrated in figure 1.4.

**Definition 5 (Graph Quotient).** A quotient over a graph is the act of reducing a subgraph into a node while preserving the external connections. All internal structure becomes ignored and the subgraph now acts like a regular node. We note it  $\div_f(g) = (\pi_f(V), \{\pi_f(e) : e \in E\})$  with  $f$  being a function that maps any vertex either toward itself or toward its quotiented vertex.

We can also combine several graphs into one using fusion:  $g_1 + g_2 = (V_1 \cup V_2, E_1 \cup E_2)$ .

#### 1.1.1.5 Hypergraphs

A generalization of graphs are **hypergraphs** where the edges are allowed to connect to more than two vertices. They are often represented using Venn-like representations but can also be represented with



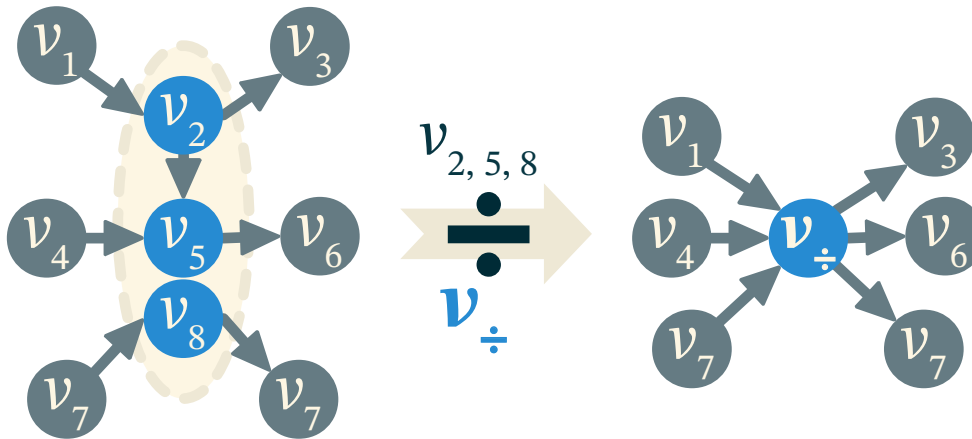


Figure 1.4: Example of graph quotient.

edges “gluing” several vertex like in figure 1.5.

An hypergraph is said to be  $n$ -uniform if the edges are restricted to connect to only  $n$  vertices together. In that regard, classical graphs are 2-uniform hypergraphs.

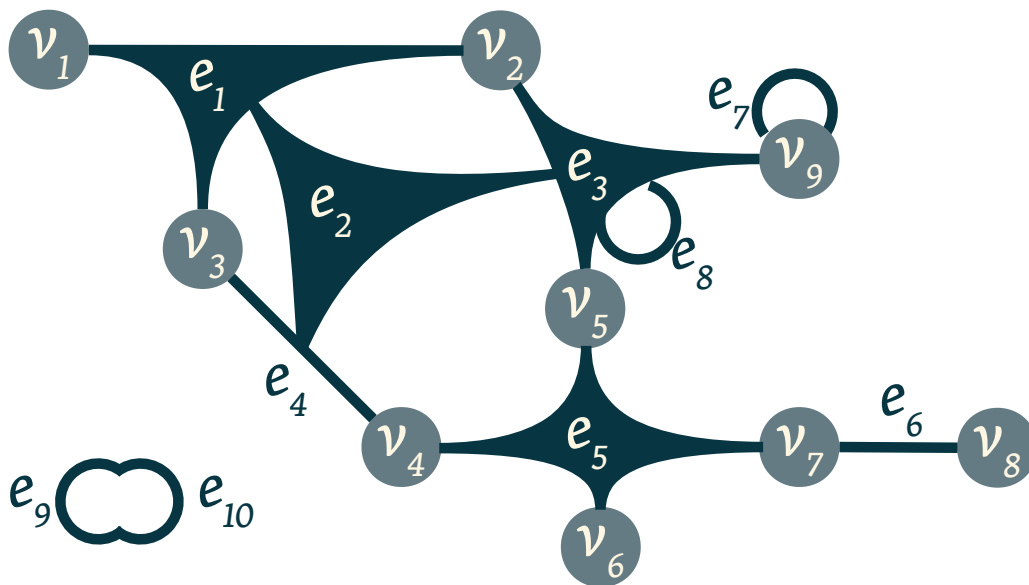


Figure 1.5: Example of hypergraph with total freedom on the edges specification.

Hypergraphs have a special case where  $E \subset V$ . This means that edges are allowed to connect to other edges. In figure 1.5, this is illustrated by the edge  $e_3$  connecting to three other edges. Information about these kinds of structures for knowledge representation is hard to come by and rely mostly on a form of “folk wisdom” within the mathematics community where knowledge is rarely published and mostly transmitted orally during lessons. One of the closest information available is this forum post (Kovitz 2018) that associated this type of graph to port graphs (Silberschatz 1981). Additional information was

Table 1.5: List of symbols and syntax for sheaves.

Symbol	Description
$\bullet, *, \leadsto$	Germ, seed and connector.
$\mathcal{F}$	Sheaf (from French <i>faisceau</i> ).

found in the form of a contribution of Vepstas (2008) on an encyclopedia article about hypergraphs. In that contribution, he says that a generalization of hypergraph allowing for edge-to-edge connections violate the axiom of **Foundation** of ZFC by allowing edge-loops. Indeed, like in figure 1.5, an edge  $e_9 = \{e_{10}\}$  can connect to another edge  $e_{10} = \{e_9\}$  causing an infinite descent inside the  $\in$  relation in direct contradiction with ZFC.

This shows the limits of standard mathematics especially on the field of knowledge representation. Some structures needs higher dimensions than allowed by the one-dimensional structure of ZFC and FOL. However, it is important not to be mistaken: such non-standard set theories are more general than ZFC and therefore contains ZFC as a special case. All is a matter of restrictions.

#### 1.1.1.6 Sheaf

In order to understand sheaves, we need to present a few auxiliary notions. Most of these definitions are adapted from (Vepstas 2008). The first of which is a seed.

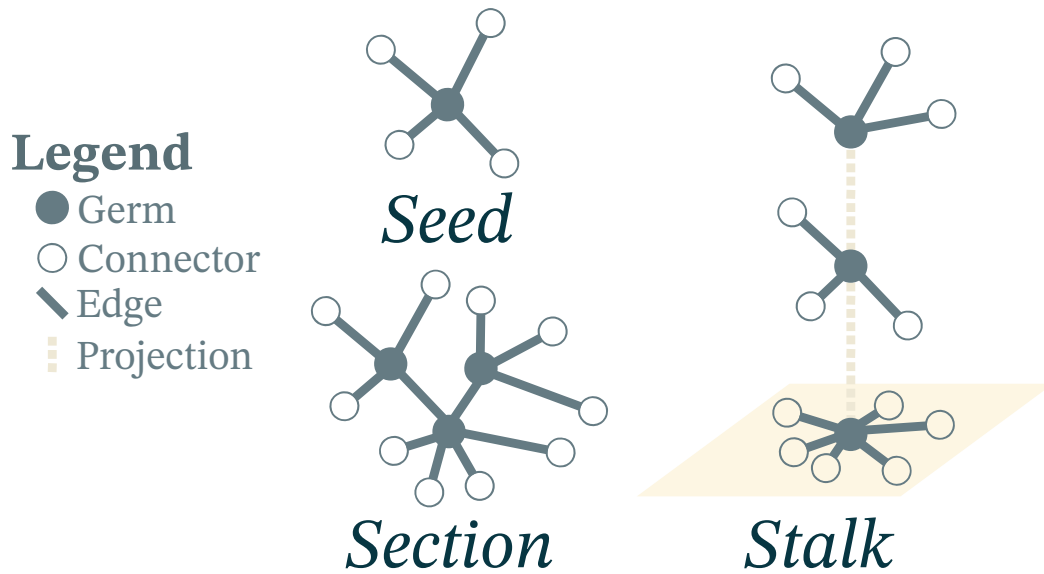


Figure 1.6: Example of a seed, a section and a stalk.

**Definition 6 (Seed).** A seed corresponds to a vertex along with the set of adjacent edges. Formally we note a seed  $\star = (\bullet, \phi_g(\bullet))$  that means that a seed build from the vertex  $\bullet$  in the graph  $g$  contains a set of adjacent edges  $\phi_g(\bullet)$ . We call the vertex  $\bullet$  the *germ* of the seed. The edges in a seed does not connect to the other vertices but keep the information and are able to match the correct vertices through typing (often a type of a single individual). We call the edges in a seed *connectors*.

Seeds are extracts of graphs that contains all information about a vertex. Illustrated in the figure 1.6,

seeds have a central germ (represented with discs) and connectors leading to a typed vertex (outlined circles). Those external vertices are not directly contained in the seed but the information about what vertex can fit in them is kept. It is useful to represent connectors like jigsaw puzzle pieces: they can match only a restricted number of other pieces that match their shape.

From there, it is useful to build a kind of partial graph from seeds called sections.

**Definition 7** (Section). A section is a set of seeds that have their common edges connected. This means that if two seeds have an edge in common connecting both germs, then the seeds are connected in the section and the edges are merged. We note  $g_* = (\bullet, \circ)$  the graph formed by the section.

In figure 1.6, a section is represented. It is a connected section composed of seeds along with the additional seeds of any vertices they have in common. They are very similar to subgraph but with an additional border of typed connectors. This tool was originally mostly meant for big data and categorization over large graphs. As graph quotient is often used in that domain, it was ported to sections instead of graphs allows us to define stalks.

**Definition 8** (Stalk). Given a projection function  $f : \bullet \rightarrow \bullet'$  over the germs of a section  $\star$ , the stalk above the vertex  $\bullet' \in \bullet'$  is the quotient of all seeds that have their germ follow  $f(\bullet) = \bullet'$ .

The quotienting is used in stalks for their projection. Indeed, as shown in figure 1.6, the stalks are simply a collection of seeds with their germs quotiented into their common projection. The projection can be any process of transformation getting a set of seeds in one side and gives object in any base space called the image. Sheaves are a generalization of this concept to sections.

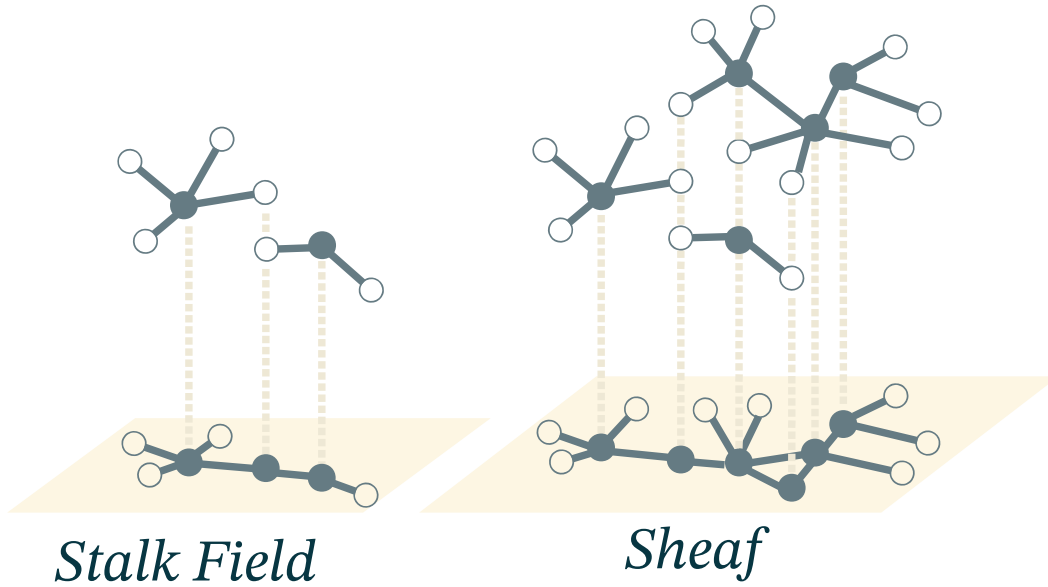


Figure 1.7: Example of sheaves.

**Definition 9** (Sheaf). A sheaf is a collection of sections, together with a projection. We note it  $\mathcal{F} = \langle G_*, \pi_g \rangle$  with the function  $g$  being the gluing axioms that the projection should respect depending on the application. The projected sheaf graph is noted  $g_{\mathcal{F}} = \sum_{g_* \in G_*} \div_g(g_*)$  as the fusion of all quotiented sections.

By merging common vertices into a section, we can build stack fields. These fields are simply a subcategory of sheaves. Illustrated in figure 1.7, a sheaf is a set of section with a projection relation.

## 1.1.2 Grammar and Parsing

Grammar is an old tool that used to be dedicated to linguists. With the funding works by Chomsky and his Context-Free Grammars (CFG), these tools became available to mathematicians and shortly after to computer scientists.

A CFG is a formal grammar that aims to generate a formal language given a set of hierarchical rules. Each rule is given a symbol as a name. From any finite input of text in a given alphabet, the grammar should be able to determine if the input is part of the language it generates.

### 1.1.2.1 BNF

In computer science, popular metalanguage called BNF was created shortly after Chomsky's work on CFG. The syntax is of the following form :

```
1 <rule> ::= <other_rule> | <terminal_symbol> | "literals"
```

A terminal symbol is a rule that does not depend on any other rule. It is possible to use recursion, meaning that a rule will use itself in its definition. This actually allows for infinite languages. Despite its expressive power, BNF is often used in one of its extended forms.

In this context, we present a widely used form of BNF syntax that is meant to be human readable despite not being very formal. We add the repetition operators `*` and `+` that respectively repeat 0 and 1 times or more the preceding expression. We also add the negation operator `~` that matches only if the following expression does not match. We also add parentheses for grouping expression and brackets to group literals.

### 1.1.2.2 Dynamic Grammar

A regular grammar is static, it is set once and for all and will always produce the same language. In order to be more flexible we need to talk about dynamic grammars and their associated tools.

One of the main tools for both static and dynamic grammar is a parser. It is the program that will interpret the input into whatever usage it is meant for. Most of the time, a parser will transform the input into another similarly structured language. It can be a storage inside objects or memory, or compiled into another format, or even just for syntax coloration. Since a lot of usage requires the same kind of function, a new kind of tool emerged to make the creation of a parser simpler. We call those tools parser or compiler generators (Paulson 1982). They take a grammar description as input and gives the program of a parser of the generated language as an output.

For dynamic grammar, these tools can get more complicated. There are a few ways a grammar can become dynamic. The most straightforward way to make a parser dynamic is to introduce code in the rule handling that will tweak variables affecting the parser itself (Souto *et al.* 1998). This allows for handling context in CFG without needing to rewrite the grammar.

Another kind of dynamic grammar is grammar that can modify themselves. In order to do this a grammar is valuated with reified objects representing parts of itself (Hutton and Meijer 1996). These parts can be modified dynamically by rules as the input gets parsed (Renggli *et al.* 2010; Alessandro and Piumarta 2007). This approach uses Parsing Expression Grammars (PEG)(Ford 2004) with Packrat parsing that Packrat parsing backtracks by ensuring that each production rule in the grammar is not tested more than

once against each position in the input stream (Ford 2002). While PEG is easier to implement and more efficient in practice than their classical counterparts (Loff *et al.* 2018; Henglein and Rasmussen 2017), it offset the computation load in memory making it actually less efficient in general (Becket and Somogyi 2008).

Some tools actually just infer entire grammars from inputs and software (Hörschele and Zeller 2017; Grünwald 1996). However, these kinds of approaches require a lot of input data to perform well. They also simply provide the grammar after expensive computations.

### 1.1.2.3 Description Logics

One of the most standard and flexible way of representing knowledge for databases is by using ontologies. They are based mostly on the formalism of Description Logics (DL). It is based on the notion of classes (or types) as a way to make the knowledge hierarchically structured. A class is a set of individuals that are called instances of the classes. Classes got the same basic properties as sets but can also be constrained with logic formula. Constraints can be on anything about the class or its individuals. Knowledge is also encoded in relations that are predicates over attributes of individuals.

It is common when using DLs to store statements into three boxes (Baader 2003):

- The TBox for terminology (statements about types)
- The RBox for rules (statements about properties) (Bürckert 1994)
- The ABox for assertions (statements about individual entities)

These are used mostly to separate knowledge about general facts (intentional knowledge) from specific knowledge of individual instances (extensional knowledge). The extra RBox is for “knowhow” or knowledge about entity behavior. It restricts usages of roles (properties) in the ABox. The terminology is often hierarchically ordered using a subsumption relation noted  $\sqsubseteq$ . If we represent classes or type as a set of individuals then this relation is akin to the subset relation of set theory.

There are several versions and extensions of DL. They all vary in expressivity. Improving the expressivity of DL system often comes at the cost of less efficient inference engines that can even become undecidable for some extensions of DL.

### 1.1.3 Ontologies and their Languages

Most AI problem needs a way to represent data. The classical way to represent knowledge has been more and more specialized for each AI community. Each their Domain Specific Language (DSL) that neatly fit the specific use it is intended to do. There was a time when the branch of AI wanted to unify knowledge description under the banner of the “semantic web”. From numerous works, a repeated limitation of the “semantic web” seems to come from the languages used. In order to guarantee performance of generalist inference engines, these languages have been restricted so much that they became quite complicated to use and quickly cause huge amounts of recurrent data to be stored because of some forbidden representation that will push any generalist inference engine into undecidability.

The most basic of these languages is perhaps RDF Turtle (Beckett and Berners-Lee 2011). It is based on triples with an XML syntax and has a graph as its knowledge structure (Klyne and Carroll 2004). A RDF graph is a set of RDF triples  $\langle sub, pro, obj \rangle$  which fields are respectively called subject, property and object. It can also be seen as a partially labeled directed graph  $(V, E)$  with  $V$  being the set of RDF nodes and  $E$  being the set of edges. This graph also comes with an incomplete label  $\phi^0 : (V \cup E) \rightarrow L_{String}^{URI}$

Table 1.6: List of classical symbols and syntax for self.

Symbol	Description
$\mathcal{D}, P, Q, S, T, U$	Sets for domains, properties, quantifiers, statements, types and universe.
$\mu^\pm$	Meta-relation for abstraction (+) and reification (−).
$\nu$	Name relation.
$\rho$	Parameter relation.

relation. Nodes without an URI are called blank nodes. It is important that, while not named, blank nodes have a distinct internal identifier from one another that allows to differentiate them.

Built on top of RDF, the W3C recommended another standard called OWL. It adds the ability to have hierarchical classes and properties along with more advanced description of their arity and constraints. OWL is, in a way, more expressive than RDF (Van Harmelen *et al.* 2008, vol. 1 p825). It adds most formalism used in knowledge representation and is widely used and interconnected. OWL comes in three versions: OWL Lite, OWL DL and OWL Full. The lite version is less advanced but its inference is decidable, OWL DL contains all notions of DL and the full version contains all features of OWL but is strongly undecidable.

The expressivity can also come from a lack of restriction. If we allow some freedom of expression in RDF statements, its inference can quickly become undecidable (Motik 2007). This kind of extremely permissive language is better suited for specific usage for other branches of AI. Even with this expressivity, several works still deem existing ontology system as not expressive enough, mostly due to the lack of classical constructs like lists, parameters and quantifiers that don't fit the triple representation of RDF.

One of the ways which have been explored to overcome these limitations is by adding a 4<sup>th</sup> field in RDF. This field is meant for context and annotations. This field is used for information about any statement represented as a triple, such as access rights, beliefs and probabilities, or most of the time the source of the data (Tolksdorf *et al.* 2004). One of the other uses of the fourth field of RDF is to reify statements (Hernández *et al.* 2015). Indeed by identifying each statement, it becomes possible to efficiently for statements about statements.

A completely different approach is done by Hart and Goertzel (2008) in his framework for Artificial General Intelligence (AGI) called OpenCog. The structure of the knowledge is based on a rhizome, a collection of trees, linked to one another. This structure is called Atomspace. Each vertex in the tree is an atom, leaf-vertexes are nodes, the others are links. Atoms are immutable, indexed objects. They can be given values that can be dynamic and, since they are not part of the rhizome, are an order of magnitude faster to access. Atoms and values alike are typed.

The goal of such a structure is to be able to merge concepts from widely different domains of AI. The major drawback being that the whole system is very slow compared to pretty much any domain specific software.

## 1.2 Self

As we have seen, most existing knowledge description systems have a common drawback: they are static. This means that they are either too inefficient or too specific. To fix this issue, a new knowledge representation system must be presented. The goal is to make a minimal language framework that can adapt to its use to become as specific as needed. If it becomes specific it must start from a generic base.

Since that base language must be able to evolve to fit the most cases possible, it must be neutral and simple.

To summarize, that framework must maximize the following criteria:

1. **Neutral:** Must be independent from preferences and be localization.
2. **Permissive:** Must allow as many data representation as possible.
3. **Minimalist:** Must have the minimum number of base axioms and as little native notions as possible.
4. **Adaptive:** Must be able to react to user input and be as flexible as possible.

In order to respect these requirements, we developed a framework for knowledge description. This Structurally Expressive Language Framework (SELF) is our answer to these criteria. SELF is inspired by RDF Turtle and Description Logic.

### 1.2.1 Knowledge Structure

SELF extends the RDF graphs by adding another label to the edges of the graph to uniquely identify each statement. This basically turns the system into a quadruple storage even if this forth field is transparent to the user.

**Axiom (Structure).** A SELF graph is a set of statements that transparently include their own identity. The closest representation of the underlying structure of SELF is as follows:

$$g_{\mathbb{U}} = (\mathbb{U}, S) : S = \{s = \langle sub, pro, obj \rangle : s \in \mathcal{D} \vdash s \wedge \mathcal{D}\}$$

with:

- $sub, obj \in \mathbb{U}$  being entities representing the *subject* and *object* of the *statement*  $s$ ,
- $pro \in P$  being the *property* of the statement  $s$ ,
- $\mathcal{D} \subset S$  is the *domain* of the world  $g_{\mathbb{U}}$ ,
- $S, P \subset \mathbb{U}$  with  $S$  the set of statements and  $P$  the set of properties,

This means that the world  $g_{\mathbb{U}}$  is a graph with the set of entities  $\mathbb{U}$  as vertices and the set of statements  $S$  as edges. This model also suppose that every statement  $s$  must be true if they belong to the domain  $\mathcal{D}$ . This graph is a directed 3-uniform hypergraph.

Since sheaves are a representation of hypergraphs, we can encode the structure of SELF into a sheaf-like form. Each seed is a statement, the germ being the statement vertex. It is always accompanied of an incoming connector (its subject), an outgoing connector (its object) and a non-directed connector (its property). The sections are domains and must be coherent. Each statement, along with its property, makes a stalk as illustrated in figure 1.8.

The difference with a sheaf is that the projection function is able to map the pair statement-property into a labeled edge in its projection space. We map this pair into a classical labeled edge that connects the subject to the object of the statement in a directed fashion. This results in the projected structure being a correct RDF graph.

#### 1.2.1.1 Consequences

The base knowledge structure is more than simply convenience. The fact that statements have their own identity, changes the degrees of freedom of the representation. RDF has a way to represent reified statements that are basically blank nodes with properties that are related to information about the

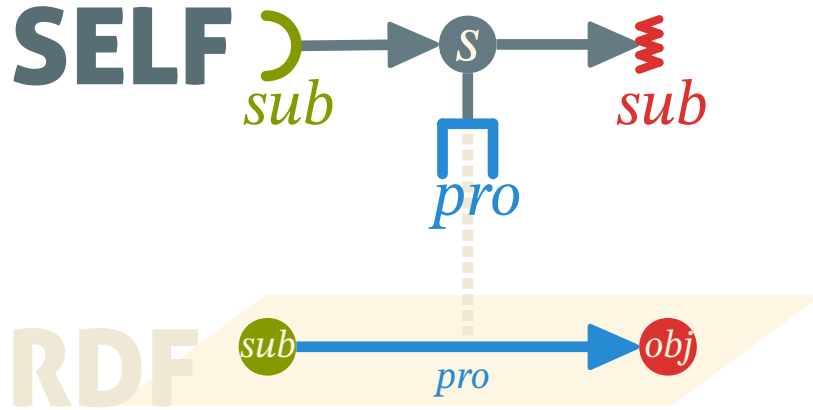


Figure 1.8: Projection of a statement from the SELF to RDF space.

subject, property and object of a designated statement. The problem is that such statements are very differently represented and need 3 regular statements just to define. Using the fourth field, it becomes possible to make statements about *any* statements. It also becomes possible to express modal logic about statements or to express, various traits like the probability or the access rights of a statement.

The knowledge structure holds several restrictions on the way to express knowledge. As a direct consequence, we can add several theorems to the logic system underlying SELF. The axiom of **Structure** is the only axiom of the system.

**Theorem 1 (Identity).** *Any entity is uniquely distinct from any other entity.*

This theorem comes from the axiom of **Extensionality** of ZFC. Indeed it is stated that a set is a unordered collection of distinct objects. Distinction is possible if and only if intrinsic identity is assumed. This notion of identity entails that a given entity cannot change in a way that would alter its identifier.

**Theorem 2 (Consistency).** *Any statement in a given domain is consistent with any other statements of this domain.*

Consistency comes from the need for a coherent knowledge database and is often a requirement of such constructs. This theorem also is a consequence of the axiom of **Structure**:  $s \in \mathcal{D} \vdash s \wedge \mathcal{D}$ .

**Theorem 3 (Uniformity).** *Any object in SELF is an entity. Any relations in SELF are restricted to  $\mathbb{U}$ .*

This also means that all native relations are closed under  $\mathbb{U}$ . This allows for a uniform knowledge database.

### 1.2.1.2 Native properties

Theorem 1 lead to the need for two native properties in the system : *equality* and *name*.

The **equality relation**  $= : \mathbb{U} \rightarrow \mathbb{U}$ , behaves like the classical operator. Since the knowledge database will be expressed through text, we also need to add an explicit way to identify entities. This identification is done through the **name relation**  $\nu : \mathbb{U} \rightarrow L_{String}$  that affects a string literal to some entities. This lead us to introduce literals into SELF that is also entities that have a native value.

The axiom of **Structure** puts a type restriction on property. Since it compartments  $\mathbb{U}$  using various named subsets, we must adequately introduce an explicit type system into SELF. That type system requires a



The theorem 3 also allows for some very interesting meta-constructs. That is why we also introduce a signed **Meta relation**  $\mu^+ : \mathbb{U} \rightarrow D$  with  $\mu^- = (\mu^+)^{-1}$ . This allows to create domain from certain entities and to encapsulate domains into entities.  $\mu^-$  is for reification and  $\mu^+$  is for abstraction. This Meta relation also allows to express value of entities, like lists or various containers.

Since axiom of **Structure** gives the structure of SELF a hypergraph shape, we must port some notions of graph theory into our framework. Introducing the **statement relation**  $\phi : S \rightarrow \mathbb{U}$  reusing the same symbol as for the adjacency and incidence relation of graphs. This isn't a coincidence as this relation has the same properties. For example,  $\phi^-(s)$  gives the subject of a statement  $s$ . Respectively,  $\phi^+$  and  $\phi^0$  give the object and property of any statement. For adjacencies,  $\phi^-$  and  $\phi^+$  can give the set of statements any entity is respectively the object and subject of. For any property  $pro$ , the notation  $\phi^0(pro)$  gives the set of statements using this property. This allows us to port all the other notions of graphs using this relation as a base.

25

## 1.2.2 Syntax

Since we need to respect the requirements of the problem, the RDF syntax cannot be used to express the knowledge. Indeed, RDF states native properties as English nodes with a specific URI that isn't neutral. It also isn't minimalist since it uses an XML syntax so verbose that it is not used for most examples in the documents that defines RDF because it is too confusing and complex (W3C 2004a; W3C 2004b). The XML syntax is also quite restrictive and cannot evolve dynamically to adapt to the usage.

So we need to define a new language that is minimalist and neutral. At the same time the language must be permissive and dynamic. These two goals are incompatible and will end up needing different solutions. So the solution to the problem is to actually define two languages that fit the criteria : one minimalist and one adaptive. The issue is that we need not make a user learn two languages and the second kind of language must be very specific and that violates the principle of neutrality we try to respect.

The only solution is to make a mechanism to adapt the language as it is used. We start off with a simple framework that uses a grammar.

The description of  $\mathcal{G}_0$  is pretty straightforward: it mostly is just a triple representation separated by whitespaces. The goal is to add a minimal syntax consistent with the axiom of [Structure](#). In listing 1.1, we give a simplified version of  $\mathcal{G}_0$ . It is written in a pseudo-BNF fashion, which is extended with the classical repetition operators  $*$  and  $+$  along with the negation operator  $\sim$ . All tokens have names in uppercase. We also add the following rule modifiers:

- $\langle \sim \text{name} \rangle$  are ignored for the parsing. However, the tokens are consumed and therefore acts like separators for the other rules.
- $\langle ? \text{name} \rangle$  are inferred rules and tokens. They play a key role for the process of derivation explained in section 1.2.3.

```
1 <~COMMENT: <INLINE: "//" (~["\n", "\r"])*>
2 | <BLOCK: "/*" (~["*/"])*> > //Ignored
3 <~WHITE_SPACE: " " | "\t" | "\n" | "\r" | "\f">
4 <LITERAL: <INT> | <FLOAT> | <CHAR> | <STRING>> //Java definition
5 <ID: <TYPE: <UPPERCASE>(<LETTERS>|<DIGITS>)* >
6 | <ENTITY: <LOWERCASE>(<LETTERS>|<DIGITS>)*>
7 | <SYMBOL: (~[<LITERALS>, <LETTERS>, <DIGITS>])*>>
8
9 <worselfld> ::= <first> <statement>* <EOF>
10 <first> ::= <subject> <?EQUAL> <?SOLVE> <?EOS>
11 <statement> ::= <subject> <property> <object> <EOS>
12 <subject> ::= <entity>
13 <property> ::= <ID> | <?meta_property>
14 <object> ::= <entity>
15 <entity> ::= <ID> | <LITERAL> | <?meta_entity>
```

Listing 1.1: Simplified pseudo-BNF description for basic SELF.

In order to respect the principle of neutrality, the language must not suppose of any regional predisposition of the user. There are few exceptions for the sake of convenience and performance. The first exception is that the language is meant to be read from left to right and have an occidental biased `subject verb object` triple description. Another exception is for liberals that use the same grammar as in classical Java. This means that the decimal separator is the dot (.). This could be fixed in later version using dynamic definitions (see section 1.3.1).

Even if sticking to the ASCII subset of characters is a good idea for efficiency, SELF can work with UTF-8 and exploits the Unicode Character Database (UCD) for its token definitions (Unicode Consortium 2018a). This means that SELF comes keywords free and that the definition of each symbol is left to the user. Each notion and symbol is inferred (with the exception of the first statement which is closer to an imposed configuration file).

In  $\mathbb{G}_0$ , the first two token definitions are ignored. This means that comments and white-spaces will act as separation and won't be interpreted. Comments are there only for convenience since they do not serve any real purpose in the language. It was arbitrarily decided to use Java-style comments. White-spaces are defined against UCD's definition of the separator category  $\text{Z\&}$  (see Unicode Consortium 2018b, chap. 4).

Line 4 uses the basic Java definition for liberals. In order to keep the independence from any natural language, boolean laterals are not natively defined (since they are English words).

Another aspect of that language independence is found starting at line 5 where the definitions of `<UPPERCASE>`, `<LOWERCASE>`, `<LETTERS>` and `<DIGITS>` are defined from the UCD (respectively categories  $\text{Lu}$ ,  $\text{Ll}$ ,  $\text{L\&}$ ,  $\text{Nd}$ ). This means that any language's upper case can be used in that context. For performance and simplicity reasons we will only use ASCII in our examples and application.

The rule at line 1 is used for the definition of three tokens that are important for the rest of the input. `<EQUAL>` is the symbol for equality and `<SOLVE>` is the symbol for the *solution quantifier* (and also the language pendant of  $\mu^-$ ). The most useful token `<EOS>` is used as a statement delimiter. This rule also permits the inclusion of other files if a string literal is used as a subject. The underlying logic of this first statement will be presented in section 1.2.5.1.

At line 11, we can see one of the most defining features of  $\mathbb{G}_0$ : statements. The input is nothing but a set of statements. Each component of the statements are entities. We defined two specific rules for the subject and object to allow for eventual runtime modifications. The property rule is more restricted in order to guarantee the non-ambiguity of the grammar.

### 1.2.3 Dynamic Grammar

The syntax we described is only valid for  $\mathbb{G}_0$ . As long as the input is conforming to these rules, the framework keeps the minimal behavior. In order to access more features, one needs to break a rule. We add a second outcome to handling with violations : **derivation**. There are several kinds of possible violations that will interrupt the normal parsing of the input :

- Violations of the `<first>` statement rule : This will cause a fatal error.
- Violations of the `<statement>` rule : This will cause a derivation if an unexpected additional token is found instead of `<EOS>`. If not enough tokens are present, a fatal error is triggered.
- Violations of the secondary rules (`<subject>`, `<entity>`, ...): This will cause a fatal error except if there is also an excess of token in the current statement which will cause derivation to happen.

Derivation will cause the current input to be analyzed by a set of meta-rules. The main restriction of these rules is given in  $\mathbb{G}_0$ : each statement must be expressible using a triple notation. This means that the goal of the meta-rules is to find an interpretation of the input that is reducible to a triple and to augment  $\mathbb{G}_0$  by adding an expression to any `<meta_*>` rules. If the input has fewer than 3 entities for a statement then the parsing fails. When there is extra input in a statement, there is a few ways the infringing input can be reduced back to a triple.

### 1.2.3.1 Containers

The first meta-rule is to infer a container. A container is delimited by at least a left and right delimiter (they can be the same symbol) and an optional middle delimiter. We infer the delimiters using the algorithm 1.

**Algorithm 1** Container meta-rule

---

```

1 function container(Token current)
2   lookahead(current, EOS) ▷ Populate all tokens of the statement
3   for all token in horizon do
4     if token is a new symbol then delimiters.append(token)
5   if length(delimiters) < 2 then
6     if coherentDelimiters(horizon, delimiters[0]) then
7       inferMiddle(delimiters[0]) ▷ New middle delimiter in existing containers
8       return Success
9     return Failure
10  while length(delimiters) > 0 do
11    for all (left, middle, right) in sortedDelimiters(delimiters) do
12      if coherentDelimiters(horizon, left, middle, right) then
13        inferDelimiter(left, right)
14        inferMiddle(middle) ▷ Ignored if null
15        delimiters.remove(left, middle, right)
16        break
17    if length(delimiters) stayed the same then return Success
18  return Success

```

---

The function sortedDelimiters at line 11 is used to generate every ordered possibility and sort them using a few criteria. The default order is possibilities grouped from left to right. All coupled delimiters that are mirrors of each other following the UCD are preferred to other possibilities.

Checking the result of the choice is very important. At line 12 a function checks if the delimiters allow for triple reduction and enforce restrictions. For example, a property cannot be wrapped in a container (except if part of parameters). This is done in order to avoid a type mismatch later in the interpretation.

Once the inference is done, the resulting calls to inferDelimiter will add the rules listed in listing 1.2 to  $\mathcal{G}_0$ . This function will create a `<container>` rule and add it to the definition of `<meta_entity>`. Then it will create a rule for the container named after the UCD name of the left delimiter (searching in the `NamesList.txt` file for an entry starting with "left" and the rest of the name or defaulting to the first entry). Those rules are added as a conjunction list to the rule `<container>`. It is worthy to note that the call to inferMiddle will add rules to the token `<MIDDLE>` independently from any container and therefore, all containers share the same pool of middle delimiters.

```

1 <meta_entity> ::= <container>
2 <container> ::= <parenthesis> | ...
3 <parenthesis> ::= "(" [<naked_entity>] (<?MIDDLE> <naked_entity>)* ")"
4 <naked_entity> ::= <statement> | <entity>

```

Listing 1.2: Rules added to the current grammar for handling the new container for parenthesis

The rule at line 4 is added once and enables the use of meta-statements inside containers. It is the language pendant of the  $\mu^+$  relation, allowing to wrap abstraction in a safe way.

### 1.2.3.2 Parameters

If the previous rule didn't fix the parsing of the statement, we continue with the following meta-rule. Parameters are extra containers that are used after an entity. Every container can be used as parameters. We detail the analysis in algorithm 2.

---

**Algorithm 2** Parameter meta-rule

---

```
1 function parameter(Entity[] statement)
2   reduced = statement
3   while length(reduced) > 3 do
4     for i from 0 to length(reduced) - 1 do
5       if name(reduced[i]) not null and
6       type(reduced[i+1]) = Container and
7       coherentParameters(reduced, i) then
8         param = inferParameter(reduced[i], reduced[i+1])
9         reduced.remove(reduced[i], reduced[i+1])
10        reduced.insert(param, i)                                ▷ Replace parameterized entity
11        break
12    if length(statement) stayed the same then return Success
13  return Failure
```

---

The goal is to match extra containers with the preceding named entity. The container is then combined with the preceding entity into a parameterized entity.

The call to inferParameter will add the rule in listing 1.3, replacing `<?container>` with the name of the container used (for example `<parenthesis>`).

```
1 <meta_entity> ::= <ID> <?container>
2 <meta_property> ::= <ID> <?container>
```

Listing 1.3: Rules added to the current grammar for handling parameters

### 1.2.3.3 Operators

A shorthand for parameters is the operator notation. It allows to affect a single parameter to an entity without using a container. It is most used for special entities like quantifiers or modifiers. This is why, once used, the parent entity takes a polymorphic type, meaning that type inference will not issue errors for any usage of them. Details of the way the operators are reduced is exposed in algorithm 3.

From the call of inferOperator, comes new rules explicated in listing 1.4. The call also adds the operator entity to an inferred token `<OP>`.

```
1 <meta_entity> ::= <?OP> <ID>
2 <meta_property> ::= <?OP> <ID>
```

Listing 1.4: Rules added to the current grammar for handling operators

If all meta-rules fail, then the parsing fails and returns an error to the user.

---

**Algorithm 3** Operator meta-rule

---

```
1 function operator(Entity[] statement)
2   reduced = statement
3   while length(reduced) > 3 do
4     for i from 0 to length(reduced) - 1 do
5       if  $\nu(\text{reduced}[i])$  not null and
6        $\nu(\text{reduced}[i+1])$  not null and
7       ( $\nu(\text{reduced}[i])$  is a new symbol or
8       reduced[i] has been parameterized before) and
9       coherentOperator(reduced, i) then
10        op = inferOperator(reduced[i], reduced[i+1])
11        reduced.remove(reduced[i], reduced[i+1])
12        reduced.insert(op, i) ▷ Replace parameterized entity
13        break
14     if length(statement) stayed the same then return Success
15 return Failure
```

---

## 1.2.4 Contextual Interpretation

While parsing another important part of the processing is done after the success of a grammar rule. The grammar in SELF is valuated, meaning that each rule has to return an entity. A set of functions are used to then populate the database with the right entities or retrieve an existing one that correspond to what is being parsed.

When parsing, the rules `<entity>` and `<property>` will ask for the creation or retrieval of an entity. This mechanism will use the name of the entity and its type to retrieve an entity with the same name in a given scope.

### 1.2.4.1 Naming and Scope

When parsing an entity by name, the system will first request for an existing entity with the same name. If such an entity is retrieved, it is returned instead of creating a new one. The validity of a name is limited by the notion of scope.

A scope is the reach of an entity's direct influence. It affects the naming relation by removing variable's names. Scopes are delimited by containers and statements. This local context is useful when wanting to restrict the scope of the declaration of an entity. The main goal of such restriction is to allow for a similar mechanism as the RDF namespaces. This also makes the use of variable (RDF blank nodes) possible.

The scope of an entity has three special values :

- Variable: This scope restricts the scope of the entity to only the other entities in its scope.
- Local: This scope means that the parsing is still populating the scope of the entity. Its scope is limited to the currently parsing statement.
- Global: This scope means the name has no scope limitation.

The scope of an entity also contains all its parent entities, meaning all containers or statement the entity is part of. This is used when choosing between the special values of the scope. The process is detailed in algorithm 4.

The process happens for each entity created or requested by the parser. If a given entity is part of any other entity, the enclosing entity is added to its scope. When an entity is enclosed in any entity while

---

**Algorithm 4** Determination of the scope of an entity

---

```
1 function inferScope(Entity  $e$ )
2   Entity[] reach = []
3   if : ( $e$ ) =  $S$  then
4     for all  $i \in \phi(e)$  do reach.append(inferVariable( $i$ ))           ▷ Adding scopes nested in statement  $e$ 
5     for all  $i \in \mu^-(e)$  do reach.append(inferVariable( $i$ ))       ▷ Adding scopes nested in container  $e$ 
6     if  $\exists \rho(e)$  then
7       Entity[] param = inferScope( $\rho(e)$ )
8       for all  $i \in \text{param}$  do param.remove(inferScope( $i$ ))         ▷ Remove duplicate scopes from parameters
9       for all  $i \in \text{param}$  do reach.append(inferVariable( $i$ ))     ▷ Adding scopes from parameters of  $e$ 
10    scope( $e$ )  $\leftarrow$  reach
11    if GLOBAL  $\notin$  scope( $e$ ) then scope( $e$ )  $\leftarrow$  scope( $e$ )  $\cup$  {LOCAL}
12  return reach
13 function inferVariable(Entity  $e$ )
14   Entity[] reach = []
15   if LOCAL  $\in$  scope( $e$ ) then
16     for all  $i \in \text{scope}(e)$  do
17       if  $\exists e^+ \in \mathbb{U} : \rho(p) = i$  then                             ▷  $e$  is already a parameter of another entity  $e^+$ 
18         scope( $e$ )  $\leftarrow$  scope( $e$ )  $\setminus$  {LOCAL}
19         scope( $e^+$ )  $\leftarrow$  scope( $e^+$ )  $\cup$  scope( $e$ )
20         scope( $e$ )  $\leftarrow$  scope( $e$ )  $\cup$  {VARIABLE,  $p$ }
21   reach.append( $e$ )
22   reach.append(scope( $e$ ))
23  return reach
```

---

already being a parameter of another entity, it becomes a variable.

### 1.2.4.2 Instanciation identification

When a parameterized entity is parsed, another process starts to identify if a compatible instance already exists. From theorem 1, it is impossible for two entities to share the same identifier. This makes mandatory to avoid creating an entity that is equal to an existing one. Given the order of which parsing is done, it is not always possible to determine the parameter of an entity before its creation. In that case a later examination will merge the new entity onto the older one and discard the new identifier.

### 1.2.5 Structure as a Definition

The derivation feature on its own does not allow to define most of the native properties. For that, one needs a light inference mechanism. This mechanism is part of the default inference engine. This engine only works on the principle of structure as a definition. Since all names must be neutral from any language, that engine cannot rely on regular mechanisms like configuration files with keys and values or predefined keywords.

To use SELF correctly, one must be familiar with the native properties and their structure or implement their own inference engine to override the default one.

#### 1.2.5.1 Quantifiers

What are quantifiers? In SELF they differ from their mathematical counterparts. The quantifiers are special entities that are meant to be of a generic type that matches any entities including quantifiers.

There are infinitely many quantifiers in SELF but they are all derived from a special one called the *solution quantifier*. We mentioned it briefly during the definition of the grammar  $\mathcal{G}_0$ . It is the language pendant of  $\mu^-$  and is used to extract and evaluate reified knowledge.

For example, the statement `bob is <SOLVE>(x)` will give either a default container filled with every value that the variable `x` can take or if the value is unique, it will take that value. If there is no value it will default to `<NULL>`, the exclusion quantifier.

How are these other quantifiers defined? We use a definition akin to Lindstöm quantifiers (1966) which is a generalization of counting quantifiers (Gradel *et al.* 1997). Meaning that a quantifier is defined as a constrained range over the quantified variable. We suppose five quantifiers as existing in SELF as native entities.

- The **solution quantifier** `<SOLVE>` noted  $\S$  in classical mathematics, makes a query that turns the expression into the possible range of its variable.
- The **universal quantifier** `<ALL>` behaves like  $\forall$  and forces the expression to affect every possible value of its variable.
- The **existential quantifier** `<SOME>` behaves like  $\exists$  and forces the expression to match *at least one* value for its variable.
- The **uniqueness quantifier** `<ONE>` behaves like  $!\exists$  and forces the expression to match *exactly one* value for its variable.
- The **exclusion quantifier** `<NULL>` behaves like  $\neg\exists$  and forces the expression to match none of the value of its variable.

The last four quantifiers are inspired from Aristotle's square of opposition (D'Alfonso 2011).

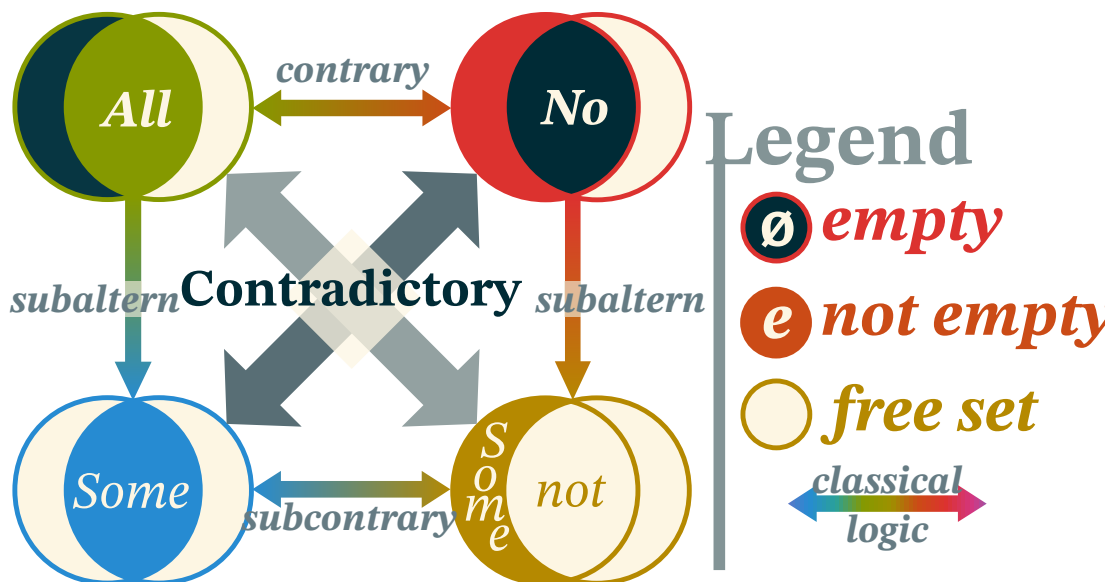


Figure 1.10: Aristotle's square of opposition

In SELF, quantifiers are not always followed by a quantified variable and can be used as a value. In that case the variable is simply anonymous. We use the exclusion quantifier as a value to indicate that there is no value, sort of like `null` or `nil` in programming languages.

In listing 1.5, we present an example file that is meant to define most of the useful native properties



along with default quantifiers.

```
1 * =? ;
2 ?(x) = x; //Optional definition
3 ?~ = { };
4 ?_ ~(=) ~;
5 ?!_ = {_};
6
7 (*e, !T) : (e :: T); *T : (T :: Type);
8 *T : (Entity / T);
9
10 :: :: Property(Entity, Type);
11 (__) :: Statement;
12 (~, !, _, *) :: Quantifier;
13 ( )::Group;
14 { }::Set;
15 [ ]::List;
16 < >::Tuple;
17 Collection/(Set,List,Tuple);
18 0 :: Integer; 0.0::Float;
19 '\0'::Character; ""::String;
20 Literal/(Boolean, Integer, Float, Character, String);
21
22 (*e, !(s::String)) : (e named s);
23 (*e(p), !p) : (e param p);
24 *(s p o):((s p o) subject s),((s p o) property p),((s p o) object o));
```

Listing 1.5: The default lang.w file.

At line 1, we give the first statement that defines the solution quantifier's symbol. The reason this first statement is shaped like this is that global statements are always evaluated to be a true statement. This means that anything equaling the solution quantifier at this level will be evaluated as a domain. If it is a string literal, then it must be either a file path or URL or a valid SELF expression. If it is a single entity then it becomes synonymous to the entire SELF domain and therefore contains everything. We can infer that it becomes the universal quantifier.

All statements up to line 5 are quantifiers definitions. On the left side we got the quantifier symbol used as a parameter to the solution quantifier using the operator notation. On the right we got the domain of the quantifier. The exclusive quantifier has as a range the empty set. For the existential quantifier we have only a restriction of it not having an empty range. At last, the uniqueness quantifier got a set with only one element matching its variable (noting that anonymous variables doesn't match necessarily other anonymous variables in the same statement).

In that file the type hierarchy can be illustrated by the figure 1.11. It consist of entities that are either parameterized or not and that have a value or not.

### 1.2.5.2 Inferring Native Properties

All native properties can be inferred by structure using quantified statements. Here is the structural definition for each of them:

- = (at line 1) is the equality relation given in the first statement.
- $\subseteq$  (at line 8) is the first property to relate a particular type relative to all types. That type becomes the entity type.



Figure 1.11: Hierarchy of types in SELF

- $\mu^-$  (at line 1) is the solution quantifier discussed above given in the first statement.
- $\mu^+$  is represented using containers.
- $\nu$  (at line 22) is the first property affecting a string literal uniquely to each entity.
- $\rho$  (at line 23) is the first property to effect to all entities a possible parameter list.
- $:$  (at line 7) is the first property that matches every entity to a type.
- $\phi$  (at line 24) is the first property to match for all statements:
  - $\phi^-$  its subject,
  - $\phi^0$  its property,
  - $\phi^+$  its object.

We limit the inference to one symbol to make it much simpler to implement and to retrieve but, except for false positives, there are no reason it should not be possible to define several notations for each relation.

### 1.2.6 Extended Inference Mechanisms

In this section we present the default inference engine. It has only a few functionalities. It isn't meant to be universal and the goal of SELF is to provide a framework that can be used by specialists to define and code exactly what tools they need.

Inference engines need to create new knowledge but this knowledge shouldn't be simply merged with the explicit domain. Since this knowledge is inferred, it is not exactly part of the domain but must remain consistent with it. This knowledge is stored in a special scope dedicated to each inference engine. This way, inference engines can use defeasible logic or have dynamic inference from any knowledge insertion in the system.

### 1.2.6.1 Type Inference

Type inference works on matching types in statements. The main mechanism consists in inferring the type of properties in a restrictive way. Properties have a parameterized type with the type of their subject and object. The goal is to make that type match the input subject and object.

For that we start by trying to match the types. If the types differ, the process tries to reduce the more general type against the lesser one (subsumption-wise). If they are incompatible, the inference uses some light defeasible logic to undo previous inferences. In that case the types are changed to the last common type in the subsumption tree.

However, this may not always be possible. Indeed, types can be explicitly specified as a safeguard against mistakes. If that's the case, an error is raised and the parsing or knowledge insertion is interrupted.

### 1.2.6.2 Instanciation

Another inference tool is instantiation. Since entities can be parameterized, they can also be defined against their parameters. When those parameters are variables, it allows entities to be instantiated later.

This is a complicated process because entities are immutable. Indeed, parsing happens from left to right and therefore an entity is often created before all the instantiation information are available. Even harder are completion of definition in several separate statements. In all cases, a new entity is created and then the inference realize that it is either matching a previous definition and will need to be merged with the older entity or it is a new instance and needs all properties duplicated and instantiated.

This gives us two mechanisms to take into account: merging and instanciating.

Merging is pretty straightforward: the new entity is replaced with the old one in all of the knowledge graph. containers, parameterized entities, quantifiers and statements must be duplicated with the correct value and the original destroyed. This is a heavy and complicated process but seemingly the only way to implement such a case with immutable entities.

Instanciating is similar to merging but even more complicated. It starts with computing a relation that maps each variable that needs replacing with their grounded value. Then it duplicates all knowledge about the parent entity while applying the replacement map.

## 1.3 Perspectives

Listing the contributions there are a couple that didn't make the cut. It is mainly ideas or projects that were too long to check or implement and needed more time to complete. SELF is still a prototype, and even if the implementation seemed to perform well on a simple example, no benchmarks have been done on it. It might be good to make a theoretical analysis of OWL compared to SELF along with some benchmark results.

On the theoretical parts there are some works that seems worthy of exposure even if unfinished.

### 1.3.1 Literal definition using Peano's axioms

The only real exceptions to the axioms and criteria are the first statement, the comments and the liberals.

For the first statement, there is yet to find a way to express both inclusion, the equality relation and solution quantifier. If such a convenient expression exists, then the language can become almost entirely self described.

Comments can be seen as a special kind of container. The difficult part is to find a clever way to differentiate them from regular containers and to ignore their content in the regular grammar. It might be possible to at first describe their structure but then they become parseable entities and fail at their purpose.

Lastly, and perhaps the most complicated violation to fix: laterals. It is quite possible to define literals by structure. First we can define boolean logic quite easily in SELF as demonstrated by listing 1.6.

```
1 ~(false) = true;
2 ( false, true ) :: Boolean;
3 true =?; //conflicts with the first statement!
4 *a : ((a | true) = true);
5 *a : ((false | a) = a);
6 *a : ((a & false) = false);
7 *a : ((true & a) = a);
```

Listing 1.6: Possible definition of boolean logic in SELF.

Starting with line 1, we simply define the negation using the exclusive quantifier. From there we define the boolean type as just the two truth values. And now it gets complicated. We could either arbitrarily say that the false literal is always parameters of the exclusion quantifier or that it comes first on either first two statements but that would just violate minimalism even more. We could use the solution quantifier to define truth but that collides with the first statement definition. There doesn't seem to be a good answer for now.

From line 4 going on, we state the definition of the logical operators  $\wedge$  and  $\vee$ . The problem with this is that we either need to make a native property for those operators or the inference to compute boolean logic will be terribly inefficient.

We can use Peano's axioms (1889) to define integers in SELF. The attempt at this definition is presented in listing 1.7.

```
1 0 :: Integer;
2 *n : (++(n) :: Integer);
3 (*m, *n) : ((m=n) : (++m = ++n));
4 *n : (++n ~= 0);
5 *n : ((n + 0) = n);
6 (*n, *m) : ((n + ++m) = ++(n + m));
7 *n : ((n × 0) = 0);
8 (*n, *m) : ((n × ++m) = (n + (n × m)));
```

Listing 1.7: Possible integration of the Peano axioms in SELF.

We got several problems doing so. The symbols  $*$  and  $/$  are already taken in the default file and so would need replacement or we should use the non-ASCII  $\times$  and  $\div$  symbols for multiplication and division. Another more fundamental issue is as previously discussed for booleans: the inference would be excruciatingly slow or we should revert to a kind of parsing similar to what we have already under the hood. The last problem is the definition of digits and bases that would quickly become exceedingly complicated and verbose.

For floating numbers this turns out even worse and complicated and such a description wasn't even attempted for now.

The last part concerns textual literals. The issue is the same as the one with comments but even worse. We get to interpret the content as literal value and that would necessitate a similar system as we already have and wouldn't improve the minimalist aspect of things much. Also we should define ways to escape characters and also to input escape sequences that are often needed in such case. And since SELF isn't meant for programming that can become very verbose and complex.

### **1.3.2 Advanced Inference**

The inference in SELF is very basic. It could be improved a lot more by simply checking the consistency of the database on most aspects. However, such a task seems to be very difficult or very slow. Since that kind of inference is undecidable in SELF, it would be all a research problem just to find a performant inference algorithm.

Another kind of inference is more about convenience. For example, one can erase singlets (containers with a single value) to make the database lighter and easier to maintain and query.

### **1.3.3 Queries**

We haven't really discussed queries in SELF. They can be made using the main syntax and the solution quantifiers but efficiency of such queries is unknown. Making an efficient query engine is a big research project on its own.

For now a very simplified query API exists in the prototype and seems to perform well but further tests are needed to assess its scalability capacities.

## 2 General Planning Framework

When making artificial intelligence systems, an important feature is the ability to make decisions and act accordingly. To act, one should plan ahead. This is why the field of automated planning is being actively researched in order to find efficient algorithms to find the best course of action in any given situation. The previous chapter allowed to lay the bases of knowledge representation. How knowledge about the planning domains are represented is a main factor to take into account in order to conceive any planning algorithm.

Automated planning really started being formally investigated after the creation of the Stanford Research Institute Problem Solver (STRIPS) by Fikes and Nilsson (1971). This is one of the most influential planner, not because of its algorithm but because of its input language. Any planning system needs a way to express the information related to the input problem. Any language done for this purpose is called an *action language*. STRIPS will be mostly remembered for its eponymous action language that is at the base of any modern derivatives.

All action language is based on mainly two notions: *actions* and *states*. A state is a set of *fluents* that describe aspects of the world modeled by the domain. Each action has a logic formula over states that allows its correct execution. This requirement is called *precondition*. The mirror image of this notion are possible *effects* which are logic formula that are enforced on the current state after the action is executed. The domain is completed with a problem, most of the time specified in a separate file. The problem basically contains two states: the *initial* and *goal* states.

### 2.1 Illustration

To illustrate how automated planners works, we introduce a typical planning problem called **block world**. In this example, a robotic grabbing arm tries to stack blocks on a table in a specific order. The arm is only capable of handling one block at a time. We suppose that the table is large enough so that all the blocks can be put on it without any stacks. Figure 2.1 illustrates the setup of this domain.

The possible actions are `pickup`, `putdown`, `stack` and `unstack`. There are at least three fluents needed:

- one to state if a given block is `down` on the table,
- one to specify which block is `held` at any moment and
- one to describe which block is stacked `on` which block.

We also need a special block to state when `noblock` is held or on top of another block. This block is a constant.

The knowledge we just described is called *planning domain*.

In that example, the initial state is described as stacks and a set of blocks directly on the table. The goal state is usually the specification of one or many stacks that must be present on the table. This part of the description is called *planning problem*.

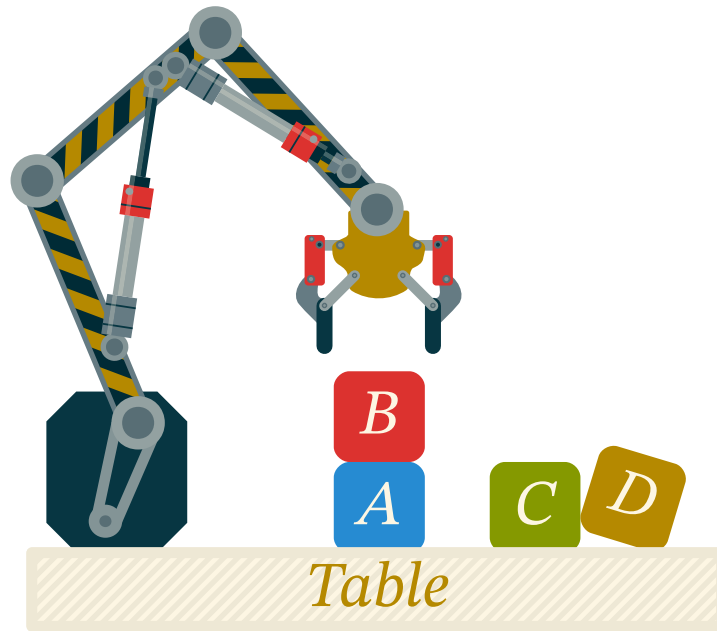


Figure 2.1: The block world domain setup.

In order to solve it we must find a valid sequence of actions called a *plan*. If this plan can be executed in the initial state and result in the goal state it is called a *solution* of the planning problem. To be executed, each action must be done in a state satisfying its precondition and will alter that state according to its effects. A plan can be executed if all its action can be executed in the sequence of the plan. For example, in the block world domain we can have an initial state with the *blockB* on top of *blockA* and the *blockC* being on the table. In figure 2.2, we give a plan solution to the problem consisting of having the stack  $\langle \text{blockA}, \text{blockB}, \text{blockC} \rangle$  from that initial state.

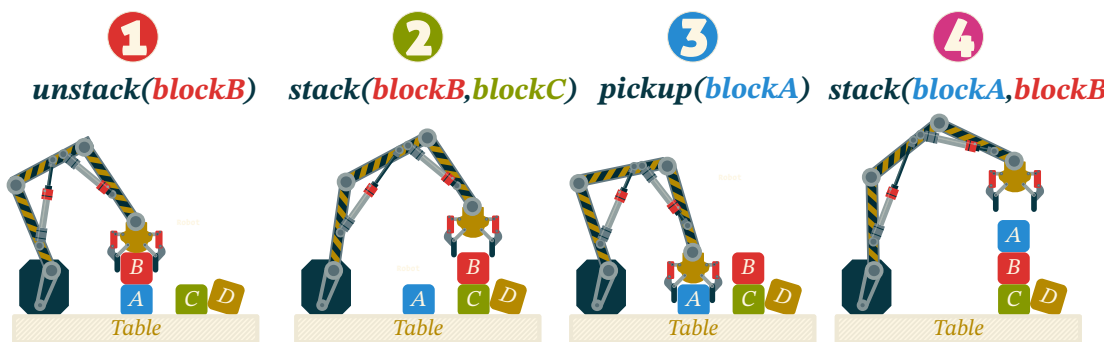


Figure 2.2: An example of a solution to a planning problem with a goal requiring three block stacked in alphabetical order.

Every automated planner aims to find at least one such solution in any way shape or form in the least amount of time with the best plan quality. The quality of a plan is often measured by how hard it is to execute, whether by its execution time or by the resources needed to accomplish it. This metric is often called *cost* of a plan and is often simply the sum of the cost of its actions.

Table 2.1: List of classical symbols and syntax for planning.

Symbol	Description
$F, \square, A$	Sets of fluents, states and actions.
$\otimes, \odot^\pm$	Sets of flaws and signed resolvers. Flaws have variants:
$\otimes^\dagger$	• unsupported subgoal.
$\otimes^\ddagger$	• causal threat to an existing causal link.
$\otimes^\circ$	• cycle in the plan.
$\otimes^*$	• decomposition of a compound action.
$\otimes^\sim$	• alternative to an existing action.
$\otimes^\emptyset$	• orphan action in the plan.
$\Pi, \mathcal{S}$	Sets of plans and search space.
$l \downarrow a$	Partial support of action $a$ by the causal link $l$ .
$\pi \downarrow a$	Full support of action $a$ by plan $\pi$ .
$<, >$	Precedence and succession relation used for order.
$\Rightarrow^*$	General shortest path algorithm.
$h$	Search heuristic.
$\mathbb{P}$	Planning problem.
$\gamma$	Constraints on the action.
$\mathfrak{c}$	Cost of an action.
$d$	Duration of an action.
$\omega$	Root operator.

Automated planning is very diverse. A lot of paradigms shifts the definition of domain, actions and even plan to widely varying extents. This is the reason why making a general planning formalism was deemed so hard or even impossible:

*"It would be unreasonable to assume there is one single compact and correct syntax for specifying all useful planning problems."* Sanner (2010)

Indeed, the block world example domain we give is mostly theoretical since there are infinitely more subtlety into this problem such as mechatronic engineering, balancing issues and partial ability to observe the environment and predict its evolution as well as failure in the execution. In our example, we didn't mention the misplaced *blockD* that could very well interfere with any execution in unpredictable ways. This is why so many planning paradigms exist and why they are all so diverse: they try to address an infinitely complex problem, one sub-problem at a time. In doing so we lose the general view of the problem and by simply stating that this is the only way to resolve it we close ourselves to other approaches that can become successful. Like once said:

*"The easiest way to solve a problem is to deny it exists."* Asimov (1973)

However, In the next section we aim to create such a general planning formalism. The main goal is to provide the automated planning community with a general unifying framework it so badly needs.

## 2.2 Formalism

In this section, a general formalism of automated planning is proposed. The goal is to explain what is planning and how it works. First we must express the knowledge domain formalism, then we describe how problems are represented and lastly how a general planning algorithm can be envisioned.



## 2.2.1 Planning domain

In order to conceive a general formalism for planning domains, we base its definition on the formalism of SELF. This means that all part of the domain must be a member of the universe of discourse  $\mathbb{U}$ .

### 2.2.1.1 Fluents

First, we need to define the smallest unit of knowledge in planning, the fluents.

**Definition 10 (Fluent).** A planning fluent is a predicate  $f(arg_1, arg_2, ..., arg_n) \in F$  where:

- $f$  is a relation/function.
- $arg_{i \in [1, n]} \in \mathbb{U}$  are the arguments (possibly quantified).
- $n = |f|$  is the arity of  $f$ .

Fluents are signed. Negative fluents are noted  $\neg f$  and behave as a logical complement. We do not use the closed world hypothesis: fluents are only satisfied when another compatible fluent is provided.

The name fluent comes from their fluctuating value. Indeed the truth value of a fluent is meant to vary with time and specifically by acting on it. In this formalism we represent fluents using either parameterized entities or using statements for binary fluents.

*Example:* In our example we have four predicates. They can form countless fluents like *held(no – block)*, *on(blockA, blockB)* or  $\neg \text{down}(\text{blockA})$ . Their when expressing a fluent we suppose its truth value is T and denote falsehood using the negation  $\neg$ .

When expressing states, we need a formalism to express sets of fluents as formulaes.

**Definition 11 (State).** A state is a set of fluent. It is provided with a truth value like a fluent and can behave like one. The truth value is the *conjunction* of all fluents within the state  $\square \vdash \bigwedge_{f \in \square} f$  denoted by a small square  $\square$ . States can contain other states in which case their truth value is the *disjunction* of the member's truth value:  $\square \vdash \bigvee_{\square' \in \square} \square'$ . This creates an and/or tree with the branches being all *or vertices* except for the ones connecting to fluents that becomes *and vertices*. All leaves of the tree are fluents.

*Example:* In the domain block world, we can express a couple of states as set of fluents:

- $\square_1 = \{\text{held}(\text{noblock}), \text{on}(\text{blockA}, \text{blockB}), \text{down}(\text{blockC})\}$
- $\square_2 = \{\text{held}(\text{blockC}), \text{down}(\text{blockA}), \text{down}(\text{blockB})\}$

In such a case, both state  $\square_1$  and  $\square_2$  have their truth value being the conjunction of all their fluents. In order to express a disjunction, one has to combine states in the following way:  $\square_3 = \{\square_1, \square_2\}$ . In that case  $\square_3$  is the root of the and/or tree and all its direct children are or vertices. The states  $\square_1$  and  $\square_2$  have their children as *and vertices* since they are fluents.

Another important part of the behavior of fluents is their ability to match and to being unified.

Matching is the relation  $f_1 :_{\square} f_2$  that affects any pair of fluents  $\langle f_1, f_2 \rangle$  along with a context state  $\square$  to another state containing the context augmented with unification constraints or  $\emptyset$  if the two fluents are contradicting one another given the context. If the two fluents are equal or have a different function, they do not influence the context. Opposite fluents will always contradict. The quantified or variable arguments may cause contradiction or add a constraint into the context.

The actual unification relation  $f_1 \vdash_{\square} f_2$  bind any matching fluents to another grounded fluent giving the constraints of the given context.

Both relations are generalized to states by merging the result of the following way:

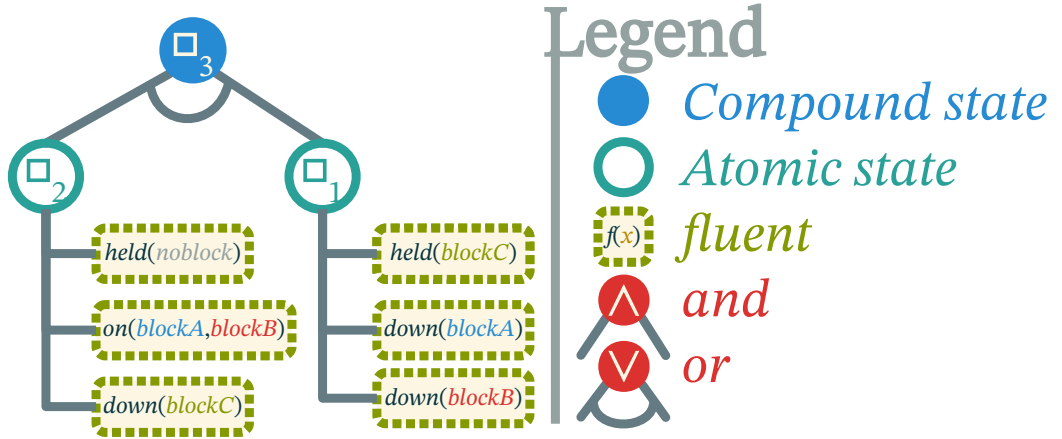


Figure 2.3: Example of a state encoded as an and/or tree.

$$\vdash (\square_r, \square_f) = \bigcup_{f_r \in \square_f, f_f \in \square_f} \vdash (f_r, f_f, \square_a)$$

with,  $\square_r$  being the reference state and  $\square_f$  being the formula state. The state  $\square_a$  is an accumulator that is result of the partial union of the previous matching iterations. This formula is the same for  $:$  and  $\vdash$ . It is interesting to note that the relations doesn't need an additional context and share the same definition domain  $\square^2 \rightarrow \square$  when taking states as arguments.

*Example:* Using previously defined example states  $\square_{1,2,3}$ , and adding the following:

- $\square_4(x) = \{\text{held}(\text{noblock}), \text{down}(x)\}$  and
- $\square_5(y) = \{\text{held}(y), \neg \text{down}(y)\}$ ,

We can express a few example of fluent matching:

- $\text{held}(\text{noblock}) : \text{held}(x) = \{x = \text{noblock}\}$
- $\neg \text{held}(x) : \text{held}(x) = \emptyset$
- $\text{held}(\text{blockA}) :_{\square_1} \text{held}(x) = \emptyset$
- $\text{down}(\text{blockD}) :_{\square_1} \text{down}(x) = \square_1 \cup \{x = \text{blockD}\}$
- $\text{down}(\text{blockC}) :_{\square_1} \text{down}(\text{blockC}) = \square_1$

Unification of fluents goes quite simply:

- $\text{held}(\text{noblock}) \vdash \text{held}(x) = \text{held}(\text{noblock})$
- $\neg \text{held}(x) \vdash \text{held}(x) = \emptyset$
- $\text{held}(\text{blockC}) \vdash_{\square_5(y)} \text{held}(y) = \{\text{held}(\text{blockC}), \neg \text{down}(\text{blockC})\}$

We also can present matching on states:

- $\square_1 : \square_2 = \emptyset$
- $\square_1 : \square_4(x) = \square_1 \cup \{x = \text{blockC}\}$

And unification too:

- $\square_1 \vdash \square_4(x) = \square_1$

**FIXME: Type check and see if application is different.**

All these relations are used to check and apply actions.

### 2.2.1.2 Actions

Actions are the main mechanism behind automated planning, they describe what can be done and how it can be done.

**Definition 12** (Action). An action is a parametrized tuple  $a(args) = \langle :, \vdash, \gamma, \phi, d, \mathbb{P}, \mathbb{M} \rangle$  where:

- $:$  and  $\vdash$  are states that are respectively the **preconditions** and the **effects** of the action.
- $\gamma$  is the state representing the **constraints**.
- $\phi$  is the intrinsic **cost** of the action.
- $d$  is the intrinsic **duration** of the action.
- $\mathbb{P}$  is the prior **probability** of the action succeeding.
- $\mathbb{M}$  is a set of **methods** that decompose the action into smaller simpler ones.

Operators take many names in difference planning paradigm : actions, steps, tasks, etc. In our case we call operators, all fully lifted actions and actions are all the instances possibles (including operators).

In order to be more generalistic, we allow in the constraints description, any time constraints, equalities or inequalities, as well as probabilistic distributions. These constraints can also express derived predicates. It is even possible to place arbitrary constraints on order and selection of actions.

Actions are often represented as state operators that can be applied in given state to alter it. The application of actions is done by using the actions as relations  $a : \square \rightarrow \square$  defined as follow:  $a(\square) = \square \vdash_{\square} a$

$$a(\square) = \begin{cases} \emptyset, & \text{if } \square : a = \emptyset \\ \square \vdash a, & \text{otherwise} \end{cases}$$

*Example:* A useful action we can define from previously defined states is the following:

$$pickup(x) = \langle \square_4(x), \square_5(x), (x : Block), 1.0\phi, 3.5s, 75\%, \emptyset \rangle$$

That action can pickup a block  $x$  in 3.5 seconds using a cost of 1.0 with a prior success probability of 75%.

### 2.2.1.3 Domain

The domain specifies the allowed operators that can be used to plan and all the fluents they use as preconditions and effects.

**Definition 13** (Domain). A domain  $\mathcal{D}$  is a set of **operators** which are fully lifted *actions*, along with all the relations and entities needed to describe their preconditions and effects.

*Example:* In the previous examples the domain was named block world. It consists in four actions: *pickup*, *putdown*, *stack* and *unstack*. Usually the domain is self contained, meaning that all fluents, types, constants and operators are contained in it.

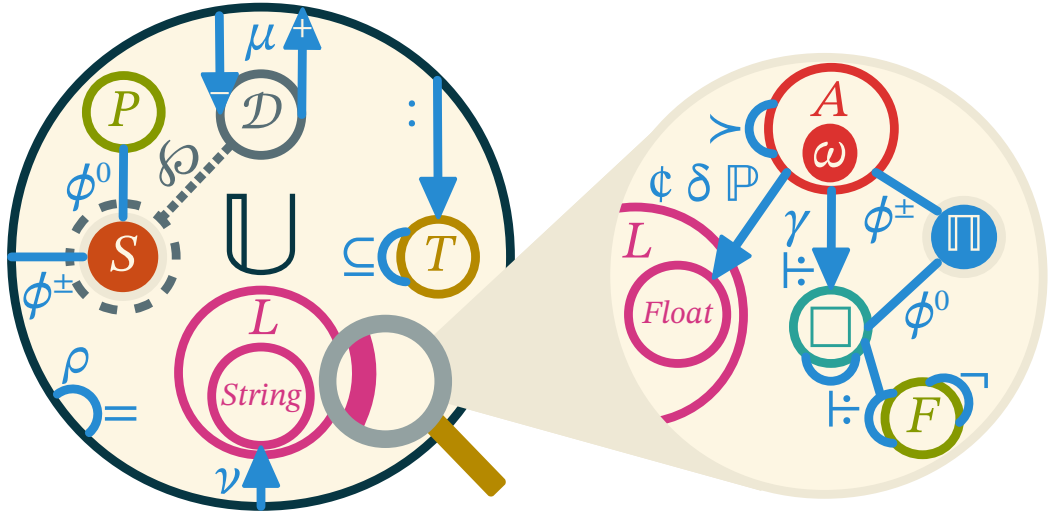


Figure 2.4: Venn diagram extended from the one from SELF to add all planning knowledge representation.

## 2.2.2 Planning problem

The aim of an automated planner is to find a plan satisfying the goal. This plan can be of multiple forms, and there can even be multiple plans that meet the demand of the problem.

### 2.2.2.1 Solution

**Definition 14** (Partial Plan / Method). A partially ordered plan is an *acyclic* directed graph  $\pi = (A_\pi, E)$ , with:

- $A_\pi$  the set of **steps** of the plan as vertices. A step is an action belonging in the plan.  $A_\pi$  must contain an initial step  $a_\pi^0$  and goal step  $a_\pi^*$  as convenience for certain planning paradigms.
- $E$  the set of **causal links** of the plan as edges. We note  $l = a_s \xrightarrow{\square} a_t$  the link between its source  $a_s$  and its target  $a_t$  caused by the set of fluents  $\square$ . If  $\square = \emptyset$  then the link is used as an ordering constraint.

This definition can express any kind of plans, either temporal, fully or partially ordered or even loose hierarchical plans (using the methods of the actions). It can even express diverse planning results.

In our framework, *ordering constraints* are defined as the transitive cover of causal links over the set of steps. We note ordering constraints:  $a_a > a_s$ , with  $a_a$  being *anterior* to its *successor*  $a_s$ . Ordering constraints cannot form cycles, meaning that the steps must be different and that the successor cannot also be anterior to its anterior steps:  $a_a \neq a_s \wedge a_s \not> a_a$ . If we need to enforce order, we simply add a link without specifying a cause. The use of graphs and implicit order constraints help to simplify the model while maintaining its properties. Totally ordered plans are done by specifying links between all successive actions of the sequence.

*Example:* In the section 2.1, we described a classical fully ordered plan, illustrated in figure 2.2. A partially ordered plan has a tree-like structure except that it also meet in a “sink” vertex (goal step). We explicit this structure in figure 2.5.

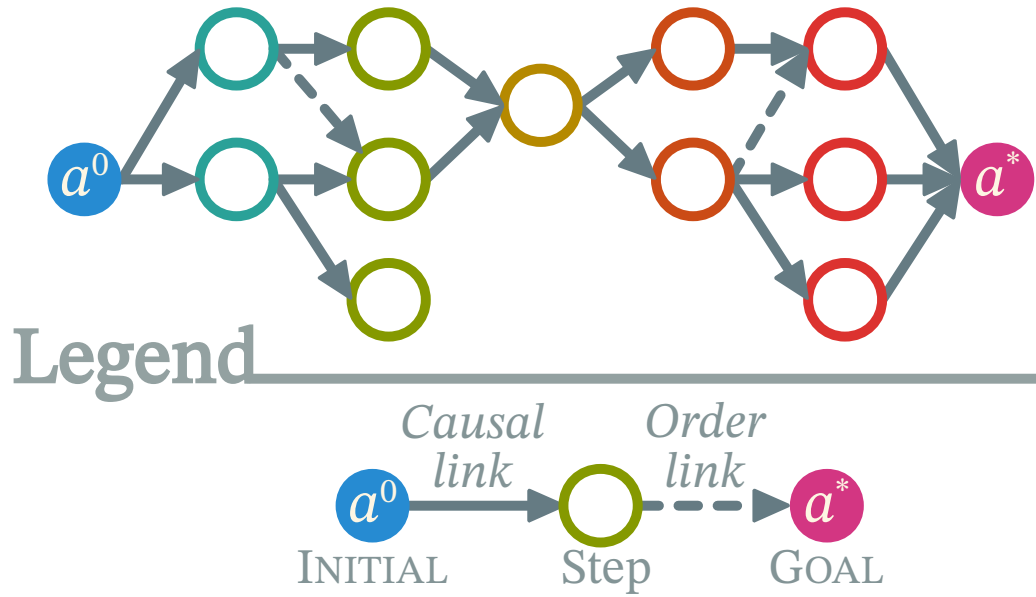


Figure 2.5: Example of the structure of a partially ordered plan.

#### 2.2.2.2 Problem

With this formalism, the problem is very simplified but still general.

**Definition 15** (Problem). The planning problem is defined as the **root operator**  $\omega$  which methods are potential solutions of the problem. Its preconditions and effects are respectively used as initial state and goal description.

As actions are very general, it is interesting to make the problem and domain space homogenous by using an action to describe any problem.

Most of the specific notions of this framework are optional. Any planner using it will probably define what features it supports when compiling input domains and problems.

All notions explained so far are represented in the figure 2.4 adding to the SELF Venn diagram.

### 2.2.3 Planning algorithm

The general planning algorithm can be described as a guided exploration of a search space. The detailed structure of the search space as well as search iterators are dependant on the planning paradigm used.

#### 2.2.3.1 Search space

**Definition 16** (Planner). A planning algorithm, often called planner, is an exploration of a search space  $\mathbb{S}$  partially ordered by an iterator  $\phi_{\mathbb{S}}^+$  guided by a heuristic  $h$ . From any problem  $\mathbb{p}$  every planner can derive two informations immediately:

- the starting point  $s_0 \in \mathbb{S}$  and
- the solution predicate  $?_{s^*}$  that gives the validity of any potential solution in the search space.

Formally the problem can be exprimed as a pathfinding problem in the dirrected graph  $g_{\mathbb{S}}$  formed by the vertex set  $\mathbb{S}$  and the adjacence function  $\phi_{\mathbb{S}}^+$ . The set of solutions is therefore expressed as:

$$\mathbb{S}^* = \{s^* : \langle s_0, s^* \rangle \in E_{\chi^+(g_{\mathbb{S}})} \wedge ?_{s^*}\}$$

In automated planning there are also other considerations about the search.

### 2.2.3.2 Diversity

Sometimes, it is necessary to find alternatives. Since re-planning from scratch is computationally demanding, it is better to find several solutions at once. This approach is called *diverse planning*. It aims to find  $k$  solutions that deviates from one another significantly. This simply make the process return when either it found  $k$  solutions or when it determined that  $k > |\mathbb{S}^*|$ .

### 2.2.3.3 Temporality

Another aspect of planning lies in its timming. Indeed sometimes acting needs to be done before a deadline and planning is useful only durring a finite timeframe. We add a predicate that specifies time constraints over algorithms  $t : \mathbb{A} \rightarrow \mathbb{A}$ . This constraint has three main type of application:

- $t_{\odot}$ : Optimal search without time limitation, finding the best solution everytime.
- $t_{\odot\odot}$ : Anytime search, finding a solution and improving its quality until stopped.
- $t_{\odot\bullet}$ : Real-time search, being able to give a solution in a given time even if it is an approximation.

### 2.2.3.4 General planner

A general planner  $\mathbb{C}^*[\mathbb{S}, \phi_{\mathbb{S}}^+, h, \rightarrow](\mathcal{D}, \mathbb{p})$  is an algorithm that can plan any formalism of automated planning. It takes two set of parameters:

- **Formalism dependant parameters**
  - $\mathbb{S}$  the search space
  - $\phi_{\mathbb{S}}^+$  the search iterator
  - $h$  the heuristic
  - $\rightarrow$  the problem transformation function
- **Domain depedant parameters**
  - $\mathcal{D}$  the *planning domain*
  - $\mathbb{p}$  the *planning problem*

The heuristic  $h(s)$  gives off the shortest predicted distance to any point of the solution space. The exploration is guided by it by minimizing its value.

Other informations must be added to any problem  $\mathbb{p}$  in the form of constraints:

$$(t(\mathbb{C}) \bowtie |\mathbb{P}(\omega)| = k) \in c(\omega)$$

The value for  $k$  is extracted from the problem and the temporality is expressed using either  $\wedge$ ,  $\vee$  or  $\wedge\perp\vee$  instead of  $\bowtie$ .

The transformation function  $\mathbb{p} \rightarrow \langle s_0, ?_{s^*} \rangle$  gives the starting point  $s_0$  and the solution predicate  $?_{s^*}$ . This predicate is derived from the problem description and its constraints.

For the algorithm itself, we simply use a parameterized instance of the  $K^*$  algorithm (Aljazzar and Leue 2011, alg. 1). This algorithm uses the classical algorithm  $A^*$  to explore the graph while using Dijkstra on some sections to find the  $k$  shortest paths. The parameters are as follow:  $K^*(g_S, s_0, ?_{s^*}, h)$ . The solution predicate contains the expression of the restriction of  $k$  solutions, therefore, it superseeds the need for the  $k$  parameter. We also add the heuristic  $h$  to guide the  $A^*$  part of the algorithm.

Of course this algorithm is merely an example of a general planner algorithm. Its efficiency hasn't been tested.

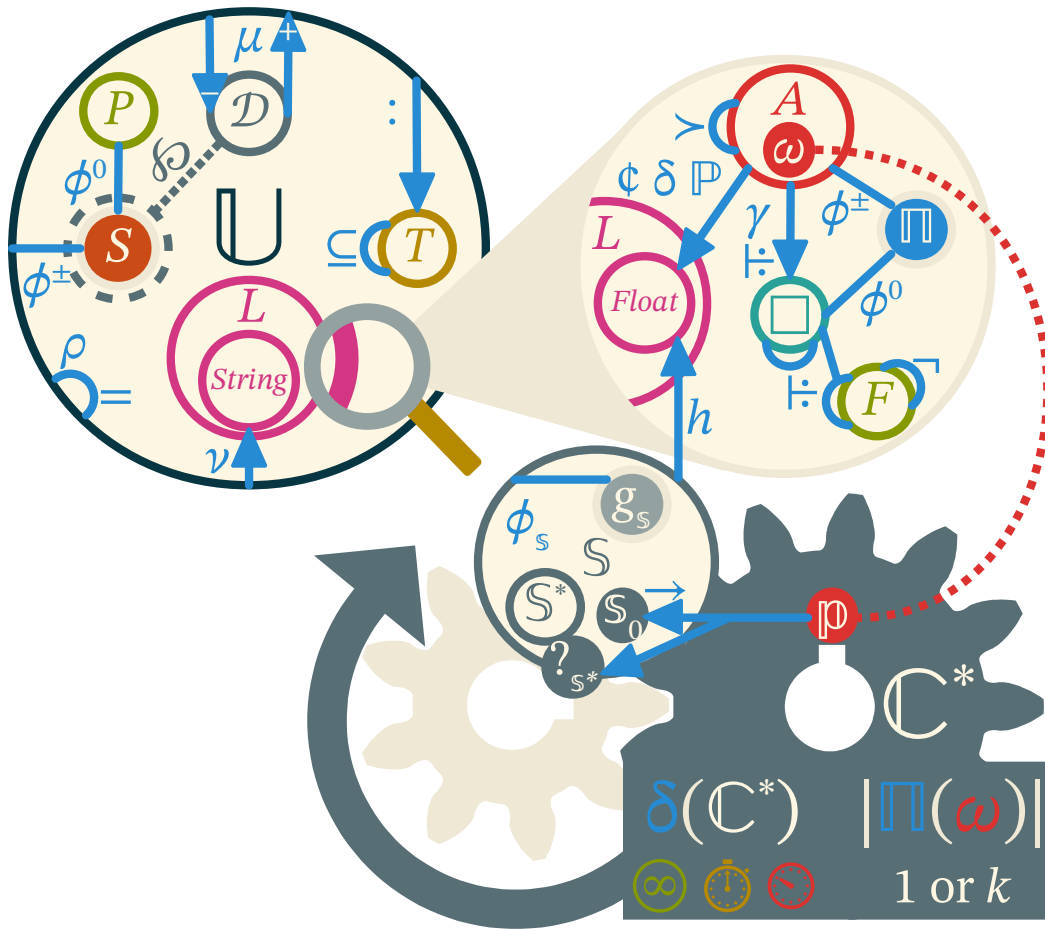


Figure 2.6: Venn diagram extended with general planning formalism.

## 2.3 Classical Formalisms

One of the most comprehensive work on summarizing the automated planning domain was done by Ghallab *et al.* (2004). This book explains the different planning paradigm of its time and gives formal

description of some of them. This work has been updated later (Ghallab *et al.* 2016) to reflect the changes occurring in the planning community.

### 2.3.1 State-transition planning

The most classical representation of automated planning is using the state transition approach: actions are operators on the set of states and a plan is a finite-state automaton. We can also see that problem description as either a graph exploration problem or even a constraint satisfaction problem. In any way that problem is isomorph to its original formulation and most efficient algorithms use a derivative of A\* exploration techniques on the state space.

This makes this kind of planning quite simple to instantiate from the general planner:

$$\mathbb{C}_{state} = \mathbb{C}^* \left[ \square, \bigcup_{a \in A} a(\mathbb{s}), h, : (\omega), \vdash (\omega) \right]$$

For this formalism, we often set  $k = 1$  and  $t(\mathbb{C}_{state}) = t_{\otimes}$  as is customary in classical planning. It can also be specified as a backward search by inverting the application of  $a$  with  $a^{-1}$  and having the starting state as  $: (\omega)$  and solution predicate as  $\vdash (\omega)$ .

State based planning usually suppose total knowledge of the state space and action behavior. No concurrency or time constraints are expressed and the state and action space must be finite as well as the resulting state graph. This process is also deterministic and doesn't allow uncertainty. The result of such a planning is a totally ordered sequence of actions called a plan. The total order needs to be enforced even if it is unnecessary.

All those features are important in practice and lead to other planning paradigms that are more complex than classical state based planning.

### 2.3.2 Plan space planning

Plan Space Planning (PSP) is a form of planning that use plan space as its search space. It starts with an empty plan and try to iteratively refine that plan into a solution.

$$\mathbb{C}_{psp} = \mathbb{C}^* \left[ \mathbb{P}, \bigcup_{f \in \otimes(\mathbb{s})}^{r \in \otimes_f^+} r(\mathbb{s}), h, (\{a_{\mathbb{w}}^0, a_{\mathbb{w}}^*\}, \{a_{\mathbb{w}}^0 \rightarrow a_{\mathbb{w}}^*\}), \otimes(\mathbb{s}) = \emptyset \right]$$

with  $a_{\mathbb{w}}^0$  and  $a_{\mathbb{w}}^*$  being the initial and goal steps of the plan  $\mathbb{s}_0$  such that  $\vdash (a_{\mathbb{w}}^0) = : (\omega)$  and  $: (a_{\mathbb{w}}^*) = \vdash (\omega)$ . The iterator is all the possible resolutions of all flaws on any plan  $\mathbb{s}$  and the solution predicate is true when the plan has no more flaws.

Details about flaws, resolver and the overall Partial Order Causal Links (POCL) algorithm will be presented **LATER**.

This approach usually can give a partial plan if we set  $t(\mathbb{C}_{psp}) < t(\exists \mathbb{w} \in \mathbb{P} \wedge ?_{\mathbb{s}}(\mathbb{w}))$ . This plan is not a solution but can eventually be engineered into having approximative properties relative to a solution.



Table 2.2: List of classical symbols and syntax for probabilities.

Symbol	Description
$\mathbb{P}(e)$	Probability of event $e$ .
$\mathcal{O}$	Set of observations.
$ $	Reward function.

### 2.3.3 Case based planning

Another plan oriented planning is called Case-Based Planning (CBP). This kind of planning relies on a library of already complete plans and try to find the most appropriate one to repair.

$$\mathbb{C}_{cbp} = \mathbb{C}^* [\mathcal{L}^{\mathbb{P}}, \odot(\mathbb{s}), h, \sigma^*(\mathcal{L}^{\mathbb{P}}, \omega), \mathbb{s}(: (\omega)) \Downarrow \vdash (\omega)]$$

with  $\mathcal{L}^{\mathbb{P}}$  being the plan library. The planner selects efficiently a plan that fit the best with the intial and goal state of the problem. This plan is then repaired and validated iteratively. The problem with this approach is that it may be unable to find a valid plan or might need to populate and maintain a good plan library. For such case an auxiliary planner is used (preferably diverse with  $k > 1$ ).

### 2.3.4 Probabilistic planning

**FIXME** Reward using rupee symbol |

Probabilistic planning tries to deal with uncertainty by generating a policy instead of a plan. The initial problem holds probability laws that govern the execution of any actions. It is sometimes accompagnated with a reward function instead of a deterministic goal.

$$\mathbb{C}_{prob} = \mathbb{C}^* \left[ \square \times A, \mathbb{s}_{+1} = \bigcup_{a \in A}^{a(\square) \neq \emptyset} \langle \pi_{(\square', a') \rightarrow a'(\square')} \sigma(\mathbb{s}_{+1}), a \rangle, h|, \bigcup_{a \in A}^{a(: (\omega)) \neq \emptyset} \langle : (\omega), a \rangle, \square \vdash \omega \right]$$

The state  $\square$  is a state chosen from the frontiere. The frontiere is updated at each iteration with the application of a non-deterministically chosen pair of the last policy insertion. The search stops when all elements in the frontiere are goal states.

### 2.3.5 Hierarchical planning

Hierarchical Task Networks (HTN) are a totally different kind of planning paradigm. Instead of a goal description, HTN uses a root task that needs to be decomposed. The task decomposition is an operation that replaces a task (action) by one of its methods  $\Pi$ .

$$\mathbb{C}_{htn} = \mathbb{C}^* = [\mathbb{I}, (\sigma\{a \in A_s : \mathbb{I}_a \neq \emptyset\} \rightarrow \sigma(\mathbb{I}_a))(\mathbb{s}), h, \omega, \forall a \in A_s : \mathbb{I}(a) = \emptyset]$$

## 2.4 Existing Languages and Frameworks

### 2.4.1 Classical

After STRIPS, one of the first language to be introduced to express planning domains like ADL (Pednault 1989). That formalism adds negation and conjunction into literals to STRIPS. It also drops the closed world hypothesis for an open world one: anything not stated in conditions (initial or action effects) is unknown.

The current standard was strongly inspired by Penberthy *et al.* (1992) and his UCPOP planner. Like STRIPS, UCPOP had a planning domain language that was probably the most expressive of its time. It differs from ADL by merging the add and delete lists in effects and to change both preconditions and effects of actions into logic formula instead of simple states.

The PDDL language was created for the first major automated planning competition hosted by AIPS in 1998 (Ghallab *et al.* 1998). It came along with a syntax and solution checker written in Lisp. It was introduced as a way to standardize notation of planning domains and problems so that libraries of standard problems can be used for benchmarks. The main goal of the language was to be able to express most of the planning problems of the time.

With time, the planning competitions became known under the name of International Planning Competitions (IPC) regularly hosted by the ICAPS conference. With each installment, the language evolved to address issues encountered the previous years. The current version of PDDL is 3.1 (Kovacs 2011). Its syntax, goes similarly as described in listing 2.1.

```
1 (define (domain <domain-name>)
2   (:requirements :<requirement-name>)
3   (:types <type-name>)
4   (:constants <constant-name> - <constant-type>)
5   (:predicates (<predicate-name> ?<var> - <var-type>))
6   (:functions (<function-name> ?<var> - <var-type>) - <function-type>)
7
8   (:action <action-name>
9     :parameters (?<var> - <var-type>)
10    :precondition (and (= (<function-name> ?<var>) <value>)
11      (<predicate-name> ?<var>))
12    :effect
13      (and (not (<predicate-name> ?<var>))
14        (assign (<function-name> ?<var>) ?<var>)))
```

Listing 2.1: Simplified explanation of the syntax of PDDL.

PDDL uses the functional notation style of LISP. It defines usually two files: one for the domain and one for the problem instance. The domain describes constants, fluents and all possible actions. The problem lays the initial and goal states description.

For example, consider the classic block world domain expressed in listing 2.2. It uses a predicate to express whether a block is on the table because several blocks can be on the table at once. However it uses a 0-ary function to describe the one block allowed to be held at a time. The description of the stack of blocks is done with an unary function to give the block that is on top of another one. To be able to express the absence of blocks it uses a constant named `no-block`. All the actions described are pretty straightforward: `stack` and `unstack` make sure it is possible to add or remove a block before doing it and `pick-up` and `put-down` manages the handling operations.

```

1 (define (domain BLOCKS-object-fluents)
2   (:requirements :typing :equality :object-fluents)
3   (:types block)
4   (:constants no-block - block)
5   (:predicates (on-table ?x - block))
6   (:functions (in-hand) - block
7               (on-block ?x - block) - block) ;;what is in top of block ?x
8
9   (:action pick-up
10    :parameters (?x - block)
11    :precondition (and (= (on-block ?x) no-block) (on-table ?x) (=
12    (in-hand) no-block))
13    :effect
14    (and (not (on-table ?x))
15         (assign (in-hand) ?x)))
16
17   (:action put-down
18    :parameters (?x - block)
19    :precondition (= (in-hand) ?x)
20    :effect
21    (and (assign (in-hand) no-block)
22         (on-table ?x)))
23
24   (:action stack
25    :parameters (?x - block ?y - block)
26    :precondition (and (= (in-hand) ?x) (= (on-block ?y) no-block))
27    :effect
28    (and (assign (in-hand) no-block)
29         (assign (on-block ?y) ?x)))
30
31   (:action unstack
32    :parameters (?x - block ?y - block)
33    :precondition (and (= (on-block ?y) ?x) (= (on-block ?x)
34    no-block) (= (in-hand) no-block))
35    :effect
36    (and (assign (in-hand) ?x)
37         (assign (on-block ?y) no-block))))

```

Listing 2.2: Classical PDDL 3.0 definition of the domain Block world

However, PDDL is far from an universal standard. Some efforts have been made to try and standardize the domain of automated planning in the form of optional requirements. The latest of the PDDL standard is the version 3.1 (Kovacs 2011). It has 18 atomic requirements as represented in figure 2.7. Most requirements are parts of PDDL that either increase the complexity of planning significantly or that require extra implementation effort to meet.

Even with that flexibility, PDDL is unable to cover all of automated planning paradigms. This caused most subdomains of automated planning to be left in a state similar to before PDDL: a zoo of languages and derivatives that aren't interoperable. The reason for this is the fact that PDDL isn't expressive enough to encode more than a limited variation in action and fluent description.

Another problem is that PDDL isn't made to be used by planners to help with their planning process. Most planners will totally separate the compilation of PDDL before doing any planning, so much so that most planners of the latest IPC used a framework that translates PDDL into a useful form before planning, adding computation time to the planning process. The list of participating planners and their use of language is presented in table 2.3.

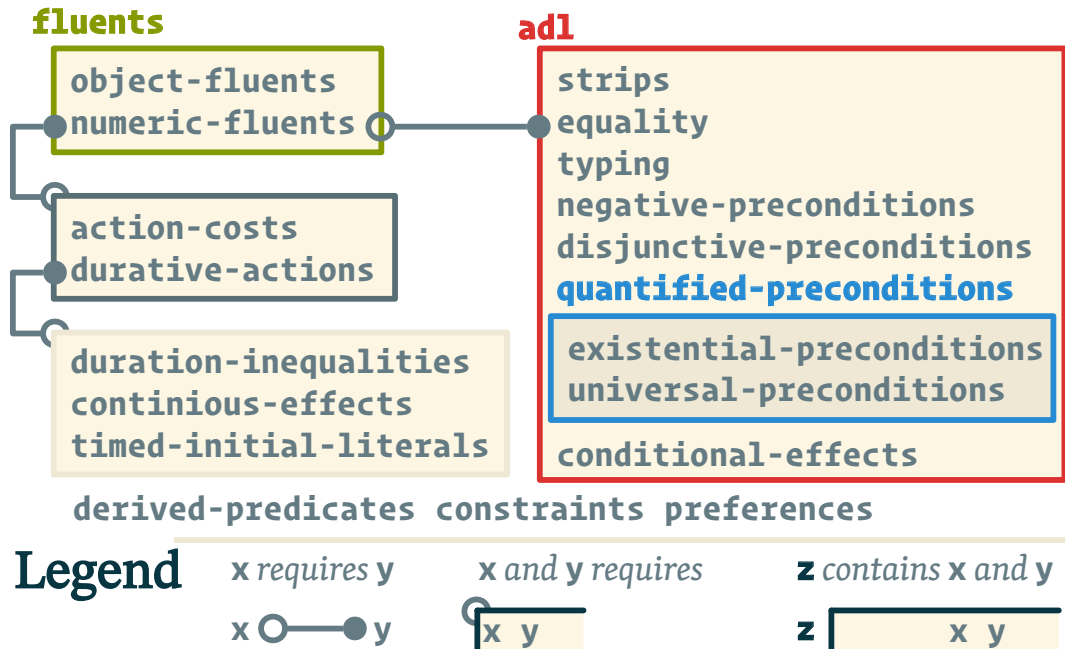


Figure 2.7: Dependencies and grouping of PDDL requirements.

Table 2.3: Planners participating in the Classic track of the 2018 International Planning Competition (IPC). The table states whether the planner used a translation and a preprocessing system to handle PDDL. Most of the planners are based on FastDownward directly.

Name	Trans	Pre	Lang	Base	Rank
Delfi	Yes	Yes	C++	FD	1
Complementary	Yes	Yes	C++	FD	2
Planning-PDBs	Yes	Yes	C++	FD	3
Scorpion	Yes	Yes	C++	FD	4
FDMS	Yes	Yes	C++	FD	5
DecStar	Yes	Yes	C++	LAMA	6
Metis	Yes	Yes	C++	FD	7
MSP	Yes	Yes	Lisp	FD	8
Symple	Yes	Yes	C++	FD	9
Ma-plan	No	Yes	C	None	10

The domain is so diverse that attempts to unify it haven't succeeded so far. The main reason behind this is that some paradigms are vastly different from the classical planning description. Sometimes just adding a seemingly small feature like probabilities or plan reuse can make for a totally different problem. In the next section we describe planning paradigms and how they differ from classical planning along with their associated languages.

## 2.4.2 Temporality oriented

When planning, time can become a sensitive constraint. Some critical tasks may be required to be completed within a certain time. Actions with durations are already a feature of PDDL 3.1. However, PDDL might not provide support for external events (i.e. events occurring independent from the agent). To do this one must use another language.

### 2.4.2.1 PDDL+

PDDL+ is an extension of PDDL 2.1 that handles process and events (Fox and Long 2002). It can be viewed as similar to PDDL 3.1 continuous effects but it differs on the expressivity. A process can have an effect on fluents at any time. They can happen either from the agent's own doing or being purely environmental. It might be possible in certain cases to modelize this using the durative actions, continuous effects and timed initial literals of PDDL 3.1.

In listing 2.3, we reproduce an example from Fox and Long (2002). It shows the syntax of durative actions in PDDL+. The timed precondition are also available in PDDL 3.1, but the `increase` and `decrease` rate of fluents is an exclusive feature of PDDL+.

```
1 (:durative-action downlink
2   :parameters (?r - recorder ?g - groundStation)
3   :duration (> ?duration 0)
4   :condition (and (at start (inView ?g))
5                 (over all (inView ?g))
6                 (over all (> (data ?r) 0)))
7   :effect (and (increase (downlinked)
8                (* #t (transmissionRate ?g)))
9              (decrease (data ?r)
10                (* #t (transmissionRate ?g))))))
```

Listing 2.3: Example of PDDL+ durative action from Fox's paper.

The main issue with durative actions is that time becomes a continuous resource that may change the values of fluents. The search for a plan in that context has a higher complexity than regular planning.

### 2.4.3 Probabilistic

Sometimes, acting can become unpredictable. An action can fail for many reasons, from logical errors down to physical constraints. This calls for a way to plan using probabilities with the ability to recover from any predicted failures. PDDL doesn't support using probabilities. That is why all IPC's tracks dealing with it always used another language than PDDL.

### 2.4.3.1 PPDDL

PPDDL is such a language. It was used during the 4<sup>th</sup> and 5<sup>th</sup> IPC for its probabilistic track (Younes and Littman 2004). It allows for probabilistic effects as demonstrated in listing 2.4. The planner must take into account the probability when choosing an action. The plan must be the most likely to succeed. But even with the best plan, failure can occur. This is why probabilistic planning often gives policies instead of a plan. A policy dictates the best choice in any given state, failure or not. While this allows for much more resilient execution, computation of policies are exponentially harder than classical planning. Indeed the planner needs to take into account every outcome of every action in the plan and react accordingly.

```
1 (define (domain bomb-and-toilet)
2   (:requirements :conditional-effects :probabilistic-effects)
3   (:predicates (bomb-in-package ?pkg) (toilet-clogged)
4               (bomb-defused))
5   (:action dunk-package
6         :parameters (?pkg)
7         :effect (and (when (bomb-in-package ?pkg)
8                        (bomb-defused))
9                    (probabilistic 0.05 (toilet-clogged)))))
```

Listing 2.4: Example of PPDDL use of probabilistic effects from Younes' paper.

### 2.4.3.2 RDDDL

Another language used by the 7<sup>th</sup> IPC's uncertainty track is RDDDL (Sanner 2010). This language has been chosen because of its ability to express problems that are hard to encode in PDDL or PPDDL. Indeed, RDDDL is capable of expressing Partially Observable Markovian Decision Process (POMDP) and Dynamic Bayesian Networks (DBN) in planning domains. This along with complex probability laws allows for easy implementation of most probabilistic planning problems. Its syntax differs greatly from PDDL, and seems closer to scala or C++. An example is provided in listing 2.5 from Sanner (2010). In it, we can see that actions in RDDDL doesn't need preconditions or effects. In that case the reward is the closest information to the classical goal and the action is simply a parameter that will influence the probability distribution of the events that conditioned the reward.

```
1 ///////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////
2 // A simple propositional 2-slice DBN (variables are not parameterized).
3 //
4 // Author: Scott Sanner (ssanner [at] gmail.com)
5 ///////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////////
6 domain prop_dbn {
7
8   requirements = { reward-deterministic };
9
10  pvariables {
11    p : { state-fluent, bool, default = false };
12    q : { state-fluent, bool, default = false };
13    r : { state-fluent, bool, default = false };
14    a : { action-fluent, bool, default = false };
15  };
16
17  cpfs {
```

```

18      // Some standard Bernoulli conditional probability tables
19      p' = if (p ^ r) then Bernoulli(.9) else Bernoulli(.3);
20
21      q' = if (q ^ r) then Bernoulli(.9)
22           else if (a) then Bernoulli(.3) else Bernoulli(.8);
23
24      // KronDelta is like a DiracDelta, but for discrete data (boolean
25      // or int)
26      r' = if (~q) then KronDelta(r) else KronDelta(r <=> q);
27
28      // A boolean functions as a 0/1 integer when a numerical value is
29      // needed
30      reward = p + q - r; // a boolean functions as a 0/1 integer when a
31                          // numerical value is needed
32 }
33
34 instance inst_dbn {
35     domain = prop_dbn;
36     init-state {
37         p = true; // could also just say 'p' by itself
38         q = false; // default so unnecessary, could also say '~q' by
39                   // itself
40         r; // same as r = true
41     };
42
43     max-nondef-actions = 1;
44     horizon = 20;
45     discount = 0.9;
46 }

```

Listing 2.5: Example of RDDDL syntax by Sanner.

## 2.4.4 Multi-agent

Planning can also be a collective effort. In some cases, a system must account for other agents trying to either cooperate or compete in achieving similar goals. The problem that arise is coordination. How to make a plan meant to be executed with several agents concurrently ? Several multi-agent action languages have been proposed to answer that question.

### 2.4.4.1 MAPL

Another extension of PDDL 2.1, MAPL was introduced to handle synchronization of actions (Brenner 2003). This is done using modal operators over fluents. In that regard, MAPL is closer to the PDDL+ extension proposed earlier. It introduce durative actions that will later be integrated into the PDDL 3.0 standard. MAPL also introduce a synchronization mechanism using speech as a communication vector. This seems very specific as explicit communication isn't a requirement of collaborative work. Listing 2.6 is an example of the syntax of MAPL domains. PDDL 3.0 seems to share a similar syntax.

```

1 (:state-variables
2   (pos ?a - agent) - location
3   (connection ?p1 ?p2 - place) - road
4   (clear ?r - road) - boolean)

```

```

5 (:durative-action Move
6   :parameters (?a - agent ?dst - place)
7   :duration (:= ?duration (interval 2 4))
8   :condition
9     (at start (clear (connection (pos ?a) ?dst)))
10  :effect (and
11    (at start (:= (pos ?a) (connection (pos ?a) ?dst)))
12    (at end (:= (pos ?a) ?dst))))

```

Listing 2.6: Example of MAPL syntax by Brenner.

#### 2.4.4.2 MA-PDDL

Another aspect of multi-agent planning is the ability to affect tasks and to manage interactions between agents efficiently. For this MA-PDDL seems more adapted than MAPL. It is an extension of PDDL 3.1, that makes easier to plan for a team of heterogeneous agents (Kovács 2012). In the example in listing 2.7, we can see how action can be affected to agents. While it makes the representation easier, it is possible to obtain similar effect by passing an agent object as parameter of an action in PDDL 3.1. More complex expressions are possible in MA-PDDL, like referencing the action of other agents in the preconditions of actions or the ability to affect different goals to different agents. Later on, MA-PDDL was extended with probabilistic capabilities inspired by PPDDL (Kovács and Dobrowiecki 2013).

```

1 (define (domain ma-lift-table)
2   (:requirements :equality :negative-preconditions
3     :existential-preconditions :typing :multi-agent)
4   (:types agent) (:constants table)
5   (:predicates (lifted (?x - object) (at ?a - agent ?o - object))
6   (:action lift :agent ?a - agent :parameters ()
7   :precondition (and (not (lifted table)) (at ?a table)
8     (exists (?b - agent)
9       (and (not (= ?a ?b)) (at ?b table) (lift ?b))))
10  :effect (lifted table)))

```

Listing 2.7: Example of MA-PDDL syntax by Kovacs.

### 2.4.5 Hierarchical

Another approach to planning is using Hierarchical Tasks Networks (HTN) to resolve some planning problem. Instead of searching to satisfy a goal, HTNs try to find a decomposition to a root task that fit the initial state requirements and that generate an executable plan.

#### 2.4.5.1 UMCP

One of the first planner to support HTN domains was UCMP by Erol *et al.* (1994). It uses Lisp like most of the early planning systems. Apparently PDDL was in part inspired by UCMP's syntax. Like for PDDL, the domain file describes action (called operators here) and their preconditions and effects (called postconditions). The syntax is demonstrated in listing 2.8. The interesting part of that language is the way decomposition is handled. Each task is expressed as a set of methods. Each method has an expansion expression that specifies how the plan should be constructed. It also has a pseudo precondition with modal operators on the temporality of the validity of the literals.



```

1 (constants a b c table) ; declare constant symbols
2 (predicates on clear) ; declare predicate symbols
3 (compound-tasks move) ; declare compound task symbols
4 (primitive-tasks unstack dostack restack) ; declare primitive task symbols
5 (variables x y z) ; declare variable symbols
6
7 (operator unstack(x y)
8     :pre ((clear x)(on x y))
9     :post ((~on x y)(on x table)(clear y)))
10 (operator dostack (x y)
11     :pre ((clear x)(on x table)(clear y))
12     :post ((~on x table)(on x y)(~clear y)))
13 (operator restack (x y z)
14     :pre ((clear x)(on x y)(clear z))
15     :post ((~on x y)(~clear z)(clear y)(on x z)))
16
17 (declare-method move(x y z)
18     :expansion ((n restack x y z))
19     :formula (and (not (veq y table))
20                 (not (veq x table))
21                 (not (veq z table))
22                 (before (clear x) n)
23                 (before (clear z) n)
24                 (before (on x y) n)))
25
26 (declare-method move(x y z)
27     :expansion ((n dostack x z))
28     :formula (and (veq y table)
29                 (before (clear x) n)
30                 (before (on x y) n)))

```

Listing 2.8: Example of the syntax used by UCMP.

### 2.4.5.2 SHOP2

The next HTN planner is SHOP2 by Nau *et al.* (2003). It remains to this day, one of the reference implementation of an HTN planner. The SHOP2 formalism is quite similar to UCMP's: each method has a signature, a precondition formula and eventually a decomposition description. This decomposition is a set of methods like in UCMP. The methods can be also partially ordered allowing more expressive plans. An example of the syntax of a method is given in listing 2.9.

```

1 (:method
2   ; head
3   (transport-person ?p ?c2)
4   ; precondition
5   (and
6     (at ?p ?c1)
7     (aircraft ?a)
8     (at ?a ?c3)
9     (different ?c1 ?c3))
10  ; subtasks
11  (:ordered
12    (move-aircraft ?a ?c1)
13    (board ?p ?a ?c1))

```

```

14      (move-aircraft ?a ?c2)
15      (debark ?p ?a ?c2)))

```

Listing 2.9: Example of method in the SHOP2 language.

### 2.4.5.3 HDDL

A more recent example of HTN formalism comes from the PANDA framework by Bercher *et al.* (2014). This framework is considered the current standard of HTN planning and allows for great flexibility in domain description. PANDA takes previous formalism and generalize them into a new language exposed in listing 2.10. That language was called HDDL after its most used file extension.

```

1 (define (domain transport)
2   (:requirements :typing :action-costs)
3   (:types
4     location target locatable - object
5     vehicle package - locatable
6     capacity-number - object
7   )
8   (:predicates
9     (road ?l1 ?l2 - location)
10    (at ?x - locatable ?v - location)
11    (in ?x - package ?v - vehicle)
12    (capacity ?v - vehicle ?s1 - capacity-number)
13    (capacity-predecessor ?s1 ?s2 - capacity-number)
14  )
15
16  (:task deliver :parameters (?p - package ?l - location))
17  (:task unload :parameters (?v - vehicle ?l - location ?p - package))
18
19  (:method m-deliver
20    :parameters (?p - package ?l1 ?l2 - location ?v - vehicle)
21    :task (deliver ?p ?l2)
22    :ordered-subtasks (and
23      (get-to ?v ?l1)
24      (load ?v ?l1 ?p)
25      (get-to ?v ?l2)
26      (unload ?v ?l2 ?p))
27  )
28  (:method m-unload
29    :parameters (?v - vehicle ?l - location ?p - package ?s1 ?s2 -
30      capacity-number)
31    :task (unload ?v ?l ?p)
32    :subtasks (drop ?v ?l ?p ?s1 ?s2)
33  )
34  (:action drop
35    :parameters (?v - vehicle ?l - location ?p - package ?s1 ?s2 -
36      capacity-number)
37    :precondition (and
38      (at ?v ?l)
39      (in ?p ?v)
40      (capacity-predecessor ?s1 ?s2)
41      (capacity ?v ?s1)
42    )
43    :effect (and

```

```

43      (not (in ?p ?v))
44      (at ?p ?l)
45      (capacity ?v ?s2)
46      (not (capacity ?v ?s1))
47    )
48  )
49 )

```

Listing 2.10: Example of HDDL syntax as used in the PANDA framework.

#### 2.4.5.4 HPDDL

A very recent language proposition was done by RAMOUL (2018). He proposes HPDDL with a simple syntax similar to the one of UCMP. In listing 2.11 we give an example of HPDDL method. Its expressive power seems similar to that of UCMP and SHOP. Except for a possible commercial integration with PDDL4J (Pellier and Fiorino 2017), there doesn't seem to have any advantages compared to earlier works.

```

1 (:method do_navigate
2   :parameters(?x - rover ?from ?to - waypoint)
3   :expansion((tag t1 (navigate ?x ?from ?mid))
4             (tag t2 (visit ?mid))
5             (tag t3 (do_navigate ?x ?mid ?to))
6             (tag t4 (unvisited ?mid)))
7   :constraints((before (and (not (can_traverse ?x ?from ?to)) (not
8                           (visited ?mid))
                           (can_traverse ?x ?from ?mid)) t1)))

```

Listing 2.11: Example of HPDDL syntax as described by Ramoul.

#### 2.4.6 Ontological

Another old idea was to merge automated planning and other artificial intelligence fields with knowledge representation and more specifically ontologies. Indeed, since the "semantic web" is already widespread for service description, why not make planning compatible with it to ease service composition ?

##### 2.4.6.1 WebPDDL

This question finds its first answer in 2002 with WebPDDL. This language, explicit in listing 2.12, is meant to be compatible with RDF by using URI identifiers for domains (McDermott and Dou 2002). The syntax is inspired by PDDL, but axioms are added as constraints on the knowledge domain. Actions also have a return value and can have variables that aren't dependant on their parameters. This allows for greater expressivity than regular PDDL, but can be partially emulated using PDDL 3.1 constraints and object fluents.

```

1 (define (domain www-agents)
2   (:extends (uri "http://www.yale.edu/domains/knowning")
3             (uri "http://www.yale.edu/domains/regression-planning")
4             (uri "http://www.yale.edu/domains/commerce"))
5   (:requirements :existential-preconditions :conditional-effects)
6   (:types Message - Obj Message-id - String)

```

```

7  (:functions (price-quote ?m - Money)
8             (query-in-stock ?pid - Product-id)
9             (reply-in-stock ?b - Boolean) - Message)
10 (:predicates (web-agent ?x - Agent)
11             (reply-pending a - Agent id - Message-id msg - Message)
12             (message-exchange ?interlocutor - Agent
13                               ?sent ?received - Message
14                               ?eff - Prop)
15             (expected-reply a - Agent sent expect-back - Message))
16 (:axiom
17   :vars (?agt - Agent ?msg-id - Message-id ?sent ?reply - Message)
18   :implies (normal-step-value (receive ?agt ?msg-id) ?reply)
19   :context (and (web-agent ?agt)
20               (reply-pending ?agt ?msg-id ?sent)
21               (expected-reply ?agt ?sent ?reply)))
22 (:action send
23   :parameters (?agt - Agent ?sent - Message)
24   :value (?sid - Message-id)
25   :precondition (web-agent ?agt)
26   :effect (reply-pending ?agt ?sid ?sent))
27 (:action receive
28   :parameters (?agt - Agent ?sid - Message-id)
29   :vars (?sent - Message ?eff - Prop)
30   :precondition (and (web-agent ?agt) (reply-pending ?agt ?sid ?sent))
31   :value (?received - Message)
32   :effect (when (message-exchange ?agt ?sent ?received ?eff) ?eff)))

```

Listing 2.12: Example of WebPDDL syntax by Mc Dermott.

#### 2.4.6.2 OPT

This previous work was updated by McDermott (2005). The new version is called OPT and allows for some further expressivity. It can express hierarchical domains with links between actions and even advanced data structure. The syntax is mostly an update of WebPDDL. In listing 2.13, we can see that the URI were replaced by simpler names, the action notation was simplified to make the parameter and return value more natural. Axioms were replaced by facts with a different notation.

```

1 (define (domain www-agents)
2   (:extends knowing regression-planning commerce)
3   (:requirements :existential-preconditions :conditional-effects)
4   (:types Message - Obj Message-id - String )
5   (:type-fun (Key t) (Feature-type (keytype t)))
6   (:type-fun (Key-pair t) (Tup (Key t) t))
7   (:functions (price-quote ?m - Money)
8             (query-in-stock ?pid - Product-id)
9             (reply-in-stock ?b - Boolean) - Message)
10  (:predicates (web-agent ?x - Agent)
11              (reply-pending a - Agent id - Message-id msg - Message)
12              (message-exchange ?interlocutor - Agent
13                                ?sent ?received - Message
14                                ?eff - Prop)
15              (expected-reply a - Agent sent expect-back - Message))
16  (:facts
17    (freevars (?agt - Agent ?msg-id - Message-id
18              ?sent ?reply - Message)
19      (<- (and (web-agent ?agt)

```

```

20         (reply-pending ?agt ?msg-id ?sent)
21         (expected-reply ?agt ?sent ?reply))
22         (normal-value (receive ?agt ?msg-id ?reply))))
23 (:action (send ?agt - Agent ?sent - Message) - (?sid - Message-id)
24   :precondition (web-agent ?agt)
25   :effect (reply-pending ?agt ?sid ?sent))
26 (:action (receive ?agt - Agent ?sid - Message-id) - (?received -
27   Message)
28   :vars (?sent - Message ?eff - Prop)
29   :precondition (and (web-agent ?agt)
30     (reply-pending ?agt ?sid ?sent))
31   :effect (when (message-exchange ?agt ?sent ?received ?eff) ?eff)))

```

Listing 2.13: Example of the updated OPT syntax as described by Mc Dermott.

## 2.5 Color and general planning representation

From the general formalism of planning proposed earlier, it is possible to create an instantiation of the SELF language for expressing planning domains. This extension was the primary goal of creating SELF and uses almost all features of the language.

### 2.5.1 Framework

In order to describe this planning framework into SELF, we simply put all fields of the actions into properties. Entities are used as fluents, and the entire knowledge domain as constraints. We use parameterized types as specified **BEFORE**.

```

1 "lang.w" = ? ; //include default language file.
2 Fluent = Entity;
3 State = (Group(Fluent), Statement);
4 BooleanOperator = (&,|);
5 (pre,eff, constr)::Property(Action,State);
6 (costs,lasts,probability) ::Property(Action,Float);
7 Plan = Group(Statement);
8 -> ::Property(Action,Action); //Causal links
9 methods ::Property(Action,Plan);

```

Listing 2.14: Content of the file "planning.w"

The file presented in listing 2.14, gives the definition of the syntax of fluents and actions in SELF. The first line includes the default syntax file using the first statement syntax. The fluents are simply typed as entities. This allows them to be either parameterized entities or statements. States are either a set of fluent or a logical statement between states or fluents. When a state is represented as a set, it represent the conjunction of all fluents in the set.

Then at line 5, we define the preconditions, effects and constraints formalism. They are represented as simple properties between actions and states. This allows for simple expression of commonly expressed formalism like the ones found in PDDL. Line 6 expresses the other attributes of actions like cost, duration and prior probability of success.

Plans are needed to be represented in the files, especially for case based and hierarchical paradims. They are expressed using statements for causal link representation. The property `->` is used in these

statements and the causes are either given explicitly as parameters of the property or they can be inferred by the planner. We add a last property to express methods relative to their actions.

### 2.5.2 Example domain

Using the classical example domain used earlier we can write the following file in listing 2.15.

```
1 "planning.w" = ? ; //include base terminology
2
3 (! on !, held(!), down(_)) :: Fluent;
4
5 pickUp(x) pre (~ on x, down(x), held(~));
6 pickUp(x) eff (~(down(x)), held(~));
7
8 putDown(x) pre (held(x));
9 putDown(x) eff (held(~), down(x));
10
11 stack(x, y) pre (held(x), ~ on y);
12 stack(x, y) eff (held(~), x on y);
13
14 unstack(x, y) pre (held(~), x on y);
15 unstack(x, y) eff (held(x), ~ on y);
```

Listing 2.15: Blockworld written in SELF to work with Color

At line line 1, We need to include the file defined in listing 2.14. After that line 3 defines the allowed arity of each relation/function used by fluents. This restricts eventually the cardinality between parameters (one to many, many to one, etc).

Line 5 encodes the action *pickUp* defined earlier. It is interesting to note that instead of using a constant to denote the absence of block, we can use an anonymous exclusive quantifier to make sure no block is held. This is quite useful to make concise domains that stays expressive and intuitive.

### 2.5.3 Differences with PDDL

SELF+Color is more concise than PDDL. It will infer most types and declaration. Variables are also inferred if they are used more than once in a statement and also part of parameters.

While PDDL uses a fixed set of extensions to specify the capabilities of the domain, SELF uses inclusion of other files to allow for greater flexibility. In PDDL, everything must be declared while in SELF, type inference allows for usage without definition. It is interesting to note that the use of variables names *x* and *y* are arbitrary and can be changed for each statement and the domain will still be functionally the same. The line 3 in listing 2.2 is a specific feature of SELF that is absent in PDDL. It is possible to specify constraints on the cardinality of properties. This limits the number of different combination of values that can be true at once. This is typically done in PDDL using several predicate or constraints.

Most of the differences can be summarized saying that 'SELF do it once, PDDL needs it twice'. This doesn't only mean that SELF is more compact but also that the expressivity allows for a drastic reduction of the search space if taken into account. Thiébaux *et al.* (2005) advocate for the recognition of the fact that expressivity isn't just a convenience but is crucial for some problem and that treating it like an obstacle by trying to compile it away only makes the problem worse. If a planner is agnostic to the domain and

problem, it cannot take advantages of clues that the instantiation of an action or even its name can hold (Babli *et al.* 2015).

Whatever the time and work that an expert spend on a planning domain it will always be incomplete and fixed. SELF allows for dynamical extension and even addresses the use of reified actions as parameters. Such a framework can be useful in multi-agent systems where agents can communicate composite actions to instruct another agent. It can also be useful for macro-action learning that allows to learn hierarchical domains from repeating observations. It can also be used in online planning to repair a plan that failed. And at last this mechanism can be used for explanation or inference by making easy to map two similar domains together. (lots of **CITATION**).

Also another difference between SELF and PDDL is the underlying planning framework. We presented the one of SELF but PDDL seems to suppose a more classical state based formalism. For example the fluents are of two kind depending if they are used as precondition or effects. In the first case, the fluent is a formula that is evaluated like a predicate to know if the action can be executed in any given state. Effects are formula enforcing the values of existing fluent in the state. SELF just suppose that the new knowledge is enforcing and that the fluents are of the same kind since verification about the coherence of the actions are made prior to its application in planning.

## 3 Online and Flexible Planning Algorithms

Since automated planning comes in a variety of paradigms, so does the planners algorithms. It amounts to such a number of planners that listing all those that exists would be a terribly long endeavour.

In that chapter, we present planners and approaches to inverted planning and intent recognition. To do that we must first have a performant online planning algorithm that can take into account observed plans or fluents and find the most likely plan being pursued by an external agent.

Classical planning can be used for such a work but lacks flexibility when needing to replan at high frequency. The planner must be either able to reuse previously found plans or be able to give quickly plans that are good approximation of the intended goal. We could use probabilistic planning, especially Partially Observable Markovian Decision Process (POMDP) to directly encode the intent recognition problem but that approach have been explored in great detail already, including numerous bayesian network approaches. We propose to create planners fit for this use by deriving from POCL and HTN planning.

### 3.1 Existing Algorithms

In order to make such a planner, few paradigms are interesting and quite useful. The first one is PSP, that allows to refine plans into solutions.

#### 3.1.1 Plan Space Planning

Every PSP algorithms works in a similar way: their search space is the set of all plans and its iteration operation is plan refinement. This means that every PSP planner searches for *flaws* in the current plan and then computes a set of *resolvers* that potentially fix it. The PSP approach has two main advantages:

1. It is very flexible since it allows for custom definition for flaws in the plan and ways to fix them and
2. It allows delayed comitment and makes it possible to cut the search tree early on.

It however has also several inconvenients:

1. Since it manipulates plans, the data structure operations are much more complex and therefore requires more overhead.
2. Backtracking is required in some cases and ammount to a drastically decreased efficiency.

##### 3.1.1.1 Existing PSP planners

Related works already tried to explore new ideas to make PSP an attractive alternative to regular state-based planners like the appropriately named "Reviving partial order planning" (Nguyen and Kambhampati 2001) and VHPOP (Younes and Simmons 2003). More recent efforts (Coles *et al.* 2011; Sapena *et al.* 2014) are trying to adapt the powerful heuristics from state-based planning to PSP's



approach. An interesting approach of these last efforts is found in (Shekhar and Khemani 2016) with meta-heuristics based on offline training on the domain. Yet, we clearly note that only a few papers lay the emphasis upon plan quality using PSP (Ambite and Knoblock 1997).

### 3.1.1.2 Definitions

In section ?? we have formalized how PSP works in the general planning formalism. However, since this formalism is very new, it isn't used by the rest of the community. This means that we still need to define the classical PSP algorithm.

The main notion of PSP is the notion of flaws in a plan.

**Definition 17** (Flaws). Flaws have a *proper fluent*  $f$  and a causing step often called the *needer*  $a_n$ . Flaws in a partial plan are either:

- **Subgoals**, *open conditions* that are yet to be supported by another step  $a_n$  often called *provider*. We note subgoals  $\downarrow_f a_n$ .
- **Threats**, caused by steps that can break a causal link with their effects. They are called *breakers* of the threatened link. A step  $a_b$  threatens a causal link  $l_t = a_p \xrightarrow{f} a_n$  if and only if  $\neg f \in \text{eff}(a_b) \wedge a_b \not\prec a_p \wedge a_n \not\prec a_b$ . Said otherwise, the breaker can cancel an effect of a providing step  $a_p$ , before it gets used by its needer  $a_n$ . We note threats  $a_b \boxtimes l_t$ .

### 3.1.2 Plan repair

In order to make an efficient online planner, we must be able to capitalize on previously computed plans. This leads to the idea of plan repair or case based planning for online planning.

Classical PSP algorithms don't take as an input an existing plan but can be enhanced to fit plan repairing, as for instance in (Van Der Krogt and De Weerd 2005). Usually, PSP algorithms take a problem as an input and use a loop or a recursive function to refine the plan into a solution. We can't solely use the refining recursive function to be able to use our existing partial plan. This causes multiples side effects if the input plan is suboptimal. This problem was already explored as of LGP-adapt (???) that explains how re-using a partial plan often implies replanning parts of the plan.

### 3.1.3 HTN

HTN is often combined with classical approaches since it allows for a more natural expression of domains making expert knowledge easier to encode. These kinds of planners are named **decompositional planners** when no initial plan is provided (Fox 1997). Most of the time the integration of HTN simply consists in calling another algorithm when introducing a composite operator during the planning process. The DUET planner by Gerevini *et al.* (2008) does so by calling an instance of a HTN planner based on task insertion called SHOP2 (Nau *et al.* 2003) to decompose composite actions. Some planners take the integration further by making the decomposition of composite actions into a special step in their refinement process. Such works include the discourse generation oriented DPOCL (Young and Moore 1994) and the work of Kambhampati *et al.* (1998) generalizing the practice for decompositional planners.

In our case, we chose a class of hierarchical planners based on Plan-Space Planning (PSP) algorithms (Bechon *et al.* 2014; Dvorak *et al.* 2014; Bercher *et al.* 2014) as a reference approach. The main difference here is that the decomposition is integrated into the classical POCL algorithm by only adding new types of flaws. This allows keeping all the flexibility and properties of POCL while adding the expressivity and abstraction capabilities of HTN.

## 3.2 Lollipop

### 3.2.1 Operator Graph

One of the main contributions of the present paper is our use of the concept of *operator graph*. First of all, we define this notion.

**Definition 18** (Operator Graph). An operator graph  $O^\Pi$  of a set of operators  $O$  is a labeled directed graph that binds two operators with the causal link  $o_1 \xrightarrow{f} o_2$  iff there exists at least one unifying fluent  $f \in \text{eff}(o_1) \cap \text{pre}(o_2)$ .

This definition was inspired by the notion of domain causal graph as explained in (Göbelbecker *et al.* 2010) and originally used as a heuristic in (Helmert *et al.* 2011). Causal graphs have fluents as their nodes and operators as their edges. Operator graphs are the opposite: an *operator dependency graph* for a set of actions. A similar structure was used in (???) that builds the operator dependency graph of goals and uses precondition nodes instead of labels. Cycles in this graph denote the dependencies of operators. We call *co-dependent* operators that form a cycle. If the cycle is made of only one operator (self-loop), then it is called *auto-dependent*.

While building this operator graph, we need a **providing map** that indicates, for each fluent, the list of operators that can provide it. This is a simpler version of the causal graphs that is reduced to an associative table easier to update. The list of providers can be sorted to drive resolver selection (as detailed in section ??). A **needing map** is also built but is only used for operator graph generation. We note  $\mathcal{D}^\Pi$  the operator graph built with the set of operators in the domain  $\mathcal{D}$ . In the figure 3.1, we illustrate the application of this mechanism on our example from ??. Continuous lines correspond to the *domain operator graph* computed during domain compilation time.



Figure 3.1: Diagram of the operator graph of example domain. Full arrows represent the domain operator graph and dotted arrows the dependencies added to inject the initial and goal steps.

The generation of the operator graph is detailed in algorithm ??. It explores the operators space and builds a providing and a needing map that gives the provided and needed fluents for each operator. Once done it iterates on every precondition and searches for a satisfying cause to add the causal links to

the operator graph.

//////////111111

To apply the notion of operator graphs to planning problems, we just need to add the initial and goal steps to the operator graph. In figure 3.1, we depict this insertion with our previous example using dotted lines. However, since operator graphs may have cycles, they can't be used directly as input to POP algorithms to ease the initial backchaining. Moreover, the process of refining an operator graph into a usable one could be more computationally expensive than POP itself.

In order to give a head start to the LOLLIPOP algorithm, we propose to build operator graphs differently with the algorithm detailed in algorithm ???. A similar notion was already presented as "basic plans" in (???). These "basic" partial plans use a more complete but slower solution for the generation that ensures that each selected steps are *necessary* for the solution. In our case, we built a simpler solution that can solve some basic planning problems but that also make early assumptions (since our algorithm can handle them). It does a simple and fast backward construction of a partial plan driven by the providing map. Therefore, it can be tweaked with the powerful heuristics of state search planning.

//////////22222

This algorithm is useful since it is specifically used on goals. The result is a valid partial plan that can be used as input to POP algorithms.

### 3.2.2 Negative Refinements

The classical POP algorithm works upon a principle of positive plan refinements. The two standard flaws (subgoals and threats) are fixed by *adding* steps, causal links, or variable binding constraints to the partial plan. Online planning needs to be able to *remove* parts of the plan that are not necessary for the solution. Since we assume that the input partial plan is quite complete, we need to define new flaws to optimize and fix this plan. These flaws are called *negative* as their resolvers apply subtractive refinements on partial plans.

**Definition 19** (Alternative). An alternative is a negative flaw that occurs when there is a better provider choice for a given link. An alternative to a causal link  $a_p \xrightarrow{f} a_n$  is a provider  $a_b$  that has a better *utility value* than  $a_p$ .

The **utility value** of an operator is a measure of usefulness at the heart of our ranking mechanism detailed in section ???. It uses the incoming and outgoing degrees of the operator in the domain operator graph to measure its usefulness.

Finding an alternative to an operator is computationally expensive. It requires searching a better provider for every fluent needed by a step. To simplify that search, we select only the best provider for a given fluent and check if the one used is the same. If not, we add the alternative as a flaw. This search is done only on updated steps for online planning. Indeed, the safe operator graph mechanism is guaranteed to only choose the best provider (@alg:safeoperatorgraph at line ??). Furthermore, subgoals won't introduce new fixable alternative as they are guaranteed to select the best possible provider.

**Definition 20** (Orphan). An orphan is a negative flaw that occurs when a step in the partial plan (other than the initial or goal step) is not participating in the plan. Formally,  $a_o$  is an orphan iff  $a_o \neq I \wedge a_o \neq G \wedge (d_\pi^+(a_o) = 0) \vee \forall l \in L_\pi^+(a_o), l = \emptyset$ .

With  $d_\pi^+(a_o)$  being the *outgoing degree* of  $a_o$  in the directed graph formed by  $\pi$  and  $L_\pi^+(a_o)$  being the set of *outgoing causal links* of  $a_o$  in  $\pi$ . This last condition checks for *hanging orphans* that are linked to the goal with only bare causal links (introduced by threat resolution).

The introduction of negative flaws requires modifying the resolver definition (cf. definition ??). :::  
 {.definition name="Signed Resolvers"} A signed resolver is a resolver with a notion of sign. We add to the resolver tuple the sign of the resolver noted  $s \in \{+, -\}$ . :::

The solution to an alternative is a negative refinement that simply removes the targeted causal link. This causes a new subgoal as a side effect, that will focus on its resolver by its rank (explained in section ??) and then pick the first provider (the most useful one). The resolver for orphans is the negative refinement that is meant to remove a step and its incoming causal link while tagging its providers as potential orphans.



Figure 3.2: Schema representing flaws with their signs, resolvers and side effects relative to each other

The side effect mechanism also needs an upgrade since the new kind of flaws can interfere with one another. This is why we extend the side effect definition (cf. definition ??) with a notion of sign.

**Definition 21** (Signed Side Effects). A signed side effect is either a regular *causal side effect* or an *invalidating side effect*. The sign of a side effect indicates if the related flaw needs to be added or removed from the agenda.

The figure 3.2 exposes the extended notion of signed resolvers and side effects. When treating positive resolvers, nothing needs to change from the classical method. When dealing with negative resolvers, we need to search for extra subgoals and threats. Deletion of causal links and steps can cause orphan flaws that need to be identified for removal.

In the method described in (Peot and Smith 1993), a **invalidating side effect** is explained under the name of *DEnd* strategy. In classical POP, it has been noticed that threats can disappear in some cases if subgoals or other threats were applied before them. For our mechanisms, we decide to gather under this notion every side effect that removes the need to consider a flaw. For example, orphans can be invalidated if a subgoal selects the considered step. Alternatives can remove the need to compute further subgoal of an orphan step as orphans simply remove the need to fix any flaws that concern the selected step.

These interactions between flaws are decisive for the validity and efficiency of the whole model, that is

why we aim to drive flaw selection in a rigorous manner.

### 3.2.3 Usefulness Heuristic

Resolvers and flaws selection are the keys to improving performances. Choosing a good resolver helps to reduce the branching factor that accounts for most of the time spent on running POP algorithms (Kambhampati 1994). Flaw selection is also important for efficiency, especially when considering negative flaws which can conflict with other flaws.

Conflicts between flaws occur when two flaws of opposite sign target the same element of the partial plan. This can happen, for example, if an orphan flaw needs to remove a step needed by a subgoal or when a threat resolver tries to add a promoting link against an alternative. The use of side effects will prevent most of these occurrences in the agenda but a base ordering will increase the general efficiency of the algorithm.

Based on the figure 3.2, we define a base ordering of flaws by type. This order takes into account the number of flaw types affected by causal side effects.

1. **Alternatives** will cut causal links that have a better provider. It is necessary to identify them early since they will add at least another subgoal to be fixed as a related flaw.
2. **Subgoals** are the flaws that cause most of the branching factor in POP algorithms. This is why we need to make sure that all open conditions are fixed before proceeding on finer refinements.
3. **Orphans** remove unneeded branches of the plan. Yet, these branches can be found out to be necessary for the plan to meet a subgoal. Since a branch can contain many actions, it is preferable to leave the orphan in the plan until they are no longer needed. Also, threats involving orphans are invalidated if the orphan is resolved first.
4. **Threats** occur quite often in the computation. Searching and solving them is computationally expensive since they need to check if there are no paths that fix the flaw already. Many threats are generated without the need of resolver application (Peot and Smith 1993). That is why we rank all related subgoals and orphans before threats because they can add causal links or remove threatening actions that will fix the threat.

Resolvers need to be ordered as well, especially for the subgoal flaws. Ordering resolvers for a subgoal is the same operation as choosing a provider. Therefore, the problem becomes “how to rank operators?”. The most relevant information on an operator is its usefulness and hurtfulness. These show how much an operator will help and how much it may cause branching after selection.

**Definition 22** (Degree of an operator). Degrees are a measurement of the usefulness of an operator. Such a notion is derived from the incoming and outgoing degrees of a node in a graph.

We note  $d_{\pi}^{+}(o)$  and  $d_{\pi}^{-}(o)$  respectively the outgoing and incoming degrees of an operator in a plan  $\pi$ . These represent the number of causal links that goes out or toward the operator. We call proper degree of an operator  $d^{+}(o) = |eff(o)|$  and  $d^{-}(o) = |pre(o)|$  the number of preconditions and effects that reflect its intrinsic usefulness.

There are several ways to use the degrees as indicators. *Utility value* increases with every  $d^{+}$ , since this reflects a positive participation in the plan. It decreases with every  $d^{-}$  since actions with higher incoming degrees are harder to satisfy. The utility value bounds are useful when selecting special operators. For example, a user-specified constraint could be laid upon an operator to ensure it is only selected as a last resort. This operator will be affected with the smallest utility value possible. More commonly, the highest value is used for initial and goal steps to ensure their selection.

Our ranking mechanism is based on scores noted  $s^\pm(o)$ . A score contains two components: a positive subscore array that acts as a participation measurement and a negative subscore array that represents the dependencies of the operator. Each component of the score is an array of *subscores*.

The first step is the computation of the **base scores**. They are computed according to the following:

- $s^+(o)$  contains only  $d_{\mathcal{D}^\Pi}^+(o)$ , the positive degree of  $o$  in the domain operator graph. This will give a measurement of the predicted usefulness of the operator.
- $s^-(o)$  containing the following subscores:
  1.  $d^-(o)$  the proper negative degree of  $o$ . Having more preconditions can lead to a potentially higher need for subgoals.
  2.  $\sum_{c \in C_o(\mathcal{D}^\Pi)} |c|$  with  $C_o(\mathcal{D}^\Pi)$  being the set of cycles where  $o$  participates in the domain operator graph. If an action is codependent (cf. section ??) it may lead to a dead-end as its addition will cause the formation of a cycle.
  3.  $|C_o^s(\mathcal{D}^\Pi)|$  is the number of self-cycle (0 or 1)  $o$  participates in. This is usually symptomatic of a *toxic operator* (cf. definition 24). Having an operator behaving this way can lead to backtracking because of operator instantiation.
  4.  $|pre(o) \setminus L_{\mathcal{D}^\Pi}^-(o)|$  with  $L_{\mathcal{D}^\Pi}^-(o)$  being the set of incoming causal links of  $o$  in the domain operator graph. This represents the number of open conditions. This is symptomatic of action that can't be satisfied without a compliant initial step.

Once these subscores are computed, the ranking mechanism starts the second phase, which computes the **realization scores**. These scores are potential bonuses given once the problem is known. It first searches the *inapplicable operators* that are all operators in the domain operator graph that have a precondition that isn't satisfied with a causal link. Then it searches the *eager operators* that provide fluents with no corresponding causal link (as they are not needed). These operators are stored in relation with their inapplicable or eager fluents.

The third phase starts with the beginning of the solving algorithm, once the problem has been provided. It computes the **effective realization scores** based on the initial and goal steps. It will increment  $s_1^+(o)$  for each realized eager links (if the goal contains the related fluent) and decrement  $s_4^-(o)$  for each inapplicable preconditions realized by the initial step.

Last, the **final score** of each operator  $o$ , noted  $h(o)$ , is computed from positive and negative scores using the following formula:

$$h(o) = \sum_{n=1}^{|s^\pm(o)|} \pm p_n^\pm s_n^\pm(o)$$

A parameterized coefficient is associated to each subscore. It is noted  $p_n^\pm$  with  $n$  being the index of the subscore in the array  $s^\pm$ . This respects the criteria of having a bound for the *utility value* as it ensures that it remains positive with 0 as a minimum bound and  $+\infty$  for a maximum. The initial and goal steps have their utility values set to the upper bound to ensure their selections over other steps.

Choosing to compute the resolver selection at operator level has some positive consequences on the performances. Indeed, this computation is much lighter than approaches with heuristics on plan space (Shekhar and Khemani 2016) as it reduces the overhead caused by real time computation of heuristics on complex data. In order to reduce this overhead more, the algorithm sorts the providing associative array to easily retrieve the best operator for each fluent. This means that the evaluation of the heuristic is done only once for each operator. This reduces the overhead and allows for faster results on smaller plans.

### 3.2.4 Algorithm

The LOLLIPOP algorithm uses the same refinement algorithm as described in algorithm ???. The differences reside in the changes made on the behavior of resolvers and side effects. In line ??? of algorithm ??, LOLLIPOP algorithm applies negative resolvers if the selected flaw is negative. In line ??, it searches for both signs of side effects. Another change resides in the initialization of the solving mechanism and the domain as detailed in algorithm ???. This algorithm contains several parts. First, the domainInit function corresponds to the code computed during the domain compilation time. It will prepare the rankings, the operator graph, and its caching mechanisms. It will also use strongly connected component detection algorithm to detect cycles. These cycles are used during the base score computation (@line:basescore). We add a detection of illegal fluents and operators in our domain initialization (@line:isillegal). Illegal operators are either inconsistent or toxic.

////////////////////3333

**Definition 23** (Inconsistent operators). An operator  $a$  is contradictory iff  $\exists f\{f, \neg f\} \in eff(o) \vee \{f, \neg f\} \in pre(o)$

**Definition 24** (Toxic operators). Toxic operators have effects that are already in their preconditions or empty effects. An operator  $o$  is toxic iff  $pre(o) \cap eff(o) \neq \emptyset \vee eff(o) = \emptyset$

Toxic actions can damage a plan as well as make the execution of POP algorithm longer than necessary. This is fixed by removing the toxic fluents ( $pre(a) \not\subseteq eff(a)$ ) and by updating the effects with  $eff(a) = eff(a) \setminus pre(a)$ . If the effects become empty, the operator is removed from the domain.

The lollipopInit function is executed during the initialization of the solving algorithm. We start by realizing the scores, then we add the initial and goal steps in the providing map by caching them. Once the ranking mechanism is ready, we sort the providing map. With the ordered providing map, the algorithm runs the fast generation of the safe operator graph for the problem's goal.

The last part of this initialization (@line:populate) is the agenda population that is detailed in the populate function. During this step, we perform a search of alternatives based on the list of updated fluents. Online updates can make the plan outdated relative to the domain. This forms liar links :

**Definition 25** (Liar links). A liar link is a link that doesn't hold a fluent in the preconditions or effect of its source and target. We note:

$$a_i \xrightarrow{f} a_j | f \notin eff(a_i) \cap pre(a_j)$$

A liar link can be created by the removal of an effect or preconditions during online updates (with the causal link still remaining).

We call lies the fluents that are held by links without being in the connected operators. To resolve the problem, we remove all lies. We delete the link altogether if it doesn't bear any fluent as a result of this operation. This removal triggers the addition of orphan flaws as side effects.

While the list of updated operators is crucial for solving online planning problems, a complementary mechanism is used to ensure that LOLLIPOP is complete. User provided plans have their steps tagged. If the failure has backtracked to a user-provided step, then it is removed and replaced by subgoals that represent each of its participation in the plan. This mechanism loops until every user provided steps have been removed.

### 3.2.5 Theoretical and Empirical Results

As proven in (Penberthy *et al.* 1992), the classical POP algorithm is *sound* and *complete*.

First, we define some new properties of partial plans. The following properties are taken from the original proof. We present them again for convenience.

∷ {#def:fullsupport .definition name="Full Support" } A partial plan  $\pi$  is fully supported if each of its steps  $o \in S$  is fully supported. A step is fully supported if each of its preconditions  $f \in pre(o)$  is supported. A precondition is fully supported if there exists a causal link  $l$  that provides it. We note:

$$\Downarrow \pi \equiv \forall o \in S \forall f \in pre(o) \exists l \in L_{\pi}^{-}(o) : (f \in l \wedge \nexists t \in S (l_{\rightarrow} > t > o \wedge \neg f \in eff(t)))$$

with  $L_{\pi}^{-}(o)$  being the incoming causal links of  $o$  in  $\pi$  and  $l_{\rightarrow}$  being the source of the link.

**Definition 26** (Partial Plan Validity). A partial plan is a **valid solution** of a problem  $\mathcal{P}$  iff it is *fully supported* and *contains no cycles*. The validity of  $\pi$  regarding a problem  $\mathcal{P}$  is noted  $\pi \models \mathcal{P} \equiv \Downarrow \pi \wedge (C(\pi) = \emptyset)$  with  $C(\pi)$  being the set of cycles in  $\pi$ .

### 3.2.5.1 Proof of Soundness

In order to prove that this property applies to LOLLIPOP, we need to introduce some hypothesis:

- operators updated by online planning are known.
- user provided steps are known.
- user provided plans don't contain illegal artifacts. This includes toxic or inconsistent actions, lying links and cycles.

Based on the definition 26 we state that:

$$\left( \begin{array}{l} \forall pre \in pre(G) : \\ \Downarrow pre \wedge \forall o \in L_{\pi}^{-}(G)_{\rightarrow} \forall pre' \in pre(o) : \\ (\Downarrow pre' \wedge C_o(\pi) = \emptyset) \end{array} \right) \implies \pi \models \mathcal{P} \quad (3.1)$$

where  $L_{\pi}^{-}(G)_{\rightarrow}$  is the set of direct antecedents of  $G$  and  $C_o(\pi)$  is the set of fluents containing  $o$  in  $\pi$ .

This means that  $\pi$  is a solution if all preconditions of  $G$  are satisfied. We can satisfy these preconditions using operators iff their preconditions are all satisfied and if there is no other operator that threatens their supporting links.

First, we need to prove that equation (3.1) holds on LOLLIPOP initialization. We use our hypothesis to rule out the case when the input plan is invalid. The algorithm ?? will only solve open conditions in the same way subgoals do it. Thus, safe operator graphs are valid input plans.

Since the soundness is proven for regular refinements and flaw selection, we need to consider the effects of the added mechanisms of LOLLIPOP. The newly introduced refinements are negative, they don't add new links:

$$\forall f \in \mathcal{F}(\pi) \forall r \in r(f) : C_{\pi}(f.n) = C_{f(\pi)}(f.n) \quad (3.2)$$

with  $\mathcal{F}(\pi)$  being the set of flaws in  $\pi$ ,  $r(f)$  being the set of resolvers of  $f$ ,  $f.n$  being the needer of the flaw and  $f(\pi)$  being the resulting partial plan after application of the flaw. Said otherwise, an iteration of LOLLIPOP won't add cycles inside a partial plan.

The orphan flaw targets steps that have no path to the goal and so can't add new open conditions or threats. The alternative targets existing causal links. Removing a causal link in a plan breaks the full support of the target step. This is why an alternative will always insert a subgoal in the agenda



corresponding to the target of the removed causal link. Invalidating side effects also don't affect the soundness of the algorithm since the removed flaws are already solved. This makes:

$$\forall f \in \mathcal{F}^-(\pi) : \Downarrow \pi \implies \Downarrow f(\pi) \quad (3.3)$$

with  $\mathcal{F}^-(\pi)$  being the set of negative flaws in the plan  $\pi$ . This means that negative flaws don't compromise the full support of the plan.

Equations (3.2) and (3.3) lead to equation (3.1) being valid after the execution of LOLLIPOP. The algorithm is sound.

### 3.2.5.2 Proof of Completeness

The soundness proof shows that LOLLIPOP's refinements don't affect the support of plans in term of validity. It was proven that POP is complete. There are several cases to explore to transpose the property to LOLLIPOP:

**Lemma (Conservation of Validity).** *If the input plan is a valid solution, LOLLIPOP returns a valid solution.*

*Proof.* With equations (3.2) and (3.3) and the proof of soundness, the conservation of validity is already proven.  $\square$

**Lemma (Reaching Validity with incomplete partial plans).** *If the input plan is incomplete, LOLLIPOP returns a valid solution if it exists.*

*Proof.* Since POP is complete and the equation (3.3) proves the conservation of support by LOLLIPOP, then the algorithm will return a valid solution if the provided plan is an incomplete plan and the problem is solvable.  $\square$

**Lemma (Reaching Validity with empty partial plans).** *If the input plan is empty and the problem is solvable, LOLLIPOP returns a valid solution.*

*Proof.* This is proven using (???) and POP's completeness. However, we want to add a trivial case to the proof:  $pre(G) = \emptyset$ . In this case the line ?? of the algorithm ?? will return a valid plan.  $\square$

**Lemma (Reaching Validity with a dead-end partial plan).** *If the input plan is in a dead-end, LOLLIPOP returns a valid solution.*

*Proof.* Using input plans that can be in an undetermined state is not covered by the original proof. The problem lies in the existing steps in the input plan. Still, using our hypothesis we add a failure mechanism that makes LOLLIPOP complete. On failure, the needer of the last flaw is deleted if it wasn't added by LOLLIPOP. User defined steps are deleted until the input plan acts like an empty plan. Each deletion will cause corresponding subgoals to be added to the agenda. In this case, the backtracking is preserved and all possibilities are explored as in POP.  $\square$

Since all cases are covered, this proves the property of completeness.

### 3.2.5.3 Experimental Results

The experimental results focused on the properties of LOLLIPOP for online planning. Since classical POP is unable to perform online planning, we tested our algorithm considering the time taken for solving the problem for the first time. We profiled the algorithm on a benchmark problem containing each of the possible issues described earlier.



Figure 3.3: Domain used to compute the results. First line is the initial and goal step along with the useful actions. Second line contains a threatening action  $t$ , two co-dependent actions  $n$  and  $l$ , a useless action  $u$ , a toxic action  $v$ , a deadend action  $w$  and an inconsistent action  $x$

In figure 3.3, we expose the planning domain used for the experiments. During the domain initialization, the actions  $u$  and  $v$  are eliminated from the domain since they serve no purpose in the solving process. The action  $x$  is stripped of its negative effect because it is inconsistent with the effect 2.

As the solving starts, LOLLIPOP computes a safe operator graph (full lines in figure 3.4). As we can see this partial plan is nearly complete already. When the main refining function starts it receives an agenda with only a few flaws remaining.

Then the main refinement function starts (time markers 1). LOLLIPOP selects as resolver a causal link from  $a$  to satisfy the open condition of the goal step. Once the first threat between  $a$  and  $t$  is resolved the second threat is invalidated. On a second execution, the domain changes for online planning with 6 added to the initial step. This solving (time markers 2) add as flaw an alternative on the link from  $c$  to the goal step. A subgoal is added that links the initial and goal step for this fluent. An orphan flaw is also added that removes  $c$  from the plan. Another solving takes place as the goal step doesn't need 3 as a precondition (time markers 3). This causes the link from  $a$  to be cut since it became a liar link. This adds  $a$  as an orphan that gets removed from the plan even if it was hanging by the bare link to  $t$ .

The measurements exposed in table 3.1 were made with an Intel® Core™ i7-4720HQ with a 2.60GHz clock. Only one core was used for the solving. The same experiment done only with the chronometer code gave a result of 70ns of error. We can see an increase of performance in the online runs because of the way they are conducted by LOLLIPOP.



Figure 3.4: In full lines the initial safe operator graph. In thin, sparse and irregularly dotted lines a subgoal, alternative and threat caused causal link.

Table 3.1: Average times of 1.000 executions on the problem. The first column is for a simple run on the problem. Second and third columns are times to replan with one and two changes done to the domain for online planning.

Experiment	Single	Online 1	Online 2
Time (ms)	0.86937	0.38754	0.48123

## 3.3 HEART

### 3.3.1 Domain Compilation

In order to simplify the input of the domain, the causes of the causal links in the methods are optional. If omitted, the causes are inferred by unifying the preconditions and effects with the same mechanism as in the subgoal resolution in our POCL algorithm. Since we want to guarantee the validity of abstract plans, we need to ensure that user provided plans are solvable. We use the following formula to compute the final preconditions and effects of any composite action  $a$ :  $pre(a) = \bigcup_{l \in L^+(I_m)}^{m \in methods(a)} causes(l)$  and  $eff(a) = \bigcup_{l \in L^-(G_m)}^{m \in methods(a)} causes(l)$ . An instance of the classical POCL algorithm is then run on the problem  $\mathcal{P}_a = \langle \mathcal{D}, \mathcal{C}_p, a \rangle$  to ensure its coherence. The domain compilation fails if POCL cannot be completed. Since our decomposition hierarchy is acyclic ( $a \notin A_a$ , see definition 28) nested methods cannot contain their parent action as a step.

### 3.3.2 Abstraction in POP

In order to properly introduce the changes made for using HTN domains in POCL, we need to define a few notions.

Transposition is needed to define decomposition.

**Definition 27** (Transposition). In order to transpose the causal links of an action  $a'$  with the ones of an existing step  $a$  in a plan  $\pi$ , we use the following operation:

$$a \triangleright_{\pi}^{-} a' = \left\{ \phi^{-}(l) \xrightarrow{causes(l)} a' : l \in L_{\pi}^{-}(a) \right\}$$

It is the same with  $a' \xrightarrow{causes(l)} \phi^{+}(l)$  and  $L^{+}$  for  $a \triangleright^{+} a'$ . This supposes that the respective preconditions and effects of  $a$  and  $a'$  are equivalent. When not signed, the transposition is generalized:  $a \triangleright a' = a \triangleright^{-} a' \cup a \triangleright^{+} a'$ .

*Example:*  $a \triangleright^{-} a'$  gives all incoming links of  $a$  with the  $a$  replaced by  $a'$ .

**Definition 28** (Proper Actions). Proper actions are actions that are “contained” within an entity (either a domain, plan or action). We note this notion  $A_a = A_a^{lv(a)}$  for an action  $a$ . It can be applied to various concepts:

- For a *domain* or a *problem*,  $A_{\mathcal{P}} = A_{\mathcal{D}}$ .
- For a *plan*, it is  $A_{\pi}^0 = S_{\pi}$ .
- For an *action*, it is  $A_a^0 = \bigcup_{m \in methods(a)} S_m$ . Recursively:  $A_a^n = \bigcup_{b \in A_a^0} A_b^{n-1}$ . For atomic actions,  $A_a = \emptyset$ .

*Example:* The proper actions of *make(drink)* are the actions contained within its methods. The set of extended proper actions adds all proper actions of its single proper composite action *infuse(drink, water, cup)*.

**Definition 29** (Abstraction Level). This is a measure of the maximum amount of abstraction an entity can express, defined recursively by:

$$lv(x) = \left( \max_{a \in A_x} (lv(a)) + 1 \right) [A_x \neq \emptyset]$$

*Example:* The abstraction level of any atomic action is 0 while it is 2 for the composite action *make(drink)*. The example domain (in listing ??) has an abstraction level of 3.

The most straightforward way to handle abstraction in regular planners is illustrated by Duet (Gerevini *et al.* 2008) by managing hierarchical actions separately from a task insertion planner. We chose to add abstraction in POCL in a manner inspired by the work of Bechon *et al.* (2014) on a planner called HiPOP. The difference between the original HiPOP and our implementation of it is that we focus on the expressivity and the ways flaw selection can be exploited for partial resolution. Our version is lifted at runtime while the original is grounded for optimizations. All mechanisms we have implemented use POCL but with different management of flaws and resolvers. The original algorithm ?? is left untouched.

One of those changes is that resolver selection needs to be altered for subgoals. Indeed, as stated by the authors of HiPOP: the planner must ensure the selection of high-level operators in order to benefit from the hierarchical aspect of the domain. Otherwise, adding operators only increases the branching factor. Composite actions are not usually meant to stay in a finished plan and must be decomposed into atomic steps from one of their methods.

**Definition 30** (Decomposition Flaws). They occur when a partial plan contains a non-atomic step. This step is the needer  $a_n$  of the flaw. We note its decomposition  $a_n \oplus$ .

- *Resolvers*: A decomposition flaw is solved with a **decomposition resolver**. The resolver will replace the needer with one of its instantiated methods  $m \in \text{methods}(a_n)$  in the plan  $\pi$ . This is done by using transposition such that:  $a_n \oplus_\pi^m = \langle S_m \cup (S_\pi \setminus \{a\}), a_n \triangleright^- I_m \cup a_n \triangleright^+ G_m \cup (L_\pi \setminus L_\pi(a_n)) \rangle$ .
- *Side effects*: A decomposition flaw can be created by the insertion of a composite action in the plan by any resolver and invalidated by its removal:

$$\bigcup_{\substack{f \in \text{pre}(a_m) \\ a_m \in S_m}} \pi' \downarrow_f a_m \bigcup_{\substack{l \in L_{\pi'} \\ a_b \in S_{\pi'}}} a_b \otimes l \bigcup_{\substack{lv(a_c) \neq 0 \\ a_c \in S_m}} a_c \oplus$$

*Example*: When adding the step *make(tea)* in the plan to solve the subgoal that needs tea being made, we also introduce a decomposition flaw that will need this composite step replaced by its method using a decomposition resolver. In order to decompose a composite action into a plan, all existing links are transposed to the initial and goal step of the selected method, while the composite action and its links are removed from the plan. The main differences between HiPOP and HEART in our implementations are the functions of flaw selection and the handling of the results (one plan for HiPOP and a plan per cycle for HEART). In HiPOP, the flaw selection is made by prioritizing the decomposition flaws. Bechon *et al.* (2014) state that it makes the full resolution faster. However, it also loses opportunities to obtain abstract plans in the process.

### 3.3.3 Planning in cycle

Illustration of how the cyclical approach is applied on the example domain. Atomic actions that are copied from a cycle to the next are omitted.

The main focus of our work is toward obtaining **abstract plans** which are plans that are completed while still containing composite actions. In order to do that the flaw selection function will enforce cycles in the planning process.

**Definition 31** (Cycle). A cycle is a planning phase defined as a triplet  $c = \langle lv(c), agenda, \pi_{lv(c)} \rangle$  where:  $lv(c)$  is the maximum abstraction level allowed for flaw selection in the *agenda* of remaining flaws in partial plan  $\pi_{lv(c)}$ . The resolvers of subgoals are therefore constrained by the following:  $a_p \downarrow_f a_n : lv(a_p) \leq lv(c)$ .

During a cycle all decomposition flaws are delayed. Once no more flaws other than decomposition flaws are present in the agenda, the current plan is saved and all remaining decomposition flaws are solved at

once before the abstraction level is lowered for the next cycle:  $lv(c') = lv(c) - 1$ . Each cycle produces a more detailed abstract plan than the one before.

Abstract plans allow the planner to do an approximate form of anytime execution. At any given time the planner is able to return a fully supported plan. Before the first cycle, the plan returned is  $\pi_{lv(a_0)}$ .

*Example:* In our case using the method of intent recognition of Sohrabi *et al.* Sohrabi *et al.* (2016), we can already use  $\pi_{lv(a_0)}$  to find a likely goal explaining an observation (a set of temporally ordered fluents). That can make an early assessment of the probability of each goal of the recognition problem.

For each cycle  $c$ , a new plan  $\pi_{lv(c)}$  is created as a new method of the root operator  $a_0$ . These intermediary plans are not solutions of the problem, nor do they mean that the problem is solvable. In order to find a solution, the HEART planner needs to reach the final cycle  $c_0$  with an abstraction level  $lv(c_0) = 0$ . However, these plans can be used to derive meaning from the potential solution of the current problem and give a good approximation of the final result before its completion.

*Example:* In the ??, we illustrate the way our problem instance is progressively solved. Before the first cycle  $c_2$ , all we have is the root operator and its plan  $\pi_3$ . Then within the first cycle, we select the composite action  $make(tea)$  instantiated from the operator  $make(drink)$  along with its methods. All related flaws are fixed until all that is left in the agenda is the abstract flaws. We save the partial plan  $\pi_2$  for this cycle and expand  $make(tea)$  into a copy of the current plan  $\pi_1$  for the next cycle. The solution of the problem will be stored in  $\pi_0$  once found.

### 3.3.4 Properties of Abstract Planning

In this section, we prove several properties of our method and resulting plans: HEART is complete, sound and its abstract plans can always be decomposed into a valid solution.

The completeness and soundness of POCL has been proven in (Penberthy *et al.* 1992). An interesting property of POCL algorithms is that flaw selection strategies do not impact these properties. Since the only modification of the algorithm is the extension of the classical flaws with a decomposition flaw, all we need to explore, to update the proofs, is the impact of the new resolver. By definition, the resolvers of decomposition flaws will take into account all flaws introduced by its resolution into the refined plan. It can also revert its application properly.

**Lemma (Decomposing preserves acyclicity).** *The decomposition of a composite action with a valid method in an acyclic plan will result in an acyclic plan. Formely,  $\forall a_s \in S_\pi : a_s \not\prec_\pi a_s \implies \forall a'_s \in S_{a \oplus \pi}^m : a'_s \not\prec_{a \oplus \pi}^m a'_s$ .*

*Proof.* When decomposing a composite action  $a$  with a method  $m$  in an existing plan  $\pi$ , we add all steps  $S_m$  in the refined plan. Both  $\pi$  and  $m$  are guaranteed to be cycle free by definition. We can note that  $\forall a_s \in S_m : (\nexists a_t \in S_m : a_s > a_t \wedge \neg f \in \text{eff}(a_t)) \implies f \in \text{eff}(a)$ . Said otherwise, if an action  $a_s$  can participate a fluent  $f$  to the goal step of the method  $m$  then it is necessarily present in the effects of  $a$ . Since higher level actions are preferred during the resolver selection, no actions in the methods are already used in the plan when the decomposition happens. This can be noted  $\exists a \in \pi \implies S_m \cup S_\pi$  meaning that in the graph formed both partial plans  $m$  and  $\pi$  cannot contain the same edges therefore their acyclicity is preserved when inserting one into the other.

□

**Lemma (Solved decomposition flaws cannot reoccur).** *The application of a decomposition resolver on a plan  $\pi$ , guarantees that  $a \notin S_{\pi'}$  for any partial plan refined from  $\pi$  without reverting the application of the resolver.*

*Proof.* As stated in the definition of the methods (@def:action):  $a \notin A_a$ . This means that  $a$  cannot be introduced in the plan by its decomposition or the decomposition of its proper actions. Indeed, once  $a$  is expanded, the level of the following cycle  $c_{lv(a)-1}$  prevents  $a$  to be selected by subgoal resolvers. It cannot either be contained in the methods of another action that are selected afterward because otherwise following definition 29 its level would be at least  $lv(a) + 1$ .

□

**Lemma (Decomposing to abstraction level 0 guarantees solvability).** *Finding a partial plan that contains only decomposition flaws with actions of abstraction level 1, guarantees a solution to the problem.*

*Proof.* Any method  $m$  of a composite action  $a : lv(a) = 1$  is by definition a solution of the problem  $\mathcal{P}_a = \langle \mathcal{D}, C_p, a \rangle$ . By definition,  $a \notin A_a$ , and  $a \notin A_{a \oplus \pi}^m$  (meaning that  $a$  cannot reoccur after being decomposed). It is also given by definition that the instantiation of the action and its methods are coherent regarding variable constraints (everything is instantiated before selection by the resolvers). Since the plan  $\pi$  only has decomposition flaws and all flaws within  $m$  are guaranteed to be solvable, and both are guaranteed to be acyclical by the application of any decomposition  $a \oplus \pi^m$ , the plan is solvable.

□

**Lemma (Abstract plans guarantee solvability).** *Finding a partial plan  $\pi$  that contains only decomposition flaws, guarantees a solution to the problem.*

*Proof.* Recursively, if we apply the previous proof on higher level plans we note that decomposing at level 2 guarantees a solution since the method of the composite actions are guaranteed to be solvable.

□

From these proofs, we can derive the property of soundness (from the guarantee that the composite action provides its effects from any methods) and completeness (since if a composite action cannot be used, the planner defaults to using any action of the domain).

### 3.3.5 Computational Profile

In order to assess its capabilities, HEART was evaluated on two criteria: quality and complexity. All tests were executed on an Intel® Core™ i7-7700HQ CPU clocked at 2.80GHz. The Java process used only one core and was not limited by time or memory (32 GB that wasn't entirely used up). Each experiment was repeated between 700 and 10 000 times to ensure that variations in speed were not impacting the results.

Figure 3.5 shows how the quality is affected by the abstraction in partial plans. The tests are made using our example domain (see listing ??). The quality is measured by counting the number of providing fluents in the plan  $|\bigcup_{a \in S_\pi} eff(a)|$ . This metric is actually used to approximate the probability of a goal given observations in intent recognition ( $P(G|O)$  with noisy observations, see (Sohrabi *et al.* 2016)). The percentages are relative to the total number of unique fluents of the complete solution. These results show that in some cases it may be more interesting to plan in a leveled fashion to solve HTN problems. For the first cycle of level 3, the quality of the abstract plan is already of 60%. This is the quality of the exploitation of the plan *before any planning*. With almost three-quarters of the final quality and less than half of the complete computation time, the result of the first cycle is a good quality/time compromise.

In the second test, we used generated domains. These domains consist of an action of abstraction level 5. This action has a single method containing a number of actions of level 4. We call this number the



Figure 3.5: Evolution of the quality with computation time.



Figure 3.6: Impact of domain shape on the computation time by levels. The scale of the vertical axis is logarithmic. Equations are the definition of the trend curves.



width of the domain. All needed actions are built recursively to form a tree shape. Atomic actions only have single fluent effects. The goal is the effect of the higher level action and the initial state is empty. These domains do not contain negative effects. Figure 3.6 shows the computational profile of HEART for various levels and widths. We note that the behavior of HEART seems to follow an exponential law with the negative exponent of the trend curves seemingly being correlated to the actual width. This means that computing the first cycles has a complexity that is close to being *linear* while computing the last cycles is of the same complexity as classical planning which is at least *P-SPACE* (depending on the expressivity of the domain) (Erol *et al.* 1995).

## 3.4 Planning Improvements

### 3.4.1 Heuristics using Semantics

### 3.4.2 Macro-Action learning

## 3.5 Recognition

### 3.5.1 Existing approaches

### 3.5.2 Rico

#### 3.5.2.1 Probabilities and approximations

We define a probability distribution over dated states of the world. That distribution is in part given and fixed and the rest needs computation. **TODO : that's super bad...**

Here is the list of given prior probabilities and assumptions :

- $P(O) = \prod_{o \in O} P(o)$
- $P(G) = \sum_{G \in \mathcal{G}} P(G) = 1$  since we assume that the agent must be pursuing one of the goals.
- $P(G|\pi) = 1$  for a plan  $\pi$  applicable in  $I$  that achieves  $G$ .

From direct application of Bayes theorem and the previous assumptions, we have :

$$P(\pi|O) = \frac{P(O|\pi)P(\pi)}{P(O)} = \frac{P(O|\pi)P(\pi|G)P(G)}{P(O)} \quad (3.4)$$

$$P(G|O) = \frac{P(O|G)P(G)}{P(O)} \quad (3.5)$$

From the total probability formula :

$$P(O|G) = \sum_{\pi \in \Pi_G} P(O|\pi)P(\pi|G) \quad (3.6)$$

$$P(O|G) = \sum_{\pi \in \Pi_G} P(O|\pi)P(\pi|G) \quad (3.7)$$

## 4 Conclusion

## **Apendix**

# References

Alessandro, W., and I. Piumarta

OMeta: An object-oriented language for pattern matching, *Proceedings of the 2007 symposium on Dynamic languages*, 2007.

Aljazzar, H., and S. Leue

K: A heuristic search algorithm for finding the k shortest paths, *Artificial Intelligence*, 175 (18), 2129–2154, 2011.

Ambite, J. L., and C. A. Knoblock

*Planning by Rewriting: Efficiently Generating High-Quality Plans.*, DTIC Document, 1997.

Asimov, I.

*The gods themselves*, Greenwich, Connecticut: Fawcett Crest, 1973.

Baader, F.

*The description logic handbook: Theory, implementation and applications*, Cambridge university press, 2003.

Babli, M., E. Marzal, and E. Onaindia

On the use of ontologies to extend knowledge in online planning, *KEPS 2018*, 54, 2015.

Backus, J. W.

The syntax and semantics of the proposed international algebraic language of the Zurich ACM-GAMM conference, *Proceedings of the International Conference on Information Processing*, 1959, 1959.

Bechon, P., M. Barbier, G. Infantes, C. Lesire, and V. Vidal

HiPOP: Hierarchical Partial-Order Planning, *European Starting AI Researcher Symposium*, IOS Press, 2014, 264,51–60.

Becket, R., and Z. Somogyi

DCGs+ memoing= packrat parsing but is it worth it?, *International Symposium on Practical Aspects of Declarative Languages*, Springer, 2008, 182–196.

Beckett, D., and T. Berners-Lee

*Turtle - Terse RDF Triple Language*, W3C Team Submission W3C, March 2011.

Bercher, P., S. Keen, and S. Biundo

Hybrid planning heuristics based on task decomposition graphs, *Seventh Annual Symposium on Combinatorial Search*, 2014.

Brenner, M.

A multiagent planning language, *Proc. Of the Workshop on PDDL, ICAPS*, 2003, 3,33–38.

Bürckert, H.-J.

Terminologies and rules, *Workshop on Information Systems and Artificial Intelligence*, Springer, 1994, 44–63.

- Cantor, G.  
On a Property of the Class of all Real Algebraic Numbers., *Crelle's Journal for Mathematics*, 77, 258–262, 1874.
- Cantor, G.  
Beiträge zur Begründung der transfiniten Mengenlehre, *Mathematische Annalen*, 46 (4), 481–512, 1895.
- Chomsky, N.  
Three models for the description of language, *IRE Transactions on information theory*, 2 (3), 113–124, 1956.
- Ciesielski, K.  
*Set Theory for the Working Mathematician*, Cambridge University Press, August 1997.
- Coles, A., A. Coles, M. Fox, and D. Long  
Popf2 : A forward-chaining partial order planner, *IPC*, 65, 2011.
- D'Alfonso, D.  
Generalized Quantifiers: Logic and Language, 2011.
- Dvorak, F., A. Bit-Monnot, F. Ingrand, and M. Ghallab  
A flexible ANML actor and planner in robotics, *Planning and Robotics (PlanRob) Workshop (ICAPS)*, 2014.
- Erol, K., J. A. Hendler, and D. S. Nau  
UMCP: A Sound and Complete Procedure for Hierarchical Task-network Planning, *Proceedings of the International Conference on Artificial Intelligence Planning Systems*, University of Chicago, Chicago, Illinois, USA: AAAI Press, June 1994, 2,249–254.
- Erol, K., D. S. Nau, and V. S. Subrahmanian  
Complexity, decidability and undecidability results for domain-independent planning, *Artificial intelligence*, 76 (1-2), 75–88, 1995.
- Fikes, R. E., and N. J. Nilsson  
STRIPS: A new approach to the application of theorem proving to problem solving, *Artificial intelligence*, 2 (3-4), 189–208, 1971.
- Ford, B.  
Packrat parsing:: Simple, powerful, lazy, linear time, functional pearl, *ACM SIGPLAN Notices*, ACM, 2002, 37,36–47.
- Ford, B.  
Parsing expression grammars: A recognition-based syntactic foundation, *ACM SIGPLAN Notices*, ACM, 2004, 39,111–122.
- Fox, M.  
Natural hierarchical planning using operator decomposition, *European Conference on Planning*, Springer, 1997, 195–207.
- Fox, M., and D. Long  
PDDL+: Modeling continuous time dependent effects, *Proceedings of the 3rd International NASA Workshop on Planning and Scheduling for Space*, 2002, 4,34.
- Fraenkel, A. A., Y. Bar-Hillel, and A. Levy  
*Foundations of set theory*, vol. 67Elsevier, 1973.

- Gerevini, A., U. Kuter, D. S. Nau, A. Saetti, and N. Waisbrot  
Combining Domain-Independent Planning and HTN Planning: The Duet Planner, *Proceedings of the European Conference on Artificial Intelligence*, 2008, 18,573–577.
- Ghallab, M., C. Knoblock, D. Wilkins, A. Barrett, D. Christianson, et al.  
PDDL – The planning domain definition language, 1998.
- Ghallab, M., D. Nau, and P. Traverso  
*Automated planning: Theory & practice*, Elsevier, 2004.
- Ghallab, M., D. Nau, and P. Traverso  
*Automated Planning and Acting*, Cambridge University Press, 2016.
- Göbelbecker, M., T. Keller, P. Eyerich, M. Brenner, and B. Nebel  
Coming Up With Good Excuses: What to do When no Plan Can be Found, *Proceedings of the International Conference on Automated Planning and Scheduling*, AAAI Press, May 2010, 20,81–88.
- Gradel, E., M. Otto, and E. Rosen  
Two-variable logic with counting is decidable, *Logic in Computer Science*, 1997. *LICS'97. Proceedings, 12th Annual IEEE Symposium on*, IEEE, 1997, 306–317.
- Grünwald, P.  
A minimum description length approach to grammar inference, in S. Wermter, E. Riloff, and G. Scheler (eds.), *Connectionist, Statistical and Symbolic Approaches to Learning for Natural Language Processing*, Lecture Notes in Computer Science; Springer Berlin Heidelberg, 1996, 203–216.
- Hart, D., and B. Goertzel  
Opencog: A software framework for integrative artificial general intelligence, *AGI*, 2008, 468–472.
- Hehner, E. C.  
*A practical theory of programming*, Springer Science & Business Media, 2012.
- Helmert, M., G. Röger, and E. Karpas  
Fast downward stone soup: A baseline for building planner portfolios, *ICAPS 2011 Workshop on Planning and Learning*, Citeseer, 2011, 28–35.
- Henglein, F., and U. T. Rasmussen  
PEG parsing in less space using progressive tabling and dynamic analysis, *Proceedings of the 2017 ACM SIGPLAN Workshop on Partial Evaluation and Program Manipulation*, ACM, 2017, 35–46.
- Hernández, D., A. Hogan, and M. Krötzsch  
Reifying RDF: What works well with wikidata?, *SSWS@ ISWC*, 1457, 32–47, 2015.
- Horrocks, I., P. F. Patel-Schneider, and F. V. Harmelen  
From SHIQ and RDF to OWL: The Making of a Web Ontology Language, *Journal of Web Semantics*, 1, 2003, 2003.
- Hörschele, M., and A. Zeller  
Mining input grammars with AUTOGRAM, *Proceedings of the 39th International Conference on Software Engineering Companion*, IEEE Press, 2017, 31–34.
- Hutton, G., and E. Meijer  
Monadic parser combinators, 1996.
- Kambhampati, S.  
Design Tradeoffs in Partial Order (Plan space) Planning., *AIPS*, 1994, 92–97.

- Kambhampati, S., A. Mali, and B. Srivastava  
Hybrid planning for partially hierarchical domains, *AAAI/IAAI*, 1998, 882–888.
- Klyne, G., and J. J. Carroll  
*Resource Description Framework (RDF): Concepts and Abstract Syntax, Language Specification*. Ed. B. McBride W3C, 2004.
- Kovacs, D. L.  
*BNF Description of PDDL 3.1*, IPC, 2011.
- Kovács, D. L.  
A multi-agent extension of PDDL3. 1, 2012.
- Kovács, D. L., and T. P. Dobrowiecki  
Converting MA-PDDL to extensive-form games, *Acta Polytechnica Hungarica*, 10 (8), 27–47, 2013.
- Kovitz, B.  
Terminology - What do you call graphs that allow edges to edges?, *Mathematics Stack Exchange*, January 2018.
- Lindström, P.  
First Order Predicate Logic with Generalized Quantifiers, 1966.
- Loff, B., N. Moreira, and R. Reis  
The Computational Power of Parsing Expression Grammars, *International Conference on Developments in Language Theory*, Springer, 2018, 491–502.
- McDermott, D.  
*OPT Manual Version 1.7. 3 (Reflects Opt Version 1.6. 11)\* DRAFT*, 2005.
- McDermott, D., and D. Dou  
Representing disjunction and quantifiers in RDF, *International Semantic Web Conference*, Springer, 2002, 250–263.
- Motik, B.  
On the properties of metamodeling in OWL, *Journal of Logic and Computation*, 17 (4), 617–637, 2007.
- Nau, D. S., T.-C. Au, O. Ilghami, U. Kuter, J. W. Murdock, et al.  
SHOP2: An HTN planning system, *J. Artif. Intell. Res.(JAIR)*, 20, 379–404, 2003.
- Nguyen, X., and S. Kambhampati  
Reviving partial order planning, *IJCAI*, 2001, 1,459–464.
- Paulson, L.  
A semantics-directed compiler generator, *Proceedings of the 9th ACM SIGPLAN-SIGACT symposium on Principles of programming languages - POPL '82*, Albuquerque, Mexico: ACM Press, 1982, 224–233. doi:[10.1145/582153.582178](https://doi.org/10.1145/582153.582178).
- Peano, G.  
*Arithmetices principia: Nova methodo exposita*, Fratres Bocca, 1889.
- Pednault, E. P.  
ADL: Exploring the Middle Ground Between STRIPS and the Situation Calculus., *Kr*, 89, 324–332, 1989.
- Pellier, D., and H. Fiorino  
PDDL4J: A planning domain description library for java, December 2017. doi:[10.1080/0952813X.2017.1409278](https://doi.org/10.1080/0952813X.2017.1409278).

- Penberthy, J. S., D. S. Weld, and others  
UCPOP: A Sound, Complete, Partial Order Planner for ADL, *Kr*, 92, 103–114, 1992.
- Peot, M. A., and D. E. Smith  
Threat-removal strategies for partial-order planning, *AAAI*, 1993, 93,492–499.
- RAMOUL, A.  
Mixed-initiative planning system to assist the management of complex IT systems PhD thesis, 2018.
- Renggli, L., S. Ducasse, T. Gîrba, and O. Nierstrasz  
Practical Dynamic Grammars for Dynamic Languages, *Workshop on Dynamic Languages and Applications*, Malaga, Spain, 2010, 4.
- Sanner, S.  
Relational dynamic influence diagram language (rddl): Language description Unpublished Ms. Australian National University 2010.
- Sapena, O., E. Onaindia, and A. Torreno  
Combining heuristics to accelerate forward partial-order planning, *CSTPS*, 25, 2014.
- Shekhar, S., and D. Khemani  
Learning and Tuning Meta-heuristics in Plan Space Planning, *arXiv preprint arXiv:1601.07483*, 2016.
- Silberschatz, A.  
Port directed communication, *The Computer Journal*, 24 (1), 78–82, January 1981. doi:[10.1093/comjnl/24.1.78](https://doi.org/10.1093/comjnl/24.1.78).
- Sohrabi, S., A. V. Riabov, and O. Udrea  
Plan Recognition as Planning Revisited, *Proceedings of the International Joint Conference on Artificial Intelligence*, Vol. 25, 2016.
- Souto, D. C., M. V. Ferro, and M. A. Pardo  
Dynamic Programming as Frame for Efficient Parsing, *Proceedings SCCC'98. 18th International Conference of the Chilean Society of Computer Science (Cat. No.98EX212)(SCCC)*, November 1998, 68. doi:[10.1109/SCCC.1998.730784](https://doi.org/10.1109/SCCC.1998.730784).
- Thiébaux, S., J. Hoffmann, and B. Nebel  
In defense of PDDL axioms, *Artificial Intelligence*, 168 (1-2), 38–69, 2005.
- Tolksdorf, R., L. Nixon, F. Liebsch, Minh NguyenD., and Paslaru BontasE.  
Semantic web spaces, 2004.
- Unicode Consortium  
Unicode Character Database, *About the Unicode Character Database*, <https://www.unicode.org/ucd/#Latest>, June 2018a.
- Unicode Consortium  
*The Unicode Standard, Version 11.0*, Core Specification 11.0 Mountain View, CA, June 2018b.
- Van Der Krogt, R., and De WeerdM.  
Plan Repair as an Extension of Planning., *ICAPS*, 2005, 5,161–170.
- Van Harmelen, F., V. Lifschitz, and B. Porter  
*Handbook of knowledge representation*, vol. 1 Elsevier, 2008.
- Vepstas, L.  
Hypergraph edge-to-edge, *Wikipedia*, May 2008.



Vepštas, L.

*Sheaves: A Topological Approach to Big Data*, 2008.

W3C

*RDF Semantics*, W3C, 2004a.

W3C

RDF Vocabulary Description Language 1.0: RDF Schema <http://www.w3.org/TR/rdf-schema/>, February 2004b.

Younes, H. akan L., and M. L. Littman

PPDDL 1.0: An extension to PDDL for expressing planning domains with probabilistic effects, *Techn. Rep. CMU-CS-04-162*, 2004.

Younes, H. akan L., and R. G. Simmons

VHPOP : Versatile heuristic partial order planner, *JAIR*, 405–430, 2003.

Young, R. M., and J. D. Moore

DPOCL: A principled approach to discourse planning, *Proceedings of the Seventh International Workshop on Natural Language Generation*, Association for Computational Linguistics, 1994, 13–20.