

## Introduction

In a previous assignment, a team I was a part of analysed data about the growth measurements of Tamar Wallabies in Australia (originally provided by the CSIRO Biometrics Unit INRE in Canberra, this version cleaned and corrected by Professor Heike Hofmann, Department of Statistics at Iowa State University in 2008, publicly available from the Statistic Science domain

<http://www.statsci.org/data/oz/wallaby.html>).

The data consists of 1463 measurements of 77 wallabies at different ages across fourteen locations. There are twelve variables, summarised below:

Attributes	Description	Format	Variable Type
Anim	Unique Animal Identifier	Number	Numeric
Sex	1= male, 2 = female	Binary Number	Categorical
Loca	Location of animal	Alphanumeric Text (two characters)	Categorical
Leng	Length of animal	Number (tenths of a millimetre)	Numeric
Head	Length of head	Number (tenths of a millimetre)	Numeric
Ear	Length of ear	Number (tenths of a millimetre)	Numeric
Arm	Length of arm	Number (tenths of a millimetre)	Numeric
Leg	Length of leg	Number (tenths of a millimetre)	Numeric
Pes	Length of foot (pes)	Number (tenths of a millimetre)	Numeric
Tail	Length of tail	Number (tenths of a millimetre)	Numeric
Weight	Weight	Number (tenths of a gram)	Numeric
Age	Days from birth	Number	Numeric

A plot of the data shows how highly correlated the physical measurements are:

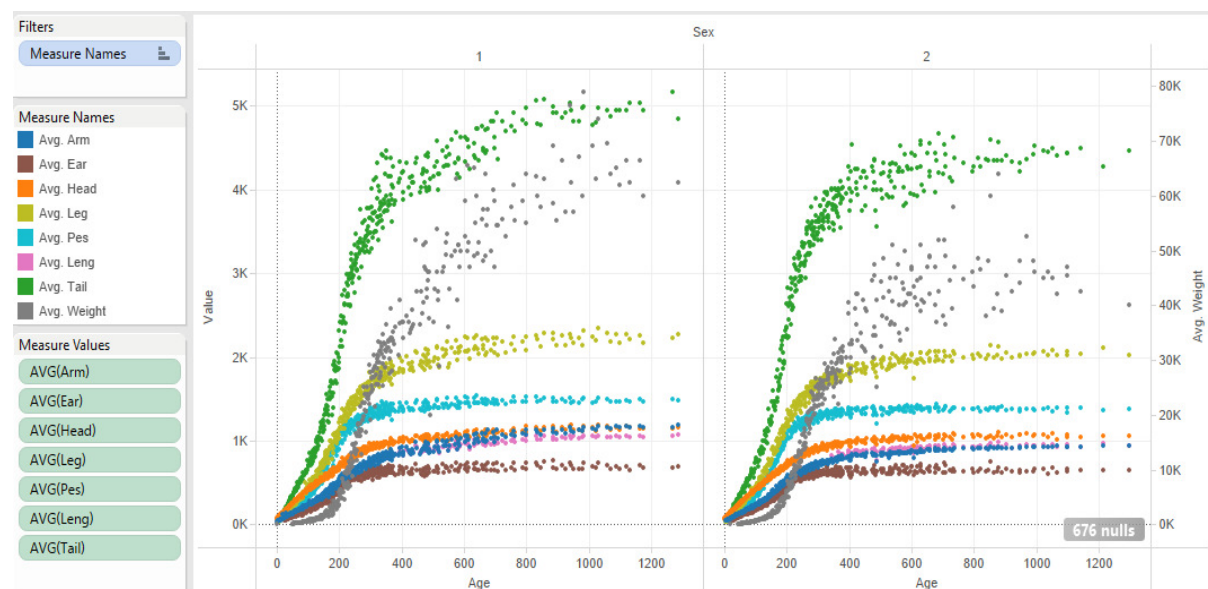


Figure1: Measurements by age and sex – with weight on separate axis

Previously, the team originally gave consideration to using Weight as the dependant variable, with some of the body part measurements as explanatory variables, in addition to age, location and gender. However, the high correlation meant that using all the variables wasn't appropriate in a regression, and did not improve a linear mixed model (LMM). Therefore, it was decided to use just

one of the body size variables. Head size was chosen instead of weight, due to there being no missing values for head.

In this assignment, a Principal Components Analysis (PCA) will be performed on the highly correlated variables. The component(s) will then be included in the LMM to see whether there is an improvement. Weight will be used instead of Head as the dependent variable. Length will still be excluded, as it is missing 1183 of the 1463 measurements. When the rows with data missing from the other variables are removed, there are 1182 of the original 1463 measurements left in the data set. A correlation matrix of the remaining variables is shown below:

	weight	Head	Ear	Arm	Leg	Pes	Tail
weight	1.0000000	0.8890429	0.8246763	0.9283592	0.8935956	0.8039926	0.9018297
Head	0.8890429	1.0000000	0.9778606	0.9878897	0.9961650	0.9798736	0.9879802
Ear	0.8246763	0.9778606	1.0000000	0.9609295	0.9837529	0.9892665	0.9788041
Arm	0.9283592	0.9878897	0.9609295	1.0000000	0.9908630	0.9604538	0.9871019
Leg	0.8935956	0.9961650	0.9837529	0.9908630	1.0000000	0.9834162	0.9943633
Pes	0.8039926	0.9798736	0.9892665	0.9604538	0.9834162	1.0000000	0.9740589
Tail	0.9018297	0.9879802	0.9788041	0.9871019	0.9943633	0.9740589	1.0000000

It appears from the graphs above that the weight does not differ significantly between male and female wallabies until approximately 400 days. Therefore, two k-means cluster analyses will also be run on the weight of wallabies older than 400 days. The first will create two clusters to see whether it separates the wallabies into male and female groups. The second will create three clusters to see whether they are grouped by location.

## **Method**

A similar process will be followed as was performed in Assignment 2, where a linear regression was run and then a LMM. Although it was found that a linear regression was not appropriate due to some of the four assumptions of independence, linearity, normality and homoscedasticity not being met, it will set a baseline to measure any improvement offered by the LMM. A PCA will then be run and the number of major component(s) identified. The models will then be run again, including the component(s), to see whether there is an improvement, and whether location and / or sex have a statistically significant impact on the weight of the wallabies.

The dataset was named wallaby\_na and the variables were assigned as follows:

```
H <- wallaby_na$Head
W <- wallaby_na$Weight
A <- wallaby_na$Age
L <- wallaby_na$Loca
An <- wallaby_na$Anim
S <- wallaby_na$Sex
```

A simple linear regression was run first with Age and Location as the explanatory variables:

```
lm1 <- lm(W ~ A + L)
```

As in assignment 2, the Box-Cox procedure was used to see whether the model could be improved by raising age to a power other than one, to better fit the curved shape of the graph.

```

a <- lm(W ~ A)
bc<-boxcox(a)
which.max(bc$y)
lambda<-bc$x[which.max(bc$y)]
lambda

```

This produced a value of 0.4646. This was included in the model as an extra variable:

```

A2 <- A^lambda
lm2 <- lm(W ~ A2 + A + L)

```

A third linear regression was run, including the Sex variable:

```
lm3 <- lm(W ~ A2 + A + L + S)
```

Two linear mixed models were then run, using Animal as the random effect:

```
lme1<-lme(W ~ A + A2 + L, data = wallaby_na, random = ~ 1 | An, correlation = corAR1(.5))
```

```
lme2<-lme(W ~ A + A2 + L + S, data = wallaby_na, random = ~ 1 | An, correlation = corAR1(.5))
```

Having created these models as a baseline, the PCA was then performed. The variables Head, Ear, Arm, Leg, Pes and Tail were included. The data was scaled first, so that larger values did not contribute inordinately to the result.

```

std_wall <- as.data.frame(scale(wallaby_na[5:10]))
wall.pca <- prcomp(std_wall)

```

A summary of the result showed that the first principal component accounted for 98.52% of the variance in the variables. This is an indication of how highly correlated the variables are. Each variable is weighted almost identically in the component.

```
summary(wall.pca)
```

Importance of components:

	PC1	PC2	PC3	PC4	PC5	PC6
Standard deviation	2.4313	0.23915	0.1224	0.08910	0.08552	0.03920
Proportion of Variance	0.9852	0.00953	0.0025	0.00132	0.00122	0.00026
Cumulative Proportion	0.9852	0.99470	0.9972	0.99852	0.99974	1.00000

```
wall.pca$rotation[,1]
```

Head	Ear	Arm	Leg	Pes	Tail
0.4095505	0.4068342	0.4066142	0.4108468	0.4065887	0.4090351

The first principal component was assigned to a variable:

```
H_PC1 <- wall.pca$x[,1]
```

The five models were then run again, this time including the component.

```
lm1_PC <- lm(W ~ H_PC1 + A + L)
lm2_PC <- lm(W ~ H_PC1 + A2 + A + L)
lm3_PC <- lm(W ~ H_PC1 + A2 + A + L + S)
lme1_PC <- lme(W ~ H_PC1 + A + A2 + L, data = wallaby_na, random = ~ 1 | An, correlation =
corAR1(.5))
lme2_PC <- lme(W ~ H_PC1 + A + A2 + L + S, data = wallaby_na, random = ~ 1 | An, correlation =
corAR1(.5))
```

A new data set was then created including only measurements for wallabies aged 400 days and over. The variables Weight, Head, Ear, Arm, Leg, Pes, Tail and Age were standardised and then the kmeans function run, splitting the data into two clusters. The cluster numbers were added to the dataset and then a table created to show how many of the measurements for male and female wallabies were added to each cluster.

```
wallaby_400 <- wallaby_na[wallaby_na$Age > 399, ]
std_wall <- as.data.frame(scale(wallaby_400[5:11]))

wall_400_fit <- kmeans(std_wall, 2)
wall_400_clust <- data.frame(wallaby_400, wall_400_fit$cluster)
table(wall_400_clust$Sex, wall_400_clust$wall_400_fit.cluster)

wall_400_fit <- kmeans(std_wall, 3)
wall_400_clust <- data.frame(wallaby_400, wall_400_fit$cluster)
table(wall_400_clust$Loca, wall_400_clust$wall_400_fit.cluster)
```

## **Results**

The R-squared and AIC results for each model were as follows:

Model	R-squared	AIC
lm1	0.8569	24290.77
lm2	0.8947	23929.81
lm3	0.8975	23900.54
lme1		21162.07
lme2		21146.92
lm1_PC	0.9066	23788.18
lm2_PC	0.9088	23762.46
lm3_PC	0.9105	23741.47
lme1_PC		21107.99
lme2_PC		21092.88

As was found in Assignment 2, the linear mixed model performed better than the linear regression, and there was a slight improvement when the Sex variable was included. There was also a slight improvement when the principal component from the PCA was included.

The full output of the final model (lme2\_PC) is shown below, without the correlation:

```

Linear mixed-effects model fit by REML
Data: wallaby_na
      AIC      BIC    logLik
21092.88 21199.13 -10525.44

Random effects:
Formula: ~1 | An
(Intercept) Residual
StdDev:    36.52957 7482.269

Correlation Structure: AR(1)
Formula: ~1 | An
Parameter estimate(s):
Phi
0.9677602
Fixed effects: W ~ H_PC1 + A + A2 + L + S
              Value Std. Error   DF   t-value p-value
(Intercept) 10282.244  3504.346 1108   2.934140  0.0034
H_PC1        1658.086   250.089 1108   6.629984  0.0000
A             72.029     5.769 1108  12.485557  0.0000
A2          -1200.373   354.768 1108  -3.383549  0.0007
LH1          6450.106  3171.598 1108   2.033709  0.0422
LH11         234.509   7625.976   56   0.030751  0.9756
LH12        -4026.850  7732.140   56  -0.520794  0.6046
LH2          2396.833  4311.366   56   0.555933  0.5805
LH3           715.509  3583.607   56   0.199662  0.8425
LH5          -53.002  7625.518   56  -0.006951  0.9945
LH7           125.018  5554.311   56   0.022508  0.9821
LH8          7230.287  6717.310   56   1.076366  0.2864
LH9          -98.646  4571.908   56  -0.021577  0.9829
LHa          2202.233  2113.623 1108   1.041923  0.2977
LHb          4493.989  3033.729   56   1.481342  0.1441
LK           6831.046  4668.793   56   1.463129  0.1490
LW           3484.987  4126.075   56   0.844625  0.4019
S2          -760.293  1923.655 1108  -0.395233  0.6927

Standardized within-Group Residuals:
      Min      Q1      Med      Q3      Max
-4.5577260 -0.6839594 -0.1932880  0.7431471  3.2799308

Number of Observations: 1182
Number of Groups: 68

```

The principal component was found to be significant. However, only location H1 has a p-value less than 0.05, showing that it is the only location likely to be a significant factor in the difference in Weight from location G. In addition, the sex does not contribute significantly to the weight of the wallaby.

However, the k-means cluster analysis seemed to indicate that sex could be significant to the weight of the wallaby once it is older than 400 days. To make the results clearer, the Sex variable was changed from 1 and 2 to M and F for male and female. The table showing the clusters and Sex is as follows:

	1	2
F	2	117
M	68	43

Nearly all the female wallaby measurements are in the same cluster, which would seem to indicate that, above 400 days of age, the weight of a wallaby is affected by the sex.

The result of segregating the data into three clusters and then comparing them by location is as follows:

	1	2	3
G	25	43	55
H1	0	2	0
H2	0	2	1
H8	0	0	1
Ha	0	20	17
Hb	26	1	12
K	0	7	14
W	0	4	0

Restricting the dataset has meant that there are only four locations with more than four measurements. This result would seem to support what was found above in the linear mixed model, that location is not a significant factor in the weight of a wallaby, as there is no clear cluster for each location.

## **Conclusion**

As with Assignment 2, neither the Principal Components Analysis nor k-means clustering indicated that the location of a wallaby is a significant factor in its size. The PCA also didn't show that the sex of the wallaby is significant. However, when restricting the data to measurements of wallabies 400 days and older, the k-means cluster analysis seemed to show that sex was significant to some extent, with nearly all the measurements of females included in the one cluster, and 61% of male measurements in the other. As was concluded in Assignment 2, a larger and more comprehensive data set would be required before the effect of location and sex could be determined more confidently.

## **References**

Box, G. E. P. and Cox, D. R. Journal of the Royal Statistical Society. Series B (Methodological). Vol. 26, No. 2 (1964), pp. 211-252

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Department of Primary Industries, Parks, Water and Environment, 2012, 'Pest risk assessment – Tammar Wallaby', viewed 1<sup>st</sup> of May 2015, <[http://dpi.pwe.tas.gov.au/Documents/Tammar-Wallaby\\_Risk-Assessment.pdf](http://dpi.pwe.tas.gov.au/Documents/Tammar-Wallaby_Risk-Assessment.pdf)>

Wood, J, CSIRO Biometrics Unit INRE, Canberra, 1994, 'Growth of Tammar Wallabies', *OzDazl* data set, viewed 05 May <<http://www.statsci.org/data/oz/wallaby.html>>

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West, B.T., Welch, K.B. & Galecki, A.T. 2007, *Linear mixed models- a practical guide using statistical software*, Taylor & Francis Group, Boca Raton.

Winter. B 2014, 'A very basic model for performing linear fixed effects analyses tutorial', *University of California*, viewed 15<sup>th</sup> of May 2016, <[http://www.bodowinter.com/tutorial/bw\\_LME\\_tutorial.pdf](http://www.bodowinter.com/tutorial/bw_LME_tutorial.pdf)>

## Appendix

```
> summary(lm1)
```

```
Call:
```

```
lm(formula = W ~ A + L)
```

```
Residuals:
```

Min	1Q	Median	3Q	Max
-52820	-4264	-601	4830	19721

```
Coefficients:
```

	Estimate	Std. Error	t value	Pr(> t )	
(Intercept)	-6135.5353	496.1502	-12.366	< 2e-16	***
A	76.2958	0.9645	79.105	< 2e-16	***
LH1	210.8395	1022.9554	0.206	0.83674	
LH11	1553.9024	4948.6403	0.314	0.75357	
LH12	-3441.0252	6979.4161	-0.493	0.62209	
LH2	1991.8574	1065.8390	1.869	0.06190	.
LH3	1146.4857	1084.8781	1.057	0.29083	
LH5	1285.5715	4948.3876	0.260	0.79507	
LH7	875.4615	2878.4291	0.304	0.76107	
LH8	1388.0238	1568.5448	0.885	0.37639	
LH9	745.0874	2144.6253	0.347	0.72834	
LHa	1607.7999	531.2692	3.026	0.00253	**
LHb	5468.6693	686.2803	7.969	3.79e-15	***
LK	5131.3350	915.7019	5.604	2.62e-08	***
LW	223.9549	1028.8996	0.218	0.82773	

```
---
```

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
Residual standard error: 6969 on 1167 degrees of freedom
```

```
Multiple R-squared:  0.8569, Adjusted R-squared:  0.8551
```

```
F-statistic: 499 on 14 and 1167 DF, p-value: < 2.2e-16
```



```
> summary(lm2)
```

```
Call:
```

```
lm(formula = w ~ A2 + A + L)
```

```
Residuals:
```

Min	1Q	Median	3Q	Max
-35093	-4488	20	4348	18669

```
Coefficients:
```

	Estimate	Std. Error	t value	Pr(> t )	
(Intercept)	-32730.975	1367.078	-23.942	< 2e-16	***
A2	3687.548	180.125	20.472	< 2e-16	***
A	3.661	3.643	1.005	0.3152	
LH1	-190.216	877.952	-0.217	0.8285	
LH11	7541.113	4256.175	1.772	0.0767	.
LH12	-5504.183	5989.443	-0.919	0.3583	
LH2	1268.352	915.212	1.386	0.1661	
LH3	-191.279	933.156	-0.205	0.8376	
LH5	6758.432	4254.306	1.589	0.1124	
LH7	5211.773	2478.864	2.102	0.0357	*
LH8	729.873	1346.253	0.542	0.5878	
LH9	4089.705	1847.405	2.214	0.0270	*
LHa	347.377	459.987	0.755	0.4503	
LHb	4788.447	589.790	8.119	1.19e-15	***
LK	3932.095	787.887	4.991	6.93e-07	***
LW	-928.221	884.626	-1.049	0.2943	

```
---
```

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
Residual standard error: 5979 on 1166 degrees of freedom
```

```
Multiple R-squared:  0.8947, Adjusted R-squared:  0.8934
```

```
F-statistic: 660.5 on 15 and 1166 DF, p-value: < 2.2e-16
```

```
summary(lm3)
```

```
Call:
```

```
lm(formula = W ~ A2 + A + L + S)
```

```
Residuals:
```

Min	1Q	Median	3Q	Max
-33827	-4297	328	4196	18190

```
Coefficients:
```

	Estimate	Std. Error	t value	Pr(> t )	
(Intercept)	-32099.552	1354.414	-23.700	< 2e-16	***
A2	3734.327	178.031	20.976	< 2e-16	***
A	2.948	3.599	0.819	0.41288	
LH1	1073.493	895.798	1.198	0.23102	
LH11	6635.125	4205.177	1.578	0.11487	
LH12	-4260.563	5917.463	-0.720	0.47167	
LH2	2526.408	931.194	2.713	0.00676	**
LH3	-1221.812	939.563	-1.300	0.19372	
LH5	5844.980	4203.384	1.391	0.16463	
LH7	6558.544	2459.178	2.667	0.00776	**
LH8	-289.109	1341.582	-0.215	0.82942	
LH9	3141.092	1831.794	1.715	0.08665	.
LHa	722.154	459.063	1.573	0.11597	
LHb	4149.570	593.406	6.993	4.53e-12	***
LK	5160.131	808.310	6.384	2.49e-10	***
LW	-925.029	873.376	-1.059	0.28975	
S2	-2279.890	407.965	-5.588	2.85e-08	***

```
---
```

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
Residual standard error: 5903 on 1165 degrees of freedom
```

```
Multiple R-squared:  0.8975, Adjusted R-squared:  0.896
```

```
F-statistic: 637.2 on 16 and 1165 DF, p-value: < 2.2e-16
```

```
> summary(lme1)
```

```
Linear mixed-effects model fit by REML
```

```
Data: wallaby_na
```

```
      AIC      BIC    logLik  
21162.07 21258.23 -10562.03
```

```
Random effects:
```

```
Formula: ~1 | An
```

```
(Intercept) Residual
```

```
StdDev:      1.759212 7650.424
```

```
Correlation Structure: AR(1)
```

```
Formula: ~1 | An
```

```
Parameter estimate(s):
```

```
Phi
```

```
0.9680672
```

```
Fixed effects: W ~ A + A2 + L
```

	Value	Std.Error	DF	t-value	p-value
(Intercept)	-8731.627	1948.987	1110	-4.480084	0.0000
A	46.919	4.434	1110	10.580602	0.0000
A2	796.187	191.146	1110	4.165324	0.0000
LH1	7357.876	2604.875	1110	2.824656	0.0048
LH11	563.143	7757.392	56	0.072594	0.9424
LH12	-4321.281	7817.226	56	-0.552790	0.5826
LH2	2009.634	4253.292	56	0.472489	0.6384
LH3	1126.338	3580.442	56	0.314581	0.7542
LH5	245.380	7757.020	56	0.031633	0.9749
LH7	-10.326	5557.635	56	-0.001858	0.9985
LH8	7815.879	6830.178	56	1.144316	0.2574
LH9	656.107	4607.732	56	0.142393	0.8873
LHa	1869.890	2156.169	1110	0.867228	0.3860
LHb	4847.464	3097.153	56	1.565136	0.1232
LK	6393.817	4637.430	56	1.378742	0.1735
LW	3134.887	4221.916	56	0.742527	0.4609

```
Correlation:
```

```
(Intr) A      A2      LH1      LH11     LH12     LH2      LH3      LH5      LH7
```

LH8									
A	0.425								
A2	-0.546	-0.938							
LH1	-0.522	-0.003	0.037						
LH11	-0.175	0.015	0.003	0.125					
LH12	-0.141	0.050	-0.044	0.120	0.041				
LH2	-0.280	0.045	-0.037	0.220	0.075	0.075			
LH3	-0.329	0.077	-0.061	0.263	0.090	0.091	0.163		
LH5	-0.173	0.018	-0.001	0.125	0.043	0.041	0.075	0.090	
LH7	-0.233	0.032	-0.012	0.173	0.059	0.058	0.105	0.126	0.059
LH8	-0.174	0.026	-0.022	0.137	0.047	0.047	0.085	0.102	0.047
LH9	-0.275	0.043	-0.022	0.208	0.071	0.070	0.127	0.152	0.071
LHa	-0.536	0.106	-0.097	0.734	0.147	0.149	0.270	0.323	0.147
LHb	-0.394	0.023	-0.020	0.301	0.102	0.101	0.185	0.221	0.102
LK	-0.262	-0.012	0.002	0.198	0.066	0.066	0.122	0.144	0.066
LW	-0.282	0.045	-0.037	0.222	0.076	0.076	0.137	0.165	0.076

```
0.079
```

```
A
```

```
A2
```

```
LH1
```

```
LH11
```

LH12  
 LH2  
 LH3  
 LH5  
 LH7  
 LH8  
 LH9  
 LHa 0.249  
 LHb 0.171 0.366  
 LK 0.112 0.241 0.169  
 LW 0.128 0.272 0.187 0.123

Standardized within-Group Residuals:

	Min	Q1	Med	Q3	Max
	-4.4935658	-0.7469041	-0.1961872	0.7675400	3.2870492

Number of Observations: 1182

Number of Groups: 68

21146.92 21248.13 -10553.46

Random effects:

Formula:  $\sim 1 \mid An$

(Intercept) Residual

StdDev: 2.000707 7695.118

Correlation Structure: AR(1)

Formula:  $\sim 1 \mid An$

Parameter estimate(s):

Phi

0.9684354

Fixed effects:  $W \sim A + A^2 + L + S$

	Value	Std. Error	DF	t-value	p-value
(Intercept)	-8423.534	2131.745	1109	-3.951473	0.0001
A	47.006	4.442	1109	10.581127	0.0000
A2	791.862	191.419	1109	4.136810	0.0000
LH1	8071.509	3255.166	1109	2.479600	0.0133
LH11	279.102	7844.902	56	0.035578	0.9717
LH12	-3889.787	7953.152	56	-0.489087	0.6267
LH2	2438.322	4443.857	56	0.548695	0.5854
LH3	849.336	3691.047	56	0.230107	0.8188
LH5	-38.065	7844.444	56	-0.004853	0.9961
LH7	414.209	5715.438	56	0.072472	0.9425
LH8	7558.445	6926.258	56	1.091274	0.2798
LH9	375.787	4704.630	56	0.079876	0.9366
LHa	1937.508	2178.115	1109	0.889534	0.3739
LHb	4766.190	3128.354	56	1.523546	0.1332
LK	6819.767	4818.759	56	1.415254	0.1625
LW	3119.330	4252.819	56	0.733474	0.4663
S2	-706.338	1982.986	1109	-0.356199	0.7218

Correlation:

(Intr)	A	A2	LH1	LH11	LH12	LH2	LH3	LH5	LH7
--------	---	----	-----	------	------	-----	-----	-----	-----

[illegible]

A

A2  
 LH1  
 LH11  
 LH12  
 LH2  
 LH3  
 LH5  
 LH7  
 LH8  
 LH9  
 LHa 0.232  
 LHb 0.181 0.358  
 LK 0.065 0.252 0.145  
 LW 0.129 0.269 0.188 0.114  
 S2 0.170 -0.078 0.073 -0.243 0.020

Standardized within-Group Residuals:

	Min	Q1	Med	Q3	Max
	-4.4146665	-0.7368546	-0.1921411	0.7751787	3.2426531

Number of Observations: 1182

Number of Groups: 68

```
> summary(lm1_PC)
```

```
Call:
```

```
lm(formula = W ~ H_PC1 + A + L)
```

```
Residuals:
```

Min	1Q	Median	3Q	Max
-35460	-4306	247	4010	18476

```
Coefficients:
```

	Estimate	Std. Error	t value	Pr(> t )	
(Intercept)	2623.886	533.243	4.921	9.87e-07	***
H_PC1	2938.514	117.930	24.917	< 2e-16	***
A	49.719	1.321	37.636	< 2e-16	***
LH1	-687.106	827.479	-0.830	0.4065	
LH11	6221.572	4003.593	1.554	0.1205	
LH12	-6554.759	5641.749	-1.162	0.2455	
LH2	98.774	864.694	0.114	0.9091	
LH3	-442.861	879.054	-0.504	0.6145	
LH5	5519.529	4002.612	1.379	0.1682	
LH7	3821.746	2329.185	1.641	0.1011	
LH8	-25.887	1268.878	-0.020	0.9837	
LH9	3101.082	1735.741	1.787	0.0743	.
LHa	-233.881	435.657	-0.537	0.5915	
LHb	3610.418	559.604	6.452	1.62e-10	***
LK	3072.321	744.617	4.126	3.95e-05	***
LW	-766.068	832.447	-0.920	0.3576	

```
---
```

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
Residual standard error: 5632 on 1166 degrees of freedom
```

```
Multiple R-squared:  0.9066, Adjusted R-squared:  0.9054
```

```
F-statistic: 754.5 on 15 and 1166 DF, p-value: < 2.2e-16
```

```
> summary(lm2_PC)
```

```
Call:
```

```
lm(formula = W ~ H_PC1 + A2 + A + L)
```

```
Residuals:
```

Min	1Q	Median	3Q	Max
-37929	-4025	546	3924	18494

```
Coefficients:
```

	Estimate	Std. Error	t value	Pr(> t )	
(Intercept)	26751.425	4619.205	5.791	8.97e-09	***
H_PC1	4662.835	348.075	13.396	< 2e-16	***
A2	-2632.682	500.731	-5.258	1.73e-07	***
A	85.980	7.019	12.249	< 2e-16	***
LH1	-927.691	819.463	-1.132	0.257837	
LH11	4686.064	3969.380	1.181	0.238021	
LH12	-6908.933	5578.783	-1.238	0.215806	
LH2	-495.551	862.422	-0.575	0.565670	
LH3	-420.409	869.190	-0.484	0.628704	
LH5	4096.733	3966.893	1.033	0.301944	
LH7	2454.769	2317.651	1.059	0.289745	
LH8	-385.692	1256.490	-0.307	0.758929	
LH9	2095.730	1726.863	1.214	0.225144	
LHa	-414.717	432.134	-0.960	0.337408	
LHb	3005.631	565.148	5.318	1.25e-07	***
LK	2720.274	739.292	3.680	0.000244	***
LW	-524.432	824.378	-0.636	0.524801	

```
---
```

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
Residual standard error: 5568 on 1165 degrees of freedom
```

```
Multiple R-squared:  0.9088, Adjusted R-squared:  0.9075
```

```
F-statistic: 725.2 on 16 and 1165 DF, p-value: < 2.2e-16
```



```
> summary(lm3_PC)
```

```
Call:
```

```
lm(formula = W ~ H_PC1 + A2 + A + L + S)
```

```
Residuals:
```

Min	1Q	Median	3Q	Max
-36822	-4085	678	3866	18115

```
Coefficients:
```

	Estimate	Std. Error	t value	Pr(> t )	
(Intercept)	25356.806	4585.735	5.529	3.96e-08	***
H_PC1	4513.767	346.260	13.036	< 2e-16	***
A2	-2393.067	498.621	-4.799	1.80e-06	***
A	82.776	6.987	11.848	< 2e-16	***
LH1	110.580	840.409	0.132	0.895	
LH11	4049.875	3934.891	1.029	0.304	
LH12	-5865.458	5531.455	-1.060	0.289	
LH2	570.997	883.068	0.647	0.518	
LH3	-1240.550	878.057	-1.413	0.158	
LH5	3448.369	3932.515	0.877	0.381	
LH7	3624.299	2309.188	1.570	0.117	
LH8	-1168.220	1255.569	-0.930	0.352	
LH9	1397.788	1717.094	0.814	0.416	
LHa	-89.427	433.505	-0.206	0.837	
LHb	2549.640	567.979	4.489	7.87e-06	***
LK	3745.067	763.155	4.907	1.05e-06	***
LW	-534.777	816.751	-0.655	0.513	
S2	-1830.637	382.813	-4.782	1.96e-06	***

```
---
```

```
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
Residual standard error: 5517 on 1164 degrees of freedom
```

```
Multiple R-squared:  0.9105, Adjusted R-squared:  0.9092
```

```
F-statistic: 696.7 on 17 and 1164 DF, p-value: < 2.2e-16
```

21107.99 21209.2 -10533.99

Random effects:

Formula:  $\sim 1 \mid An$

(Intercept) Residual

StdDev: 2.37582 7439.118

Correlation Structure: AR(1)

Formula:  $\sim 1 \mid An$

Parameter estimate(s):

Phi

0.967386

Fixed effects:  $W \sim H\_PC1 + A + A2 + L$

	value	Std.Error	DF	t-value	p-value
(Intercept)	9955.540	3399.657	1109	2.928396	0.0035
H_PC1	1658.545	250.066	1109	6.632436	0.0000
A	71.939	5.762	1109	12.485077	0.0000
A2	-1196.129	354.554	1109	-3.373617	0.0008
LH1	5688.070	2547.516	1109	2.232791	0.0258
LH11	539.731	7541.227	56	0.071571	0.9432
LH12	-4492.099	7600.658	56	-0.591014	0.5569
LH2	1934.484	4126.695	56	0.468773	0.6411
LH3	1013.678	3476.321	56	0.291595	0.7717
LH5	251.570	7540.854	56	0.033361	0.9735
LH7	-332.483	5401.661	56	-0.061552	0.9511
LH8	7509.119	6624.097	56	1.133607	0.2618
LH9	202.771	4477.971	56	0.045282	0.9640
LHa	2127.947	2092.279	1109	1.017047	0.3094
LHb	4580.843	3003.351	56	1.525244	0.1328
LK	6371.617	4492.912	56	1.418148	0.1617
LW	3501.863	4096.154	56	0.854915	0.3962

Correlation:

	(Intr)	H_PC1	A	A2	LH1	LH11	LH12	LH2	LH3	LH5
H_PC1	0.829									
A	0.725	0.656								
A2	-0.866	-0.848	-0.931							
LH1	-0.368	-0.096	-0.065	0.101						
LH11	-0.097	0.000	0.011	0.002	0.124					
LH12	-0.081	-0.003	0.036	-0.021	0.119	0.041				
LH2	-0.157	-0.002	0.033	-0.018	0.219	0.075	0.075			
LH3	-0.186	-0.004	0.056	-0.029	0.261	0.090	0.091	0.163		
LH5	-0.096	0.000	0.014	0.000	0.123	0.043	0.041	0.075	0.090	
LH7	-0.137	-0.009	0.018	0.001	0.172	0.059	0.058	0.105	0.126	0.05
LH8	-0.102	-0.006	0.016	-0.007	0.136	0.046	0.047	0.085	0.101	0.04
LH9	-0.165	-0.015	0.023	0.001	0.207	0.071	0.070	0.126	0.152	0.07
LHa	-0.281	0.020	0.094	-0.068	0.725	0.147	0.149	0.269	0.322	0.14
LHb	-0.230	-0.013	0.009	0.001	0.300	0.101	0.101	0.185	0.221	0.10
LK	-0.146	0.000	-0.009	0.001	0.197	0.066	0.066	0.122	0.144	0.06
LW	-0.144	0.015	0.044	-0.032	0.219	0.075	0.076	0.137	0.164	0.07
H_PC1	LH7	LH8	LH9	LHa	LHb	LK				

A							
A2							
LH1							
LH11							
LH12							
LH2							
LH3							
LH5							
LH7							
LH8	0.065						
LH9	0.099	0.079					
LHa	0.206	0.167	0.248				
LHb	0.142	0.115	0.171	0.365			
LK	0.092	0.076	0.111	0.241	0.169		
LW	0.105	0.085	0.127	0.272	0.186	0.123	

Standardized within-Group Residuals:

	Min	Q1	Med	Q3	Max
	-4.642937	-0.667319	-0.193920	0.709247	3.327137

Number of Observations: 1182

Number of Groups: 68

```
> summary(lme2_PC)
```

```
Linear mixed-effects model fit by REML
```

```
Data: wallaby_na
```

```
      AIC      BIC    logLik  
21092.88 21199.13 -10525.44
```

```
Random effects:
```

```
Formula: ~1 | An
```

```
(Intercept) Residual
```

```
StdDev:    36.52957 7482.269
```

```
Correlation Structure: AR(1)
```

```
Formula: ~1 | An
```

```
Parameter estimate(s):
```

```
Phi
```

```
0.9677602
```

```
Fixed effects: W ~ H_PC1 + A + A2 + L + S
```

	Value	Std.Error	DF	t-value	p-value
(Intercept)	10282.244	3504.346	1108	2.934140	0.0034
H_PC1	1658.086	250.089	1108	6.629984	0.0000
A	72.029	5.769	1108	12.485557	0.0000
A2	-1200.373	354.768	1108	-3.383549	0.0007
LH1	6450.106	3171.598	1108	2.033709	0.0422
LH11	234.509	7625.976	56	0.030751	0.9756
LH12	-4026.850	7732.140	56	-0.520794	0.6046
LH2	2396.833	4311.366	56	0.555933	0.5805
LH3	715.509	3583.607	56	0.199662	0.8425
LH5	-53.002	7625.518	56	-0.006951	0.9945
LH7	125.018	5554.311	56	0.022508	0.9821
LH8	7230.287	6717.310	56	1.076366	0.2864
LH9	-98.646	4571.908	56	-0.021577	0.9829
LHa	2202.233	2113.623	1108	1.041923	0.2977
LHb	4493.989	3033.729	56	1.481342	0.1441
LK	6831.046	4668.793	56	1.463129	0.1490
LW	3484.987	4126.075	56	0.844625	0.4019
S2	-760.293	1923.655	1108	-0.395233	0.6927

```
Correlation:
```

(Intr)	H_PC1	A	A2	LH1	LH11	LH12	LH2	LH3	LH5
H_PC1	0.806								
A	0.711	0.655							
A2	-0.846	-0.848	-0.931						
LH1	-0.150	-0.075	-0.032	0.067					
LH11	-0.119	-0.001	0.008	0.004	0.039				
LH12	-0.043	-0.002	0.040	-0.024	0.183	0.025			
LH2	-0.085	-0.001	0.041	-0.024	0.328	0.045	0.112		
LH3	-0.229	-0.005	0.047	-0.023	0.079	0.109	0.055	0.096	
LH5	-0.117	0.000	0.010	0.002	0.039	0.053	0.025	0.045	0.110
LH7	-0.082	-0.008	0.025	-0.004	0.258	0.037	0.087	0.154	0.076
LH8	-0.126	-0.006	0.012	-0.004	0.042	0.058	0.029	0.050	0.123
LH9	-0.199	-0.015	0.017	0.005	0.065	0.087	0.043	0.075	0.183
LHa	-0.256	0.020	0.096	-0.070	0.632	0.138	0.159	0.280	0.297
LHb	-0.242	-0.013	0.006	0.002	0.199	0.108	0.089	0.159	0.231
LK	-0.081	0.001	0.000	-0.005	0.298	0.039	0.100	0.179	0.084
LW	-0.146	0.014	0.043	-0.032	0.165	0.077	0.072	0.127	0.165

S2	-0.237	-0.004	-0.035	0.024	-0.590	0.102	-0.150	-0.266	0.215	0.10
2										

	LH7	LH8	LH9	LHa	LHb	LK	LW
--	-----	-----	-----	-----	-----	----	----

H\_PC1

A

A2

LH1

LH11

LH12

LH2

LH3

LH5

LH7

LH8	0.039
-----	-------

LH9	0.060	0.097
-----	-------	-------

LHa	0.217	0.157	0.231
-----	-------	-------	-------

LHb	0.123	0.123	0.181	0.358
-----	-------	-------	-------	-------

LK	0.138	0.045	0.065	0.252	0.145
----	-------	-------	-------	-------	-------

LW	0.099	0.087	0.129	0.269	0.187	0.114
----	-------	-------	-------	-------	-------	-------

S2	-0.207	0.116	0.170	-0.079	0.074	-0.244	0.020
----	--------	-------	-------	--------	-------	--------	-------

Standardized within-Group Residuals:

	Min	Q1	Med	Q3	Max
	-4.5577260	-0.6839594	-0.1932880	0.7431471	3.2799308

Number of Observations: 1182

Number of Groups: 68