Brain tissue temperature dynamics during functional activity and possibilities for Imaging

by

GREGGORY H. ROTHMEIER

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Dedication

 ${\bf Mama.}$

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Brain tissue temperature dynamics during functional activity and possibilities for Imaging

A thesis presented in Partial Fulfilment of Requirements for the Degree of Master of Science in the College of Arts and Sciences Georgia State University 2012 by Greggory Rothmeier Committee:

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Chapter 1

Introduction

Chapter 2

Calculating Temperature Changes using the fMRI BOLD Response

2.1 Background

2.1.1 Generation of the Blood Oxygen Level Dependent (BOLD) Response

Since its invention in the 1950's [1] and later development in the 1970's [2], Magnetic Resonance Imaging (MRI) has allowed physicians and scientists a detailed view within the human body.

2.1.2 Previously Proposed Temperature Models

Current efforts to model temperature changes be can categorized into two classes. The first class approaches the problem by considering a single voxel deep within the brain (single-voxel approach) while the second approach considers the brain and head as an entire system (multi-voxel approach). Each of these methods has their own pros and cons which will be discussed below.

Single-Voxel Approach

A single-voxel model of temperature was first proposed by SOMEONE, but has been refined over the past HOWLONG years CITEABUNCH to include more terms. Although different approaches consider different contributions to the temperature change, they all narrow the problem down to a single voxel which is usually 2mm x 2mm. By simplifying the model, the heat equation can be simplified and the calculation is much easier to undertake. However, since the brain is not homogenous, the values used for parameters

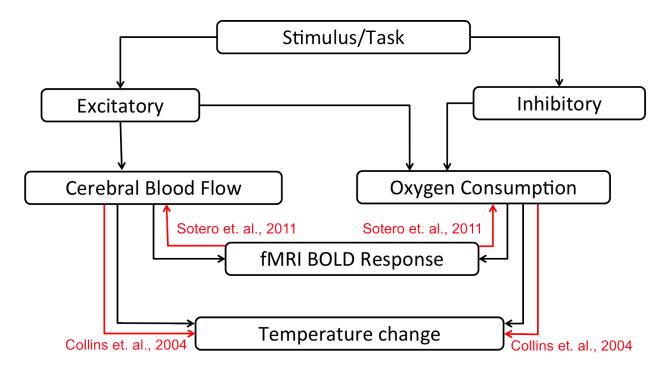


Figure 2.1: Generation of the fMRI BOLD response from changes in neuronal activity. Black arrows indicate a causal relationship while red arrows indicate existing models for the relationship. Modified from Sotero and Trujillo-Barreto [3]

such as heat production and thermal conductivity are taken from an average of the tissues. As a result, this reduces the possible accuracy of such a model when applied to a subject. The most recently published iteration of a single-voxel model was published by Sotero and Iturria-Medina [4]. The basis of this model is a modification of the Penne's Bioheat Equation [5, 4].

$$C_{t} \frac{dT(t)}{dt} = (\Delta H^{\circ} - \Delta H_{b})CMRO_{2} \mid_{0} m(t) - \rho_{b}C_{b}CBF \mid_{0} f(t)(T(t) - T_{a}) - \frac{C_{t}}{\tau}(T(t) - T_{0})$$
 (2.1)

where BLA BLA. One advantage of using eq. (2.1) is that the resting state temperature can be analytically determined by substituting $\frac{dT(t)}{dt} = 0$ [4].

$$T_{0} = T_{a} + \frac{(\Delta H \mid^{\circ} - \Delta H_{b})CMRO_{2}\mid_{0}}{\rho_{B}C_{B}CBF\mid_{0}}$$
(2.2)

If the values provided in table 2.1 are substitued into eq. (2.2), a resting temperature of 37.3057°C is found. Since the resting temperature is always greater than the arterial blood temperature, it limits the ability of the model to account for all experimental results.

While eq. (2.1) is appears complicated, conceptually the equation can be easily understood.

change in temperature = heat generated by metabolism - heat lost to convection - heat lost to conduction (2.3)

The system is a balance between heat generation (metabolism) and heat transfer (conduction and convection). The direction of heat transfer by convection is determined by the difference between the voxel temperature and the arterial blood temperature $(T(t) - T_a)$. Similarly, the direction of heat transfer by conduction is determined by the difference between the voxel temperature and the temperature of the surrounding tissue $(T(t) - T_0)$. Since T_a is less than T(0), an increase in blood flow (f(t)) will remove heat from the voxel thereby decreasing the temperature. Conversely, an increase in metabolism (m(t)) without a corresponding change in blood flow, will result in tissue warming.

$$f(t) = \frac{\alpha + \beta c}{b\beta} W(y(t)) \tag{2.4}$$

$$m(t) = af^{c+1}(t)e^{-bf(t)}$$
 (2.5)

$$y(t) = -\frac{b\beta}{\alpha + \beta c} \left[\frac{\left(A - \frac{S(t)}{S_0} - 1\right)}{Aa^{\beta}} \right]^{\left(\frac{1}{\alpha + \beta c}\right)}$$
(2.6)

Multi-Voxel Approach

Table 2.1: Parameters used to solve the single-voxel Penne's Bioheat Equation. (modified from Sotero and Iturria-Medina [4])

Parameter	Meaning	Value
$\overline{\mathrm{T}_a}$	Arterial blood temperature	37°C
C_{tissue}	Tissue Heat Capacity	$3.664 \; J/(gK)$
ΔH°	Enthalpy released by oxidation of glucose	$4.710^5 \ { m J}$
ΔH_b	Enthalpy used to release O ₂ from hemoglobin	2.810^4 J
$CMRO_2 \mid_0$	Cerebral metabolic rate of O_2 consumption at rest	$0.026310^{-6} \text{ mol/(gs)}$
$CBF _0$	Cerebral blood flow at rest	$0.0093 \text{ cm}^3/(\text{gs})$
$ ho_b$	Blood density	$1.05 \mathrm{g/cm^3}$
C_B	Blood heat capacity	3.894 J/(gK)
au	Time constant for conductive heat loss from the ROI to the surrounding tissue	190.52 s
a, b, c	Parameters of the gamma function fitted from E(f) vs. f	0.4492,0.2216,-0.9872
A	Maximum BOLD signal change	0.22
α	Steady state flow-volume relation	0.4
eta	Field-strength dependent parameter	1.5
Variable	Meaning	
m(t)	CMRO ₂ normalized to baseline	
f(t)	CBF normalized to baseline	
T(t)	Temperature	
W(t)	Lambert W Function	
$frac\Delta S(t)S_0$	Change in BOLD signal normalized to rest	

2.2 Modeling the BOLD Response

2.3 Modeling Temperature

2.3.1 The Approach

How the temperature is calculated

$$\rho c \frac{dT}{dt} = k \nabla^2 T - \rho_{blood} f(t) w c_{blood} (T - T_{blood}) + m(t) Q_m$$
(2.7)

Calculating the equilibrium temperature

Calculating Metabolism and Blood Flow Changes

Calculating the change in temperature in the active brain

2.3.2 Results

Using Theoretical BOLD Data

Using Experimental BOLD Data

Chapter 3

Detector Applications to measuring the active brain

3.1 Functional Near-Infrared fNIR Imaging

$$I = I_0 e^{-\alpha x} \tag{3.1}$$

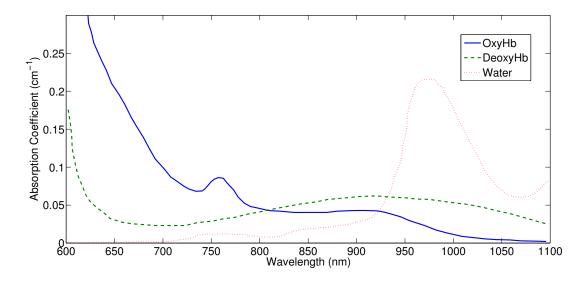


Figure 3.1: Absorption spectra of water, Hb and Dhb. From Cope [6] and HB stuff from Horecker [7]

3.2 Temperature Measurements

From the Beer-Lambert law eq. (3.1), the penetration depth, δ_p can be expressed as

$$\delta = \frac{1}{\alpha} \tag{3.2}$$

where α is the absorption coefficient. At body temperature (37°) the peak wavelength in the blackbody spectrum is approximately BLA. For water at this wavelength, α is approximately HUGE, so δ is VERY SMALL.

Chapter 4

Conclusion

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Appendix A

Code

The following sections include the code used. It was written for Matlab 2011(b) and requires SPM8 to run. Additionally, it is recommended that you have at least 4 GB of RAM in order to work with the large datasets that are produced. For information about how to visualize the data produced, see appendix B. All of the code is available through the temptools github page (https://github.com/greggroth/tempcalc)

A.1 Creating the Head Matrix

Before any calculations can be done, a matrix containing tissue-specific parameters must be created. First, a T1 contrast image should be segmented using SPM8 (http://www.fil.ion.ucl.ac.uk/spm/software/spm8/). For ease of consistency, the one provided by SPM8 in ./canonical/ is best to use. Using SPM's "New Segmentation" algorithm will segment the image into five different tissue types (gray matter, white matter, cerebral spinal fluid, soft tissue and bone). Once this is complete, run BulkImportNII() within this directory and it will return a matrix that has been populated with the tissue-specific parameters required for accurate temperature calculations. The functions fillAir() (A.1.2) and fillholes() (A.1.3) are functions required by BulkImportNII(). More information about this procedure is in section 2.3.1.

A.1.1 BulkImportNII()

```
function [ total ] = BulkImportNII(varargin)

% BulkImportNII Import NII files from a directory

% Must be run within the directory containing the files

%

% Output: head data as single with variables stored in the 4th dimension.
```

```
6
   %
7
   %
       Author: Greggory Rothmeier (greggroth@gmail.com)
8
   %
       Georgia State University
       Created: 5/31/11
9
10
   statusbar = waitbar(0,'Initializing');
11
12
   if size(varargin) == 1
13
       oldFolder = cd(varargin{1});
14
15
   end
16
17
18
   % ===========
   % = Tissue Parameters =
   % ==========
20
21
   % Each tissue type is assigned an integer index (i.e. gray matter -> 11) such that
22
   % tissue-specific parameters can be found by looking at that element within the
   % corresponding storage matrix (i.e. QmSTORE(11) -> gray matter Qm)
23
24
   % Parameters taken from Colins, 2004
25
26
   tisorder = [11 15 5 13 3]; % Using: [GM WM CSF Muscle Bone]
27
28
29
   QmSTORE = [0 0 26.1 11600 0 26.1 697 0 0 302 15575 0 697 1100 5192];
30
   cSTORE = [1006 4600 2110 3640 3800 1300 3720 3000 4200 2300 3680 3500 3720 3150
      3600];
   rhoSTORE = [1.3 1057 1080 1035.5 1007 1850 1126 1076 1009 916 1035.5 1151 1041
      1100 1027.4];
   kSTORE = [0.026 0.51 0.65 0.534 0.5 0.65 0.527 0.4 0.594 0.25 0.565 0.4975 0.4975
32
      .342 .503];
   wSTORE = [0 1000 3 45.2 0 1.35 40 0 0 2.8 67.1 3.8 3.8 12 23.7];
33
34
   % ==========
35
   % = Import the pre-segmented T1 files =
36
37
```

```
38
   % The T1 contrast image sould be segmented using SPM8.
39
        This loop needs to complete before the next one can begin
40
   for i = 1:5
        eval(strcat('dat',num2str(i),' = loadNII(''rc',num2str(i),'single_subj_T1.nii'
41
           ');')) % Import all of the datat and store as 'cdat1','cdat2', etc.
        eval(strcat('out',num2str(i),' = zeros(cat(2,size(dat',num2str(i),'),7));'))
42
            % Preallocate
    end
43
44
45
   % = Populate the head matrix =
46
   % ===============
47
        For each data file, it fills in the data from the data storage arrays
48
        for that particular type of tissue. It picks which ever tissue is the
49
   %
        most likely candidate for that voxel based on the segmented data
50
51
        PROBLEM: It returns 0 (later filled with air) if there is equal
52
53
   %
        probability of a voxel being two or more different types of tissue.
        SOLVED BY fillholes()
54
55
56
57
   for i = 1:5
        % Preallocate
58
        holder = zeros(cat(2, size(dat1),7), 'single');
59
60
        mask = zeros(size(dat1));
        final = zeros(size(holder), 'single');
61
62
        % Create a mask that indicates whether it is the mostly likely tissue type
        guide = [1 2 3 4 5 1 2 3 4 5]; % This guides it through the data correctly
64
        eval(strcat('mask = (dat',num2str(i),'>dat',num2str(guide(i+1)),') & (dat',
65
          num2str(i), '>dat', num2str(guide(i+2)),') & (dat', num2str(i), '>dat', num2str(
          guide(i+3)),') & (dat',num2str(i),'>dat',num2str(guide(i+4)),') & (dat',
          num2str(i), '~=0);'))
        holder(:,:,:,1) = mask;
66
                                                      % move structure data to new
          matrix
```

```
67
       a = find(holder(:,:,:,1) == 1);
                                                 % get indicies of tissues
68
       [x y z t] = ind2sub(size(holder),a);
                                                % gets coordinates from index
       for j = 1:length(a)
                                                % go to each tissue point and
70
          store the info
           final(x(j),y(j),z(j),:) = [tisorder(i) 0 QmSTORE(tisorder(i)) cSTORE(
71
             tisorder(i)) rhoSTORE(tisorder(i)) kSTORE(tisorder(i)) wSTORE(tisorder(
             i))];
       end
72
73
       eval(strcat('out',num2str(i),'= final;')) % Saves the result to a unique
74
          output variable (out1, out2, etc)
75
       clearvars a x y z t holder final;
       waitbar(i/6,statusbar,sprintf(['File ',num2str(i),' Import Compete']));
   end
78
   % The filleAir() function checks for any voxels which were not assigned a
80
   % tissue type and fills them in with air
81
   82
      model
   % The fillholes() function corrects for a voxel having two equally-probable tissue
83
      types
   total = single(fillholes(dat1,dat2,dat3,dat4,dat5,almostthere));
84
85
   waitbar(1, statusbar, 'Saving Data')
86
   cd(oldFolder);
87
   close(statusbar);
89
90
   end
  A.1.2 fillAir()
  function [ output ] = fillAir( tissue )
   % fillAir() fills gaps in data with air
```

Once you import all of the data using loadNII(), run it thought this to

2

3

```
4
        fill in the remaining spaces with air.
5
   airdata = [1 0 0 1006 1.3 0.026 0];
7
   % Picks out air spots
8
   a = find(tissue(:,:,:,1) == 0);
9
    [x y z t] = ind2sub(size(tissue),a);
10
11
   for i = 1:length(a)
12
        tissue(x(i),y(i),z(i),:) = airdata;
13
    end
14
15
16
   output = tissue;
17
18
   end
```

A.1.3 fillholes()

```
function [ out_head ] = fillholes( in1,in2,in3,in4,in5,headin)
1
   % fillholes() checks for misassigned voxels
2
3
   % Solves an issue where a voxel with two equally probable tissue
4
   \% types resulted in being assigned as air. This checks for air
5
   % voxels that are surrounded by tissue and decides a tissue it
6
   % it would be best suited as
7
8
9
   head = squeeze(headin(:,:,:,1)); % I only need the tissue indices so this makes
      things easier down the line
10
   %% Data Storage
11
   QmSTORE = [0 0 26.1 11600 0 26.1 697 0 0 302 15575 0 697 1100 5192];
12
    cSTORE = [1006 4600 2110 3640 3800 1300 3720 3000 4200 2300 3680 3500 3720 3150
13
      3600];
   rhoSTORE = [1.3 1057 1080 1035.5 1007 1850 1126 1076 1009 916 1035.5 1151 1041
14
      1100 1027.4];
```

```
kSTORE = [0.026 0.51 0.65 0.534 0.5 0.65 0.527 0.4 0.594 0.25 0.565 0.4975 0.4975
             .342 .503];
       wSTORE = [0 1000 3 45.2 0 1.35 40 0 0 2.8 67.1 3.8 3.8 12 23.7];
16
17
              Get locations of holes
18
               Where two tissue types have the same probability
19
20
       idx1 = (in1==in2 | in1 == in3 | in1==in4 | in1==in5) & logical(in1);
21
       idx2 = (in1==in2 | in2 == in3 | in2==in4 | in2==in5) & logical(in2);
22
       idx3 = (in1==in3 | in2 == in3 | in3==in4 | in3==in5) & logical(in3);
23
       idx4 = (in1==in4 | in2 == in4 | in3==in4 | in4==in5) & logical(in4);
24
       idx5 = (in1==in5 | in2 == in5 | in3==in5 | in4==in5) & logical(in5);
25
       % This array will have a zero anywhere there were two or more common
26
       % elements between any of the five arrays.
27
       idx = idx1|idx2|idx3|idx4|idx5;
28
29
       [xmax ymax zmax] = size(in1)
30
31
       [x \ y \ z] = ind2sub(size(in1),find(idx)); % get x, y and z coordinates of the
             holes
32
       for i = 1:length(x) % go to each hole and do work
33
               34
                     &&(headin(x(i),y(i),z(i),1)==1) % keeps away from the edge and only looks
                       at voxels that were assigned air
35
                       [commonesttissue nouse secondbest] = mode([head(x(i)+1,y(i),z(i)))) head(x(i)+1,y(i),z(i))
                             (x_i)^{-1}, 
                             y(i),z(i)+1) head(x(i),y(i),z(i)-1));
                       if commonesttissue == 1 && length(secondbest{1})>=2 % if air and
36
                             something else are equally common, it'll choose air. This forces it to
                               pick the tissue if possible.
                               commonesttissue = secondbest{1}(2);
37
38
                       end
                       headin(x(i),y(i),z(i),:) = [commonesttissue 0 QmSTORE(commonesttissue)
39
                             cSTORE(commonesttissue) rhoSTORE(commonesttissue) kSTORE(
                             commonesttissue) wSTORE(commonesttissue)];
```

```
40 end
41 end
42 
43 out_head = headin;
44 
45 end
```

A.1.4 build_skin()

```
function [ head_out ] = build_skin( head_in )
   1
              %build_skin Summary of this function goes here
   2
   3
                               Detailed explanation goes here
   4
              if ndims(head_in) == 4
   5
   6
                              head_in = head_in(:,:,:,1);
               end
   8
               muscle_voxels = find(head_in==13);
   9
10
11
               for i=1:length(muscle_voxels)
                           [x y z] = ind2sub(size(head_in), muscle_voxels(i));
12
                          % if a muscle voxel borders any air voxels, it's set to skin
13
                          if (x^{-1}) & (x^{-1}) & (x^{-1}) & (x^{-1}) & (y^{-1}) & (y^{-1
14
                                     (head_in,3))
                                          if ((head_in(x+1,y,z)==1)||(head_in(x-1,y,z)==1)||(head_in(x,y+1,z)==1)||(
15
                                                     head_in(x,y-1,z)==1) | | (head_in(x,y,z+1)==1) | | (head_in(x,y,z-1)==1) |
                                                          head_in(x,y,z) = 14;
16
17
                                          end
                           end
               end
19
20
              head_out = repair_headdata(head_in);
21
22
23
               end
24
```

A.2 Loading the fMRI Data

The following code automates the procedure of processing and doing all the calculations on the dataset reported in Dhamala et al. [8]. It can be used to gain a better understanding of the procedure. For a conceptual explanation, see section 2.3.1.

```
1
          How to process preprocessed BOLD data to calculate temperature
2
3
   4
   % This Matlab script was used to automate the the process of using BOLD data
5
   \% stored in NIFTI (*.nii) format to calculate temperature changes. The
6
   % particulars of the code may be specific to this case, but the procedure
7
8
   % should be the same when doing these calculations on other datasets. All
   \% required functions are included as an attachment to my thesis and are
   % available on my github (https://github.com/greggroth/tempcalc)
10
11
12
   cd('/Users/Greggory/Documents/Data/fmri_rhythmic_tapping01/NIFTI')
13
   directories = dir('*01');
14
15
   %% Move coregistered files to new Directory
16
   for i = 1:length(directories)
17
       dir_name = directories(i).name;
18
       main_path = cd( [dir_name filesep dir_name '_NIFTI_1'] );
19
20
       mkdir 'Coregistered'
       movefile('r*.nii','Coregistered')
21
       main_path = cd( [dir_name filesep dir_name '_NIFTI_2'] );
       mkdir 'Coregistered'
       movefile('r*.nii','Coregistered')
24
       cd(main_path)
25
   end
26
27
   %% Calculate Rest State
28
   disp('Calculating Rest State')
29
   for i = 1:length(directories)
```

```
31
        dir_name = directories(i).name;
32
        avg_NII_rest([dir_name filesep dir_name '_NIFTI_1' filesep 'Coregistered']);
33
        avg_NII_rest([dir_name filesep dir_name '_NIFTI_2' filesep 'Coregistered']);
34
   end
35
36
   %% Normalize to Rest and Mask
37
   disp('Normalize to Rest and Mask')
38
   for i = 1:length(directories)
39
        dir_name = directories(i).name;
40
        avg_NII_normalize([dir_name filesep dir_name '_NIFTI_1' filesep 'Coregistered'
41
          ], fullfile(dir_name, [dir_name '_NIFTI_1'], 'Coregistered', 'RestState', '
          RestStateAvg.nii'), 'fullBrainMask.nii');
42
        avg_NII_normalize([dir_name filesep dir_name '_NIFTI_2' filesep 'Coregistered'
          ], fullfile(dir_name, [dir_name '_NIFTI_2'], 'Coregistered', 'RestState', '
          RestStateAvg.nii'), 'fullBrainMask.nii');
43
   end
44
45
   %% Calculate metabolism and blood flow change
46
   disp('Calculate metabolism and blood flow change')
47
   for i = 1:length(directories)
48
        dir_1 = [ directories(i).name filesep directories(i).name '_NIFTI_1' filesep
49
           'Coregistered' filesep 'Normalized_to_rest'];
50
        dir_2 = [ directories(i).name filesep directories(i).name '_NIFTI_2' filesep
           'Coregistered' filesep 'Normalized_to_rest'];
        BOLDtoMF(dir_1);
51
        BOLDtoMF(dir_2);
53
   end
54
55
       Calculate the change in temperature based on metabolism and blood flow
56
57
   % load('equil.mat'); % equillibriumT
58
   % load('tt_headdata.mat');  % headdata
59
```

```
mask = loadNII('fullBrainMask.nii');
61
   for i = 1:length(directories)
62
        disp([int2str(i) '-1 started'])
63
        tic
64
        % Part I
65
        actResult.dat = tempCalcDynMF(headdata, 37, 24, 720, 360, equillibriumT, ...
66
            fullfile(directories(i).name,[directories(i).name '_NIFTI_1'],'
67
               Coregistered', 'Normalized_to_rest', 'Output_18-Sep-2011', 'm.mat'),
            fullfile(directories(i).name,[directories(i).name '_NIFTI_1'],'
68
               Coregistered', 'Normalized_to_rest', 'Output_18-Sep-2011', 'f.mat'),
               . . .
            4, mask);
69
        % Store the parameters used for the calculations for reference in the future
        [c lmax] = max(actResult.dat(:));
72
        [likelymax x y z] = ind2sub(size(actResult.dat),lmax);
        actResult.likelymaxslice = round(likelymax/2);
73
        actResult.bloodT = 37;
74
        actResult.airT = 24;
75
        actResult.tmax = 360;
76
        actResult.stepf = 2;
77
        actResult.savestepf = 4;
78
        actResult.metabandflowdata = 'From Dataset';
79
80
        save(fullfile(directories(i).name,[directories(i).name '_NIFTI_1'],'
          Coregistered', 'Normalized_to_rest', 'Output_18-Sep-2011','tt_act_res.mat')
           , 'actResult');
        old = cd([directories(i).name,filesep,[directories(i).name '_NIFTI_1'],filesep
81
           ,'Coregistered', filesep,'Normalized_to_rest', filesep,'Output_18-Sep-2011'
          ]);
        writeT_to_nii(actResult, equillibriumT, exp_nii);
82
        cd(old)
83
        clear actResult
84
        % Part II
85
        disp([int2str(i) '-2 started'])
86
```

```
87
         actResult.dat = tempCalcDynMF(headdata, 37, 24, 720, 360, equillibriumT, ...
             fullfile(directories(i).name,[directories(i).name '_NIFTI_2'],'
               Coregistered', 'Normalized_to_rest', 'Output_18-Sep-2011', 'm.mat'),
             fullfile(directories(i).name,[directories(i).name '_NIFTI_2'],'
89
               Coregistered', 'Normalized_to_rest', 'Output_18-Sep-2011', 'f.mat'),
                . . .
             4, mask);
90
         [c lmax] = max(actResult.dat(:));
91
         [likelymax x y z] = ind2sub(size(actResult.dat),lmax);
92
         actResult.likelymaxslice = round(likelymax/2);
93
         actResult.bloodT = 37:
94
95
         actResult.airT = 24;
         actResult.tmax = 360;
96
         actResult.stepf = 2;
         actResult.savestepf = 4;
         actResult.metabandflowdata = 'From Dataset';
99
100
         save(fullfile(directories(i).name,[directories(i).name '_NIFTI_2'],'
           Coregistered', 'Normalized_to_rest', 'Output_18-Sep-2011','tt_act_res.mat')
           , 'actResult');
101
        old = cd([directories(i).name,filesep,[directories(i).name '_NIFTI_2'],filesep
           ,'Coregistered', filesep,'Normalized_to_rest', filesep,'Output_18-Sep-2011'
           ]);
102
        writeT_to_nii(actResult, equillibriumT, exp_nii);
103
        clear actResult
104
        disp([int2str(i) ' finished in ' num2str(toc)])
105
106
    end
```

A.2.1 avg_NII_normalize()

```
function [ ] = avg_NII_normalize( varargin )

VuntitleD6 Normalize to rest state

Detailed explanation goes here
```

```
%% Setup
5
6
    switch length(varargin)
7
        case 0
            fold_name = uigetdir('Directory Containing Data');
8
            if ~fold_name % Cancel Button
9
                 return
10
            end
11
12
            [rest_file rest_path rest_index] = uigetfile('*.nii', 'Resting State NIFTI
13
               File');
            switch rest_index
14
                case 0
15
16
                     return
                 case 1
17
                     rest_dat = load_nii(fullfile(rest_path,rest_file));
18
                     rest_dat = double(rest_dat.img);
19
20
                 otherwise
                     error('An error has occured loading the resting state data')
21
            end
22
23
            [mask_file mask_path mask_index] = uigetfile('*.nii', 'Mask');
24
            switch mask_index
25
                 case 0
26
                     return
27
28
                 case 1
                     mask_dat = load_nii(fullfile(mask_path, mask_file));
29
                     mask_dat = logical(mask_dat.img);
30
                     if max(size(mask_dat) ~= size(rest_dat))
                         error('The Mask and Resting State files must have the same
32
                            size')
                     end
33
                 otherwise
34
                     error('An error has occured loading the resting state data')
35
36
            end
        case 1
37
```

```
38
            fold_name = varargin{1};
39
            [rest_file rest_path rest_index] = uigetfile('*.nii', 'Resting State NIFTI
               File');
            switch rest_index
40
                case 0
41
42
                     return
                case 1
43
                     rest_dat = load_nii(fullfile(rest_path,rest_file));
44
                     rest_dat = double(rest_dat.img);
45
                otherwise
46
                     error('An error has occured loading the resting state data')
47
            end
48
        case 2
49
            fold_name = varargin{1};
50
            rest_dat = loadNII(varargin{2});
51
            [mask_file mask_path mask_index] = uigetfile('*.nii', 'Mask');
52
            switch mask_index
54
                case 0
                     return
55
                case 1
56
                     mask_dat = load_nii(fullfile(mask_path, mask_file));
57
                     mask_dat = logical(mask_dat.img);
58
                     if max(size(mask_dat) ~= size(rest_dat))
59
                         error('The Mask and Resting State files must have the same
60
                            size')
                     end
61
                otherwise
62
                     error ('An error has occured loading the resting state data')
64
            end
        case 3
65
            fold_name = varargin{1};
66
            rest_dat = loadNII(varargin{2});
67
            mask_dat = loadNII(varargin{3});
68
        otherwise
69
            return
70
```

```
71
    end
    % Go to the folder containing the files
73
    oldfold = cd(fold_name);
74
    file_list = dir('*.nii');
75
    file_count = length(file_list);
76
77
    % Make a directoy to save the normalized data to
78
    saveDir = 'Normalized_to_rest';
79
    if ~isdir(saveDir)
80
        mkdir(saveDir);
81
    end
82
83
    statusbar = waitbar(0,'Initializing');
84
85
    % for each file: load it, devide by the rest state and save it
86
87
    for i=1:file_count
88
        try
             waitbar(i/file_count, statusbar, [fold_name sprintf('%d%%', round((i/
89
               file_count) *100))]);
        catch err
90
             return
91
         end
92
        [file_path file_name file_ext] = fileparts(file_list(i).name);
93
94
        file_hold = load_nii(file_list(i).name);
        file_hold.img = double(file_hold.img)./rest_dat - 1;
95
        file_hold.img(~mask_dat) = 0;
                                                    % set everything outside the mask to
            0
        file_hold.img(isnan(file_hold.img)) = 0; % set all NaN's to 0
97
        file_hold.img(isinf(file_hold.img)) = 0; % set all inf's to 0
98
        file_hold.img(file_hold.img == -1) = 0; % correct these for voxels that are
99
           giving me problems
100
        file_hold.hdr.dime.datatype = 16;  % set the datatype to single
        file_hold.hdr.dime.bitpix = 16;
101
        save_nii(file_hold,fullfile(saveDir,[file_name '_rn' file_ext]))
102
```

```
103 end
104
105 close(statusbar)
106 cd(oldfold)
107
108 end
```

A.2.2 avg_NII_rest()

```
function [ ] = avg_NII_rest( varargin )
   %UNTITLED4 Summary of this function goes here
2
3
       Detailed explanation goes here
4
   %% Setup
5
   switch length(varargin)
       case 0
            fold_name = uigetdir;
            if ~fold_name % Cancel Button
9
                return
10
            end
11
        case 1
12
            fold_name = varargin{1};
13
        otherwise
14
   end
15
16
   \% Go to the folder containing the files
17
18
   oldfold = cd(fold_name);
   file_list = dir('*.nii');
19
20
   \% We're only interested in the rest period
21
   % (first and last 10 steps in this case)
22
   file_list = file_list([1:10 170:180]);
23
   file_count = length(file_list);
24
25
26
   % Cell array to store all of the datasets in.
   datHolder = cell(file_count,1);
```

```
28
29
    statusbar = waitbar(0, 'Initializing');
30
   for j=1:file_count
31
32
        try
            waitbar(j/file_count, statusbar, sprintf('%d%%', round((j/file_count)*100)));
33
        catch err
34
            return
35
        end
36
        fi = load_nii(file_list(j).name);
37
        datHolder{j} = fi.img;
38
    end
39
40
   %% Calculate the mean
41
   ymax = size(datHolder{1},2);
42
43
    zmax = size(datHolder{1},3);
44
    output = zeros(size(datHolder{1}));
45
   for i=1:ymax
46
        try
47
            waitbar(i/ymax, statusbar, sprintf('%d%%', round((i/ymax)*100)));
48
        catch err
49
            return
50
        end
51
52
        for k=1:zmax
            excStr = cell(length(datHolder),1);
53
            for l=1:length(datHolder)
54
                 excStr{1} = [',datHolder{' int2str(1) '}(:,' int2str(i) ',' int2str(k)
                     ')'''];
56
            end
            comb = eval(['cat(1' cell2mat(excStr')')']);
57
            output(:,i,k) = mean(comb);
58
        end
59
60
    end
61
```

```
close(statusbar)

fi.img = output;

mkdir('RestState')

save_nii(fi,fullfile('RestState','RestStateAvg.nii'));

cd(oldfold)

end
```

A.2.3 BOLDtoMF()

```
function [ ] = BOLDtoMF( varargin)
   %BOLDtoMF Calculate metabolism and blood from from BOLD reponse
3
       Input: Directory containing a series of *.nii files of the BOLD
4
5
   %
       response.
   %
6
       Output: Two new files will be created in a new subdirectory with a
7
   %
   %
       variable for each time step.
8
   %
9
10
   %
       Usage:
          BOLDtoMF
   %
11
   %
          BOLDtoMF(directory)
12
13
   %
   %
       If a directory is not provided, one will be requested.
14
   %
15
16
   %
       From Sotero, et. al. 2010
17
   %% Setup
18
19
   % Check input
20
   21
       case 0
22
23
          fold_name = uigetdir;
24
          if ~fold_name % Cancel Button
```

```
return
26
            end
        case 1
            fold_name = varargin{1};
28
        otherwise
29
            error('Input is not understood')
30
    end
31
32
   % Go to the folder containing the files
33
   oldfold = cd(fold_name);
34
   file_list = dir('*.nii');
35
   file_count = length(file_list);
36
37
   % Set up a directory for the outputs
38
   newFolder = ['Output_', datestr(clock,1)];
40
   mkdir(newFolder)
41
   % Make *.mat files to append the data to
42
   m0001 = 0; f0001 = 0;
43
   save(['./' newFolder '/m.mat'],'m0001');
44
   save(['./' newFolder '/f.mat'],'f0001');
45
46
47
48
49
   %% Norm
   s = loadNII(file_list(1).name);
50
   norm = ones(size(s));
51
   %% Calculate
53
54
   \% This will calculate the metabolism and blood flow. The output is
55
56
   % = 10^{-2} appended to 'm.mat' and 'f.mat' within a new folder created within the
   % directory containing the data.
57
58
59
   statusbar = waitbar(0,'Initializing');
```

```
60
61
   maxBOLD = 0.22;
   % {
   %% Find the max BOLD response
63
   for j=1:file_count
64
65
        try
            waitbar(j/file_count, statusbar, sprintf('Finding max change in BOLD: %d%%
66
              ',round((j/file_count)*100)));
        catch err
67
            return
68
        end
69
        s = loadNII(file_list(j).name); % Load up the file
70
71
        if max(s(:)) > maxBOLD
                                  % if the max value beats the current max,
          take it
            maxBOLD = max(s(:));
73
            disp([j maxBOLD])
74
        end
   end
75
   %}
76
   % Required Parameters
77
   p = [0.4 \ 1.5 \ 0.1870 \ 0.1572 \ -0.6041 \ maxBOLD]; % [alpha beta a b c A]
78
79
   %% Calc flow and metabolism (when BOLD = 1)
80
        I thought that the equations should work out so that an input of s = 1
81
82
   %
       returns f and m = 1, but until I sort that out here is a cheating work
        around. Make sure this is valid before publishing.
83
84
   s = 0;
85
   y = -((p(4)*p(2))/(p(1)+p(2)*p(5)))*((p(6)-s)/(p(6)*p(3)^p(2)))^(1/(p(1)+p(2)*p(5)))
      ));
   fNOACT = -((p(1)+p(2)*p(5))/(p(4)*p(2)))*lambertw(y);
87
   mNOACT = p(3)*fNOACT^(p(5)+1)*exp(-p(4)*fNOACT);
88
89
90
91
   %% Calc flow and metabolism
```

```
disp(fold_name)
93
    for j=1:file_count
94
         tic
         %avgtime = mean(timelist);
95
         %disp(avgtime)
96
         %timeremaining = (file_count-j)*avgtime;
97
98
         try
             waitbar(j/file_count, statusbar, sprintf('%d%%', round((j/file_count)*100)));
99
         catch err
100
             return
101
102
         end
         s = loadNII(file_list(j).name); % Load up the file
103
104
         s(isnan(s)) = 1; %what to do with NaNs and INFS? Not sure. maybe set to zero
           for now.
         s(isinf(s)) = 1;
105
106
         y = -((p(4)*p(2))/(p(1)+p(2)*p(5))).*((p(6)-s)./(p(6)*p(3)^p(2))).^(1/(p(1)+p(2)*p(3))).
            (2)*p(5));
         if (size(y,1)==91) &&(size(y,2)==109) &&(size(y,3)==91)
107
108
             f = -((p(1)+p(2)*p(5))/(p(4)*p(2))).*lambw_mex(real(y)); % <-- compiled
                version: runs faster
109
         else
             f = -((p(1)+p(2)*p(5))/(p(4)*p(2))).*lambw(y); % <-- not compiled, but
110
                still pretty fast
111
         end
112
         m = p(3)*f.^(p(5)+1).*exp(-p(4)*f);
113
         % Clean up NaNs
         m(isnan(m))=1;
114
        f(isnan(f))=1;
115
         \% make sure that if the BOLD was 1 then the meabolism/flow is 1
116
         % DOUBLE CHECK THAT THIS IS OK!!!!!!!
117
         m = m./mNOACT;
118
119
         f = f./fNOACT;
120
         eval(['m' sprintf('%04d',j) ' = m;']);
121
         eval(['f' sprintf('%04d',j) ' = f;']);
122
```

```
123
         eval(['save(''./' newFolder '/m.mat'', ''m' sprintf('%04d',j) ''',''-append'')
         eval(['save(''./' newFolder '/f.mat'', ''f' sprintf('%04d',j) ''',''-append'')
124
           ; ']);
         clear m0* f0*  % prevent holding onto variables after they're done being used
125
126
127
        t = toc;
        rem = ((file_count-j)*t)/60;
128
         disp([file_list(j).name ' num2str(rem,4) ' minutes remaining'])
129
    end
130
131
132
    close(statusbar)
    cd(oldfold)
133
134
135
    %% OLD METHOD
136
137
    %{
138
    tic
139
    y = -((p(4)*p(2))/(p(1)+p(2)*p(5))).*((p(6)-s)./(p(6)*p(3)^p(2))).^(1/(p(1)+p(2)*p(3))).
140
       (5)));
    f = -((p(1)+p(2)*p(5))/(p(4)*p(2))).*lambertw(y);
141
142
    m = p(3)*f.^(p(5)+1).*exp(-p(4)*f);
143
    toc
144
    %}
145
    %f_out = f;
146
147
    %m_out = m;
    % m = s;
148
    % f = s;
149
    %% Output
150
    % = 1000 % In order to make it easier when calculating the change in temperature,
151
    \% this function will create one *.mat file with a seperate variable for
152
153
    \% each time step. It's a little anoying but since it's such a large file
```

```
154
    % when combined, it's the only way to do it.
155
    %{
156
    newFolder = ['Output', datestr(clock)];
157
    mkdir(newFolder)
158
    oldFolder = cd(newFolder);
159
    varsM = cell(size(s,1), 1);
160
    varsF = cell(size(s,1), 1);
161
162
    for k = 1:size(s,1);
         eval(strcat('m',num2str(k),' = squeeze(m(k,:,:,:));'));
163
         eval(strcat('f',num2str(k),' = squeeze(f(k,:,:,:));'));
164
        varsM{k} = strcat(',''m',num2str(k),''');
165
         varsF{k} = strcat(',','f',num2str(k),''');
166
167
    end
    mfin = strcat(cell2mat(varsM'));
168
169
    ffin = strcat(cell2mat(varsF'));
170
    eval(strcat('save(''m_BOLD.mat''', mfin,');'));
    eval(strcat('save(''f_BOLD.mat''',ffin,');'));
171
172
    cd(oldFolder);
    %}
173
174
175
    end
```

A.2.4 lambw() and lambw_mex()

The lambw() function is a wrapper for the wapr() function available on Matlab FileExchange (http://www.mathworks.com/matlabcentral/fileexchange/3644-real-values-of-the-lambert-w-function/content/Lambert/wapr.m). A compiled version of this function (lambw_mex()) runs much faster and is recommended. This function is used over Matlab's built-in Lambert-W function for the sake of performance.

```
%#codegen
7
8
   if ndims(array_in) ~= 3
        error('This only works (for now) with a three dimensional array.')
10
   end
11
12
13
   xmax = size(array_in,1);
   ymax = size(array_in,2);
14
15
16
   array_out = zeros(size(array_in));
17
   for ix=1:xmax
        for iy=1:ymax
18
            array_out(ix,iy,:) = wapr(array_in(ix,iy,:));
19
        end
20
   end
21
22
   end
23
```

A.3 Calculating the Equilibrium Temperature

In order to determine the temperature fluctuations due to changes in activity, the baseline temperature must first be established for each voxel. The function tempCalcEquilibrium() will update the temperature using the Penne's bioheat equation (eq. (2.7)) until the change in temperature for each voxel falls below a certain threshold. Details about this procedure are available in section 2.3.1.

```
function temperature_Out = tempCalcEquillibrium(tissue, bloodT, airT, nt, tmax, pastCalc, printp
\% temp CalcEquillibrium Find the equillibrium values
%
    tissue: holds all of the strucual information
%
    bloodT: Temperature of the blood
%
    airT:
             Temperature of the surrounding ait
%
    nt:
             Max number of time steps
%
             Total amount of time the simulation should run over
    tmax:
%
%
    This is based off of tempCalc() but loops until the rate of change of
%
    a each voxel is sufficiently small then outputs what's
%
    calculated. If if takes too long to do all at once, split it up into
%
    smaller time chunks and use the last step from the previous dataset as
%
    pastCalc in order to resume.
%
%
    Note: This does not save the time corse because it can take a lot of step to
    find \ the \ equillibrium \, . \quad It \ outputs \ the \ last \ time \ step \, .
%
%
    Writen\ by\ Greggory\ Rothmeier\ (greggroth@gmail.com)
%
%
    Georgia State University Dept. Physics and Astronomy
%
    May, 2011
tic
     Default Values
if nargin < 2, bloodT = 37;
                                  end
if nargin < 3, airT = 24;
                                  end
if nargin < 4, nt = 100;
                                  end
if nargin < 5, tmax = 50;
                                  end
if nargin < 6, pastCalc = 0;
                                  end
```

```
if nargin < 7, printprogress = 1; end
% These rescue the data if the calculation is interrupted.
global temperature
global dirty
c = onCleanup (@InterCatch);
dirty = 1;
dx = 2*10^{-3};
                    % Voxel size (m)
if nt < (2*tmax),
   warning ('Time_step_size_is_not_large_enough.__Results_will_be_unreliable.__Consider_inc
end
% Constants used that aren't already stored in tissue
[xmax ymax zmax t] = size(tissue);
clear t;
dt = tmax/(nt-1);
\% \ rhoBlood = 1057;
\% wBlood = 1000;
\% \ cBlood = 3600;
% ======
\% = Setup =
% ======
    Starts all tissue voxels at bloodT (default 37) and maintains air at airT (default 24)
%
    The condition squeeze (tissue (:,:,:,) \tilde{} = airIndex picks out the elements that are
%
    tissue
temperature = ones(3,xmax,ymax,zmax,'single')*airT;
```

```
if pastCalc == 0
          temperature (1, \text{squeeze}(\text{tissue}(:,:,:,1))^{\sim} = 1) = \text{bloodT};
else
          temperature (1,:,:,:) = pastCalc;
end
numElements = numel(temperature(1,:,:,:));
% ======
\% = Do\ Work =
% ======
          This is a vectorized version of the next section. For the love of god
%
          don't make any changes to this without first looking below to make sure
%
          you know what you're changing. This is [nearly] impossible to
\%
          understand, so take your time and don't break it.
%
          data is stored in 'tissue' as such :
%
          [tissuetype\ 0\ Qm\ c\ rho\ k\ w]; <-- second\ element\ is\ blank\ for\ all.
%
          1 2 3 4 5 6 7
        This makes an array that has smoothed out variations in k by averaging all
      of the k's around each voxel (including itself). This is a hap-hazard
% solution to the problem that if you only take the value of k for the voxel
% without considering what surrounds it, it doesn't matter whether the head
% is surrounded by air, water or anything else. Since water is a better
      thermal conductor than air, we need a way of accounting for this. This is
     one way:
averagedk = (circshift(tissue(:,:,:,6),[1 \ 0 \ 0]) + circshift(tissue(:,:,:,6),[-1 \ 0 \ 0]) + circshift(tissue(:,:,-6),[-1 \ 0 \ 0]) + cir
rhoblood = 1057;
cblood = 3600;
% Specify Percision Goal
tolerence = 1; % fraction of voxels have a slope less than 'zeropoint'
zeropoint = 2.5e-7; % point at which the slope between two *steps* is considered essential
```

```
goal = numElements - tolerence*numElements;
  goon = numElements; % Forces the while loop to run the first time
  format shortG;
  \% temperature (1,:,:,:) = Current Temperature
  \% temperature (2,:,:,:) = Next Temperature
  % Resets after each update
  if printprogress
                    disp(['Goal: __', num2str(goal), '_remaining_voxels'])
  end
  t2 = 1;
 while goon(1)>goal && t2<=nt % runs until either 'goal' elements have a slope greater tha
                if printprogress
                    disp([t2 goon(1) ((numElements-goon(1))/numElements)*100]) % progress
               end
                temperature (2, :, :, :) = squeeze (temperature (1, :, :, :)) + ...
                                      dt/(tissue(:,:,:,5).*tissue(:,:,:,4)).* ...
                                      ((averagedk/dx^2).*...
                                     (\; \texttt{circshift} \; (\; \texttt{squeeze} \; (\; \texttt{temperature} \; (\; 1 \; , : \; , : \; )) \; , [\; 1 \quad 0 \quad 0]) \; - \; 2 * \; \texttt{squeeze} \; (\; \texttt{temperature} \; (\; 1 \; , : \; , : \; )) \; + \; \; \text{squeeze} \; (\; \texttt{temperature} \; (\; 1 \; , : \; , : \; )) \; + \; \; \text{squeeze} \; (\; \texttt{temperature} \; (\; 1 \; , : \; , : \; )) \; + \; \; \text{squeeze} \; (\; \texttt{temperature} \; (\; 1 \; , : \; , : \; )) \; + \; \; \text{squeeze} \; (\; \texttt{temperature} \; (\; 1 \; , : \; , : \; )) \; + \; \; \text{squeeze} \; (\; \texttt{temperature} \; (\; 1 \; , : \; , : \; )) \; + \; \; \text{squeeze} \; (\; \texttt{temperature} \; (\; 1 \; , : \; , : \; )) \; + \; \; \text{squeeze} \; (\; \texttt{temperature} \; (\; 1 \; , : \; , : \; )) \; + \; \; \text{squeeze} \; (\; \texttt{temperature} \; (\; 1 \; , : \; , : \; )) \; + \; \; \text{squeeze} \; (\; \texttt{temperature} \; (\; 1 \; , : \; , : \; )) \; + \; \; \text{squeeze} \; (\; \texttt{temperature} \; (\; 1 \; , : \; , : \; )) \; + \; \; \text{squeeze} \; (\; \texttt{temperature} \; (\; 1 \; , : \; , : \; )) \; + \; \; \text{squeeze} \; (\; \texttt{temperature} \; (\; 1 \; , : \; , : \; )) \; + \; \; \text{squeeze} \; (\; \texttt{temperature} \; (\; 1 \; , : \; , : \; )) \; + \; \; \text{squeeze} \; (\; \texttt{temperature} \; (\; 1 \; , : \; , : \; )) \; + \; \; \text{squeeze} \; (\; \texttt{temperature} \; (\; 1 \; , : \; , : \; )) \; + \; \; \text{squeeze} \; (\; \texttt{temperature} \; (\; 1 \; , : \; , : \; )) \; + \; \; \text{squeeze} \; (\; \texttt{temperature} \; (\; 1 \; , : \; , : \; )) \; + \; \; \text{squeeze} \; (\; \texttt{temperature} \; (\; 1 \; , : \; , : \; )) \; + \; \; \text{squeeze} \; (\; \texttt{temperature} \; (\; 1 \; , : \; , : \; )) \; + \; \; \text{squeeze} \; (\; \texttt{temperature} \; (\; 1 \; , : \; , : \; )) \; + \; \; \text{squeeze} \; (\; \texttt{temperature} \; (\; 1 \; , : \; , : \; )) \; + \; \; \text{squeeze} \; (\; \texttt{temperature} \; (\; 1 \; , : \; , : \; )) \; + \; \; \text{squeeze} \; (\; \texttt{temperature} \; (\; 1 \; , : \; , : \; )) \; + \; \; \text{squeeze} \; (\; \texttt{temperature} \; (\; 1 \; , : \; , : \; )) \; + \; \; \text{squeeze} \; (\; \texttt{temperature} \; (\; 1 \; , : \; , : \; )) \; + \; \; \text{squeeze} \; (\; \texttt{temperature} \; (\; 1 \; , : \; , : \; )) \; + \; \; \text{squeeze} \; (\; \texttt{temperature} \; (\; 1 \; , : \; , : \; )) \; + \; \; \text{squeeze} \; (\; \texttt{temperature} \; (\; 1 \; , : \; , : \; )) \; + \; \; \text{squeeze} \; (\; \texttt{temperature} \; (\; 1 \; , : \; , : \; )) \; + \; \; \text{squeeze} \; (\; \texttt{temperature} \; (\; 1 \; , : \; )
% shift along x
                                          circshift (squeeze (temperature (1,:,:,:)), [0 \ 1 \ 0]) -2* squeeze (temperature (1,:,:,:)) +
% shift along y
                                          circshift (squeeze (temperature (1,:,:,:)), [0\ 0\ 1]) -2*squeeze (temperature (1,:,:,:)) +
% shift along z
                                                        -(1/6000)*rhoblood*tissue(:,:,:,7)*cblood.*(squeeze(temperature(1,:,:,:)) - blood
                   %
                                       resets the air temperature back since it's also modified above, but
                                       it needs to be kept constant throughout the calculations
                    temperature (2, \text{squeeze}(\text{tissue}(:,:,:,1)) == 1) = \text{airT};
                   %
                                       checks how quickly the temperature is changing and if it is close
                                       enough to zero to be considered stopped ('zeropoint')
                   goon = size(temperature(abs(squeeze(temperature(2,:,:,:) - temperature(1,:,:,:))) > zeropoonup ze
```

```
temperature (1,:,:,:) = temperature (2,:,:,:); % moves 2 back to 1
    t2 = t2 + 1;
end
temperature\_Out = temperature (2,:,:,:); \quad \% \ \textit{Only outputs the last time step}
dirty = 0;
% equilTemperature = temperature_Out;
% save('equil.mat', 'equilTemperature');
% To Combine Datasets
\% use this technique if there are seperate datasets that need combining
     vertcat(squeeze(res1(:,:,:,:)), squeeze(res2(2:end,:,:,:)))
% Where for all by the first dataset, you need to do the time from 2:end
% so that there are no repeats (remember that the last timestep from the
% previous dataset serves as the first for the new one)
time = toc;
end
function InterCatch
global dirty
if dirty
    disp ('Interupt_Intercepted . __Inprepretating_Interworkspace_Data .')
    global temperature
    % equilibrium T = zeros([1 \ size(temperature(1,:,:,:))]);
    \% equillibrium T(1,:,:,:) = temperature(1,:,:,:); \%might be better to swtich equil T(1,:,:,:)
    equillibriumT = temperature;
    save('equiltempAbortDump.mat', 'equillibriumT');
    % setappdata(0, 'InterpOut', temperature);
end
```

 \mathbf{end}

A.4 Calculating the Temperature Change

More details about this algorithm can be found in section 2.3.1.

```
function temperatureOut = tempCalcDynMF(tissue,bloodT,airT,nt,tmax,pastCalc,metab,
       flow, savesteps, region)
   % tempCalcChaning Metabolism How does changin metabolism
3
   % affect things?
4
        tissue: holds all of the strucual information
5
   %
        bloodT: Temperature of the blood
6
        airT:
                 Temperature of the surrounding ait
7
   %
   %
                 Number of time steps
8
        nt:
        tmax:
                 Total amount of time the simulation should run over
9
   %
10
   %
        region: logical matrix same size as head
11
   %
12
   %
        Writen by Greggory Rothmeier (greggroth@gmail.com)
13
        Georgia State University Dept. Physics and Astronomy
14
        May, 2011
15
16
    statusbar = waitbar(0, 'Initializing');
17
18
         Default Values
19
   %%
   if nargin<2, bloodT = 37;</pre>
20
                                           end
    if nargin<3, airT = 24;</pre>
                                           end
21
   if nargin<4, nt = 3;</pre>
                                           end
22
   if nargin <5, tmax = 1;</pre>
                                           end
23
24
   if nargin < 6, pastCalc = 0;</pre>
                                           end
25
27
   % Length of one side of a voxel (m)
    dx = 2*10^-3;
28
29
   if nt<(2*tmax),</pre>
30
       warning('Time step size is not large enough. Results will be unreliable.
31
          Consider increasing the number of steps or reducing tmax.')
```

```
32
    end
33
34
   % Constants used that aren't already stored in tissue
35
    [xmax ymax zmax t] = size(tissue);
36
    clear t;
37
   dt = ones([xmax ymax zmax])*(tmax/(nt-1));
38
   % rhoBlood = 1057;
39
   % wBlood = 1000;
40
   % cBlood = 3600;
41
42
   %% Determine Metab/Flow Data Storage System
43
44
    if ischar(metab)&&ischar(flow)
      % if file locations are given rather than data
45
46
        option = 1;
47
    else
      % Preallocate matrices for holding metabolism and blood flow data
48
        metabMulti = ones([xmax ymax zmax], 'single');
49
        flowMulti = ones([xmax ymax zmax],'single');
50
        option = 0;
51
    end
52
53
   %% Maps
54
   % Creates a map that identifies where there is tissue
55
56
   % the condition squeeze(tissue(:,:,:,)~=airIndex picks out the
    % elements that are tissue
57
58
   tmax = ceil((nt-1)/savesteps);
59
    temperatureOut = ones(tmax,xmax,ymax,zmax,'single');
60
    temperature = ones(2,xmax,ymax,zmax,'single')*airT;
61
    if pastCalc == 0
62
63
        temperature(1, squeeze(tissue(:,:,:,1))~=1) = bloodT;
    else
64
      % Starts everything off at the pre-determined equilibium temperatures
65
66
        temperature(1,:,:,:) = pastCalc(end,:,:,:);
```

```
67
   end
68
   temperatureOut(1,:,:,:) = temperature(1,:,:,:);
70
   % =======
71
   % = Do Work =
72
   % =======
73
       This is a vectorized version of the next section. For the love of
74
       god don't make any changes to this without first looking below to
75
   %
       make sure you know what you're changing. This is [nearly]
76
   %
       impossible to understand, so take your time and don't break it.
77
   %
       data is stored in 'tissue' as such :
78
79
      [tissuetype 0 Qm \ c \ rho \ k \ w] <-- second element is blank for all.
          1
                  2 3 4 5 6 7]
80
81
   % This makes an array that has smoothed out variations in k by
82
   83
84
   % is a hap-hazard solution to the problem that if you only take the
   % value of k for the voxel without considering what surrounds it, it
85
   \% doesn't matter whether the head is surrounded by air, water or
86
   % anything else. Since water is a better thermal conductor than air, we
87
   \% need a way of accounting for this. This is one way:
88
89
90
   averagedk = (circshift(tissue(:,:,:,6),[1 0 0])+circshift(tissue(:,:,:,6),[-1 0
      0])+circshift(tissue(:,:,:,6),[0 1 0])+circshift(tissue(:,:,:,6),[0 -1 0])+
      circshift(tissue(:,:,:,6),[0 0 1])+circshift(tissue(:,:,:,6),[0 0 -1])+tissue
      (:,:,:,6))/7;
   rhoblood = 1057;
91
   cblood = 3600;
92
93
   %% Only saves every 4 steps to reduce the final matrix size
94
   for t2 = 1:nt-1
95
      waitbar(t2/(nt-1), statusbar, sprintf('%d%%', round(t2/(nt-1)*100)));
96
97
   \% if a variable needs to be used multiple times for the same time step.
98
```

```
99
       t3 = floor((t2-1)/4)+1; % 1 1 1 1 2 2 2 2 3 3 . . .
100
101
       \% if a file is specified, pulls the data from the file for each step
       if option
102
            eval(strcat('load(fullfile(metab),''-mat'',''m',sprintf('%04d',t3),''');'))
103
104
            eval(strcat('load(fullfile(flow),''-mat'',''f',sprintf('%04d',t3),''');'));
105
            eval(strcat('metabMulti = m', sprintf('%04d',t3),';'));
106
            eval(strcat('flowMulti = f', sprintf('%04d',t3),';'));
107
            eval(strcat('clear f', sprintf('%04d',t3),' m',sprintf('%04d',t3)))
       else
108
            metabMulti(region) = metab(t2);  % region is hardcoded here
109
110
            flowMulti(region) = flow(t2);
       end
111
112
113
       temperature(2,:,:,:) = squeeze(temperature(1,:,:,:)) + ...
114
             dt./(tissue(:,:,:,5).*tissue(:,:,:,4)).* ...
115
             ((averagedk/dx^2).*...
116
             (circshift(squeeze(temperature(1,:,:,:)),[1 0 0])-2*squeeze(temperature
                (1,:,:,:))+circshift(squeeze(temperature(1,:,:,:)),[-1 0 0])+... %
               shift along x
              circshift(squeeze(temperature(1,:,:,:)),[0 1 0])-2*squeeze(temperature
117
                 (1,:,:,:))+circshift(squeeze(temperature(1,:,:,:)),[0 -1 0])+... %
                shift along v
118
              circshift(squeeze(temperature(1,:,:,:)),[0 0 1])-2*squeeze(temperature
                 (1,:,:,:))+circshift(squeeze(temperature(1,:,:,:)),[0 0 -1]))... %
                 shift along z
                 -(1/6000)*rhoblood*flowMulti.*tissue(:,:,:,7)*cblood.*(squeeze(
119
                    temperature(1,:,:,:))-bloodT)+metabMulti.*tissue(:,:,:,3));
        % resets the air temperature back since it's also modified above,
120
        % but it needs to be kept constant throughout the calculations
121
199
         temperature(2, squeeze(tissue(:,:,:,1))==1) = airT;
123
         temperatureOut(ceil(t2/savesteps),:,:,:) = temperature(2,:,:,:);
         temperature(1,:,:,:) = temperature(2,:,:,:); % moves 2 back to 1
124
         clear metabMulti flowMulti
125
```

```
126
     end
    close(statusbar);
127
128
    % ========
129
    % = Old Code =
130
    % ========
131
    % This is what used to be used. It's much slower (~60 times slower),
132
133
    % but it's much easier to understand compared to the above code. If any
134
    % changes need to be made above, first look through this code to ensure
    % you understand what's happening before making changes. It's really
135
    \% easy to mess up the code above and nearly impossible to figure out
136
    % where.
137
138
       good luck.
139
140
141
    % for t2 = 1:nt-1
142
           for x2 = 2:xmax-1
               for y2 = 2:ymax-1
143
    %
                   for z2 = 2:zmax-1
144
    %
                        if tissue(x2,y2,z2,1) ~= 1,
    %
145
146
    %
                            temperature (t2+1,x2,y2,z2) = temperature (t2,x2,y2,z2) + (dt
       /(tissue(x2,y2,z2,5)*tissue(x2,y2,z2,4)))*((tissue(x2,y2,z2,6)/dx^2)*...
147
    %
                              (temperature(t2,x2+1,y2,z2)-2*temperature(t2,x2,y2,z2)+
       temperature (t2, x2-1, y2, z2)+...
148
    %
                              temperature(t2, x2, y2+1, z2)-2*temperature(t2, x2, y2, z2)+
       temperature (t2, x2, y2-1, z2)+...
149
    %
                              temperature (t2, x2, y2, z2+1) -2*temperature (t2, x2, y2, z2) +
       temperature(t2,x2,y2,z2-1))...
    %
                              -(1/6000)*rhoBlood*wBlood*cBlood*(temperature(t2,x2,y2,z2)
150
       -bloodT)+tissue(x2,y2,z2,3));
                        end
    %
151
152
    %
                   end
153
    %
               end
    %
154
           end
155
    % end
```

157 end

Appendix B

Visualization Tools

B.1 Visualizing the data

Requires SliceBrowser (http://www.mathworks.com/matlabcentral/fileexchange/20604).

B.1.1 tsliceplot

This is a visualization tool I wrote that allows you to view the change in temperature versus time for a line passing through the head. Screenshots of the tool can be seen in figs. B.1 and B.2.

Usage:

```
tsliceplot(temperature_data, equilibrium_temperature_data)
```

The script is available as part of temptools (https://github.com/greggroth/tempcalc/tree/master/t/supportfcts/tsliceplot).

Figure B.1: Experimental data for activity in the motor cortex visualized with tsliceplot.

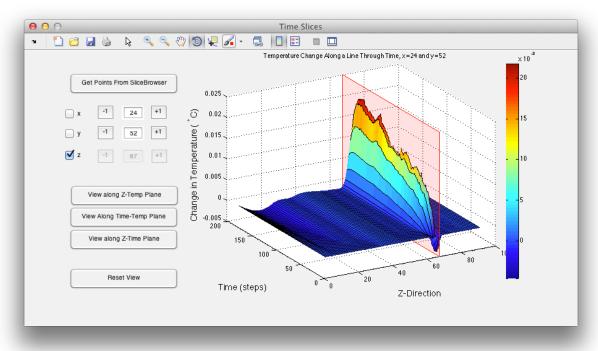


Figure B.2: The same data as is presented in fig. B.1, but viewed flat-on along the z vs. time plane.

