

Confidence Interval - STAT110 Otago

Students also viewed

Statistic

10 terms

 [Franziska_Klein](#)

Preview

ACCY330 Final Exam

10 terms

 [amelia2433](#)

Preview

Terms in this set (21)

the standard normal critical value for a 95% interval	1.96
confidence interval formula	$\text{estimate for the mean} \pm \text{multiplier} \pm \text{standard error for the mean}$ $1 - \alpha/2)$
the standard normal critical value for a 99% interval	2.58
Multiplier formula	$z = (x - \text{mean}) / \text{sd}$
what is the α in the multiplier	tail probability
Multiplier pattern	when CI is bigger (e.g., 95% to 99%,) the multiplier will be bigger

s_X	<p>sample standard deviation</p> <p><i>In practice the true standard deviation σ_X is not known.</i></p> <p><i>We estimate it with the sample standard deviation.</i></p> <p><i>This means our critical values must now come from the 't' distribution, not the standard normal.</i></p>
t distribution CI	$\pm t_{\left(1-\frac{\alpha}{2}, \nu\right)} \frac{s}{\sqrt{n}}$
ν (degree of freedom) for t-distribution	$\nu = n - 1$
The t-distribution will be the correct sampling distribution if	<p>either</p> <p><i>the underlying distribution of X is normal,</i></p> <p>and/or</p> <p><i>the sample size is sufficiently large (Central Limit Theorem holds).</i></p>
what is degree of freedom in t-distribution	<p>to replace the mean and sd in normal distribution</p> <p>(because t-distribution is always standardised)</p>
when to use t-distribution	when the sample size is small
calculate the estimate sample size when knows the CI	<p>assuming knows the sd and mean (normally given in the question)</p> <p>solve the equation</p> <p>rounding UP</p>
Comparing means with CI	$\pm t_{\left(1-\frac{\alpha}{2}, \nu\right)} \frac{s}{\sqrt{n}}$

Using CLT to test appropriate normal distribution	<p>gives two values between 0 and n</p> <p>if not, then fail the test.</p> <p><i>This approximation is good only when:</i></p> <p><i>n is large</i></p> <p><i>π is not close to 0 or 1 (this increases symmetry)</i></p>
formula for estimating π	<p>$P = X / n$</p> <p>$p = x / n$</p> <p><i>x is the observed value of X.</i></p> <p>(and more)</p>
Using the Central Limit Theorem , the resulting distribution of these proportions is approximately normal if	<p><i>n is large enough</i></p> <p><i>π far enough from 0 or 1.</i></p> <p><i>As before, we judge this using:</i></p> <p><i>$n\pi \pm \sqrt{n\pi(1 - \pi)}$ gives values between 0 and n.</i></p>
Derivation of the mean of the sampling distribution	<p>If $P = X / n$, then</p> <p>$\mu_P = \pi$</p> <p>$sd = \sigma_P = \sqrt{[\pi(1 - \pi) / n]}$</p>
95% confidence interval for π (use the sample proportion (p) to estimate the unknown true population proportion (π))	$1.96 \sqrt{\frac{p(1 - p)}{n}}$
margin of error	multipliers * sd
note for CI	<p><i>This confidence interval (and margin of error) are correct only if the normal approximation to the binomial is appropriate.</i></p> <p><i>In practice, bias due to non-response should also be considered in our interpretation of an estimate.</i></p>