

# Algorithm 1: CCC algorithm

1 **Function** get\_partitions( $\mathbf{v}$ ,  $k_{\max}$ ):

**Input:**

$\mathbf{v}$ : feature values on  $n$  objects

$k_{\max}$ : maximum number of clusters

**Output:**

$\Pi$ : a set of partitions over  $n$  objects

2 **if**  $\mathbf{v} \in \mathbb{R}^n$  **then**

3     **for**  $k \leftarrow 2$  **to**  $\min\{k_{\max}, |\mathbf{v}| - 1\}$  **do**

4          $\rho \leftarrow (\rho_\ell \mid \Pr(v_i < \rho_\ell) \leq (\ell - 1)/k), \forall \ell \in [1, k + 1]$

5          $\pi_\ell \leftarrow \{i \mid \rho_\ell < v_i \leq \rho_{\ell+1}\}, \forall \ell \in [1, k]$

6          $\Pi_k \leftarrow \pi$

7 **else**

8      $\mathcal{C} \leftarrow \{v_i \mid v_i \in \mathbf{v}\}$

9      $k \leftarrow |\mathcal{C}|$

10      $\pi_c \leftarrow \{i \mid v_i = \mathcal{C}_c\}, \forall c \in [1, k]$

11      $\Pi_k \leftarrow \pi$

12  $\Pi \leftarrow \{\Pi_k \mid |\Pi_k| > 1\}, \forall k$

13 **return**  $\Pi$

14  
15 **Function** ccc( $\mathbf{x}$ ,  $\mathbf{y}$ ,  $k_{\max}$ ):

**Input:**

$\mathbf{x}$ : feature values on  $n$  objects

$\mathbf{y}$ : feature values on  $n$  objects

$k_{\max}$ : maximum number of clusters

**Output:**

$c$ : correlation value for  $\mathbf{x}$  and  $\mathbf{y}$  ( $c \in [0, 1]$ )

16  $\Pi^{\mathbf{x}} = \text{get\_partitions}(\mathbf{x}, k_{\max})$

17  $\Pi^{\mathbf{y}} = \text{get\_partitions}(\mathbf{y}, k_{\max})$

18  $c \leftarrow \max\{\text{ARI}(\pi_j, \pi_l)\}, \forall \pi_j \in \Pi^{\mathbf{x}}, \pi_l \in \Pi^{\mathbf{y}}$

19 **return**  $\max(c, 0)$