# Sudoku Solver

### Usage

Requires python 3.6+

```
python3 sudoku/solver.py sudoku.txt
more log.info
```

Log output: log.info

### **Optional Docker Usage**

```
docker build -t sudoku:1.0 .
docker run -it sudoku:1.0 bash
```

And once in the container:

```
python3 sudoku/solver.py sudoku.txt
more log.info
```

#### **Tests**

Requires pytest

```
pytest -s -v tests/tester.py
```

# Approaches

In the large space of potential approaches for Sudoku solvers, I started with the simplest, non-exhaustive approach, and measured the performance. Then, by applying two Sudoku-specific heuristics to this approach, I was able to reach a satisfactory level of performance.

Brute-force wasn't an option as a first approach since the complexity is  $0 \, (n^m)$ , where n is the number of possible values per cell (9) and m is the number of unsolved cells.

# 1. Depth first search with backtracking

Note: code not included

### Algorithm:

- 1. Find the first unsolved cell (in raster-scan order)
  - a. If we cannot find an unsolved cell, the board is solved (base case)
- 2. For each possible candidate (1-9)
  - a. If candidate is valid (does not break Sudoku rules), assign that cell with candidate, and return (recurse) to step 1.
- 3. If no candidates in step 2) are valid, undo the candidate assignment, backtrack up the tree and try a new candidate for the previous node

#### Pseudocode:

```
func solve(board):
    pos = find_unsolved_cell(board)
    if no pos exists:
        return True

for each candidate:
        if is_valid(board, pos, candidate):
            board[pos] = candidate
            if solve(board):
                return True
            backtrack(board[pos])
    return False
```

#### **Results**

Total time for the 50 Sudoku puzzles: 25s

Hardware: 2015 Intel Core i7

# 2. DFS with backtracking + heuristics

DFS can be interpreted as traversal through an N-ary tree. In our case, the first unsolved cell is the root node, and each candidate can be represented as a child node.

#### **Heuristic:**

In approach 1), we made two arbitrary decisions:

- 1. Evaluate 1-9 as candidates for each unsolved cell
- 2. Solve cells in raster-scan order

We instead, can

- 1. Eliminate candidates of unknown cells based on the initial known cell values
- 2. Solve cells in order of increasing # of candidates

By eliminating candidates and choosing the cells with the least # of candidates to solve first, we significantly constrain the search space.

For example, if we start by choosing an unsolved cell with 6 candidates, there are 6 child nodes for DFS to visit, whereas if we choose an unsolved cell with 2 candidates, there are only 2 different DFS paths available.

This is known as the branching factor of the tree, and a reduction in the branching factor can reduce the real-world execution time almost exponentially.

### **Algorithm:**

0. For each unsolved cell, compute the set of candidates and store this in a map. A cell's existence in this map indicates that it is still unsolved.

Then, the algorithm is the same as in Approach 1 except for a couple details (bolded):

- 1. Find the first unsolved cell (with the least # of candidates, precomputed in step 0.)
  - a. If we cannot find an unsolved cell, the board is solved
- 2. For each candidate (from the precomputed map)
  - a. If candidate is valid (does not cause peers to have 0 candidates\*), assign that cell with that value, and return (recurse) to step 1.
- 3. If no candidates in step 3) are valid, backtrack\*\* up the tree and try a new candidate for the previous node
- \* This is the backtracking trigger. As we assign a candidate to a cell, we can remove that candidate from the cell's peers. If this removal causes the peer to not have any candidates left, we've made an error and must backtrack.

#### Pseudocode:

The overall structure of the algorithm remains the same. <- indicates modifications to how this method is implemented compared to approach 1)

#### Results

Total time for the 50 Sudoku puzzles: 0.351s

Hardware: 2015 Intel Core i7

<sup>\*\*</sup> We'll need to keep track of the deleted candidates for backtracking purposes

# **Assumptions**

• input file format of sudoku.txt