

- **Subjective Probability:** The individual's personal estimate of the chance of loss.
- **Probability as the Degree of Belief:** In a statement.
- **Objective Probability:** The long-run relative frequency of an event based on the assumptions of an infinite number of observations and of no change in the underlying conditions.
- **Sample Space Definition:** The sample space is the set of all possible outcomes of an experiment, e.g., in the case of a fair die, $\{1, 2, 3, 4, 5, 6\}$.

- **Complementary Events:**

$$Pr(A) + Pr(\bar{A}) = 1$$

- **Mutually Exclusive Events:** There is no intersection between the two events

$$Pr(A \cap B) = 0$$

e.g., Māori and Chinese.

- **Conditional Probability Multiplication Rule:**

$$Pr(A \cap B) = Pr(A)Pr(B|A)$$

- **Conditional Probability Addition Rule:**

$$Pr(A \cup B) = Pr(A) + Pr(B) - Pr(A \cap B)$$

- **Independent Events:** The outcome of one event does not affect the outcome of the second event.

- **Independence Check** (true if):

$$Pr(B) \neq Pr(B|A)$$

or

$$Pr(A) \neq Pr(A|B)$$

- **Definitions of Diagnostic Tests:** Sensitivity, Specificity, False positive fraction, Positive Predictive Value, Negative Predictive Value

- **Sensitivity (Diagnostic Tests):**

$$Pr(B|A)$$

The probability that a person with the disease has a positive test. Think of this as "the probability of a positive test result, given the person actually has the disease."

- **Specificity (Diagnostic Tests):**

$$Pr(\bar{B}|\bar{A})$$

The probability that a person without the disease has a negative test. Think of this as "the probability of a negative test result, given the person does NOT have the disease."

- **Negative Predictive Value:**

$$Pr(\bar{A}|\bar{B})$$

The proportion of patients with negative test results who don't have the disease. The proportion of patients with negative test results who are correctly diagnosed.

- **False positive fraction (Diagnostic Tests):**

$$1 - \textit{specificity} = Pr(\bar{B}|\bar{A})$$

.

- **Positive Predictive Value:**

$$Pr(A|B)$$

The proportion of patients with positive test results who have the disease. The proportion of patients with positive test results who are correctly diagnosed.