GEA environment, selection and outliers - Melbourne Bernd Gruber (based on code from Brenna Forrester) 2019-06-10

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Foreword

This tutorial is based on code and comments from Brenna Forrester, Colorado State University. The Wolf data set is from Schweizer et al. 2016. Genetic subdivision and candidate genes under selection in North American grey wolves Molecular Ecology 25, 380-402. Dryad doi:10.5061/dryad.c9b25.

Multivariate GEA: Redundancy Analysis

RDA is a multivariate ordination technique that analyzes matricies of loci and environmental predictors simultaneously. RDA determines how groups of loci covary in response to the multivariate environment.

RDA is a two-step analysis in which genetic and environmental data are analyzed using multivariate linear regression, producing a matrix of fitted values. Then PCA of the fitted values is used to produce canonical axes, which are linear combinations of the predictors.

More information on RDA & other multivariate GEAs (such as Random Forest) can be found in our paper: Forester BR, Lasky JR, Wagner HH, Urban DL (2018) Comparing methods for detecting multilocus adaptation with multivariate genotype-environment associations Molecular Ecology 27, 2215-2233.

RDA can be used on both individual and population-based sampling designs. The distinction between the two may not be straightforward in all cases. A simple guideline would be to use an individual-based framework when you have individual coordinates for most of your samples, and the resolution of your environmental data would allow for a sampling of environmental conditions across the site/study area. More on RDA with population level data in the notes below.

To run RDA on population level data, calculate allele frequencies (columns) for populations (rows). Applying a Hellinger transformation/standardization to the data will ensure it behaves well in the RDA, e.g. if our input of population allele frequencies was called "pop.data":

```
pop.data.hellinger <- decostand(pop.data, method = "hellinger") # square root of (allele frequency / popula
```

RDA does not require corrections for multiple tests because it analyzes the genomic and environmental data simultaneously!

I highly recommend the following book for more information on interpreting RDA output from vegan: Borcard et al. (2011) Numerical Ecology with R.

Load necessary libraries

```
library(psych)
library(GGally)
## Loading required package: ggplot2
##
## Attaching package: 'ggplot2'
```



```
## The following objects are masked from 'package:psych':
##
##
       %+%, alpha
library(robust)
## Loading required package: fit.models
library(vegan)
## Loading required package: permute
## Loading required package: lattice
## This is vegan 2.5-4
library(qvalue)
                 #bioconductor
```

Before we can start with our redundancy analysis we need to make sure, we select "suitable" environmental predictors. Meaning the predictors should have a "good" chance to have an effect on our response (the genetic structure) and should not be correlated between each other.

Please see Dormann et al. (2013) Ecography for a discussion of these issues. Generally, the |r| > 0.7 "rule of thumb" is a good guideline for removing correlated predictors. We will also check for multicollinearity below using Variance Inflation Factors.

We will use the Wolf data set mentioned above to run an examplary redundancy analysis. To convert a genlight object into the correct format simply use:

```
gen <- as.matrix(gl)</pre>
```

Load the genetic data set from a csv file:

94 10000

[1]

```
##
        chr9.22100598 chr2.19649684
## [1,]
                      0
                                     0
## [2,]
                                     0
                      1
                                     2
                      0
## [3,]
## [4,]
                                     0
                      0
## [5,]
                      1
        chr38.14463749 chr13.20658362
##
## [1,]
## [2,]
                       0
                                        2
## [3,]
                       0
                                        1
## [4,]
                       0
                                        2
## [5,]
                       1
                                        0
```



```
##
        chr23.16849044
## [1,]
## [2,]
                      1
## [3,]
                      0
## [4,]
                      1
## [5,]
# Read from github
fp <- "https://raw.githubusercontent.com/green-striped-gecko/dartRworkshop/master/data"
gen <- read.csv(file.path(fp, "Wolf_Gen_sample_6pops_94indiv.csv"))</pre>
dim(gen) # 94 individuals in rows; 10,000 SNPs in columns
gen[1:5, 1:5] # coded as 0/1/2
Load the environmental data set
    [1] "individual"
##
    [2] "ecotype"
    [3] "long"
##
##
    [4] "lat"
    [5] "ann_mean_temp"
##
    [6] "mean_diurnal_range"
##
    [7] "temp_seasonality"
##
    [8] "max_temp_warmest_month"
##
##
   [9] "min_temp_coldest_month"
## [10] "ann_precip"
## [11] "precip_seasonality"
## [12] "precip_coldest_quarter"
## [13] "land_cover"
## [14] "ndvi"
## [15] "elev"
## [16] "percent_tree_cover"
# Read from github
fp <- "https://raw.githubusercontent.com/green-striped-gecko/dartRworkshop/master/data"
env <- read.csv(file.path(fp, "Wolf_Env_6pops_94indiv.csv"))</pre>
names (env)
```

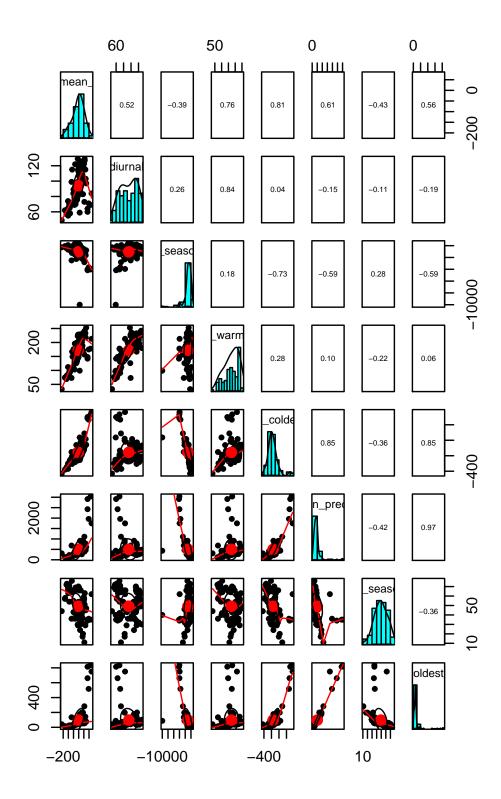
Or in case you are using a genlight object you should be able to use the @other\$ind.metrics table from a genlight data set.



env <- @other\$ind.metrics</pre>

Check for multicollinearity between predictors (|r|>0.7)

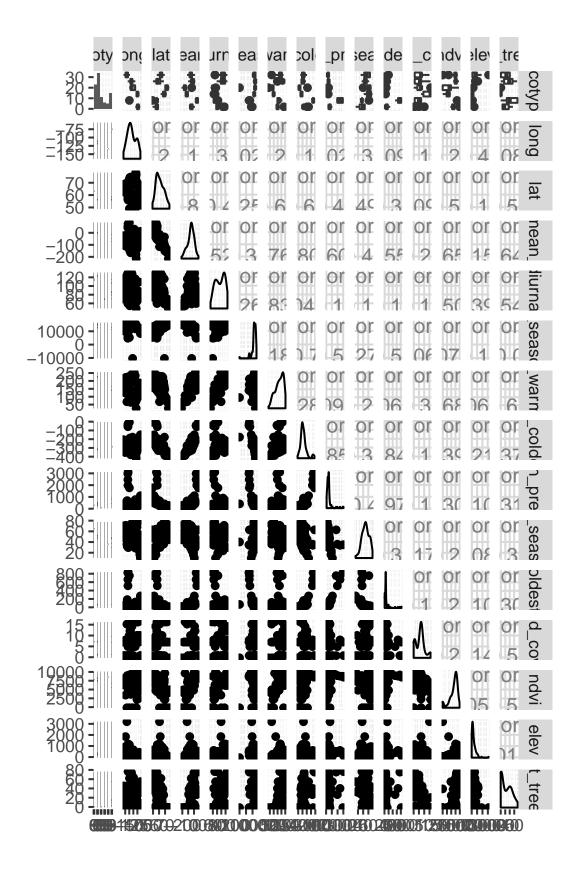
pairs.panels(env[, 5:12]) #good for contineous predictors only





ggpairs(env[, -1]) #allows also factors [except individual]

```
## `stat_bin()` using `bins = 30`. Pick
## better value with `binwidth`.
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## better value with `binwidth`.
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## better value with `binwidth`.
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## better value with `binwidth`.
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## better value with `binwidth`.
## `stat bin()` using `bins = 30`. Pick
## better value with `binwidth`.
```





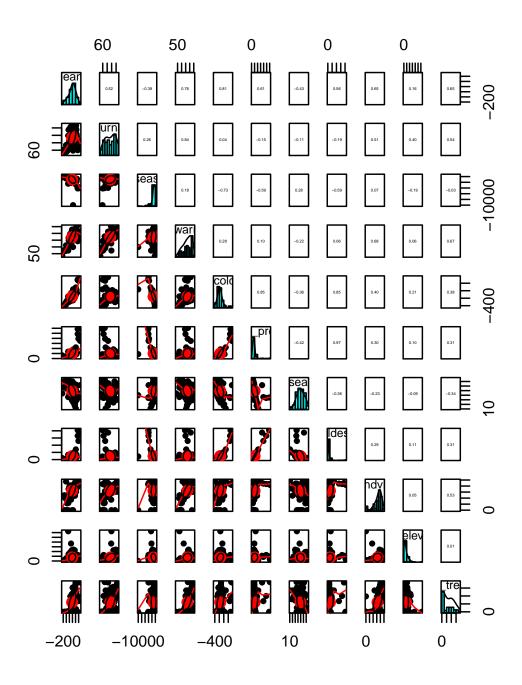
Next we look at landscape cover (a factor)

```
table(env$land_cover) # let's look at land cover, which is a factor
##
           7 8 10 12 14 15 16
        5
   3 23 7 40 7 4 2 1 1 6
```

The distribution of the factor levels is very uneven and dominated by classes 1,7 & 8, so either we would need to combine classes or delete the predictor.

```
env <- env[, -13] #remove land cover
pairs.panels(env[, 5:15], scale = T)
```

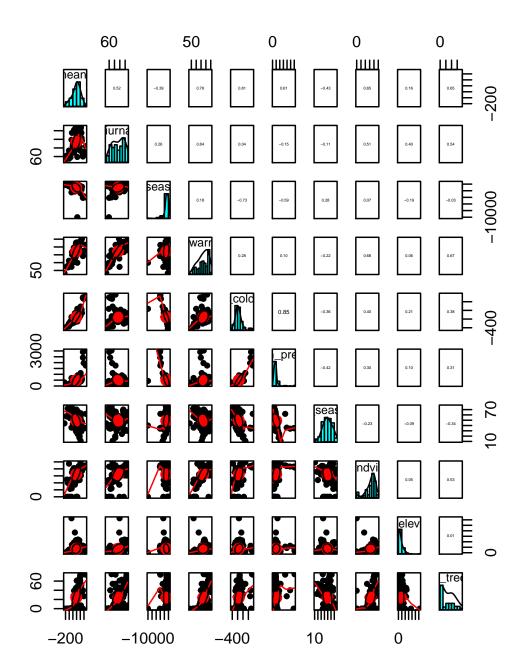




And we also remove factors with high collinearity

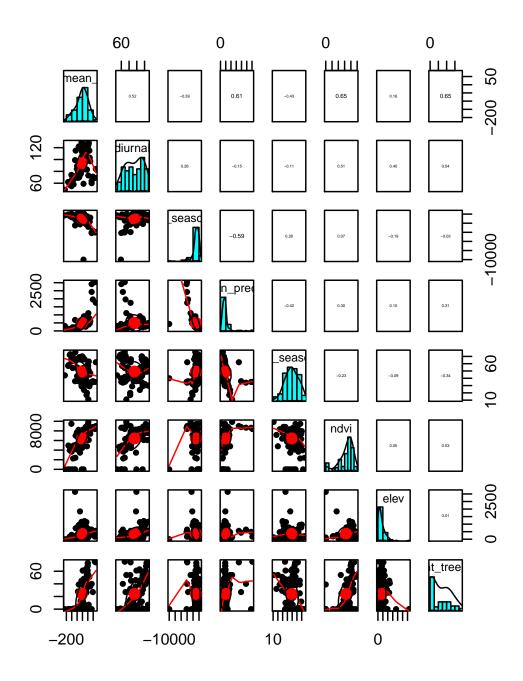
```
env <- env[, -12] # remove precip coldest quarter: 0.97 corr with annual precip
pairs.panels(env[, 5:14], scale = T)
```





 $env \leftarrow env[, -c(8, 9)]$ # remove maxT_warm, minT_cold; covers remaining strong correlations in a small # of property of the strong correlations in a small # of property of the strong correlations in a small # of property of the strong correlations in a small # of property of the strong correlations in a small # of property of the strong correlations in a small # of property of the strong correlations in a small # of property of the strong correlations in a small # of property of the strong correlations in a small # of property of the strong correlations in a small # of property of the strong correlations in a small # of property of the strong correlations in a small # of property of the strong correlations in a small # of property of the strong correlations in a small # of property of the strong correlations in a small # of property of the strong correlations in a small # of property of the strong correlations in the strong correlations and the strong correlations are strong correctly as the strong correct for the str pairs.panels(env[, 5:12], scale = T)





```
# Try this reduced set of predictors:
pred <- env[, 5:12]</pre>
colnames(pred) <- c("AMT", "MDR", "sdT", "AP",</pre>
    "cvP", "NDVI", "Elev", "Tree")
```



Finally we need to scale those predictors (as they are in different units)

```
pred <- scale(pred, scale = TRUE, center = TRUE) # default is center and scale = T; this subtracts the mean
  Running the actual RDA is fairly simple:
wolf.rda <- rda(gen ~ ., data = as.data.frame(pred),</pre>
    scale = T) # vegan wants data frames, not matrices
wolf.rda
## Call: rda(formula = gen ~ AMT + MDR +
```

```
## sdT + AP + cvP + NDVI + Elev + Tree,
## data = as.data.frame(pred), scale = T)
##
##
                   Inertia Proportion Rank
## Total
                 1.000e+04 1.000e+00
## Constrained
                1.357e+03 1.357e-01
                                         8
## Unconstrained 8.643e+03 8.643e-01
                                        85
## Inertia is correlations
##
## Eigenvalues for constrained axes:
   RDA1 RDA2 RDA3 RDA4 RDA5 RDA6 RDA7
## 344.8 267.2 226.8 125.2 106.4 102.5 94.3
##
   RDA8
   89.4
##
##
## Eigenvalues for unconstrained axes:
                             PC5
    PC1
           PC2
                 PC3
                       PC4
                                         PC7
## 341.7 279.6 215.1 160.2 147.1 141.6 130.2
    PC8
##
## 128.6
```

(Showing 8 of 85 unconstrained eigenvalues)

We have as many constrained ("RDA") axes as we have predictors. Residual variance is then modeled by PCA (the unconstrained "PC" axes). Variance explained by the environmental predictors is under "Proportion" and "Constrained" = equivalent to R2 in multiple regression, so it is biased & should be adjusted based on the # of predictors:

RsquareAdj (wolf.rda)

```
## $r.squared
## [1] 0.1356641
##
## $adj.r.squared
## [1] 0.05431482
```



Our constrained ordination explains about 5% of the variation [Not to surprising given our large # of SNPs and other processes at work]

How many of our 8 constrained axes should we retain for detecting outliers?

We can do a formal significance test, but it takes quite a while to run...(& is probably not necessary!)

```
signif.axis <- anova.cca(wolf.rda, by = "axis")
# takes a few HOURS for the full 41K SNP data
# set [See ?anova.cca for more details and
# options]
```

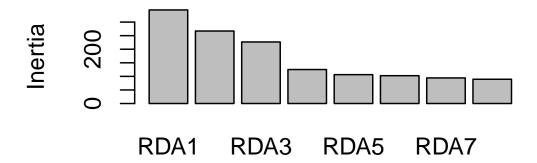
Instead, let's look at the eigenvalues for the constrained axes & plot them

```
summary(eigenvals(wolf.rda, model = "constrained"))
```

```
## Importance of components:
##
                             RDA1
                                       RDA2
## Eigenvalue
                         344.7729 267.1741
## Proportion Explained
                           0.2541
                                    0.1969
## Cumulative Proportion
                           0.2541
                                     0.4511
##
                             RDA3
                                        RDA4
                         226.8258 125.22824
## Eigenvalue
## Proportion Explained
                           0.1672
                                    0.09231
## Cumulative Proportion
                           0.6183
                                    0.71058
##
                              RDA5
                                        RDA6
## Eigenvalue
                         106.38043 102.54389
## Proportion Explained
                           0.07841
                                      0.07559
## Cumulative Proportion
                           0.78899
                                      0.86458
                             RDA7
                                       RDA8
##
## Eigenvalue
                         94.34423 89.37134
## Proportion Explained
                          0.06954 0.06588
## Cumulative Proportion 0.93412 1.00000
screeplot(wolf.rda) # variance explained drops off after 3 axes
```



wolf.rda



Finally let's check VIFs for our predictors (they should be ok)

vif.cca(wolf.rda)

```
MDR
                           sdT
## 7.854243 6.495892 2.775059 4.051610 1.318631
       NDVI
                Elev
                         Tree
## 2.285632 2.028377 2.260139
```

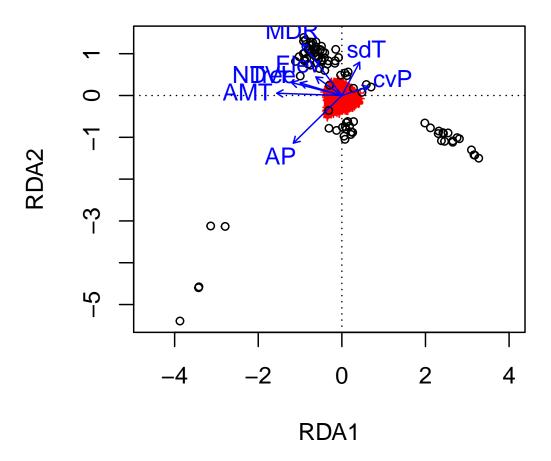
All are below 10 and most are below 5 = multicollinearity shouldn't be a problem.

Plot the RDA

Simple plots

```
plot(wolf.rda, scaling = 3)
```

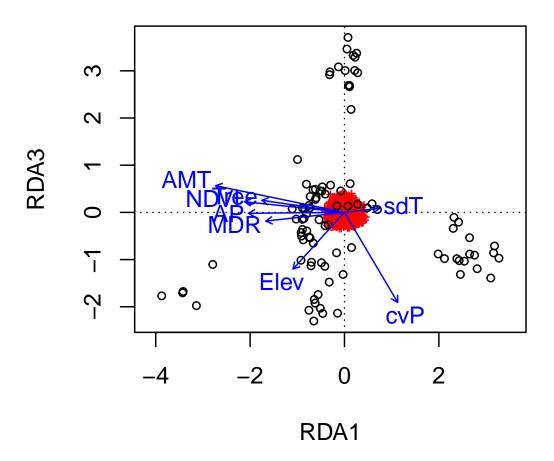




scaling=3 means symmetrical scaling (SNP & indiv scores are scaled by the square root of the eigenvalues) [See Borcard et al. 2011 or vegan help for more information on scaling RDA plots]

plot(wolf.rda, choices = c(1, 3), scaling = 3) # axes 1 and 3





SNPs are in red; individuals are black circles; blue vectors are predictors.

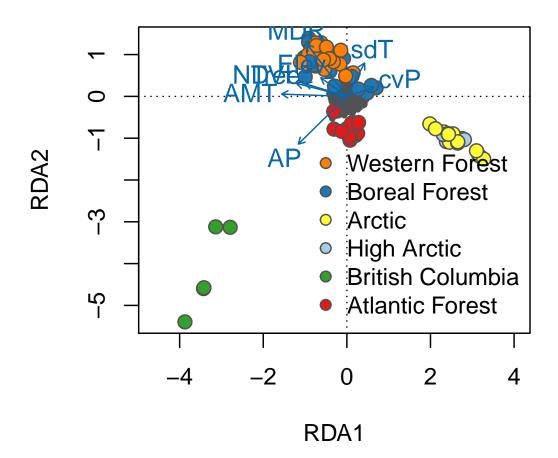
The relative arrangement of these items in the ordination space reflects their relationship with the ordination axes, which are linear combinations of the predictor variables

Let's make some nicer plots:

```
levels(env$ecotype) <- c("Western Forest", "Boreal Forest",</pre>
    "Arctic", "High Arctic", "British Columbia",
    "Atlantic Forest")
colorby <- env$ecotype</pre>
bg \leftarrow c("#ff7f00", "#1f78b4", "#ffff33", "#a6cee3",
    "#33a02c", "#e31a1c")
# axes 1 & 2
```

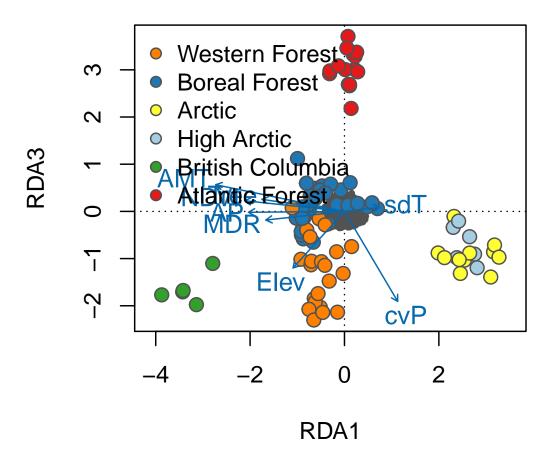


```
plot(wolf.rda, type = "n", scaling = 3)
points(wolf.rda, display = "species", pch = 20,
    cex = 0.7, col = "gray32", scaling = 3) # the snps
points(wolf.rda, display = "sites", pch = 21,
    cex = 1.3, col = "gray32", scaling = 3, bg = bg[colorby]) # the wolves
text(wolf.rda, scaling = 3, display = "bp", col = "#0868ac",
    cex = 1.1) # the predictors
legend("bottomright", legend = levels(colorby),
    bty = "n", col = "gray32", pch = 21, cex = 1,
   pt.bg = bg)
```





```
# axes 1 & 3
plot(wolf.rda, type = "n", scaling = 3, choices = c(1,
    3))
points(wolf.rda, display = "species", pch = 20,
    cex = 0.7, col = "gray32", scaling = 3, choices = c(1,
       3))
points(wolf.rda, display = "sites", pch = 21,
    cex = 1.3, col = "gray32", scaling = 3, bg = bg[colorby],
    choices = c(1, 3))
text(wolf.rda, scaling = 3, display = "bp", col = "#0868ac",
    cex = 1.1, choices = c(1, 3))
legend("topleft", legend = levels(colorby), bty = "n",
    col = "gray32", pch = 21, cex = 1, pt.bg = bg)
```



The impact of continental scale climate is reflected in these plots: BC is wet with low temp seasonality; Arctic areas have small mean diurnal range, low annual temps, andlow tree cover and veg. greenness (NDVI); Atlatic and Western Forsts show weak & strong precip seasonality, respectively.

Identify candidates

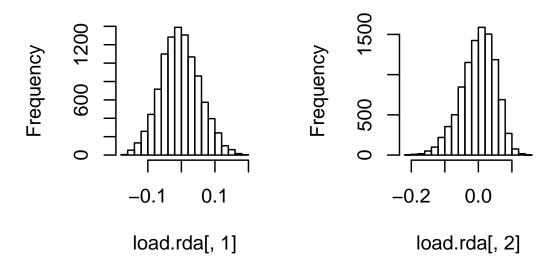
In their publication (Forester et al. 2018, ME), they pulled SNPs with extreme loadings from relevant constrained axes:

```
load.rda <- summary(wolf.rda) $species[, 1:3] # RDA loadings ('species') for axes 1:3
par(mfrow = c(2, 2))
```

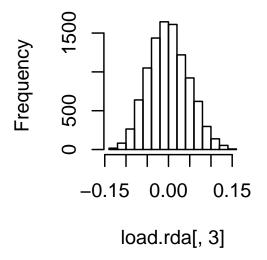


```
hist(load.rda[, 1])
hist(load.rda[, 2])
hist(load.rda[, 3]) # loadings relatively normally distributed
par(mfrow = c(1, 1))
```

Histogram of load.rda[, Histogram of load.rda[,



Histogram of load.rda[,



This approach works well when selection gradients are well understood (high TP, low FP).



For analyses with many predictors, or where the analysis is more exploratory, a multidimensional outlier identification approach will help reduce FP rates (though this also brings down TP rates, of course).

Mahalanobis post-processing of RDA outlier detection results:

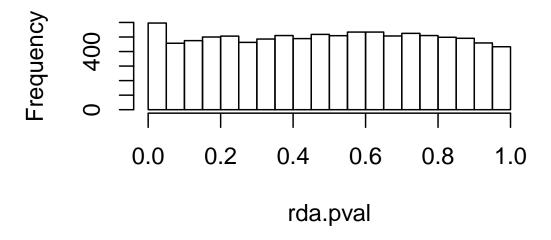
Capblancq T, Luu K, Blum MGB, Bazin E (2018) Mol Ecol Resources

For code to pull outliers on each axis, see our tutorial/vignette: https://popgen.nescent. org/2018-03-27_RDA_GEA.html

We will just use the Mahalanobis distance approach suggested by Capblancq et al.

```
K <- 3 # the number of RDA axes you're looking at
zscale <- apply(load.rda, 2, scale) # I'm not sure scaling is the best approach here...
mscale <- covRob(zscale, distance = TRUE, na.action = na.omit,</pre>
    estim = "pairwiseGK")$dist
gif <- median(mscale)/qchisq(0.5, df = K)
rda.pval <- pchisq(mscale/gif, df = K, lower.tail = FALSE) # Remember: you can always change the GIF!!
hist(rda.pval) #looks a little conservative
```

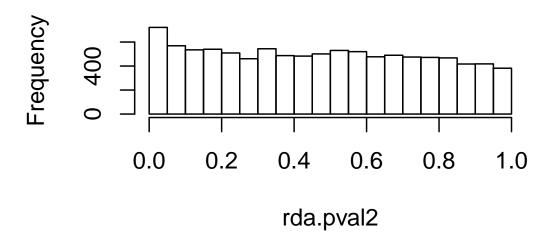
Histogram of rda.pval



```
rda.pval2 <- pchisq(mscale/1.15, df = K, lower.tail = FALSE) # Less conservative GIF (smaller)
hist(rda.pval2)
```



Histogram of rda.pval2

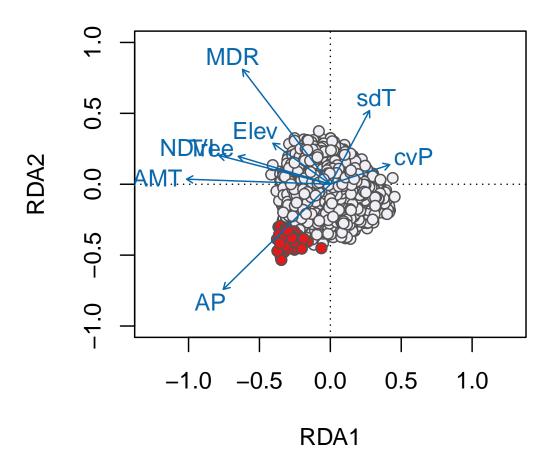


```
rda.qval <- qvalue(rda.pval2)$qvalues
rda.FDR.1 <- colnames(gen)[which(rda.qval < 0.1)]
```

Let's look at where these candidates are in the ordination space:

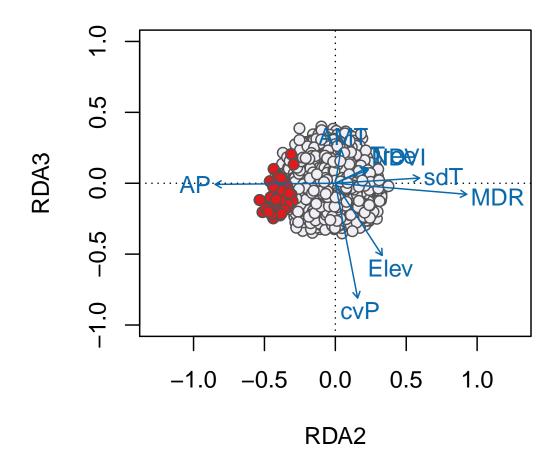
```
# color by predictor:
snp.color <- as.data.frame(colnames(gen), stringsAsFactors = F)</pre>
snp.color[, 2] <- apply(snp.color, 1, function(x) if (x %in%)</pre>
    rda.FDR.1) "gray32" else "#00000000")
snp.color[, 3] <- apply(snp.color, 1, function(x) if (x %in%</pre>
    rda.FDR.1) "#e31a1c" else "#00000000")
# axes 1 & 2
plot(wolf.rda, type = "n", scaling = 3, xlim = c(-1,
    1), ylim = c(-1, 1)
points(wolf.rda, display = "species", pch = 21,
    cex = 1, col = "gray32", bg = "#fleef6", scaling = 3)
points(wolf.rda, display = "species", pch = 21,
    cex = 1, col = snp.color[, 2], bg = snp.color[,
        3], scaling = 3)
text(wolf.rda, scaling = 3, display = "bp", col = "#0868ac",
    cex = 1)
```





```
# axes 2 & 3
plot(wolf.rda, type = "n", scaling = 3, xlim = c(-1,
    1), ylim = c(-1, 1), choices = c(2, 3))
points(wolf.rda, display = "species", pch = 21,
    cex = 1, col = "gray32", bg = "#f1eef6", scaling = 3,
    choices = c(2, 3))
points(wolf.rda, display = "species", pch = 21,
    cex = 1, col = snp.color[, 2], bg = snp.color[,
        3], scaling = 3, choices = c(2, 3))
text(wolf.rda, scaling = 3, display = "bp", col = "#0868ac",
    cex = 1, choices = c(2, 3))
```







Well done!!

That is the end. Well done you finished. Feel free to have another go or have a well deserved beverage!!!

