NETFLIX

EM Mixture Model

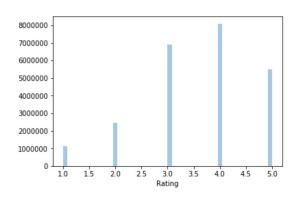
Xin Jin Xuan Guo

Data Exploration

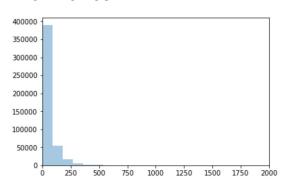
- Original data has 100498277 rows and 3 columns(Time, Customer Id and Ratings);
- We focus on the first data set due to computation limit;
- The dataset includes 4499 movies and 470758 customers.
- In the form of matrix, there exists more than 98% missing values.

Data Exploration

The Distribution of Ratings

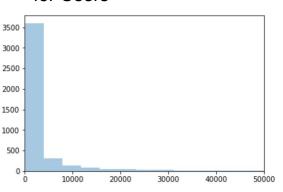


The Distribution of Reviews for Movies



Right-skewed

The Distribution of Reviews for Users



Right-skewed

Data Cleaning

Original dataset

1:		
1488844	3	2005-09-06
822109	5	2005-05-13
885013	4	2005-10-19

Cleaned dataset

Cust_ld	Movie_Id	Rating
1488844	1	3
822109	1	5
885013	1	4

Matrix Form

Cust_ld\ Movie_ld	1	2
1488844	3	
822109	5	
885013	4	

Model Assumptions

Quirky(pi):

In quirky mode, rater i has a private rating distribution with probability mass function $q(x|\alpha i)$ that applies to every movie regardless of its intrinsic merit.

Consensus(1-pi):

In consensus mode, rater i rates movie j according to a distribution with probability mass function $c(x|\beta j)$ shared with all other raters in consensus mode.

$$q(k|\alpha_i) = \binom{d-1}{k-1} * \alpha_i^{k-1} * (1-\alpha_i)^{d-k}$$

$$L(\theta) = \prod_i \prod_{j \in M_i} [\pi_i q(x_{ij}|\alpha_i) + (1-\pi_i)c(x_{ij}|\beta_j)],$$

$$c(k|\beta_j) = \binom{d-1}{k-1} * \beta_j^{k-1} * (1-\beta_j)^{d-k}$$

EM Algo Implementation for (pi, alpha, beta)

$$\ln\left(\sum_{i=1}^{m} \gamma_i\right) \ge \sum_{i=1}^{m} \frac{\gamma_i^n}{\sum_{j=1}^{m} \gamma_j^n} \ln\left(\frac{\sum_{j=1}^{m} \gamma_j^n}{\gamma_i^n} \gamma_i\right).$$

$$\ln L(\theta) \ge \sum_{i} \left[\ln \pi_{i} \sum_{j \in M_{i}} w_{ij}^{n} + \ln(1 - \pi_{i}) \sum_{j \in M_{i}} (1 - w_{ij}^{n}) \right]$$

$$+ \sum_{i} \sum_{j \in M_{i}} w_{ij}^{n} \ln q(x_{ij} | \alpha_{i}) + \sum_{i} \sum_{j \in M_{i}} (1 - w_{ij}^{n}) \ln c(x_{ij} | \beta_{j}) + \sum_{i} \sum_{j \in M_{i}} c_{ij}^{n}.$$

Convergence:

$$\frac{\left|\ln L(\theta^n) - \ln L(\theta^{n-1})\right|}{\left|\ln L(\theta^{n-1})\right| + 1} < \varepsilon$$

Updates:

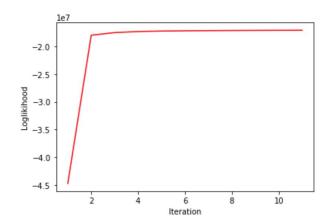
$$\pi_i^{n+1} = \frac{\sum_{j_{x_{ij}} > 0} w_{ij}^n}{m_i}$$

$$\alpha_i^{n+1} = \frac{\sum_{j_{x_{ij}>0}} w_{ij}^n * (x_{ij} - 1)}{(d-1) * \sum_{j_{x_{ij}>0}} w_{ij}^n}$$

$$\beta_j^{n+1} = \frac{\sum_i (1 - w_{ij}^n) * (x_{ij} - 1)}{(d-1) * \sum_i (1 - w_{ij}^n)}$$

Implementation Results

EM Convergence:



```
c = 0
while c<20:
    w = get_w(pi,alpha,beta,x,w)
    pi = get_pi(pi,w)
    alpha = get_alpha(x,w)
    beta = get_beta(x,w)
    like = loglikeli(pi,alpha,beta,x)
    if ((l[-1]-like)/l[-1])<0.0005:
        break

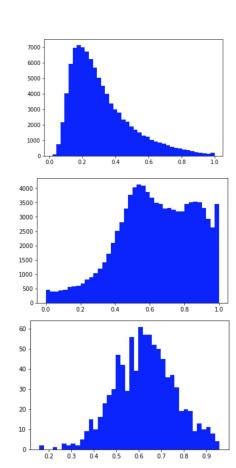
l.append(like)
    c += 1</pre>
```

Final Parameters

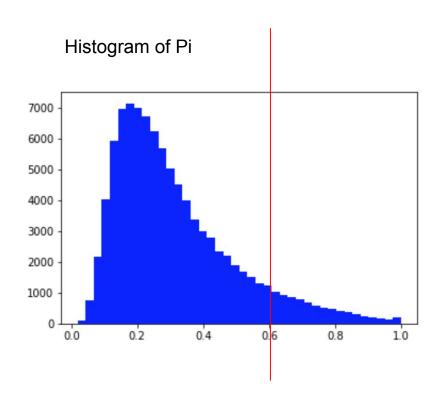
Final Distribution of Pi

Final Distribution of Alpha

Final Distribution of Beta



Identify Unusual Users

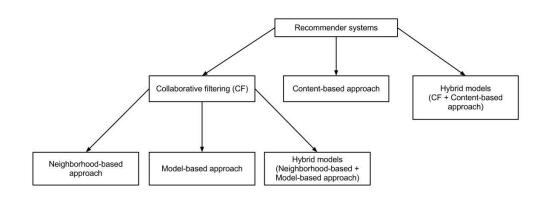


Remove users who have more probability to be in the quirky mode.

The threshold we choose to identify unusual users is pi > 0.6.

Remove 7266 unusual users. 7%

Collaborative Filtering



User-based

Item-based

$$L(\theta) = \prod_{i} \prod_{j \in M_i} [\pi_i q(x_{ij} | \alpha_i) + (1 - \pi_i) c(x_{ij} | \beta_j)],$$

EM Mixture Model learns both user-based info and iterm-based info.

Collaborative Filtering

Cust_ld\ Movie_ld	1	2	3	4
1488844	3	1	2	3
822109	5	3	2	
885013	4	•		3

Similarity

Pearson-Correlation Similarity

$$ext{simil}(x,y) = rac{\sum\limits_{i \in I_{xy}} (r_{x,i} - ar{r_x}) (r_{y,i} - ar{r_y})}{\sqrt{\sum\limits_{i \in I_{xy}} (r_{x,i} - ar{r_x})^2} \sqrt{\sum\limits_{i \in I_{xy}} (r_{y,i} - ar{r_y})^2}}$$

Cosine-Based Similarity

$$ext{simil}(x,y) = \cos(ec{x},ec{y}) = rac{ec{x}\cdotec{y}}{||ec{x}|| imes||ec{y}||} = rac{\sum\limits_{i\in I_{xy}}r_{x,i}r_{y,i}}{\sqrt{\sum\limits_{i\in I_x}r_{x,i}^2}\sqrt{\sum\limits_{i\in I_y}r_{y,i}^2}}$$

SVD Algo

The prediction \hat{r}_{ui} is set as:

$$\hat{r}_{ui} = \mu + b_u + b_i + q_i^T p_u$$

Optimization Goal: Min

$$\sum_{r_{ui} \in R_{train}} (r_{ui} - \hat{r}_{ui})^2 + \lambda (b_i^2 + b_u^2 + ||q_i||^2 + ||p_u||^2)$$

Gradient Descent

$$b_{u} \leftarrow b_{u} + \gamma(e_{ui} - \lambda b_{u})$$

$$b_{i} \leftarrow b_{i} + \gamma(e_{ui} - \lambda b_{i})$$

$$p_{u} \leftarrow p_{u} + \gamma(e_{ui} \cdot q_{i} - \lambda p_{u})$$

$$q_{i} \leftarrow q_{i} + \gamma(e_{ui} \cdot p_{u} - \lambda q_{i})$$

 $e_{ui} = r_{ui} - \hat{r}_{ui}.$

Comparison after Unusual User Identification

MAE	RMSE
0.73327766	0.93505776
0.73297882	0.93468037
0.73231072	0.93444277
0.73095701	0.93125733
0.73001626	0.92982399

MAE	RMSE
0.72625528	0.92592605
0.7286607	0.92794139
0.72662997	0.9263454
0.72764525	0.92663783
0.72870872	0.9272608

	MAE	RMSE
SVD(Before)	0.732	0.933
SVD(After)	0.727	0.926

Future Work

- Normalize Ratings
- Predict using EM mixture Model
- Use the time column
- Improve the data structure to increase computation speed

Thank you!