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[1]

(a) $Z = \frac{X-M}{\sigma}$, $f_z(x) = e^{-\frac{1}{2}x^2} \cdot \frac{1}{\sqrt{2\pi}}$ 常態分布

$E(Z) = 0$, $E(Z-M)^2 = 1$

$E(Z_0 + Z_1) = 0$; $E(Z_0 + Z_1 - M)^2 = 1+1=2$ 卡方分布

(b) $Q_1 = Z^2 : \chi^2 (df=1)$ 卡方分布

(c) $Q_2 = Z_1^2 + Z_2^2 : \chi^2 (df=2)$

(d) 柯西分布

[2] (a) $P(Z_0 + Z_1 \leq 1) = 0.6914$, (1-st. norm. sf (1, 0.2))

(b) $P(Z_0^2 \leq 1) = 0.8413$, (1-st. norm. sf (1, 0.1))

(c) $P(Z_1^2 + Z_2^2 \leq 1) = 0.6914$, (1-st. norm. sf (1, 0.2))

(d) $P(\frac{Z_0}{Z} \leq 1)$

[3]

[3] (a) $\mu_A = 65$
 $Z = \frac{\bar{X}_A - 65}{\frac{3}{5}}$

$P(\bar{X}_A \leq 64) = P\left(\frac{\bar{X}_A - 65}{\frac{3}{5}} \leq \frac{64 - 65}{\frac{3}{5}}\right)$

$= P(Z \leq -1.67) \doteq 0.04746 \doteq 4.7\%$