User's Guide for SNOPT-MATLAB: Matlab interface for nonlinear optimizer SNOPT

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Abstract

This article serves as documentation for the Matlab interface for SNOPT, a general-purpose system for constrained optimization. SNOPT minimizes a linear or nonlinear function subject to bounds on the variables and sparse linear or nonlinear constraints. It is suitable for large-scale linear and quadratic programming and for linearly constrained optimization, as well as for general nonlinear programs.

The Matlab m-files associated with the interface are available on github at:

http://github.com/snopt/snopt-matlab/releases.

The latest version is 2.3.0 and is fully compatible with SNOPT Version 7.5 and later. For full details on SNOPT, please see the User's Guide for SNOPT.

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1. Introduction

snOpt-matlab is a Matlab interface for nonlinear optimization software SNOPT. (In particular, the Matlab interface utilizes SNOPTA interface of SNOPT). It minimizes a linear or nonlinear function subject to bounds on the variables and sparse linear or nonlinear constraints. It is suitable for large-scale linear and quadratic programming and for linearly constrained optimization, as well as for general nonlinear programs of the form

NPA minimize
$$F_{obj}(x)$$
 subject to $l_x \le x \le u_x$, $l_F \le F(x) \le u_F$,

where x is an n-vector of variables, the upper and lower bounds are constant, F(x) is a vector of smooth linear and nonlinear constraint functions $\{F_i(x)\}$, and $F_{obj}(x)$ is one of the components of F to be minimized, as specified by the input parameter ObjRow. (An optional parameter Maximize may specify that $F_{obj}(x)$ should be maximized instead of minimized.)

Ideally, the first derivatives (gradients) of F_i should be known and coded by the user. If only some gradients are known, then the missing ones are estimated by finite differences.

Note that upper and lower bounds are specified for all variables and functions. This form allows full generality in specifying various types of constraint. Special values are used to indicate absent bounds ($l_j = -\infty$ or $u_j = +\infty$ for appropriate j). Free variables and free constraints ("free rows") have both bounds infinite. Fixed variables and equality constraints have $l_j = u_j$.

In general, the components of F are *structured* in the sense that they are formed from sums of linear and nonlinear functions of just some of the variables. This structure can be exploited (see Section 3.1).

For more details on the algorithm implemented in SNOPT, please see

- P. E. Gill, W. Murray, M. A. Saunders, Elizabeth Wong. SNOPT 7.6 User's Manual. CCoM Technical Report 17-1, Center for Computational Mathematics, University of California, San Diego.
- P. E. Gill, W. Murray and M. A. Saunders. SNOPT: An SQP algorithm for large-scale constrained optimization. SIAM Review 47 (2005), 99-131.

2. Compiling and Installing the Matlab interface

To compile a new Matlab mex-file, the SNOPT optimization package must be configured with the Matlab option:

>> ./configure --with-matlab=/path/to/matlab

with the appropriate path to Matlab set.

On a Linux system, the user must also configure with the option '-with-pic'.

>> ./configure --with-matlab=/path/to/Matlab --with-pic

By default, SNOPT uses its own BLAS subroutines. However, it is possible to compile the mex-file to utilize Matlab's own built-in BLAS library.

In addition to providing the location of Matlab, the user must also indicate that a third-party BLAS library will be used and also that SNOPT should be compiled with 64-bit integers. 64-bit integers are required as Matlab's built-in BLAS library only accepts 64-bit integers.

>> ./configure --with-matlab=/path/to/Matlab --with-blas=matlab --with-64

After successful configuration, the mex-file can be built with the following command

>> make matlab

A new Matlab mex-file will be compiled and placed in the directory \${SNOPT}/matlab.

2.1. Using precompiled Matlab libraries

The SNOPT optimization package comes with precompiled Matlab mex-files inside the directory: \$\{\SNOPT\}/\matlab/\precompiled.

Libraries for several types of machines are provided:

• Linux: *.mexa64

• Mac OS: *.mexmaci64

• Windows 64-bit Matlab: *.mexw64

• Windows 32-bit Matlab: *.mexw32

The directory containing the precompiled mex-file and the SNOPT Matlab m-files (usually located in $\{SNOPT\}/matlab\}$) need to be added to the Matlab path either by using the setpath command or by clicking on Home \rightarrow Environment \rightarrow Set Path.

3. Matlab subroutines for SNOPT

The Matlab interface for SNOPT is accessed via the following Matlab subroutines:

```
snopt (Section 3.2) snopt is the main subroutine called to solve the nonlinear problem NLP using SNOPT.
snsolve (Section 3.3) is the alternative method for calling SNOPT. It is based on the Matlab function fmincon.
snJac (Section 3.4) is used to define the derivative structures needed by SNOPT.
snend (Section 3.5) is called at the end of a program.
snspec (Section 3.6) allows the user to provide a file of option specifications.
snget, sngeti, sngetr (Section 3.7) obtain the current value of a given option.
snset, snseti, snsetr (Section 3.8) set the value of the given option.
snscreen (Section 3.9) controls the output of SNOPT to the Matlab command screen.
snprint (Section 3.10) allows the user to provide the name of an output print file.
snsummary (Section 3.11) allows the user to redirect the summary output to a file.
snsetwork (Section 3.12) is an advanced routine that lets the user define the sizes of the initial integer and real workspaces for SNOPT.
```

3.1. Exploiting problem structure

In many cases, the vector F(x) is a sum of linear and nonlinear functions. sn0pt-matlab allows these terms to be specified separately, so that the linear part is defined just once by

the input arguments iAfun, jAvar, and A. Only the nonlinear part is recomputed at each x.

Suppose that each component of F(x) is of the form

$$F_i(x) = f_i(x) + \sum_{j=1}^{n} A_{ij} x_j,$$

where $f_i(x)$ is a nonlinear function (possibly zero) and the elements A_{ij} are constant. The $nF \times n$ Jacobian of F(x) is the sum of two sparse matrices of the same size: F'(x) = G(x) + A, where G(x) = f'(x) and A is the matrix with elements $\{A_{ij}\}$. The two matrices must be non-overlapping in the sense that every element of the Jacobian F'(x) = G(x) + A is an element of G(x) or an element of A, but not both.

For example, the function

$$F(x) = \begin{pmatrix} 3x_1 + e^{x_2}x_4 + x_2^2 + 4x_4 - x_3 + x_5 \\ x_2 + x_3^2 + \sin x_4 - 3x_5 \\ x_1 - x_3 \end{pmatrix}$$

can be written as

$$F(x) = f(x) + Ax = \begin{pmatrix} e^{x_2}x_4 + x_2^2 + 4x_4 \\ x_3^2 + \sin x_4 \\ 0 \end{pmatrix} + \begin{pmatrix} 3x_1 - x_3 + x_5 \\ x_2 - 3x_5 \\ x_1 - x_3 \end{pmatrix},$$

in which case

$$F'(x) = \begin{pmatrix} 3 & e^{x_2}x_4 + 2x_2 & -1 & e^{x_2} + 4 & 1\\ 0 & 1 & 2x_3 & \cos x_4 & -3\\ 1 & 0 & 0 & 0 & 0 \end{pmatrix}$$

can be written as F'(x) = f'(x) + A = G(x) + A, where

$$G(x) = \begin{pmatrix} 0 & e^{x_2}x_4 + 2x_2 & 0 & e^{x_2} + 4 & 0 \\ 0 & 0 & 2x_3 & \cos x_4 & 0 \\ 0 & 0 & 0 & 0 & 0 \end{pmatrix}, \quad A = \begin{pmatrix} 3 & 0 & -1 & 0 & 1 \\ 0 & 1 & 0 & 0 & -3 \\ 1 & 0 & -1 & 0 & 0 \end{pmatrix}.$$

The nonzero elements of A and G are provided to $\mathtt{snOpt-matlab}$ in coordinate form. The elements of A are entered as triples (i,j,A_{ij}) in the arrays \mathtt{iAfun} , \mathtt{jAvar} , \mathtt{A} . The sparsity pattern of G is entered as pairs (i,j) in the arrays \mathtt{iGfun} , \mathtt{jGvar} . The corresponding entries G_{ij} (any that are known) are assigned to appropriate array elements $G(\mathtt{k})$ in the user's subroutine userfun.

The elements of A and G may be stored in any order. Duplicate entries are ignored. As mentioned, iffun and jfvar may be defined automatically by subroutine snJac (p. 9) when Derivative option 0 is specified and userfun does not provide any gradients.

3.2. Subroutine snopt

This is the main subroutine to solve problem NLP using SNOPT. The following are valid call sequences for snopt:

```
[...] = snopt( x, xlow, xupp, xmul, xstate, ...
                  Flow, Fupp, Fmul, Fstate, ...
                  userfun [, options] )
   [...] = snopt( x, xlow, xupp, xmul, xstate, ...
                  Flow, Fupp, Fmul, Fstate, ...
                  userfun, ObjAdd, ObjRow [, options] )
   [...] = snopt( x, xlow, xupp, xmul, xstate, ...
                  Flow, Fupp, Fmul, Fstate, ...
                  userfun, ...
                  A, iAfun, jAvar, iGfun, jGvar [, options] )
   [...] = snopt( x, xlow, xupp, xmul, xstate, ...
                  Flow, Fupp, Fmul, Fstate, ...
                  userfun, ObjAdd, ObjRow, ...
                  A, iAfun, jAvar, iGfun, jGvar [, options] )
The output from snopt is:
   [x,F,inform,xmul,Fmul,xstate,Fstate,output] = snopt( ... )
```

On entry:

x,xlow,xupp,xmul define the initial value of the variable x, the lower and upper bounds on x, and the initial value of the multipliers for x. If nothing is known about x, set x and xmul to 0.0.

Flow, Fupp, Fmul define the lower and upper bounds on the problem functions F(x), and the initial value of the multipliers for the problem functions. If nothing is known about Fmul, set Fmul to 0.0.

xstate defines the initial states of the variables x.

If there is no wish to provide special information, you may set $\mathtt{xstate}(j) = 0$, $\mathtt{x}(j) = 0.0$ for all $j = 1:\mathtt{n}$. All variables will be eligible for the initial basis.

Less trivially, to say that the optimal value of x_j will probably be one of its bounds, set $\mathtt{xstate}(j) = 4$ and $\mathtt{x}(j) = \mathtt{xlow}(j)$ or $\mathtt{xstate}(j) = 5$ and $\mathtt{x}(j) = \mathtt{xupp}(j)$ as appropriate.

A CRASH procedure is used to select an initial basis. The initial basis matrix will be triangular (ignoring certain small entries in each column). The values $\mathtt{xstate}(j) = 0, 1, 2, 3, 4, 5$ have the following meaning:

$\mathtt{xstate}(j)$	State of variable j during CRASH
{0,1,3}	Eligible for the basis. 3 is given preference
$\{2, 4, 5\}$	Ignored

After CRASH, variables for which $\mathtt{xstate}(j) = 2$ are made superbasic. Other variables not selected for the basis are made nonbasic at the value $\mathtt{x}(j)$ (or the closest value inside their bounds). See the description of \mathtt{xstate} below (on exit).

Fstate defines the initial states of the problem functions F. See the description for xstate.

- userfun is a user-defined function that computes the nonlinear portion f(x) of the vector of problem functions F(x) = f(x) + Ax, and optionally, its Jacobian G(x) for a given vector x. userfun is either a string containing the Matlab function name or a function handle. See Section 3.13.1.
- ObjAdd is a constant that will be added to the objective row F(Objrow) for printing purposes. Typically, ObjAdd = 0.0d+0.
- ObjRow says which row of F(x) is to act as the objective function. If there is no such row, set ObjRow = 0. Then SNOPT will seek a *feasible point* such that $l_F \leq F(x) \leq u_F$ and $l_X \leq x \leq u_X$. $(0 \leq \text{ObjRow} \leq \text{nF})$
- A,iAfun,jAvar define the coordinates (i,j) and values A_{ij} of the nonzero elements of the linear part A of the function F(x) = f(x) + Ax.

The entries may define the elements of A in any order.

iGfun, jGvar define the coordinates (i, j) of G_{ij} , the nonzero elements of the nonlinear part of the derivatives G(x) + A of the function F(x) = f(x) + Ax.

The entries may define the elements of G in any order, but subroutine userfun must define the values of G in exactly the same order.

- options is an optional parameter. It is a struct containing options for snOpt-matlab. Currently, only two options exist:
 - options.name provides the name of the problem
 - options.stop is an advanced feature that allows the user to specify the "snSTOP" function called at every major iteration. options.stop is either a string containing the name of the Matlab function or a function handle. (See Section 3.14)
 - options.start can be set to 'Cold' or 'Warm' to specify how a starting point will be obtained. For Cold starts, SNOPT starts "from scratch" to find an initial starting point. For Warm starts, the xstate and Fstate inputs should define a valid starting point (usually from a previous run).

On exit:

- x,F are the values of the variables and constraints at the solution.
- inform is the exit code returned by SNOPT. Please see the SNOPT documentation for a full description of the codes.

xmul, Fmul are the values of the multipliers for the variables and constraints at the solution.

xstate, Fstate are the final states of the variables and constraints.

output is a struct containing the following components:

- output.info is the same as inform
- output.iterations returns the total number of minor iterations for the problem
- output.majors is the total number of major iterations for the problem

3.3. Subroutine snsolve

This is the alternative *fmincon-style* subroutine to solve the following nonlinear problem using SNOPT:

```
fmincon-NP \min_{x} f(x) subject to c(x) \le 0 c_{eq}(x) = 0 Ax \le b \qquad A_{eq}(x) = b_{eq} x_{low} \le x \le x_{upp}
```

The following are valid call sequences for snsolve:

The output from snsolve is:

```
[x,fval,exitflag,output,lambda,states] = snsolve( ... )
```

On entry:

myobj is a user-defined function that computes the objective function f(x) at a given point x. myobj should be a string containing the name of the Matlab function or a function handle. See Section 3.13.2.

x0 is the initial value of the variables.

A,b define the linear inequality constraints of the problem.

Aeq, beq define the linear equality constraints of the problem.

xlow, xupp define the lower and upper bounds on the variables.

nonlcon is a user-defined function that computes the nonlinear equality and inequality constraints of the problem, and optionally, the Jacobian matrix of these functions at a given point. nonlcon is either a string containing the name of a Matlab function or a function handle. See Section 3.13.2.

options is an optional parameter. It is a struct containing options for snOpt-matlab. Currently, the only valid options are:

- options.name provides the name of the problem
- options.stop is an advanced feature that allows the user to specify the "snSTOP" function called at every major iteration. options.stop is either a string containing the name of the Matlab function or a function handle. (See Section 3.14)

On exit:

x contains the values of the variables at the solution.

fval is the objective value at x.

exitflag is the exit code returned by SNOPT. Please see the SNOPT documentation for a full description of the codes.

lambda is a struct containing the multipliers at the solution.

- lambda.lower are the final multipliers for lower bounds
- lambda.upper are the final multipliers for upper bounds
- lambda.ineqnonlin are the final multipliers for nonlinear inequalities
- lambda.eqnonlin are the final multipliers for nonlinear equalities
- lambda.ineqlin are the final multipliers for linear inequalities
- lambda.eqlin are the final multipliers for linear equalities

states are the final states of the variables and constraints.

- states.x are the final states of the variables
- states.inequonlin are the final states for nonlinear inequalities
- states.eqnonlin are the final states for nonlinear equalities
- states.ineqlin are the final states for linear inequalities
- states.eqlin are the final states for linear equalities

output is a struct containing the following components:

- output.info is the same as inform
- output.iterations returns the total number of minor iterations for the problem
- output.majors is the total number of major iterations for the problem

3.4. Subroutine snJac

If the "Derivative option" is set to 0 and your user-defined routine for the objective and constraints do not provide any derivatives, you can call snJac to determine the input arrays iAfun, jAvar, A, iGfun, and jGvar. The call sequence to snJac is:

```
[A,iAfun,jAvar,iGfun,jGvar] = snJac(usrfun,x0,xlow,xupp,nF)
```

On entry:

userfun is a user-defined function that computes the nonlinear portion f(x) of the vector of problem functions F(x) = f(x) + Ax, and optionally, its Jacobian G(x) for a given vector x. userfun is either a string containing the Matlab function name or a function handle. See Section 3.13.1.

x0 is the initial point x. If nothing is known, x0 can be set to zero.

xlow, xupp are the lower and upper bounds on the variables.

nF is the number of constraints in the problem.

On exit:

A,iAfun,jAvar define the coordinates (i,j) of the nonzero elements of the linear part A of the function F(x) = f(x) + Ax.

iGfun, jGvar define the coordinates (i, j) of G, the nonzero elements of the nonlinear part of the derivatives G(x) + A of the function F(x) = f(x) + Ax.

3.5. Subroutine snend

The routine snend should be called at the end to deallocate any memory used by SNOPT.

3.6. Subroutine snspec

snspec lets the user provide the name of a file with option specifications for SNOPT.

```
[inform] = snspec( filename )
```

On entry:

filename is a string containing the name of the specifications file to be read by SNOPT.

On exit:

inform reports the result of calling snspec. Here is a summary of possible values.

Finished successfully

101 Specs file read.

Errors while reading Specs file

- No Specs file specified (iSpecs ≤ 0 or iSpecs > 99).
- 132 End-of-file encountered while looking for Specs file. snspec encountered end-of-file or Endrun before finding Begin (see the Options section of the SNOPT Manual). The Specs file may not be properly assigned.
- 133 End-of-file encountered before finding End. Lines containing Skip or Endrun may imply that all options should be ignored.
- 134 Endrun found before any valid sets of options.
- > 134 There were i = INFO 134 errors while reading the Specs file.

3.7. Subroutines snget, sngeti, sngetr

snget, sngeti, and sngetr let the user retrieve the current value of a given option. The following are the valid call sequences:

```
[option] = snget ( keyword )
[option] = sngeti( keyword )
[option] = sngetr( keyword )
```

On entry:

keyword is a string containing the keyword of the option to be retrived.

On exit:

option is the value (integer or real) of the option specified by keyword.

3.8. Subroutines snset, snseti, snsetr

```
snset ( keyword )
snseti( keyword, ivalue )
snsetr( keyword, rvalue )
```

On entry:

keyword is a string containing the keyword of the option to be retrived. For snset, the keyword should contain both the option name and the desired option value.

ivalue/rvalue is the (integer or real) value that the specified option will be set to.

3.9. Subroutine snscreen

snscreen controls the output of SNOPT to the Matlab command screen.

```
snscreen on snscreen off
```

3.10. Subroutine snprint

snprint lets the user provide a filename for the print output from SNOPT.

```
snprint( filename )
```

On entry:

filename should be a string specifying the filename to be used.

3.11. Subroutine snsummary

snsummary controls the summary output of SNOPT.

```
snsummary off
snsummary( filename )
```

On entry:

off turns the summary output off.

filename is the name of the file that the summary output is redirected to.

3.12. Subroutine snsetwork

snsetwork is an advanced subroutine that allows the user to define the initial sizes of the integer and real workspaces for SNOPT. By default, workspace size is initialized to 5000. However, for larger problems or dense problems, a much larger value may be required. This subroutine should be called before any other subroutines.

```
snsetwork( leniw, lenrw )
```

On entry:

leniw,lenrw are integers specifying the size of the integer and real workspace for SNOPT.

These values should be at least 500.

3.13. User-defined subroutines

Both snopt and snsolve require user-defined functions as arguments. These functions compute the objective function and constraints, and if necessary, the gradients of these functions, at a given point.

3.13.1. Function userfun

For snopt, the user provides a function userfun that computes the nonlinear portion f(x) of the vector of problem functions F(x) = f(x) + Ax, and optionally, its Jacobian G(x) for a given vector x.

The valid function declarations for userfun are:

```
[F] = myFun(x)
[F,G] = myFun(x)
```

If the user does not provide any derivative information for F, then G can be omitted from the output. In this case, snOpt-matlab will estimate the derivatives by finite differences. The user can also provide some of the derivatives of F. Any unknown derivatives should be marked by a NaN.

In addition, the user can check the variable nargout to determine if computation of the derivatives is necessary. In particular, if nargout is greater than 1, then G is requested and should be computed if possible. Otherwise, only F is required.

3.13.2. Functions myobj and nonlcon

For snsolve, the user provides myobj, which computes the objective function f(x) at a given point x, and (possibly) nonlcon, which computes the nonlinear equality and inequality constraints of the problem, and optionally, the Jacobian matrix of these functions at a given point.

The valid function declarations for myobj and nonlcon are:

```
[f] = my0bj(x)
[f,g] = my0bj(x)
```

The valid function declarations for nonlcon are:

```
[c,ceq] = myCon(x)
[c,ceq,dc,dceq] = myCon(x)
```

where c and ceq are the nonlinear inequality and equality constraints, and dc and dceq are the gradients of the nonlinear inequality and equality constraints.

If no derivative information is provided, then the user can omit g, dc, and dceq from the output. In this case, snOpt-matlab will estimate the derivatives by finite differences.

For both myobj and nonlcon, the user can provide *some* of the derivatives of the objective and constraints. Any unknown derivatives should be marked by a NaN.

In addition, the user can check the variable nargout to determine if computation of the derivatives is necessary. In particular, for myobj, if nargout is greater than 1, then g is requested and should be computed if possible; for nonlcon, if nargout is greater than 2, then dc and dceq are requested and should be computed if possible.

3.14. snSTOP Feature

snSTOP is an advanced feature for SNOPT. The user can provide a function with the following declaration:

This function will be called at the end of *every* major iteration. Current values relevant to the run are passed to the STOP function. If **iAbort** is set to a nonzero value, then SNOPT will terminate the current run.

4. Frequently Asked Questions

• Why is the Matlab interface to SNOPT so slow compared with (fmincon | the Fortran version of SNOPT/NPSOL| etc.)?

There could be a number of things affecting the speed of snOpt-matlab:

- 1. There is a lot of overhead in the Matlab interface. The interface works by taking the Matlab input, and transforming and converting it into Fortran input for the SNOPT library. In particular, for every callback to the user-defined functions (myobj, nonlcon, or userfun), the interface has to allocate memory for input and output, and then copy that data between the Fortran library and Matlab. We try to minimize the work for these callbacks as much as possible.
- 2. Are you providing derivative information to SNOPT? The more information you give SNOPT, the better. If no derivative information is provided, then SNOPT uses finite-differencing to estimate the values, which can take more time. Even partial derivative information can help speed things up. Providing the derivatives in sparse format would also speed things up.
- 3. Is your problem very dense? SNOPT is intended for *sparse* problems. In particular, if the Jacobian matrix is very dense, then the interface has to copy a dense matrix back and forth between Fortran and Matlab with every callback to the user-defined functions. It would be ideal if the Jacobian of the constraints be provided in a sparse format (and not as a dense matrix).
- I tried to compile the Matlab mex-files on my Linux machine, but I get the error:

/usr/bin/ld: ./lib/libsnmex7.a(snopta.o): relocation R_X86_64_32 against '.rodata' can not be used when making a shared object; recompile with -fPIC

How do I fix this?

Reconfigure the software package with "–with-pic" and then recompile. Also make sure to do a "make veryclean" before you compile again.