



Joint 1

Rotation Z			
cθ1	-sθ1	0	0
sθ1	cθ1	0	0
0	0	1	0
0	0	0	1

Translation Z			
1	0	0	0
0	1	0	0
0	0	1	d1
0	0	0	1

Rotation X			
1	0	0	0
0	ca1	-sa1	0
0	sa1	ca1	0
0	0	0	1

cθ1	-sθ1	0	0
sθ1	cθ1	0	0
0	0	1	d1
0	0	0	1

1	0	0	0
0	0	-1	0
0	1	0	0
0	0	0	1

Reduce: $s(\pi/2) = 1$
 $c(\pi/2) = 0$

cθ1	0	sθ1	0
sθ1	0	-cθ1	0
0	1	0	d1
0	0	0	1

Full Move List							
Joint	θ		l		d		α
J1	φ + 0	θ1	0	l1	0.077	d1	π/2 α1
J2	φ + 0.7131	θ2	0.1957	l2	0	d2	0 α2
J3	φ - 0.7131	θ3	0.126	l3	0	d3	-π/2 α3

Joint 2

Rotation Z			
c θ_2	-s θ_2	0	0
s θ_2	c θ_2	0	0
0	0	1	0
0	0	0	1

x

Translation X			
1	0	0	l ₂
0	1	0	0
0	0	1	0
0	0	0	1

c θ_2	-s θ_2	0	c θ_2 *l ₂
s θ_2	c θ_2	0	s θ_2 *l ₂
0	0	1	0
0	0	0	1

Full Move List

Joint	θ		l		d		α	
J1	$\varphi + 0$	θ_1	0	l_1	0.077	d_1	$\pi/2$	α_1
J2	$\varphi + 0.7131$	θ_2	0.1957	l_2	0	d_2	0	α_2
J3	$\varphi - 0.7131$	θ_3	0.126	l_3	0	d_3	$-\pi/2$	α_3

Joint 3

Rotation Z			
cθ1	-sθ1	0	0
sθ1	cθ1	0	0
0	0	1	0
0	0	0	1

Translation X			
1	0	0	l3
0	1	0	0
0	0	1	0
0	0	0	1

Rotation X			
1	0	0	0
0	cα1	-sα1	0
0	sα1	cα1	0
0	0	0	1

Full Move List								
Joint	θ		l		d		α	
J1	φ + 0	θ1	0	l1	0.077	d1	π/2	α1
J2	φ + 0.7131	θ2	0.1957	l2	0	d2	0	α2
J3	φ - 0.7131	θ3	0.126	l3	0	d3	-π/2	α3

Reduce: $s(-\pi/2) = -1$
 $c(\pi/2) = 0$

cθ3	-sθ3	0	cθ3*l3
sθ3	cθ3	0	sθ3*l3
0	0	1	0
0	0	0	1

x

1	0	0	0
0	0	1	0
0	-1	0	0
0	0	0	1

=

cθ3	0	-sθ3	cθ3*l3
sθ3	0	cθ3	sθ3*l3
0	-1	0	0
0	0	0	1

Combination

Joint 1			
cθ1	0	sθ1	0
sθ1	0	-cθ1	0
0	1	0	d1
0	0	0	1

Joint 2			
cθ2	-sθ2	0	cθ2*l2
sθ2	cθ2	0	sθ2*l2
0	0	1	0
0	0	0	1

Joint 3			
cθ3	0	-sθ3	cθ3*l3
sθ3	0	cθ3	sθ3*l3
0	-1	0	0
0	0	0	1

Full Move List								
Joint	θ	l		d		α		
J1	φ + 0	θ1	0	l1	0.077	d1	π/2	α1
J2	φ + 0.7131	θ2	0.1957	l2	0	d2	0	α2
J3	φ - 0.7131	θ3	0.126	l3	0	d3	-π/2	α3

cθ2cθ3 - sθ2sθ3	0	-cθ2sθ3 - sθ2cθ3	cθ2cθ3*l3 - sθ2sθ3*l3 + cθ2*l2
sθ2cθ3 + cθ2sθ3	0	-sθ2sθ3 + cθ2cθ3	sθ2cθ3*l3 + cθ2sθ3*l3 + sθ2*l2
0	-1	0	0
0	0	0	1

cθ1	0	sθ1	0
sθ1	0	-cθ1	0
0	1	0	d1
0	0	0	1

c(θ2+θ3)	0	-s(θ2+θ3)	l3(c(θ2+θ3)) + cθ2*l2
s(θ2+θ3)	0	c(θ2+θ3)	l3(s(θ2+θ3)) + cθ2*l2
0	-1	0	0
0	0	0	1

Reduced With Trig	cφcθ - sφsθ =	c(φ + θ)
Identities:	sφcθ + cφsθ =	s(φ + θ)

cθ1c(θ2+θ3)	-sθ1	-cθ1s(θ2+θ3)	cθ1(l3(c(θ2+θ3)) + cθ2*l2)
sθ1s(θ2+θ3)	cθ1	-sθ1s(θ2+θ3)	sθ1(l3(c(θ2+θ3)) + cθ2*l2)
s(θ2+θ3)	0	c(θ2+θ3)	l3(s(θ2+θ3)) + sθ2*l2 + d1
0	0	0	1

θ1	= arctan2(T[0,1], T[1,1])	✓
sθ2	= ((T[0,3]/cθ1) - (T[2,2]/l2)) / l2	
θ2	= arctan2(sθ2, cθ2)	
θ3	= arctan2(T[2,0], T[2,2])	✓
	- θ2	

$$\theta_2: \sin 2: P_z = l_3 \cdot s(\theta_2 + \theta_3) + d_1 + s\theta_2 \cdot l_2 \Rightarrow P_z - l_3 \cdot s(\theta_2 + \theta_3) - d_1 = s\theta_2 \cdot l_2 \Rightarrow s\theta_2 = \frac{T[2,3] - l_3 \cdot s(\theta_2 + \theta_3) - d_1}{l_2}$$

$$\cos 2: P_x = c\theta_1 (l_3 \cdot c(\theta_2 + \theta_3) + c\theta_2 \cdot l_2) \Rightarrow \frac{P_x}{c\theta_1} = l_3 \cdot c(\theta_2 + \theta_3) + c\theta_2 \cdot l_2 \Rightarrow c\theta_2 = \frac{\frac{P_x}{c\theta_1} - l_3 \cdot c(\theta_2 + \theta_3)}{l_2}$$

$$\theta_2 = \frac{T[0,3]}{T[1,1]} - l_3 \cdot c(\theta_2 + \theta_3)$$