



# Precedence and Associativity to Resolve conflicts

# Consider the Grammar

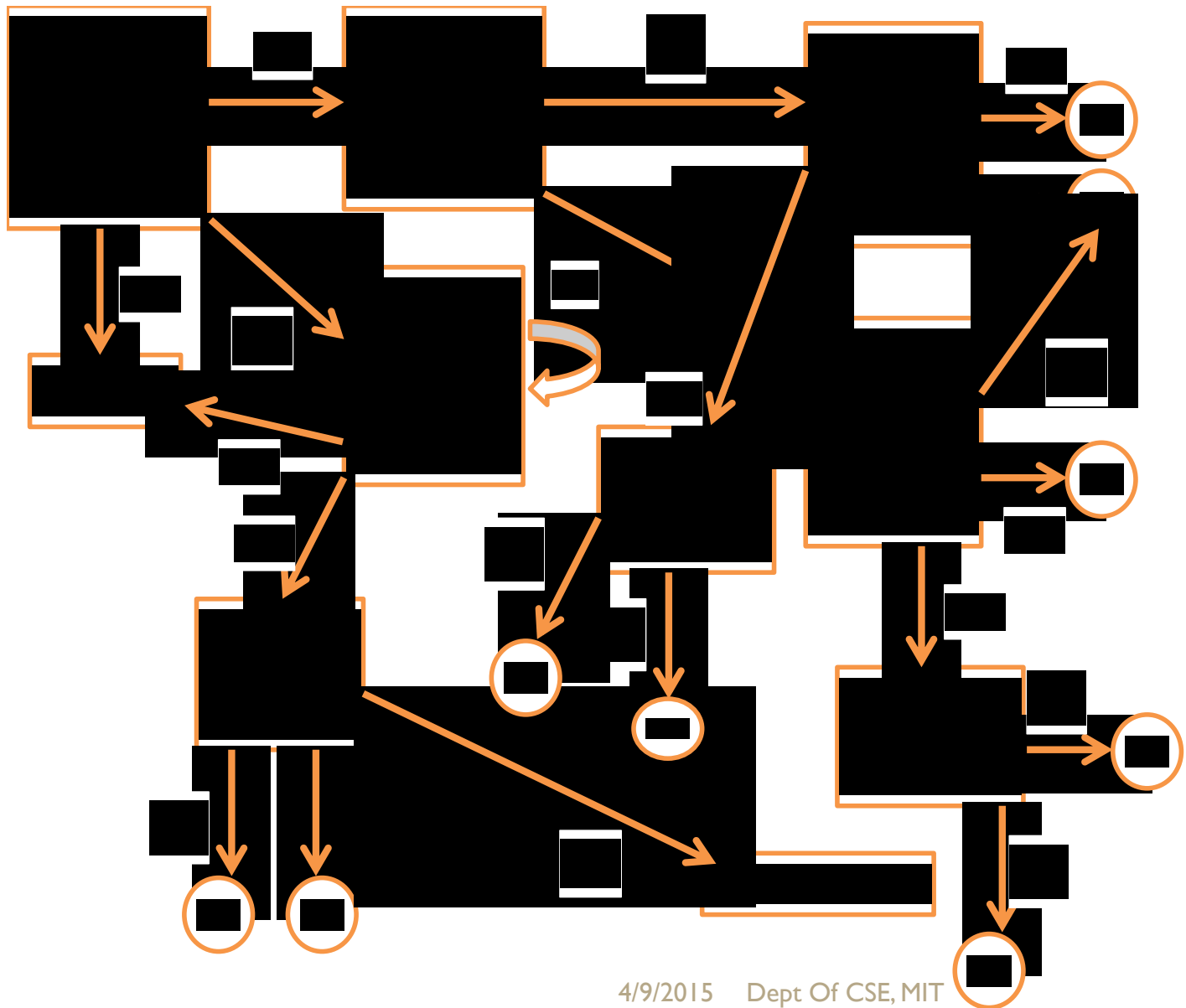
$E \rightarrow E + E$

$E \rightarrow E * E$

$E \rightarrow ( E )$

$E \rightarrow \text{id}$

# DFA:



# Initial Parse Table

State	id	+	*	(	)	\$	E
0	s3			s2			1
1		s4	s5			accept	
2	s3			s2			6
3		r4	r4		r4	r4	
4	s3			s2			7
5	s3			s2			8
6		s4	s5		s9		
7		r1,s4	r1,s5		r1	r1	
8		r2,s4	r2,s5		r2	r2	
9		r3	r3		r3	r3	

# How to resolve conflict??

- Conflict occurs in state 7 and 8.
- Consider four different cases
  - $\text{id} + \text{id} + \text{id}$
  - $\text{id} * \text{id} * \text{id}$
  - $\text{id} + \text{id} * \text{id}$
  - $\text{id} * \text{id} + \text{id}$
- **Solution:** In case of '+' and '\*' give more precedence to \*  
In case of '+' and '+' or '\*' and '\*' go for left associativity.

# Case I: $id+id+id$

Stack	Symbol	Input	Action
03	id	+id+id\$	reduce; $e \rightarrow id$
014	E+	+id+id\$	shift
0147	E+E	+id\$	conflict; reduce
014	E+	id\$	shift
0147	E+E	\$	reduce; $e \rightarrow e+e$

Left Associative rule is applied. So reduce

# Parse table will be

State	id	+	*	(	)	\$	E
0	s3			s2			1
1		s4	s5			accept	
2	s3			s2			6
3		r4	r4		r4	r4	
4	s3			s2			7
5	s3			s2			8
6		s4	s5		s9		
7		r1	r1,s5		r1	r1	
8		r2,s4	r2,s5		r2	r2	
9		r3	r3		r3	r3	

## Case 2: $\text{id} + \text{id} * \text{id}$

Stack	Symbol	Input	Action
03	id	+id*id\$	reduce; $e \rightarrow \text{id}$
014	E+	Id*id\$	shift
0147	E+E	*id\$	conflict; Shift
014753	E+E*id	\$	Reduce $E \rightarrow \text{id}$
0147	E+E	\$	reduce; $E \rightarrow E+E$

Shift since \* has > precedence than +



# Parse table will be

State	id	+	*	(	)	\$	E
0	s3			s2			1
1		s4	s5			accept	
2	s3			s2			6
3		r4	r4		r4	r4	
4	s3			s2			7
5	s3			s2			8
6		s4	s5		s9		
7		r1	s5		r1	r1	
8		r2,s4	r2,s5		r2	r2	
9		r3	r3		r3	r3	

# Case 3: id\*id\*id

Stack	Symbol	Input	Action
03	id	*id*id\$	reduce; $E \rightarrow id$
015	E*	id*id\$	shift
0158	E*E	*id\$	conflict; Reduce
015	E*	id\$	shift
0158	E*E	\$	reduce; $E \rightarrow E*E$

Consider Left  
associativity for \* so  
reduce

# Parse table will be

State	id	+	*	(	)	\$	E
0	s3			s2			1
1		s4	s5			accept	
2	s3			s2			6
3		r4	r4		r4	r4	
4	s3			s2			7
5	s3			s2			8
6		s4	s5		s9		
7		r1	s5		r1	r1	
8		r2,s4	r2		r2	r2	
9		r3	r3		r3	r3	

# Case 3: $id * id + id$

Stack	Symbol	Input	Action
03	id	*id+id\$	reduce; $E \rightarrow id$
015	$E^*$	id+id\$	shift
0158	$E^*E$	+id\$	conflict; Reduce
014	$E^+$	id\$	shift
0147	$E^+E$	\$	reduce; $E \rightarrow E^+E$

Give more precedence to \*. So reduce.

# Parse table will be

State	id	+	*	(	)	\$	E
0	s3			s2			1
1		s4	s5			accept	
2	s3			s2			6
3		r4	r4		r4	r4	
4	s3			s2			7
5	s3			s2			8
6		s4	s5		s9		
7		r1	s5		r1	r1	
8		r2	r2		r2	r2	
9		r3	r3		r3	r3	

# The “Dangling-Else” ambiguity

$$\begin{array}{l} stmt \rightarrow \text{if } expr \text{ then } stmt \text{ else } stmt \\ \quad \quad | \text{if } expr \text{ then } stmt \\ \quad \quad | \text{other} \end{array}$$

Simplifying the above grammar

$$\begin{array}{l} S' \rightarrow S \\ S \rightarrow i S e S \mid i S \mid a \end{array}$$

where,

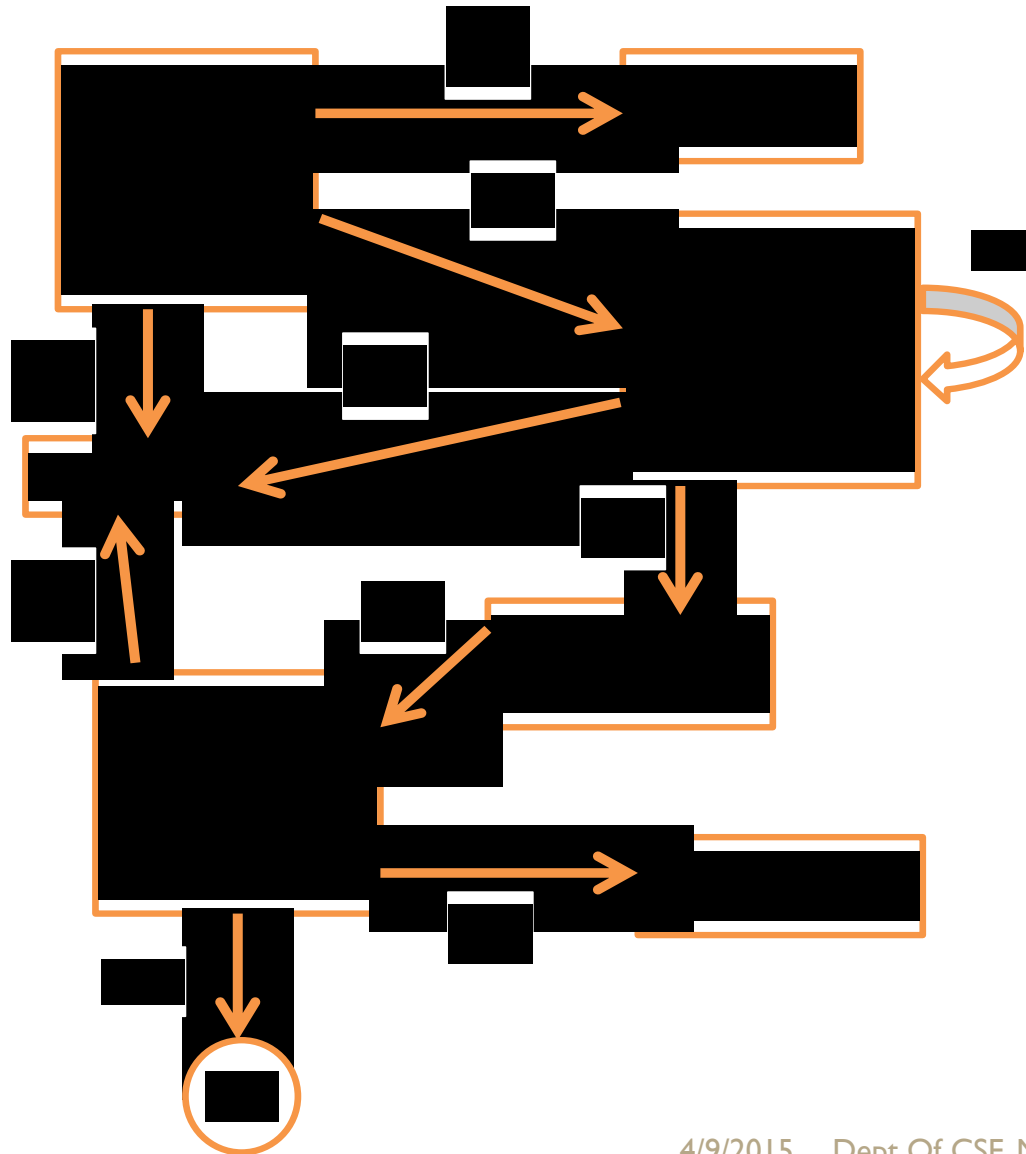
i - if expr then

e- else

a- all other statements

S- stmt

# LR(0) automaton



# Parse table

States	i	e	a	\$	S
0	s2				
1					
2	s2				4
3		r3		r3	
4		s5,r2		r2	
5	s2		s3		
6		r1		r1	

Conflict; So use disambiguating rule to match else with nearest unmatched then. Hence Shift

accept



# Resulting Parse table

States	i	e	a	\$	S
0	s2		s3		1
1				accept	
2	s2		s3		4
3		r3		r3	
4		S5		r2	
5	s2		s3		
6		rl		rl	

# Parsing Actions for “iiaea”

Stack	Symbols	Input	Action
0		iiaea\$	Shift
02	I	iaea\$	Shift
022	ii	aea\$	Shift
0223	iia	ea\$	Reduce $S \rightarrow a$
0224	iiS	ea\$	Shift
02245	iiSe	a\$	Shift
022453	iiSea	\$	$S \rightarrow a$
022456	iiSes	\$	$S \rightarrow iSeS$
024	iS	\$	$S \rightarrow iS$
01	S	\$	accept